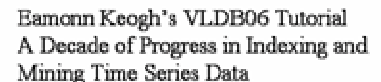


# Slides from Keogh Eamonn's tutorial:



# Outline of Tutorial

- Introduction, Motivation
- The Utility of Similarity Measurements

- Properties of distance measures
- The Euclidean distance
- Preprocessing the data
- Dynamic Time Warping
- Uniform Scaling



## ~~• Indexing Time Series~~

~~Spatial Access Methods and the curse of dimensionality~~

- ~~• The GEMINI Framework~~
- ~~• Dimensionality reduction~~
  - ~~• Discrete Fourier Transform~~
  - ~~• Discrete Wavelet Transform~~
  - ~~• Singular Value Decomposition~~
  - ~~• Piecewise Linear Approximation~~
  - ~~• Symbolic Approximation~~
  - ~~• Piecewise Aggregate Approximation~~
  - ~~• Adaptive Piecewise Constant Approximation~~

- ~~• Empirical Comparison~~

## • Data Mining

- Anomaly/Interestingness detection
- Motif (repeated pattern) discovery
- ~~• Visualization/Summarization~~
- ~~• What we should be working on!~~

Summary, Conclusions



25.1750  
25.2250  
25.2500  
25.2500  
25.2750  
25.3250  
25.3500  
25.3500  
25.4000  
25.4000  
25.3250  
25.2250  
25.2000  
25.1750

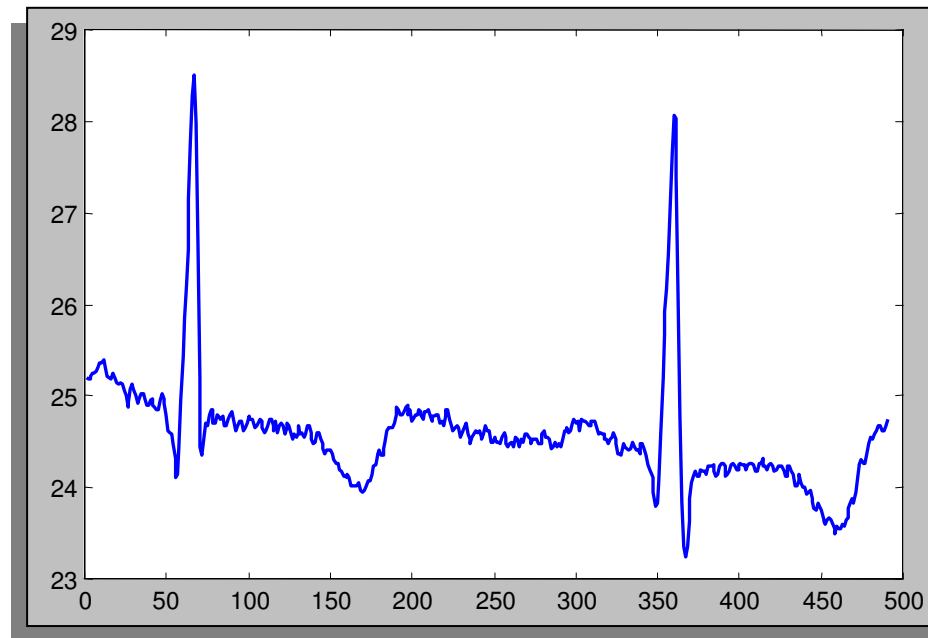
••

••

24.6250  
24.6750  
24.6750  
24.6250  
24.6250  
24.6250  
24.6750  
24.7500

# What are Time Series?

A time series is a collection of observations made sequentially in time.



Virtually all similarity measurements, indexing and dimensionality reduction techniques discussed in this tutorial can be used with other data types

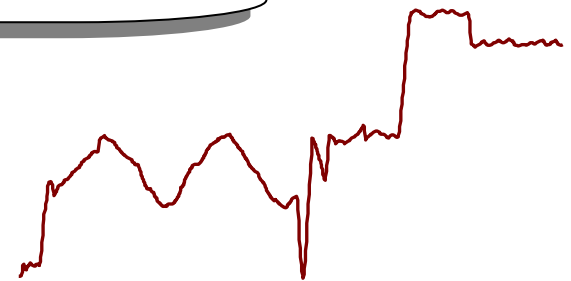
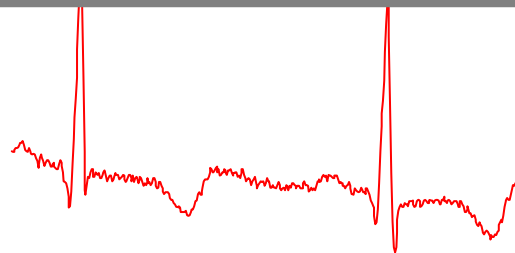
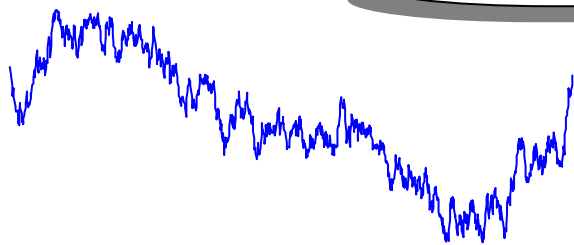


# Time Series are Ubiquitous! I

People measure things...

