

$$y(n) - \frac{3}{4}y(n-1) + \frac{1}{8}y(n-2) = x(n) - \frac{1}{3}x(n-1)$$

$$Y(z) - \frac{3}{4} \frac{Y(z)}{z} + \frac{1}{8} \frac{Y(z)}{z^2} = X(z) - \frac{1}{3} \frac{X(z)}{z}$$

$$Y(z) \left[ 1 - \frac{3}{4}z^{-1} + \frac{1}{8}z^{-2} \right] = X(z) \left[ 1 - \frac{1}{3}z^{-1} \right]$$

$$\frac{Y(z)}{X(z)} = \frac{\left[ 1 - \frac{1}{3}z^{-1} \right]}{\left[ 1 - \frac{3}{4}z^{-1} + \frac{1}{8}z^{-2} \right]}$$

$$= \frac{\left[ 1 - \frac{1}{3}z^{-1} \right]}{\left[ 1 - \frac{1}{2}z^{-1} \right] \left[ 1 - \frac{1}{4}z^{-2} \right]}$$

$$\frac{1}{1 - \frac{1}{3}z^{-1}} = \frac{B}{\left[ 1 - \frac{1}{2}z^{-1} \right]} + \frac{A}{\left[ 1 - \frac{1}{4}z^{-2} \right]}$$

$$\left[ 1 - \frac{1}{3}z^{-1} \right] = B \left[ 1 - \frac{1}{4}z^{-2} \right] + A \left[ 1 - \frac{1}{2}z^{-1} \right]$$

$$z^2 = \frac{1}{4}$$

$$z = \pm \frac{1}{2}$$

$$z = -\frac{1}{2}$$

$$\cancel{1} \cancel{2} \left[ 1 - \frac{2}{3} = A \cdot 2 \right]$$

$$A = \frac{2}{3}$$

$$z = \frac{1}{2}$$

$$B = \frac{1}{3}$$

$$H(z) = \frac{\left(\frac{1}{3}\right)}{\left[1 - \frac{1}{2}z^{-1}\right]} + \frac{\left(\frac{2}{3}\right)}{1 - \frac{1}{4}z^{-2}}$$