

Module 4

Structures for Realization of Discrete time systems:

Realization of FIR and IIR filters using direct form structures and cascade form structures, Lattice structure for FIR Filters.

Introduction to Digital Signal (DS) Processors:

Introduction, Digital Signal Processor Architecture- Von Neumann architecture and Harvard architecture, Fixed- and Floating-Point Format for DS processors.

Text Books

Proakis&Manolakis, "Digital signal processing – Principles Algorithms & Applications", *Pearson education*, 4th Edition, New Delhi, 2007.

Li Tan, "Digital Signal Processing", Academic Press, *Elsevier*, 2007.

Basic IIR Filter Structures

The causal IIR digital filters we are concerned with in this course are characterized by a real rational transfer function of z^{-1} or, equivalently by a constant coefficient difference equation

From the difference equation representation, it can be seen that the realization of the causal IIR digital filters requires some form of feedback

An N -th order IIR digital transfer function is characterized by $2N+1$ unique coefficients, and in general, requires $2N+1$ multipliers and $2N$ two-input adders for implementation

Direct form IIR filters: Filter structures in which the multiplier coefficients are precisely the coefficients of the transfer function

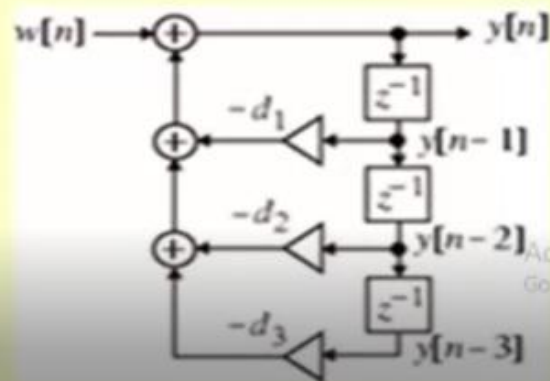
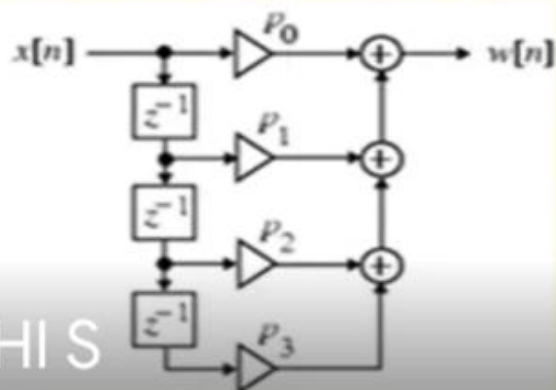
Contd...

$$H(z) = \frac{P(z)}{D(z)} = \frac{p_0 + p_1 z^{-1} + p_2 z^{-2} + p_3 z^{-3}}{1 + d_1 z^{-1} + d_2 z^{-2} + d_3 z^{-3}}$$

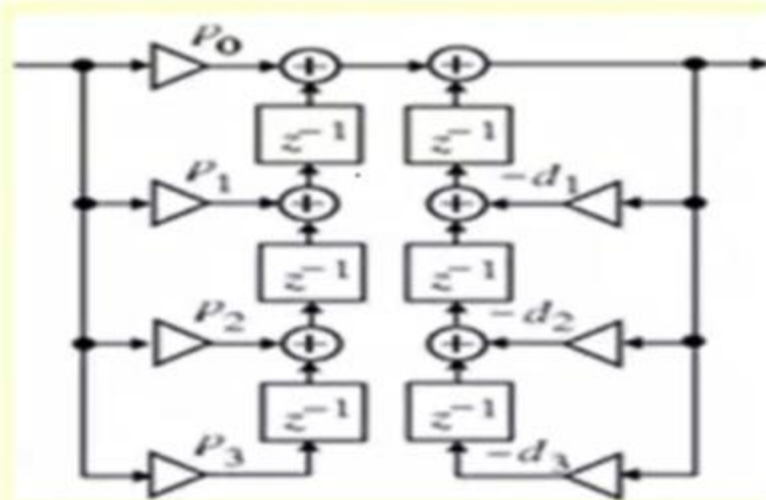
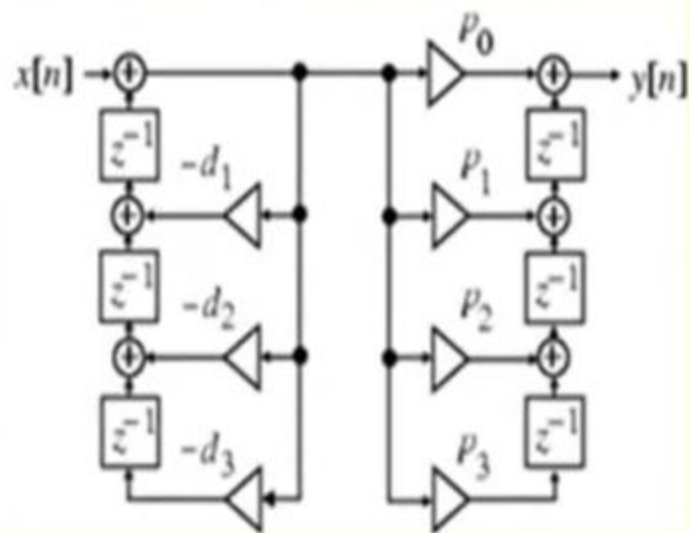
$$H_1(z) = \frac{W(z)}{X(z)} = P(z) = p_0 + p_1 z^{-1} + p_2 z^{-2} + p_3 z^{-3}$$