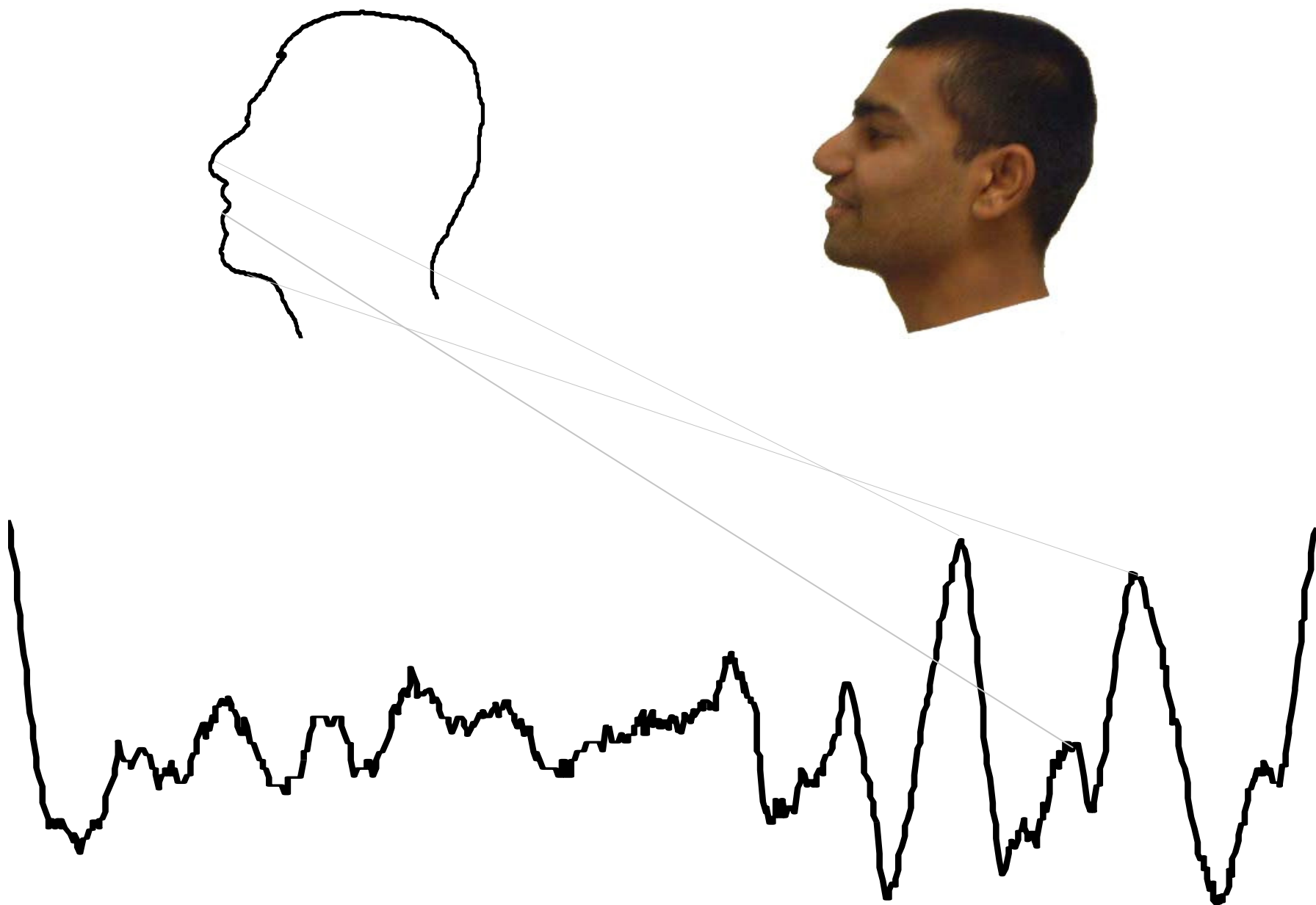
- *Their blood pressure*
- *George Bush's popularity rating*
- *The annual rainfall in Seattle*
- *The value of their Google stock*

...and things change over time...



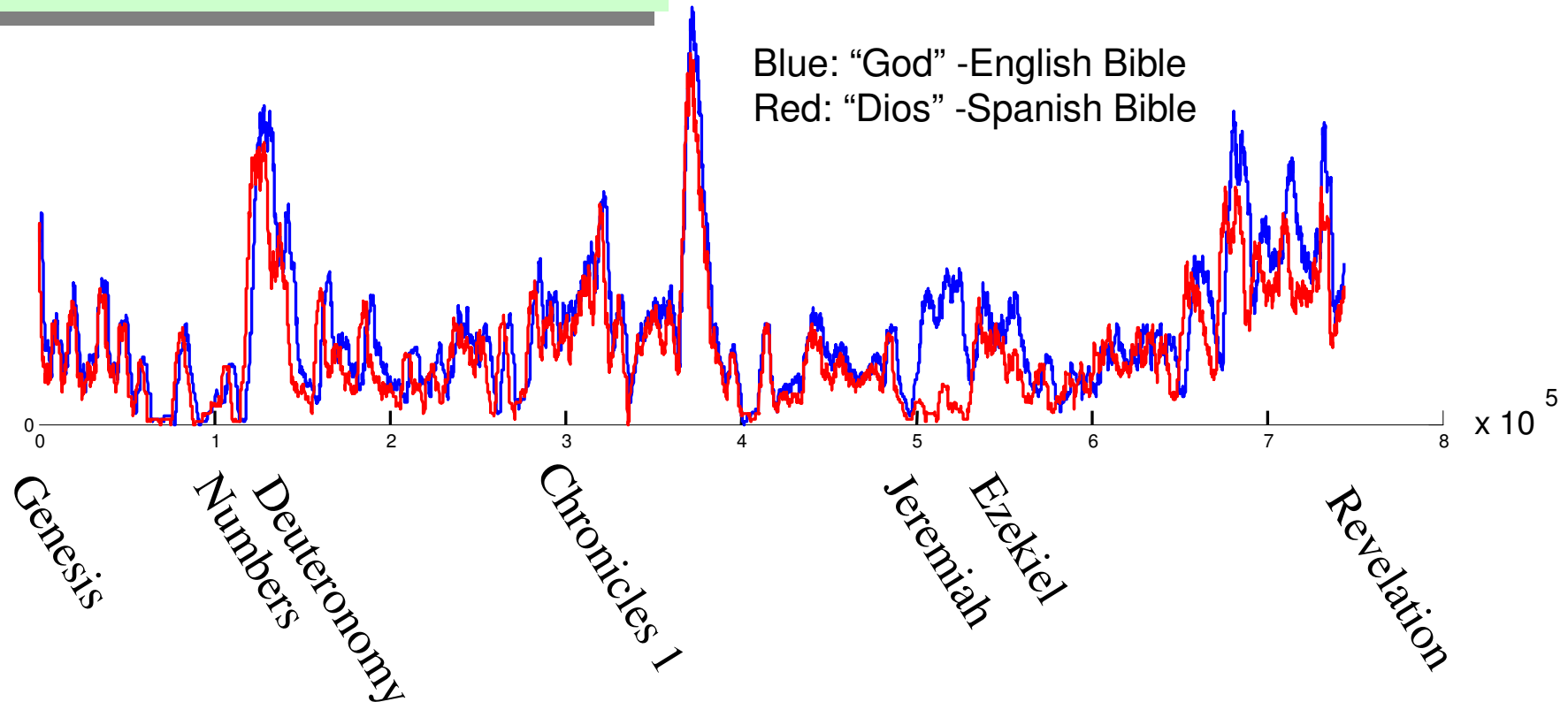
Thus time series occur in virtually every medical, scientific and businesses domain

