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Chapter 3: Histogram and Point Operations

Histogram calculation

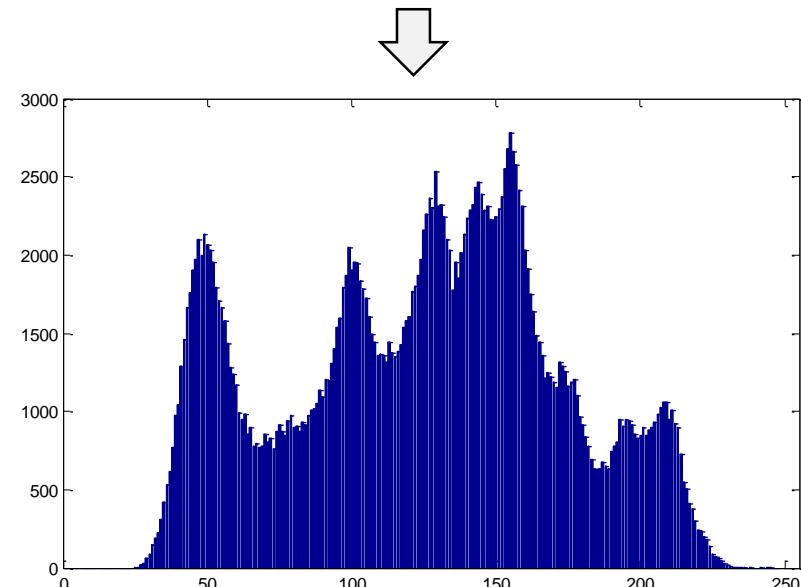
- Each pixel represents a quantized measurement of the intensity
- The Histogram is a vector, which contains one element of each quantization level
 - N-bit resolution $\rightarrow 2^N$ quantization levels $\rightarrow K=2^N$ histogram elements
 - E.g. 8-bit $\rightarrow K=2^8=256$ entries
- Each element contains the number of pixels whose value corresponds to the index of the element
- Example: calculation of a histogram in MATLAB:

```
% read image
I = imread('image.bmp');
[rows cols] = size(I);

% initialize histogram with zeros
h = zeros(256,1);

% iterate over all pixels
for n = 1:rows
    for m = 1:cols
        % increment histogram value at index I(n,m)
        h(I(n,m)+1) = h(I(n,m)+1) + 1;
    end
end

% show histogram
bar(h);
```



Mean value (expectation value)

- Provides information about the brightness of the image

Calculation from the histogram: $\mu = \sum_{i_{\min}}^{i_{\max}} i \cdot h_n(i)$

Calculation from the image: $\mu = \frac{1}{M \cdot N} \sum_{m=0}^{M-1} \sum_{n=0}^{N-1} I(n, m)$

Variance

- Provides information about the dispersion of the values

Calculation from the histogram: $\sigma^2 = \sum_{i_{\min}}^{i_{\max}} (i - \mu)^2 \cdot h_n(i)$

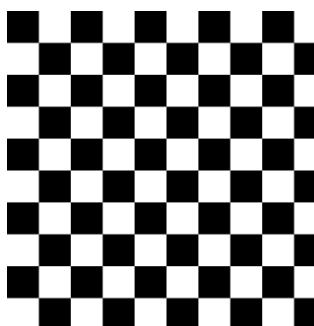
Calculation from the image: $\sigma^2 = \frac{1}{M \cdot N} \sum_{m=0}^{M-1} \sum_{n=0}^{N-1} I^2(n, m) - \mu^2$

Examples:



