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Theory:

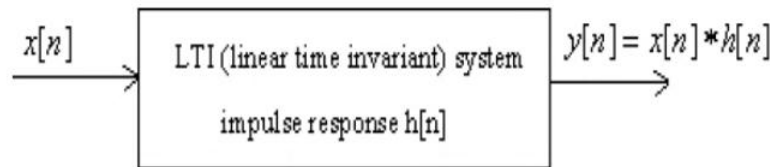


Fig.2.1 A LTI system

A complete **characterization of any LTI system** can be represented in terms of its **response to an unit impulse**, which is referred to as **Impulse response** of the system. Alternatively, the impulse response is the output of a LTI system due to an impulse input applied at $t=0$, or $n=0$.

- A discrete time LTI system (also called digital filters) as shown in Fig.2.1 is represented by
 - A linear constant coefficient difference equation, for example, $y[n] + a_1 y[n-1] - a_2 y[n-2] = b_0 x[n] + b_1 x[n-1] + b_2 x[n-2]$;
 - A system function $H(z)$ (obtained by applying Z transform to the difference equation).

$$H(z) = \frac{Y(z)}{X(z)} = \frac{b_0 + b_1 z^{-1} + b_2 z^{-2}}{1 + a_1 z^{-1} - a_2 z^{-2}}$$

- Given the difference equation or $H(z)$, the impulse response of the LTI system is found using

PROBLEM:

Obtain the Impulse response of a system described by the difference equation-
 $y(n) - 3/4 y(n-1) + 1/8 y(n-2) = x(n) - 1/3 x(n-1)$

Solution:

$$Y(z) - 3/4 Y(z)z^{-1} + 1/8 Y(z)z^{-2} = X(z) - 1/3 X(z)z^{-1}$$

$$H(z) = Y(z) / X(z) = (1 - 1/3 z^{-1}) / (1 - 3/4 z^{-1} + 1/8 z^{-2})$$

Applying partial fractions,

$$H(z) = (1 - 1/3 z^{-1}) / (1 - 1/2 z^{-1})(1 - 1/4 z^{-1}) = A / (1 - 1/2 z^{-1}) + B / (1 - 1/4 z^{-1})$$

$$A = 2/3;$$

$$B = 1/3;$$

$$H(z) = (2/3) / (1 - 1/2 z^{-1}) + (1/3) / (1 - 1/4 z^{-1})$$

$$h(n) = (2/3) (1/2)^n u(n) + (1/3) (1/4)^n u(n)$$

$$h(0) = 1$$

$$h(1) = 0.416$$

$$h(2) = 0.187$$

$$h(3) = 0.088$$

$$h(4) = 0.0429$$

$$h(5) = 0.02116$$

$$h(6) = 0.0105$$

$$h(7) = 0.0052$$

$$h(8) = 0.0026$$

$$h(9) = 0.0013$$

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```
4 - N=input('Length of response required=');
5 - b=[1]; %x[n] coefficient
6 - a=[1,-1,0.9]; %y coefficients
7 - x=[1,zeros(1,N-1)]; %impulse input
8 - n=0:1:N-1; %time vector for plotting
9 - h=filter(b,a,x); %impulse response
10 - disp(h);
11 - subplot(2,1,1);
12 - stem(n,x);
13 - title('impulse input ....');
14 - xlabel('n');
15 - ylabel('x(n)');
16 - subplot(2,1,2);
17 - stem(n,h);
18 - title('impulse response');
19 - xlabel('n');
```

Workspace

Name	Value	Min	Max
a	[1,-0.7500,0.1250]	-0.7500	1
b	[1,-0.3333]	-0.3333	1
h	[1;0.4167;0.1875;0.088...	0.0013	1
k	[]		
N	10	10	10
p	[0.5000;0.2500]	0.2500	0.50
r	[0.6667;0.3333]	0.3333	0.66
t	[0;1;2;3;4;5;6;7;8;9]	0	9

Command Window

```
0.5000
0.2500

k =

[]

f_h =
```

script Ln 20 Col 1

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2b.2 To find step response:

```
clc; close all; clear all
```

```
b=input('Enter the co-efficients of b ie x[n]=');
```

```
a=input('Enter the co-efficients of a ie y[n]=');
```

```
N=input('Enter the length of response required N=');
```

```
n=0:1:N-1;
```

```
x=[ones(1,N)];
```

```
y=filter(b,a,x)
```

```
subplot(211); stem(n,x); title('Step input');
```

```
subplot(212); stem(n,y); title('Step response');
```

Result:

Enter the co-efficients of b ie $x[n]=[1]$

Enter the co-efficients of a ie $y[n]=[1 \ -1 \ 0.9]$

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```
1 - clc;
2 - close all;
3 - clear all;
4 - b=input('Enter the co-efficients of b ie x[n]=');
5 - a=input('Enter the co-efficients of a ie y[n]=');
6 - N=input('Enter the length of response required N=');
7 - n=0:N-1;
8 - x=cos(0.05*pi*n);
9 - y=filter(b,a,x);
10 - subplot(211);
11 - stem(n,x);
12 - title('Steady input');
13 - subplot(212);
14 - stem(n,y);
15 - title('Steady State response');
```

Workspace:

Name	Value	Min	Max
a	[1,-0.8000]	-0.8000	1
b	1	1	1
n	[0,1,2,3,4,5,6,7,8,9]	0	9
N	10	10	10
x	[1,1,1,1,1,1,1,1,1,1]	1	1
y	[1,1.8000,2.4400,2.952...	1	4.46

Command Window:

```
Enter the co-efficients of b ie x[n]=1
fx Enter the co-efficients of a ie y[n]=
```

Waiting for input

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