Image data, may best be thought of as time series...



# Text data, may best be thought of as time series...

## The local frequency of words in the Bible



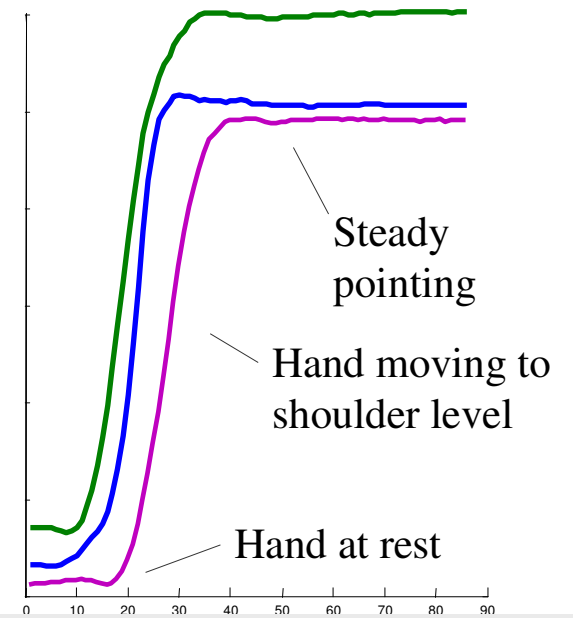
Gray: "El Senor" -Spanish Bible



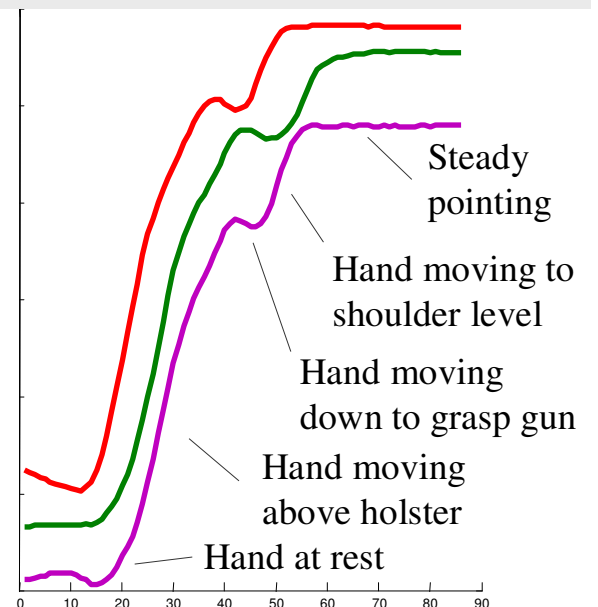
# Video data, may best be thought of as time series...