$$\mu = 127$$

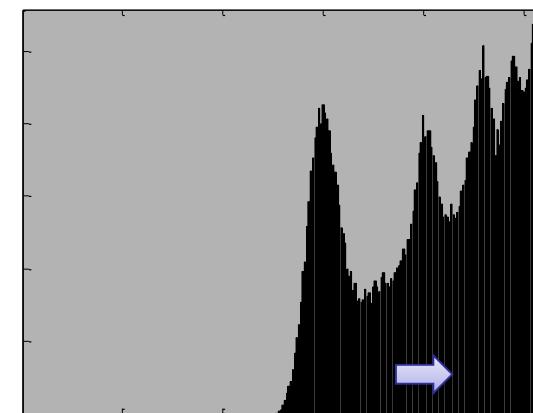
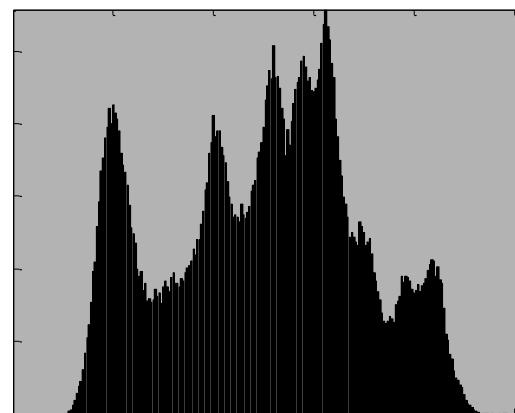
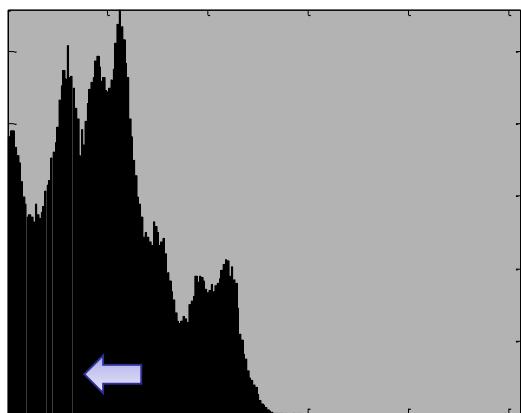
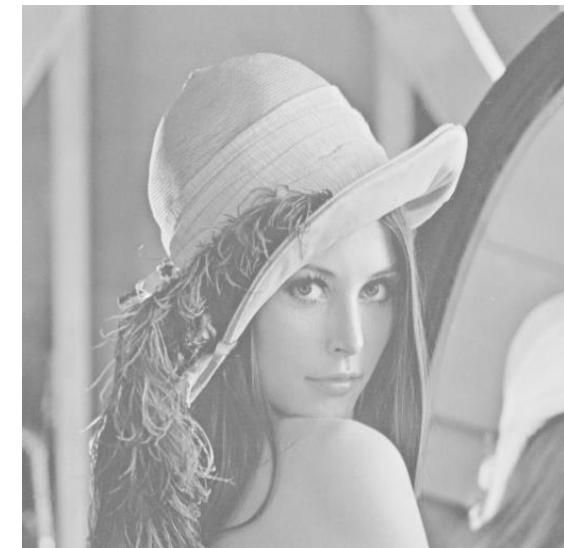
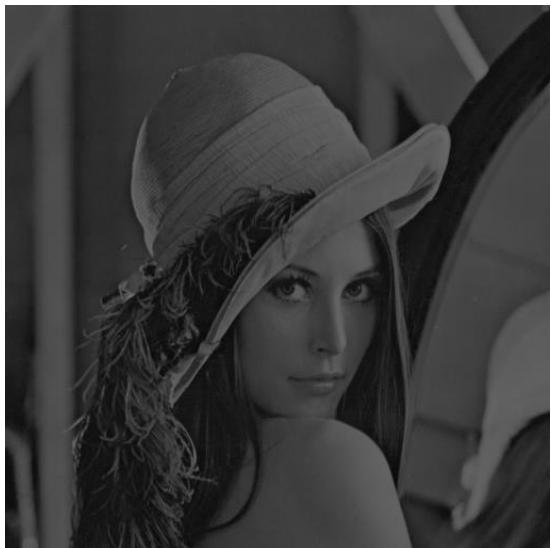
$$\sigma^2 = 0$$



