

## Click to add title

- $(-307.1875)_{10}$
- $000100110011.0011$
- $1.001100110011 \times 2^{-8}$
- $S=1; E=8, E'=8+127=135=87H=10000111$
- $M=001100110011$





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- $0.125 \times 2 = 0.25 \rightarrow 0$
- $0.25 \times 2 = 0.5 \rightarrow 0$
- $0.5 \times 2 = 1.0 \rightarrow 1$

# Fractions

If  $b$  is a binary vector, then we have seen that it can be interpreted as an unsigned integer by:

$$V(b) = b_{31} \cdot 2^{31} + b_{30} \cdot 2^{30} + b_{29} \cdot 2^{29} + \dots + b_1 \cdot 2^1 + b_0 \cdot 2^0$$

This vector has an implicit binary point to its immediate right:

$$b_{31}b_{30}b_{29}\dots\dots\dots b_1b_0 \quad \text{implicit binary point}$$

Suppose if the binary vector is interpreted with the implicit binary point is just left of the sign bit:

$$\text{implicit binary point} \quad .b_{31}b_{30}b_{29}\dots\dots\dots b_1b_0$$

The value of  $b$  is then given by:

$$V(b) = b_{31} \cdot 2^{-1} + b_{30} \cdot 2^{-2} + b_{29} \cdot 2^{-3} + \dots + b_1 \cdot 2^{-31} + b_0 \cdot 2^{-32}$$

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- $(10011101011.001)_2$
- $1.0011101011001 \cdot 2^{10}$
- $S=0; E=10; E'=137; M=0011101011001; E'=89H=10001001$

I

0	10001001	00111010110010000000....0
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## Single precision format

- Fixed point
- 011111(+ve)
- 111111(-ve)
- $6.024 \times 10^{23}$
- $6.625 \times 10^{-34}$
- **$\pm 1.M \times 2^E$**
- Mantissa -fraction
- E exponent +ve/-ve
- $E' = E' \mp 127 \quad 0 < E' < 255$
- $1 < E' < 254$
- $E \quad -126 < E' < 127$
- $2^{-126}$  to  $2^{127}$

# Normalization

Consider the number:

$$x = 0.0004056781 \times 10^{12}$$

If the number is to be represented using only 7 significant mantissa digits, the representation ignoring rounding is:

$$x = 0.0004056 \times 10^{12}$$

If the number is shifted so that as many significant digits are brought into 7 available slots:

$$x = 0.4056781 \times 10^9 = 0.0004056 \times 10^{12}$$

Exponent of  $x$  was decreased by 1 for every left shift of  $x$ .

A number which is brought into a form so that all of the available mantissa digits are optimally used (this is different from all occupied which may not hold), is called a normalized number.

Same methodology holds in the case of binary mantissas

$$0001101000(10110) \times 2^8 = 1101000101(10) \times 2^5$$

$(+1259.125)_{10}$

- 2 1259
- 2 629  $\rightarrow 1$
- 2 314  $\rightarrow 1$
- 2 157  $\rightarrow 0$
- 2 78  $\rightarrow 1$
- 2 39  $\rightarrow 0$
- 2 19  $\rightarrow 1$
- 2 9  $\rightarrow 1$
- 2 4  $\rightarrow 1$
- 2 2  $\rightarrow 0$
- 1  $\rightarrow 0$

## A sample representation