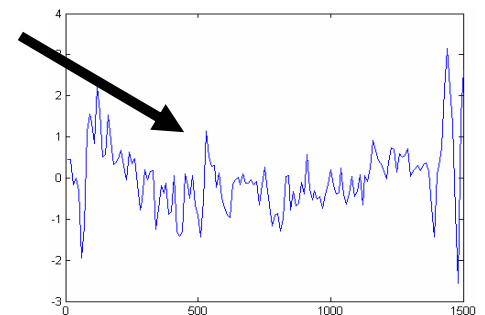
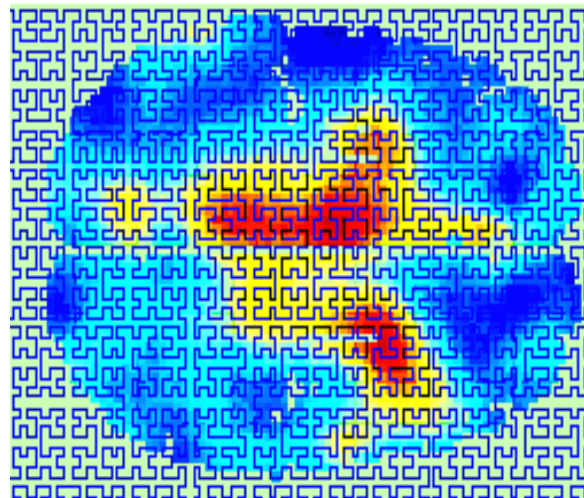
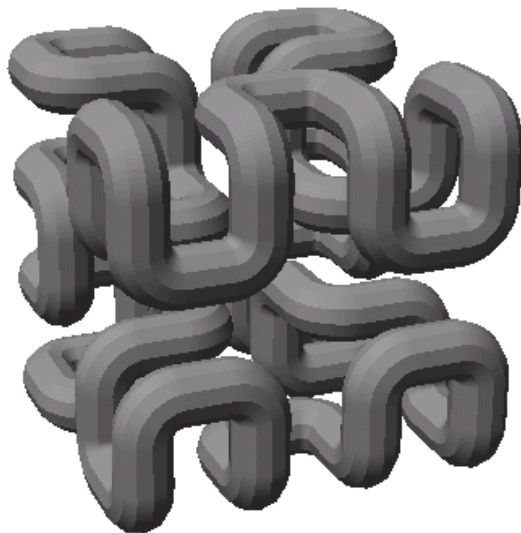
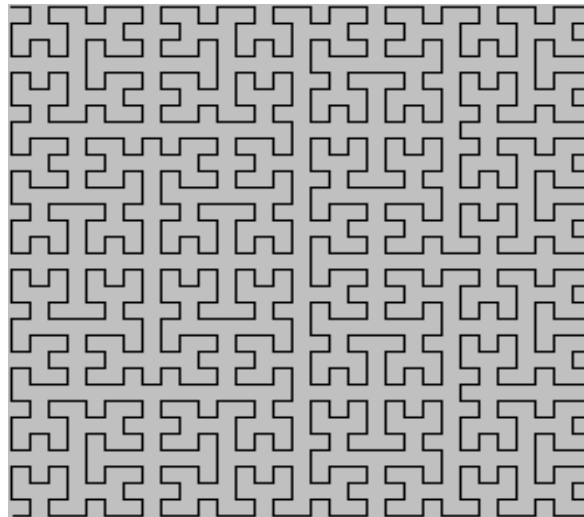
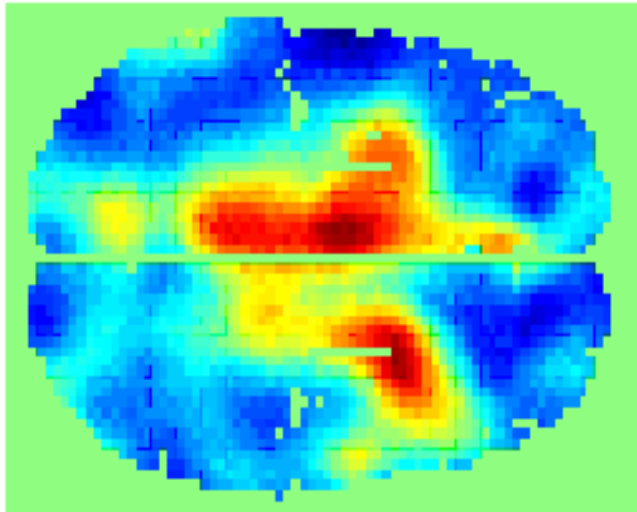
**Point**



**Gun-Draw**



Brain scans (3D voxels), may best be thought of as time series..





# Why is Working With Time Series so Difficult? Part I

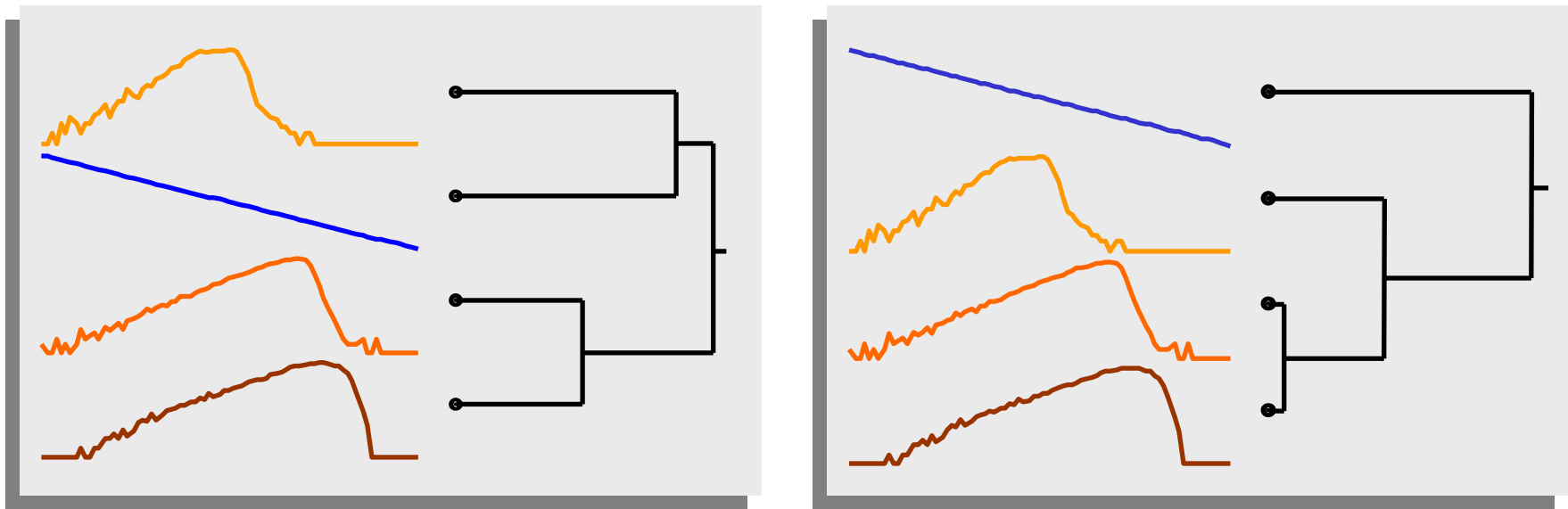
**Answer:** How do we work with very large databases?

- ◆ 1 Hour of EKG data: 1 Gigabyte.
- ◆ Typical Weblog: 5 Gigabytes per week.
- ◆ Space Shuttle Database: 200 Gigabytes and growing.
- ◆ Macho Database: 3 Terabytes, updated with 3 gigabytes a day.

Since most of the data lives on disk (or tape), we need a representation of the data we can efficiently manipulate.

# Why is Working With Time Series so Difficult? Part II

**Answer:** We are dealing with subjectivity



The definition of similarity depends on the user, the domain and the task at hand. We need to be able to handle this subjectivity.