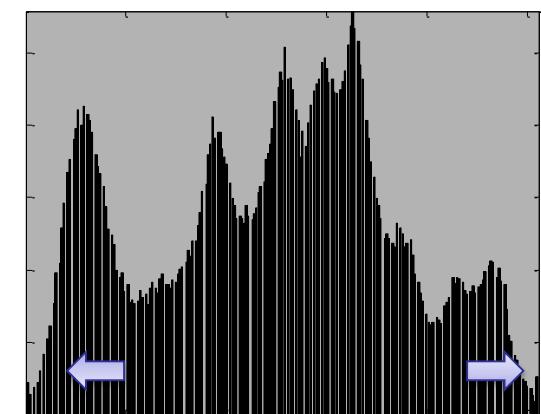
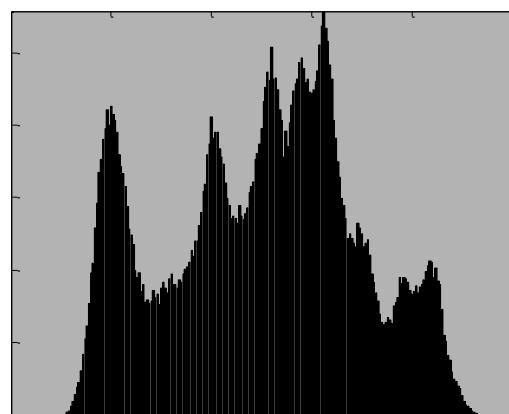
$$\mu = 127,5$$

$$\sigma^2 = 127,5^2 = 16256,25$$

Examples: Brightness



Examples: Contrast



Examples: Quantization noise

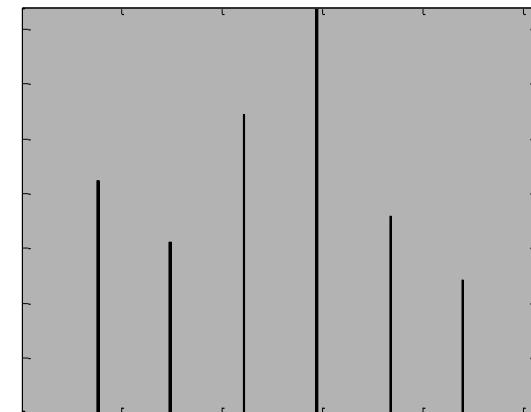
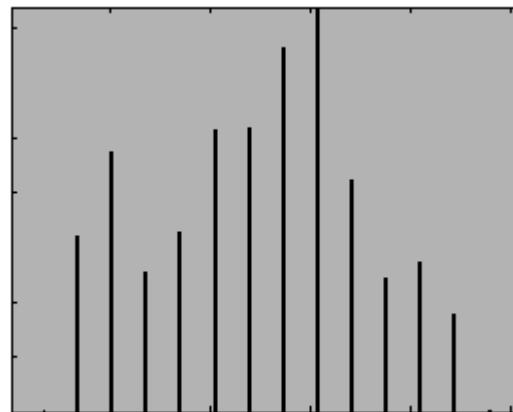
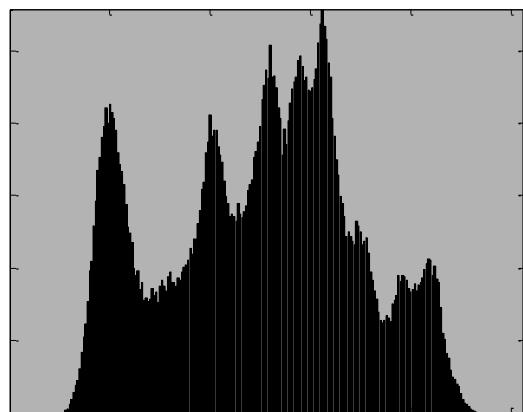
Original: 8-bit



