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# **Polynomial Regression**

#### **About this Notebook**

In this notebook, we learn how to use scikit-learn for Polynomial regression. We download a dataset that is related to fuel consumption and Carbon dioxide emission of cars. Then, we split our data into training and test sets, create a model using training set, evaluate our model using test set, and finally use model to predict unknown value.

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### **Importing Needed packages**

```
In [15]: import matplotlib.pyplot as plt
   import pandas as pd
   import pylab as pl
   import numpy as np
   %matplotlib inline
```

## **Downloading Data**

To download the data, we will use !wget to download it from IBM Object Storage.

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## **Understanding the Data**

#### FuelConsumption.csv:

We have downloaded a fuel consumption dataset, FuelConsumption.csv, which contains model-specific fuel consumption ratings and estimated carbon dioxide emissions for new light-duty vehicles for retail sale in Canada. <a href="Dataset source">Dataset source (http://open.canada.ca/data/en/dataset/98f1a129-f628-4ce4-b24d-6f16bf24dd64)</a>

- MODELYEAR e.g. 2014
- MAKE e.g. Acura
- MODEL e.g. ILX
- VEHICLE CLASS e.g. SUV
- ENGINE SIZE e.g. 4.7
- **CYLINDERS** e.g 6
- TRANSMISSION e.g. A6
- FUEL CONSUMPTION in CITY(L/100 km) e.g. 9.9
- FUEL CONSUMPTION in HWY (L/100 km) e.g. 8.9
- FUEL CONSUMPTION COMB (L/100 km) e.g. 9.2
- CO2 EMISSIONS (g/km) e.g. 182 --> low --> 0

## Reading the data in

```
In [17]: df = pd.read_csv("FuelConsumption.csv")
# take a look at the dataset
df.head()
```

Out[17]:

	MODELYEAR	MAKE	MODEL	VEHICLECLASS	ENGINESIZE	CYLINDERS	TRANSMISSION	FUELTYPE	FU
0	2014	ACURA	ILX	COMPACT	2.0	4	AS5	Z	
1	2014	ACURA	ILX	COMPACT	2.4	4	M6	Z	
2	2014	ACURA	ILX HYBRID	COMPACT	1.5	4	AV7	Z	
3	2014	ACURA	MDX 4WD	SUV - SMALL	3.5	6	AS6	Z	
4	2014	ACURA	RDX AWD	SUV - SMALL	3.5	6	AS6	Z	

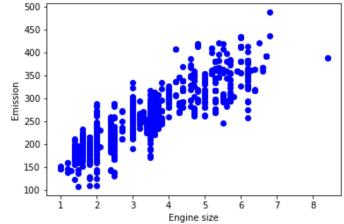
Lets select some features that we want to use for regression.

#### Out[18]:

	ENGINESIZE	CYLINDERS	FUELCONSUMPTION_COMB	CO2EMISSIONS
0	2.0	4	8.5	196
1	2.4	4	9.6	221
2	1.5	4	5.9	136
3	3.5	6	11.1	255
4	3.5	6	10.6	244
5	3.5	6	10.0	230
6	3.5	6	10.1	232
7	3.7	6	11.1	255
8	3.7	6	11.6	267

Lets plot Emission values with respect to Engine size:

```
In [19]: plt.scatter(cdf.ENGINESIZE, cdf.CO2EMISSIONS, color='blue')
    plt.xlabel("Engine size")
    plt.ylabel("Emission")
    plt.show()
```



#### Creating train and test dataset

Train/Test Split involves splitting the dataset into training and testing sets respectively, which are mutually exclusive. After which, you train with the training set and test with the testing set.

```
In [20]: msk = np.random.rand(len(df)) < 0.8
    train = cdf[msk]
    test = cdf[~msk]</pre>
```

## Polynomial regression

Sometimes, the trend of data is not really linear, and looks curvy. In this case we can use Polynomial regression methods. In fact, many different regressions exist that can be used to fit whatever the dataset looks like, such as quadratic, cubic, and so on, and it can go on and on to infinite degrees.

In essence, we can call all of these, polynomial regression, where the relationship between the independent variable x and the dependent variable y is modeled as an nth degree polynomial in x. Lets say you want to have a polynomial regression (let's make 2 degree polynomial):

$$y = b + \theta_1 x + \theta_2 x^2$$

Now, the question is: how we can fit our data on this equation while we have only x values, such as **Engine Size**? Well, we can create a few additional features: 1, x, and  $x^2$ .

**PloynomialFeatures()** function in Scikit-learn library, drives a new feature sets from the original feature set. That is, a matrix will be generated consisting of all polynomial combinations of the features with degree less than or equal to the specified degree. For example, lets say the original feature set has only one feature, *ENGINESIZE*. Now, if we select the degree of the polynomial to be 2, then it generates 3 features, degree=0, degree=1 and degree=2:

**fit\_transform** takes our x values, and output a list of our data raised from power of 0 to power of 2 (since we set the degree of our polynomial to 2).

$$egin{bmatrix} v_1 \ v_2 \ dots \ v_n \end{bmatrix} \longrightarrow egin{bmatrix} [1 & v_1 & v_1^2] \ [1 & v_2 & v_2^2] \ dots & dots & dots \ [1 & v_n & v_n^2] \end{bmatrix}$$

in our example

$$\begin{bmatrix} 2. \\ 2.4 \\ 1.5 \\ \vdots \end{bmatrix} \longrightarrow \begin{bmatrix} [1 & 2. & 4.] \\ [1 & 2.4 & 5.76] \\ [1 & 1.5 & 2.25] \\ \vdots & \vdots & \vdots \end{bmatrix}$$