# Why is working with time series so difficult? Part III

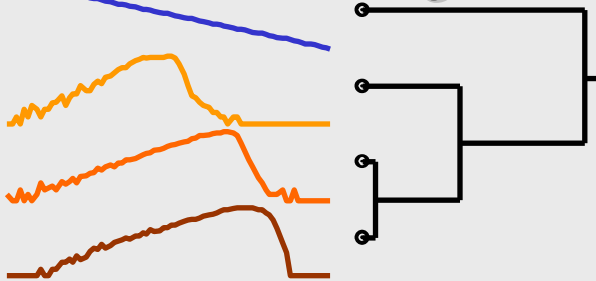
**Answer:** Miscellaneous data handling problems.

- Differing data formats.
- Differing sampling rates.
- Noise, missing values, etc.

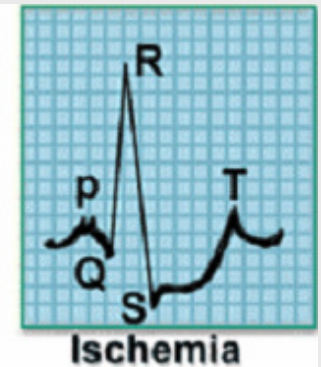
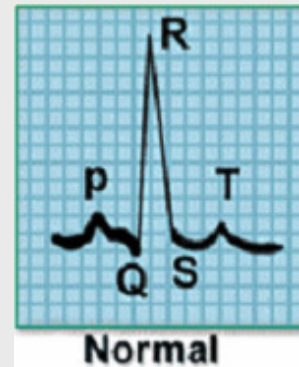
We will not focus on these issues in this tutorial.

# What do we want to do with the time series data?

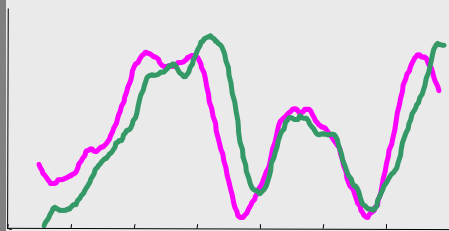
## Clustering



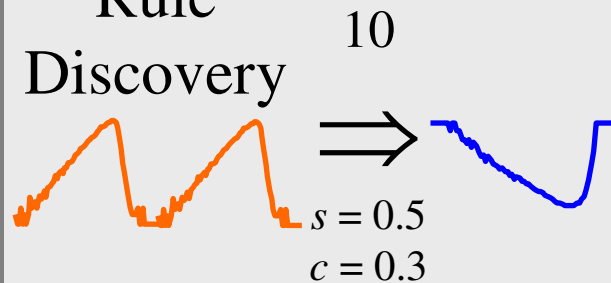
## Classification



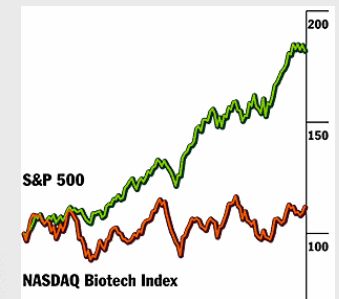
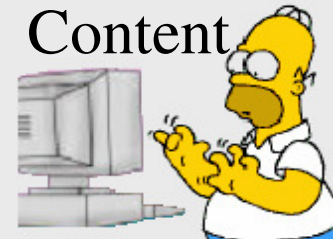
## Motif Discovery



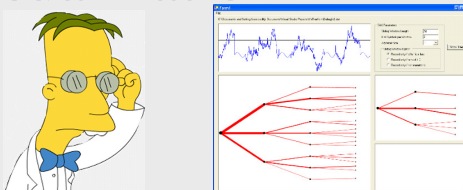
## Rule Discovery



## Query by Content



## Visualization

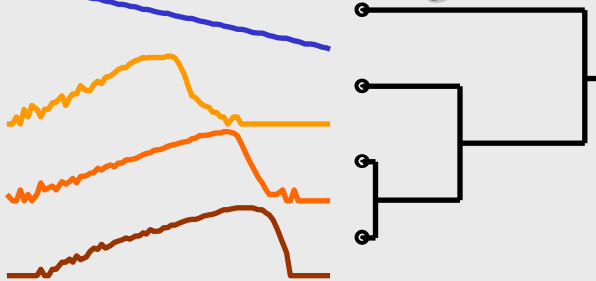


## Novelty Detection

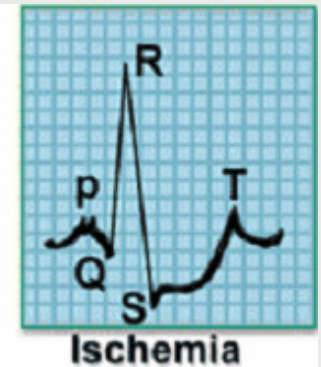
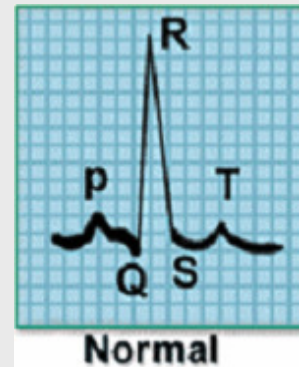