Quantized: 4-bit



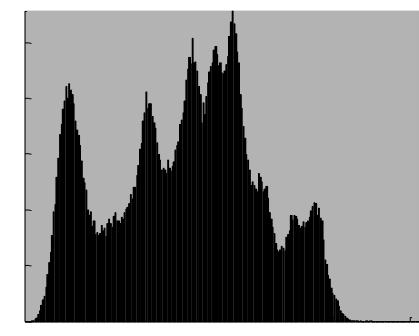
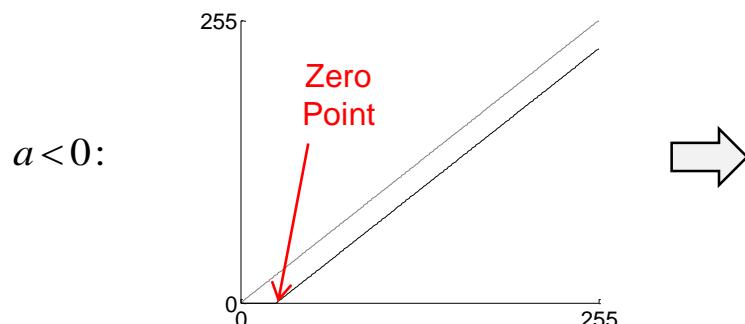
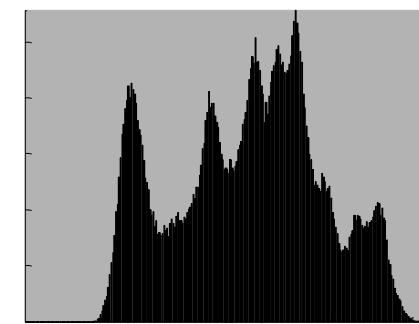
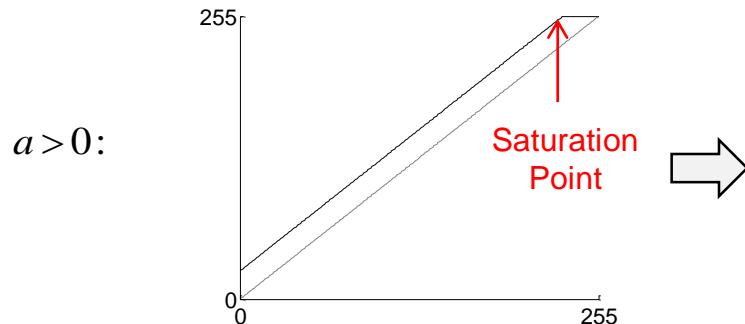
Quantized: 3-bit



Brightness Adjustment

$$f(m, n) = I(m, n) + a \quad a \in [-255, 255]$$

$$J(m, n) = \begin{cases} f(m, n), & \text{if } 0 \leq f(m, n) \leq 255 \\ 0, & \text{if } f(m, n) < 0 \\ 255, & \text{if } f(m, n) > 255 \end{cases}$$

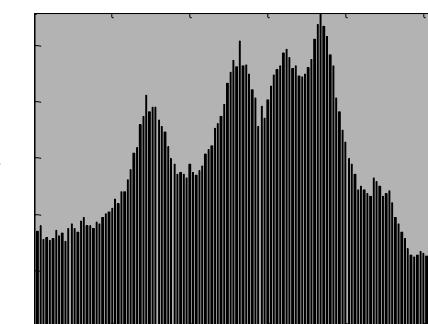
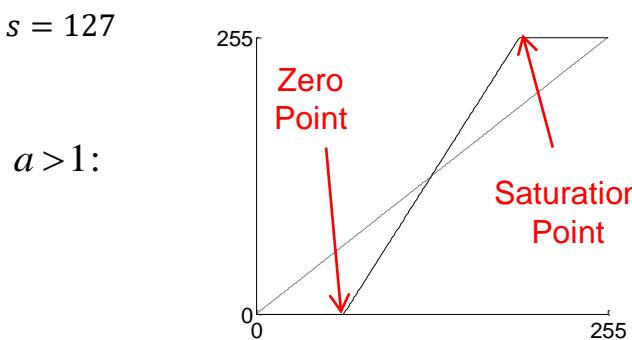
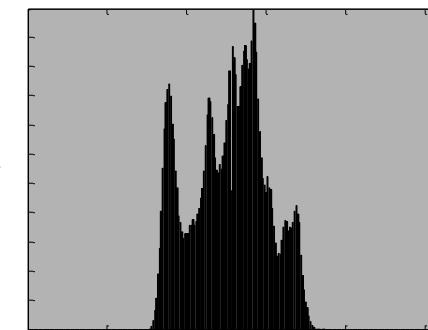
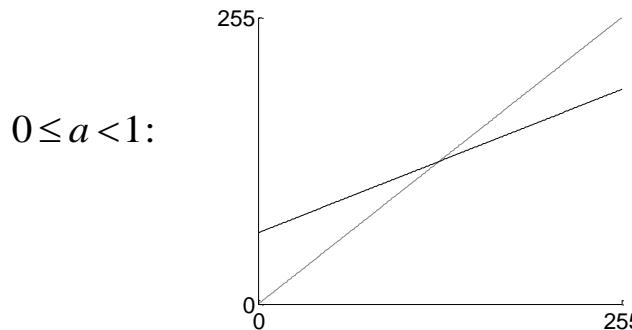


