

# Facility location problem

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## Notations

$m$  = number of facilities, index:  $i = 0, 1, 2, \dots$

$n$  = number of customer nodes, index:  $j = 0, 1, 2, \dots$

$k$  = X and Y coordinates:  $(0, 1)$

$d_{jk}$  =  $k$  coordinate (X, Y) of customer  $j$

## Decision variables

$f_{ik}$  = coordinate  $k$  of facility  $i$

$x_{ij}$  = distance between facility  $i$  and customer  $j$

$y_{ij}$  = 1 if customer  $j$  is assigned to cluster of facility  $i$ , 0 otherwise

## Problem formulation

### objective function

$$\text{minimize: } \sum_{i,j} y_{ij} x_{ij} \quad (\text{non-linear}) \quad (1)$$

**s.t:**

$$\sum_j y_{ij} = 1 \quad \forall i \quad (2)$$

$$x_{ij} = \text{euclidean distance } (f_i, d_j) \quad \forall i, j \quad (3)$$

$$y_{ij} \in (0, 1) \quad (4)$$