$$H_2(z) = \frac{Y(z)}{W(z)} = \frac{1}{D(z)} = \frac{1}{1 + d_1 z^{-1} + d_2 z^{-2} + d_3 z^{-3}}$$

$$w[n] = p_0 x[n] + p_1 x[n-1] + p_2 x[n-2] + p_3 x[n-3] \quad y[n] = w[n] - d_1 y[n-1] - d_2 y[n-2] - d_3 y[n-3]$$



- The direct form-I structure is non canonical as it requires 6 delay elements to realize a 3rd order transfer function



$$A_p = 20 \log(0.6) = -4.4 \text{ dB}$$

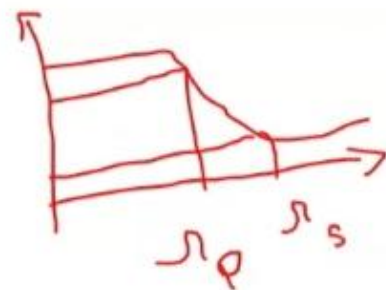
$$A_s = 20 \log(0.1) = -20 \text{ dB}$$

$$\omega_p = 0.35 \pi$$

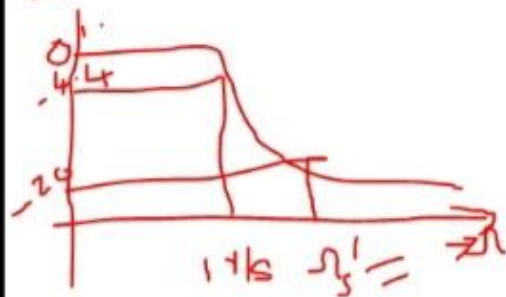
$$\omega_s = 0.75 \pi$$

II V

$$\Omega_p = \frac{\omega_p}{T}$$



1x1 in 10dB



BLT

$$\Omega_p = \left(\frac{2 + \tan^2\left(\frac{\omega_p}{2}\right)}{1} \right)^{1/2}$$

$$\Omega_s = \frac{2}{1} \tan\left(\frac{\omega_s}{2}\right)$$

$$S \rightarrow \left(\frac{2}{T} \right) \left(\frac{1 - z^{-1}}{1 + z^{-1}} \right)$$

$$⑤ H_n(s) = \frac{1}{s_n^2 + 1.414s_n + 1}$$

$$⑥ H_a(s) = H_n(s) \Big|_{s \rightarrow \frac{s}{\Omega_c}} =$$

$$\Omega_c' = \Omega_p \Omega_c$$

$$= 0.613(0.87)$$

$$\Omega_c' = 0.53$$

$s_n \rightarrow \frac{s}{\Omega_c}$ if Ω_c is calculated for $\frac{1}{\Omega_c}$

$s_n \rightarrow \frac{s}{\Omega_c}$ if Ω_c is given $\frac{\Omega_p}{\Omega_c}$