# All these problems require similarity matching

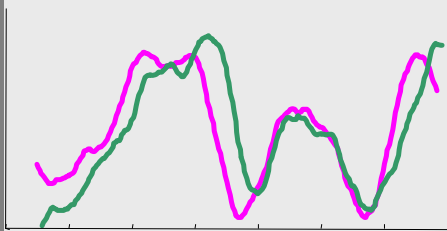
## Clustering



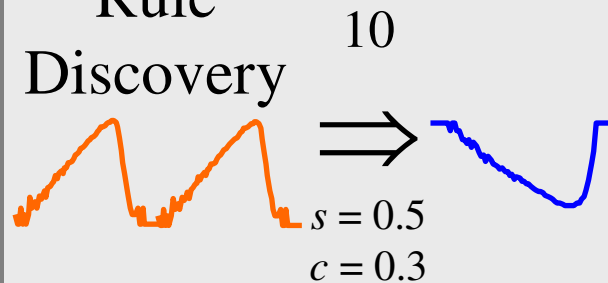
## Classification



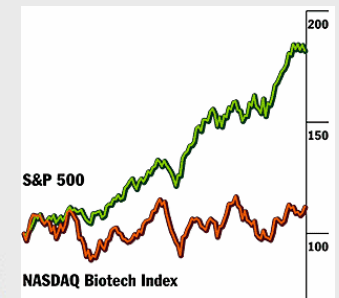
## Motif Discovery



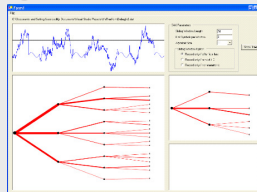
## Rule Discovery



## Query by Content



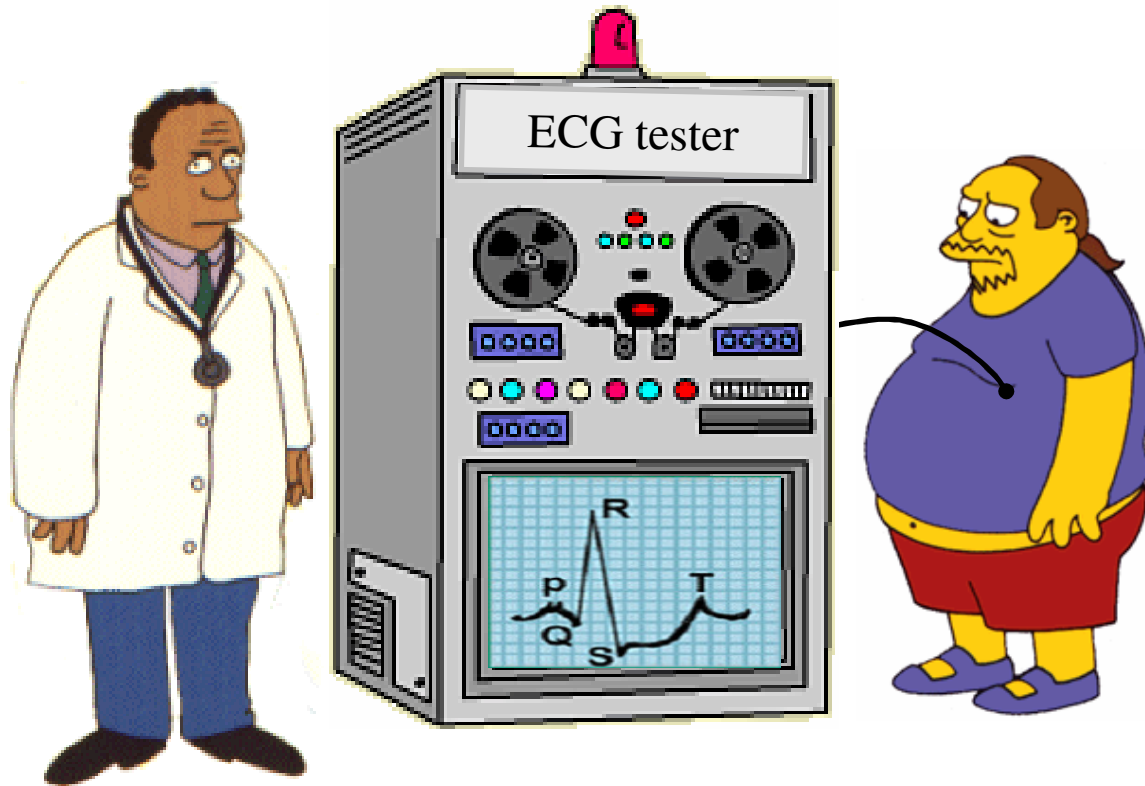
## Visualization



## Novelty Detection



Here is a simple motivation for the first part of the tutorial



You go to the doctor because of chest pains. Your ECG looks strange...

You doctor wants to search a database to find **similar** ECGs, in the hope that they will offer clues about your condition...

Two questions:

- **How do we define similar?**
- How do we search quickly?

# What is Similarity?

The quality or state of being similar; likeness; resemblance; as, a similarity of features. Webster's Dictionary



Similarity is hard to define, but...  
*"We know it when we see it"*

The real meaning of similarity is a philosophical question.

We will take a more pragmatic approach.

# Two Kinds of Similarity

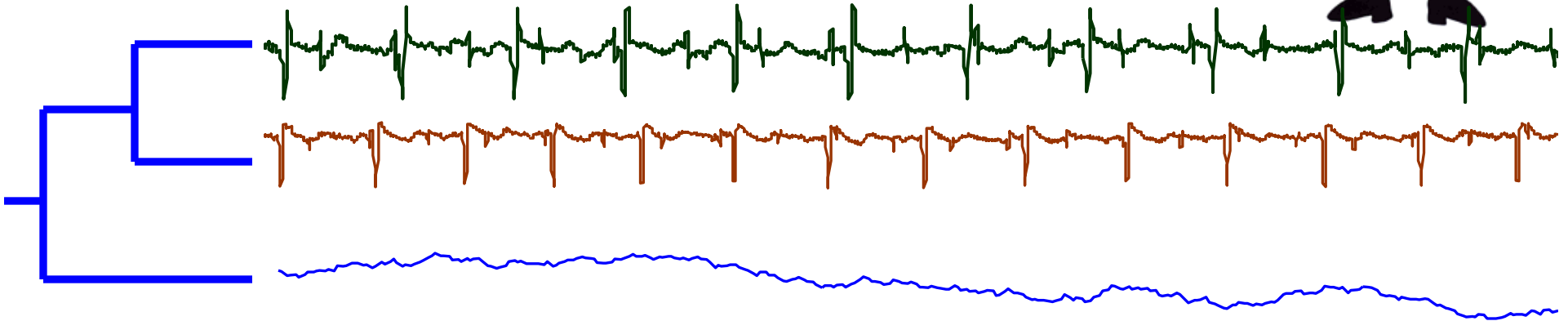
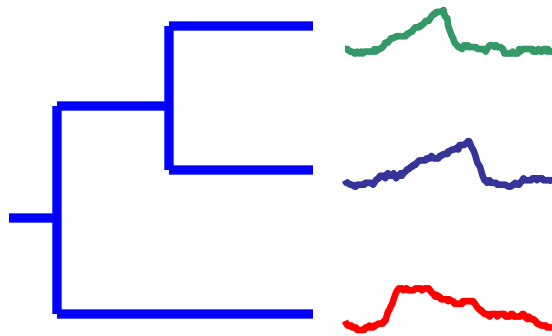
time series

