

1) Design a Butterworth filter (LP) for the following specifications.

$$K_p = -3\text{dB}, \quad K_s = -15\text{dB}, \quad \omega_p = 500\text{ rad/s}, \quad \omega_s = 1000\text{ rad/s}$$

2) Design a Butterworth HPF to meet the following specifications.

- i) Passband attenuation = 3dB
- ii) — " — edge freq = 200 rad/s.
- iii) Stopband attenuation  $\geq 25\text{dB}$
- iv) — " — edge freq  $\leq 100\text{ rad/s}$ .

3) Transform a 3rd order Butterworth normalized filter to HPF with passband edge freq of 2 rad/s.

4) If  $H_n(s) = \frac{1}{s^2 + \sqrt{2}s + 1}$  is TF of LPF with passband of 1 rad/s. use freq. transformation to find TF of following analog filters.

- i) A LPF with passband of 10 rad/s.
- ii) A HPF with passband of 100 rad/s.

5) Consider 2nd order LPF with cutoff freq of 500 Hz. Find the attenuation in dB at 1 kHz.

6) Design a Chebyshev -I analog filter to meet following specification.

- i) Passband attenuation of 2dB at 4 rad/s.
- ii) Stopband attenuation of 10dB at 7 rad/s.

7) Find half power freq of fifth order chebyshev -I LPT with 2dB passband edge at 1 kHz.  
 [Hint: find TF  $H(j\omega)$  & substitute  $|H(j\omega)| = \frac{1}{2}$  & find  $\omega$ ]

8) Let  $\omega_p$  &  $\omega_s$  denote desired passband & stopband edge freq. of an analog filter. Let  $\delta_p$  &  $\delta_s$  be passband & stopband attenuations. s.t the order of the filter required to meet given specifications is

$$N \geq \log(1/\delta) \div \log(1/k)$$

where  $d = \sqrt{\frac{(1-\delta_p)^{-2} - 1}{\delta_s^{-2} - 1}}$  is discrimination factor

&  $k = \frac{\omega_p}{\omega_s}$  is selectivity factor.

9) Find order for analog butterworth filter & chebyshev -I filter for the following specification and comment on the result.

Pass band attenuation = 0.1

Stop band — " — = 0.1

Pass band edge freq = 100 Hz

stop — " — = 200 Hz.

10) Design a analog chebyshev -I filter (High pass) to have -3dB cut  $\omega_0$  freq of 100 Hz. & a stopband attenuation of  $\geq 25$  dB for all freq. below 100 Hz.



- (11) using bilinear transformation design HPF monotonic in passband with cut off frequency of  $1000 \text{ Hz}$  &  $10 \text{ dB}$  attenuation at  $350 \text{ Hz}$ . Sampling frequency  $5000 \text{ Hz}$ .  
 [Hint: Passband attenuation not given so can be assumed as  $3 \text{ dB}$ ]  
 RB-5.49, 50

- (12) Obtain an analog chebyshev-I filter <sup>Transfer</sup> function that satisfies the constraints  $\frac{1}{\sqrt{2}} \leq |H(j\Omega)| \leq 1$ ;  $0 \leq \Omega \leq 2 \text{ r/s}$  RB-5.25  
 $|H(j\Omega)| \leq 0.1$ ;  $\Omega \geq 4 \text{ r/s}$ .

- (13) The system function of an analog filter is given by. ch-4.82  
 $H(s) = \frac{1}{(s+1)(s+2)}$  obtain  $H(z)$  using impulse invariant method.  
 Take sampling frequency of  $5 \text{ samples/sec}$ .  
 ch-4-129

- (14) The specification of the LPF are given as

$$0.8 \leq |H(\omega)| \leq 1 \quad \text{for } 0 \leq \omega \leq 0.2\pi$$

$$|H(\omega)| \leq 0.2 \quad \text{for } 0.32\pi \leq \omega \leq \pi$$

Design chebyshev filter using Bilinear transformation. ch-4-118  
 Assuming  $T=2$ .

- (15) Design IIR filter that when used in prefilter A/D-H(z)-D/A structure will satisfy the following equivalent analog specification.

- (i) LPF with  $-1 \text{ dB}$  at  $100\pi \text{ r/s}$
- (ii) Stopband attenuation of  $35 \text{ dB}$  or greater.  $1000\pi \text{ r/s}$
- (iii) Monotonic passband & stopband
- (iv) Sampling rate of  $2000 \text{ sample/seconds}$ . ch-4-131

- (16) Design a digital LPF to satisfy the following passband ripple  $1 \leq |H(j\Omega)| \leq 0$  for  $0 \leq \Omega \leq 1404 \pi \text{ r/s}$  & Stopband attenuation  $H(j\Omega) \geq 60 \text{ dB}$  for  $\Omega \geq 8268 \pi \text{ r/s}$ . Sampling interval  $T = \frac{2}{10^4} \text{ sec}$ . Use bilinear transformation. assuming  $\frac{2}{T} = 1$ .