

Solution for Assignment 3

1. 5 years from now, a future receipt of Rs 20,000 at 14% compounded semiannually will be equivalent to present value of Rupees

a. 10,167

b. 9,501

c. 13,223

d. 14,000

Solution: Given, $n = 5$ year, $F = 20000$

1st method to solve: Nominal interest rate = 14% compounded semiannually, $n = 5$

Effective annual interest rate = $i_a = (1 + 0.14/2)^2 - 1 = 14.49\%$ per annum

$P = 20000 \times (1 + 0.1449)^{-5} = 10167$ (Ans)

2nd method to solve: Effective Interest rate = 7% per six month, $n = 10$

$P = 20000 (P/F, 7, 10) = 20000 \times 0.5083 = 10166$ (Ans)

2. What value of equal payment series is equivalent to present amount of Rs 65,000 in six years at 8% interest rate compounded quarterly with quarterly payments?

a. 2,940

b. 3,067

c. 3,439

d. 4,480

Solution: Given, $P = 65000$, $n = 6 \times 4 = 24$, effective interest rate = $8/4 = 2\%$

$A = 65000 (A/P, 2, 24) = 65000 \times 0.0529 = 3438.5 \approx 3439$ (Ans)

3. For present amount, $P = \text{Rs } 10,000$ and future amount, $F = \text{Rs } 30,000$, if compounding is quarterly, what effective annual interest rate and nominal interest rate will make P and F equivalent for $n = 6$ years.

a. 20.1% per year and 18.7% compounded quarterly

b. 18.1% per year and 16.2% compounded quarterly

c. 22.7% per year and 20.9% compounded quarterly

d. 15.2% per year and 14.8% compounded quarterly

Solution: Given, $P = 10000$, $F = 30000$, $n = 6$ years, i = effective annual interest rate,

r = nominal interest rate compounded quarterly

$(1+i)^n = F/P \Rightarrow (1+i)^6 = 3 \Rightarrow \ln(1+i) = (\ln 3)/6 \Rightarrow i = 0.201 = 20.1\%$ (Ans)

Now, $0.201 = (1 + r/4)^4 - 1 \Rightarrow r = 0.1874 = 18.7\%$ (Ans)

4. Single amount at the end of fifth year, which will be equivalent to uniform annual series of Rs 20,000 per year for 12 years at 7% interest rate compounded annually will be Rupees

a. 1,87,867

b. 2,00,879

c. 2,22,796

d. 2,45,480

Solution: Given, $A = 20000$, $I = 7\%$, F_5 (equivalent future value at $n = 5$) = ?

Equivalent value of F_5 at present time = Equivalent value of annual payment series at present time

$F_5 (P/F, 7, 5) = 20000 (P/A, 7, 12) \Rightarrow F_5 (0.7130) = 20000 (7.9427) \Rightarrow F_5 = 222796$ (Ans)

5. The annual equivalent of series of payment of Rs 20,000 per year, received at the end of each of the next 3 year, at an interest rate of 10% is

a. Rs 20,000/year

b. Less than Rs 20,000/year

c. More than Rs 20,000/year

d. 20,000 (A/P, 10, 3)

Solution: Annual equivalent is nothing but annual payment of the series, which is given already in the question as 2000 per year.

6. A machine is purchased for Rs 9,00,000 with useful life of 10 years and a salvage value at the end of its life Rs 1,50,000. At 15% interest rate compounded annually, the capital cost of machine will be
- Rs 1,95,587
 - Rs 1,49,501
 - Rs 1,87,722
 - Rs 1,71,974

Solution: Given, P (First cost of machine) = 900000, F (Salvage value) = 150000, $i = 15\%$, $n = 10$
 $CR(i) = (P-F) (A/P, i, n) + Fi = (900000 - 150000) (A/P, 15, 10) + 150000 (0.15)$
 $= 750000 (0.1993) + 150000 (0.15)$
 $= 171974$ (Ans)

7. The element which is not involved while calculating equivalence of sums of money is
- Amount of sums
 - Times of occurrence of sum
 - Interest rate
 - Type of investment

Solution: Type of investment does not affect the equivalent value of sum of money.

8. Principle of equivalence states that actual interest rate earned is the one which sets

- Equivalent receipts equal to equivalent disbursements
- Equivalent receipts more than equivalent disbursements
- Equivalent receipts less than equivalent disbursements
- None of these

9. Future worth of payment series of Rs 10,000 at the end of each year for 5 years at 10% interest rate compounded annually will be

- 10000 (F/A, 10, 5)
- 10000 (F/A, 5, 10)
- 10000 (A/F, 10, 5)
- 10000 (A/F, 5, 10)

10. If you wish to withdraw Rs 50,000, Rs 80,000, Rs 1,10,000 and Rs 1,40,000 at the end of 2nd, 3rd, 4th and 5th year from now from a savings accounts which earns 8% interest rate compounded annually, the amount you should deposit now is

- $[50000 + 30000 (A/G, 8, 4)](P/A, 8, 5)(P/F, 8, 1)$
- $[50000 + 30000 (A/G, 8, 4)](P/A, 8, 4)(P/F, 8, 1)$
- $[50000 + 30000 (A/G, 8, 4)](A/P, 8, 5)(P/F, 8, 1)$
- $[50000 + 30000 (A/G, 8, 4)](A/P, 8, 4)(P/F, 8, 1)$