Similarity at  
the level of  
*shape*

Next 40 minutes

Similarity at  
the *structural*  
level

Another 10 minutes





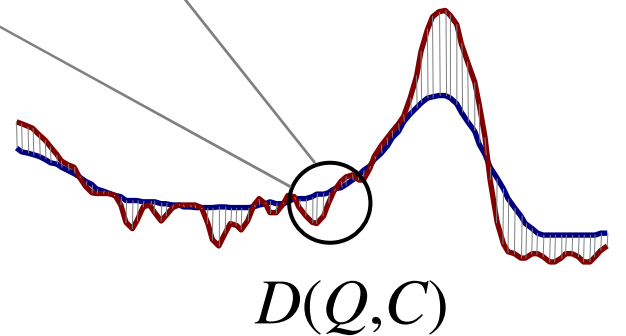
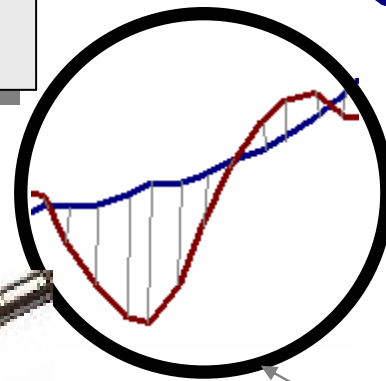
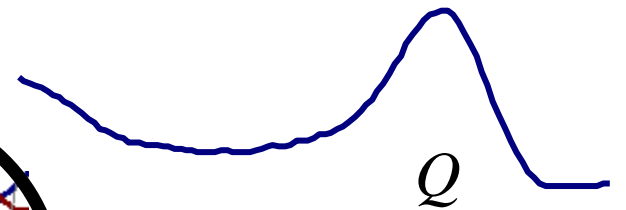
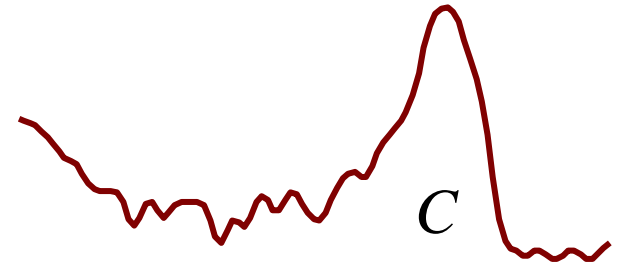
# Euclidean Distance Metric

Given two time series:

$$Q = q_1 \dots q_n$$

$$C = c_1 \dots c_n$$

$$D(Q, C) \equiv \sqrt{\sum_{i=1}^n (q_i - c_i)^2}$$



About 80% of published work in data mining uses Euclidean distance

# Preprocessing the data before distance calculations



If we naively try to measure the distance between two "raw" time series, we may get very unintuitive results