Contrast Adjustment

$$f(m, n) = a(I(m, n) - s) + s \quad a, s \in [0, 255]$$

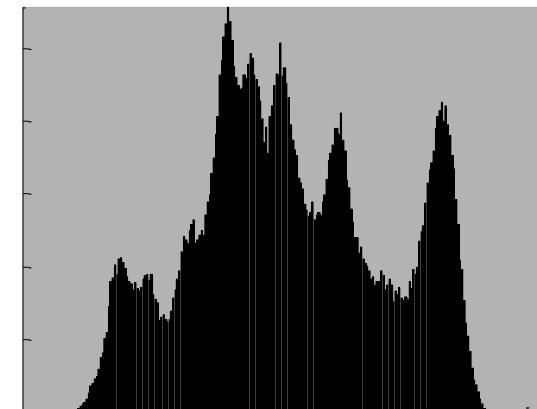
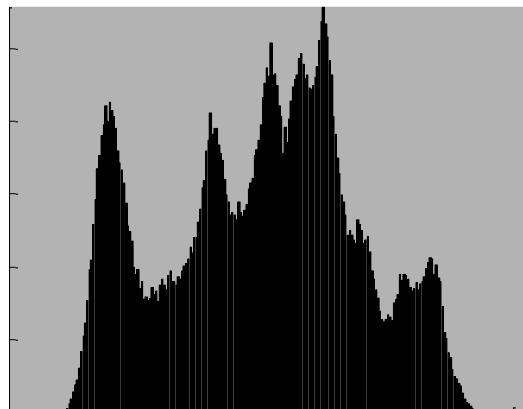
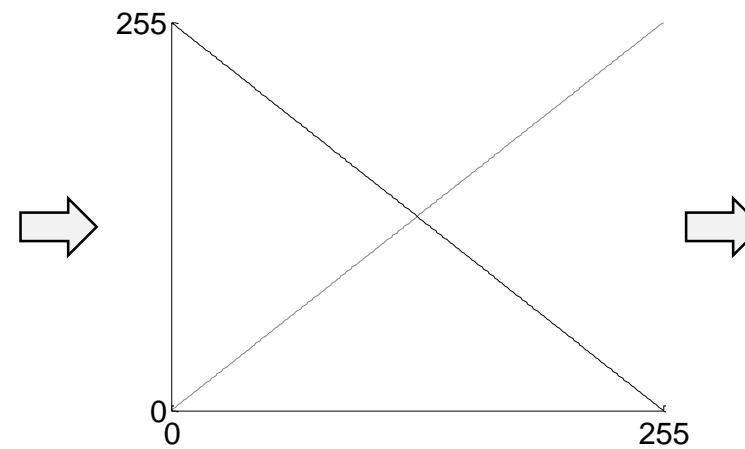
$$J(m, n) = \begin{cases} f(m, n), & \text{if } 0 \leq f(m, n) \leq 255 \\ 0, & \text{if } f(m, n) < 0 \\ 255, & \text{if } f(m, n) > 255 \end{cases}$$

s is the center of the contrast function,
e.g. $s = 127$



Inversion

$$J(m, n) = 255 - I(m, n)$$



Binning (quantization)

- Images with a high bit depth would generate huge histograms
 - Example: 14-bit $\rightarrow K=2^{14}=16384$ histogram entries
- To reduce the size of the histogram, binning can be done
- The intensity values are counted in B intervals (bins) $[i_j, i_{j+1})$
- For equally sized bins, the interval size is $k_B=K/B$
- The bin index can be calculated with $j = \left\lfloor I(m, n) \frac{B}{K} \right\rfloor$

Example: 14-bit image, histogram with 256 bins

$$\begin{array}{llll} h(0) & \leftarrow 0 & \leq I(n, m) < & 64 \\ h(1) & \leftarrow 64 & \leq I(n, m) < & 128 \\ \vdots & \leftarrow \vdots & \leq I(n, m) < & \vdots \\ h(j) & \leftarrow i_j & \leq I(n, m) < & i_{j+1} \\ \vdots & \leftarrow \vdots & \leq I(n, m) < & \vdots \\ h(255) & \leftarrow 16320 & \leq I(n, m) < & 16384 \end{array}$$

Third exercise

- Implement histogram calculation and some point operations

Expected Output (3 of 6)

Adjusted Brightness



Quantized



Inverted

