

22/133-C

**B.C.A (Second Semester)****Examination, 2022****Paper: Fourth****(BCA-204)****Discrete Mathematics***Time : Three Hours / [ Maximum Marks : 70***Note :** Attempt all sections as per instructions.**Section-A****(Very Short Answer Type Questions)****Note :** Attempt all parts of this question.

1.5x10=15

1. (i) If  $A=\{1,2,3\}$ ,  $B=\{3,4,5\}$  and  $C=\{0,2,3\}$ , find  $(A \cap B) \times C$ .
- (ii) In a group of 850 persons, 600 can speak hindi and 340 can speak Tamil. Find how many can speak Hindi only?
- (iii) Define an abelian group.

**P.T.O.****(2)**

- (iv) Let  $A=\{1,2,3,4,6\}$ . Let  $R$  be the relation defined by  $R=\{(a,b) | a \in A, b \in A \text{ a divides b}\}$ . Write the elements of  $R$ .
- (v) Define Path and circuits.
- (vi) Define Bipartite graph.
- (vii) Explain De-Morgans Law
- (viii) Define equivalence relation.
- (ix) Define conjunction and Disjunction.
- (x) Define Radius and Diameter of a tree.

**Section-B****(Short Answer Type Questions)****Note :** Attempt all questions. 7x5=35

2. Prove that  $\{[(P \rightarrow q) \vee P] \wedge q\} \rightarrow q$  is a Tautology.

**OR**

Given the relation  $R=\{(1,1), (1,2), (2,1), (2,2), (3,3), (4,4)\}$  decide whether it is reflexive or symmetric or anti-symmetric or transitive.

3. Discuss Ford- Fulkerson algorithm for maximum flow problem.

**OR**

Explain Groups, Subgroups and Normal Subgroups.

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- (3)
4. Explain Predicate calculus with suitable example.

OR

Explain the following:

- (a) Hamiltonian graph
  - (b) Eulerian graph.
5. When it can be said that two graphs  $G_1$  and  $G_2$  are isomorphic?

OR

Explain Handshaking Lemma.

6. What is spanning tree? Prove that a simple graph has a spanning tree, iff it is connected.

OR

Let  $f(x)=x^2-1$  and  $g(x)=(3x+1)$ , describe

- (a)  $\text{gof}$
- (b)  $\text{fog}$
- (c)  $\text{fof}$

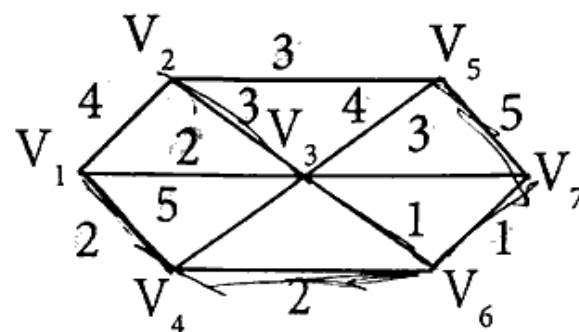
### Section-C

#### (Long Answer Type Questions)

**Note :** Attempt any **two** questions.  $10 \times 2 = 20$   
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(4)

7. Find the minimum spanning tree by Krushkal's algorithm.



8. State and prove Edmonds- Karp algorithm.
9. Show that the following argument is a valid argument.

$$\begin{array}{l}
 P \\
 q \\
 2P \rightarrow r \\
 q \rightarrow \sim r \\
 \hline
 \sim r
 \end{array}$$

10. Explain the concept of chinese Postman problem.
11. Write short notes on any two of the following:
- (a) Logarithmic function
  - (b) Short Path problem
  - (c) Menger's theorem