It looks like feature sets for multiple linear regression analysis, right? Yes. It Does. Indeed, Polynomial regression is a special case of linear regression, with the main idea of how do you select your features. Just consider replacing the x with  $x_1$ ,  $x_1^2$  with  $x_2$ , and so on. Then the degree 2 equation would be turn into:

$$y = b + \theta_1 x_1 + \theta_2 x_2$$

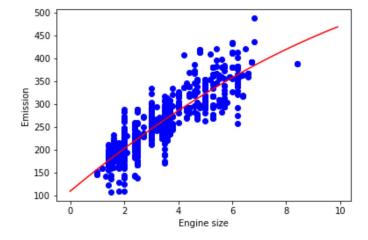
Now, we can deal with it as 'linear regression' problem. Therefore, this polynomial regression is considered to be a special case of traditional multiple linear regression. So, you can use the same mechanism as linear regression to solve such a problems.

so we can use LinearRegression() function to solve it:

As mentioned before, **Coefficient** and **Intercept**, are the parameters of the fit curvy line. Given that it is a typical multiple linear regression, with 3 parameters, and knowing that the parameters are the intercept and coefficients of hyperplane, sklearn has estimated them from our new set of feature sets. Lets plot it:

```
In [23]: plt.scatter(train.ENGINESIZE, train.CO2EMISSIONS, color='blue')
    XX = np.arange(0.0, 10.0, 0.1)
    yy = clf.intercept_[0]+ clf.coef_[0][1]*XX+ clf.coef_[0][2]*np.power(XX, 2)
    plt.plot(XX, yy, '-r')
    plt.xlabel("Engine size")
    plt.ylabel("Emission")
```

Out[23]: Text(0, 0.5, 'Emission')



#### **Evaluation**

```
In [24]: from sklearn.metrics import r2_score

    test_x_poly = poly.fit_transform(test_x)
    test_y_ = clf.predict(test_x_poly)

print("Mean absolute error: %.2f" % np.mean(np.absolute(test_y_ - test_y)))
    print("Residual sum of squares (MSE): %.2f" % np.mean((test_y_ - test_y) ** 2))
    print("R2-score: %.2f" % r2_score(test_y_ , test_y) )

Mean absolute error: 24.13
    Residual sum of squares (MSE): 1022.11
    R2-score: 0.67
```

### **Practice**

Try to use a polynomial regression with the dataset but this time with degree three (cubic). Does it result in better accuracy?

```
In [27]: # write your code hereDouble-click
                                                                                                                                 here for the solution.
                          poly3 = PolynomialFeatures(degree=3)
                          train_x_poly3 = poly3.fit_transform(train_x)
                          clf3 = linear model.LinearRegression()
                          train y3 = clf3.fit(train_x_poly3, train_y)
                           # The coefficients
                          print ('Coefficients: ', clf3.coef_)
                          print ('Intercept: ',clf3.intercept )
                          plt.scatter(train.ENGINESIZE, train.CO2EMISSIONS, color='blue')
                          XX = np.arange(0.0, 10.0, 0.1)
                          yy = clf3.intercept_[0] + clf3.coef_[0][1]*XX + clf3.coef_[0][2]*np.power(XX, 2) + c
                          lf3.coef [0][3]*np.power(XX, 3)
                          plt.plot(XX, yy, '-r')
                          plt.xlabel("Engine size")
                          plt.ylabel("Emission")
                          test_x_poly3 = poly3.fit_transform(test_x)
                          test_y3_ = clf3.predict(test_x_poly3)
                          print("Mean absolute error: %.2f" % np.mean(np.absolute(test_y3_ - test_y)))
                          print("Residual sum of squares (MSE): %.2f" % np.mean((test_y3_ - test_y) ** 2))
                          print("R2-score: %.2f" % r2_score(test_y3_ , test_y) )
                          Coefficients: [[ 0.
                                                                                                            28.86973273 4.28924254 -0.46161503]]
                          Intercept: [131.202534]
                          Mean absolute error: 24.18
                          Residual sum of squares (MSE): 1019.84
                          R2-score: 0.68
                                 500
                                 450
                                 400
                                 350
                            Emission
                                 300
                                 250
                                 200
                                 150
                                 100
                                                                                                                                 8
                                                                                                                                                     10
                                                                                         Engine size
```

Double-click here for the solution.

#### Want to learn more?

IBM SPSS Modeler is a comprehensive analytics platform that has many machine learning algorithms. It has been designed to bring predictive intelligence to decisions made by individuals, by groups, by systems – by your enterprise as a whole. A free trial is available through this course, available here: SPSS Modeler (http://cocl.us/ML0101EN-SPSSModeler)

Also, you can use Watson Studio to run these notebooks faster with bigger datasets. Watson Studio is IBM's leading cloud solution for data scientists, built by data scientists. With Jupyter notebooks, RStudio, Apache Spark and popular libraries prepackaged in the cloud, Watson Studio enables data scientists to collaborate on their projects without having to install anything. Join the fast-growing community of Watson Studio users today with a free account at <a href="Watson Studio">Watson Studio</a> (https://cocl.us <a href="ML0101EN\_DSX">/ML0101EN\_DSX</a>)

### Thanks for completing this lesson!

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