(ii) Binary Symmetric Channel (BSC):

BSC is one of the most commonly and widely used channels, whose channel diagram is shown in figure 4.7.

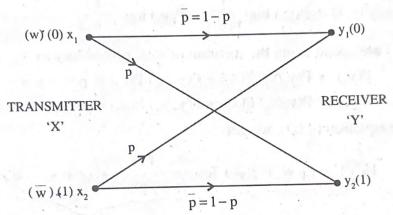


Fig. 4.7: Channel diagram of a BSC

Let
$$P(x_1) = w$$
 and $P(x_2) = 1 - w = \overline{w}$ (say)

Let $p = \text{probability of error}$
 $= \text{probability of reception of '1' when '0' is transmitted}$
 $= \text{probability of reception of '0' when '1' is transmitted.}$

Note that in a BSC, the symbol x_1 is encoded as '0' and x_2 as '1'.

The channel matrix of a BSC can be written looking at the channel diagram of figure 4.7

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$$P(Y/X) = \begin{cases} x_1 & y_2 \\ x_2 & P(y_1/x_1) & P(y_2/x_1) \\ P(y_1/x_2) & P(y_2/x_2) \end{cases}$$

$$P(Y/X) = \begin{bmatrix} \overline{p} & \overline{p} \\ \overline{p} & \overline{p} \end{bmatrix}$$

The matrix of equation (4.67) is a symmetric matrix and b