

WISSENAIRE (Maths Olympiad)

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① Given, $(\sqrt{8} + i)^{50} = 3^{49}(a + ib)$

Taking modulus on both sides,

$$(\sqrt{8+1})^{50} = 3^{49}(\sqrt{a^2+b^2})$$

Squaring on both sides.

$$9^{50} = (3^{49})^2 (a^2 + b^2)$$

$$\boxed{a^2 + b^2 = 9}$$

\therefore Required answer: $a^2 + b^2 = 9$.