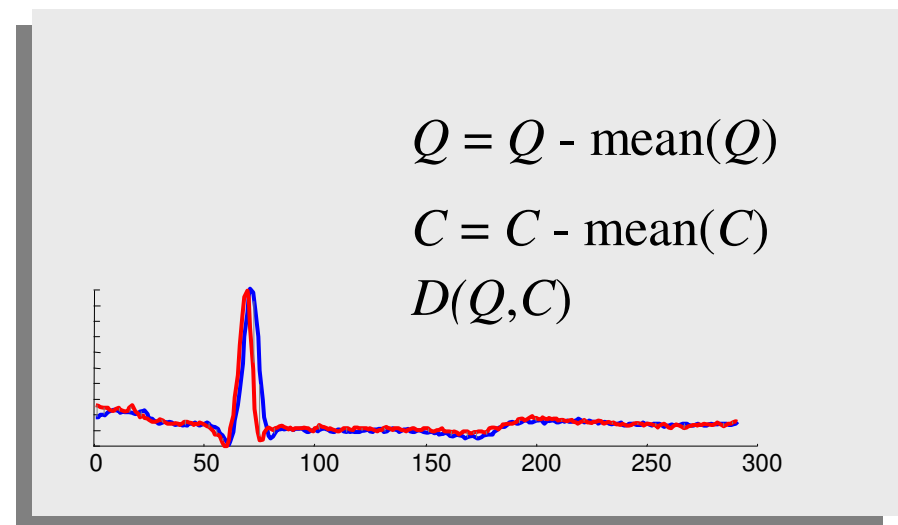
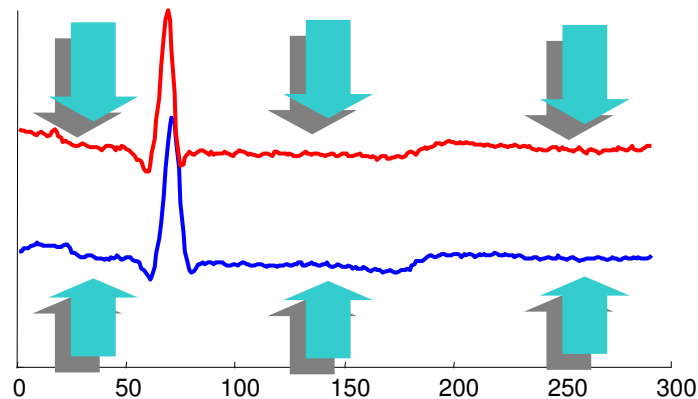
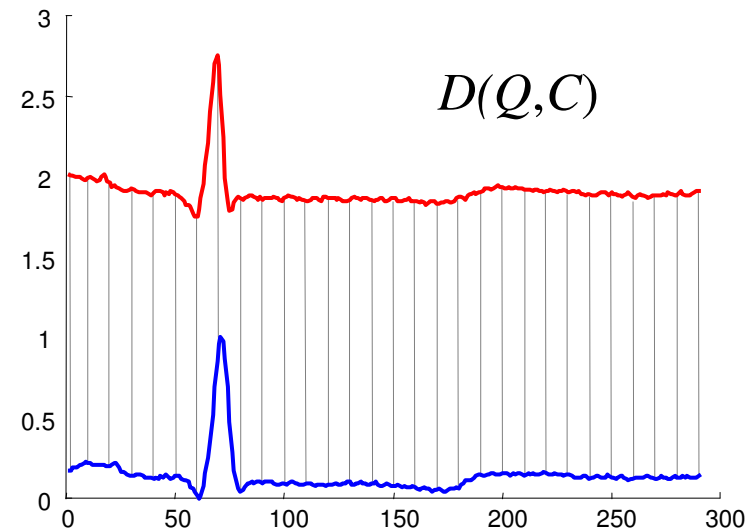
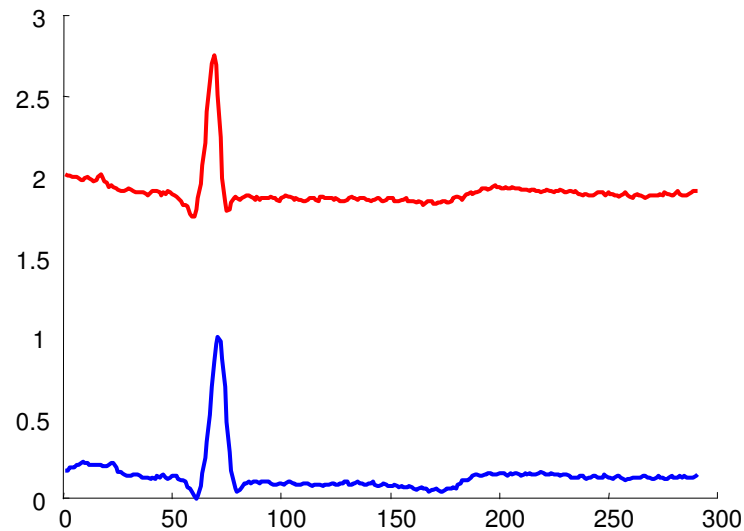
This is because Euclidean distance is very sensitive to some "distortions" in the data. For most problems these distortions are not meaningful, and thus we can and should remove them



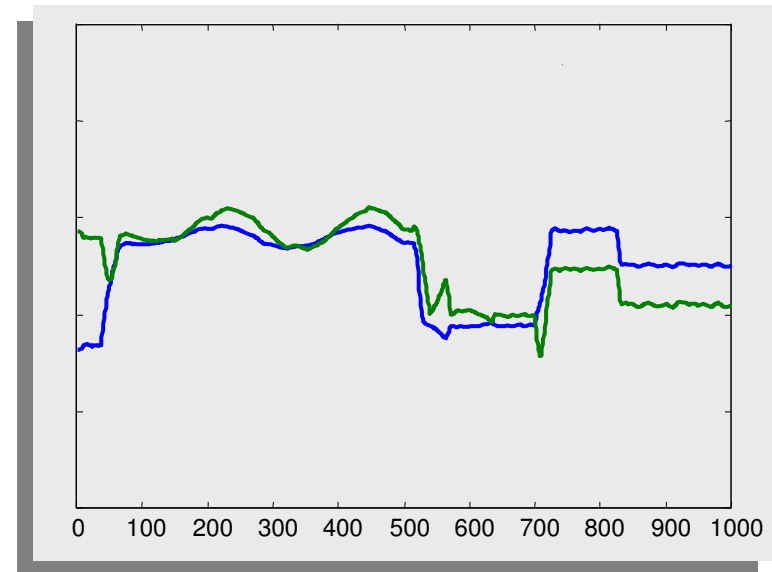
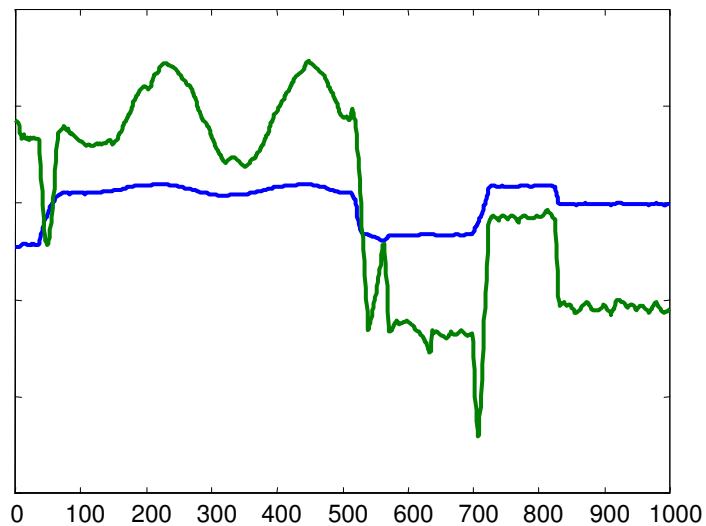
In the next few slides we will discuss the 4 most common distortions, and how to remove them

- Offset Translation
- Amplitude Scaling
- Linear Trend
- Noise

# Transformation I: Offset Translation



# Transformation II: Amplitude Scaling

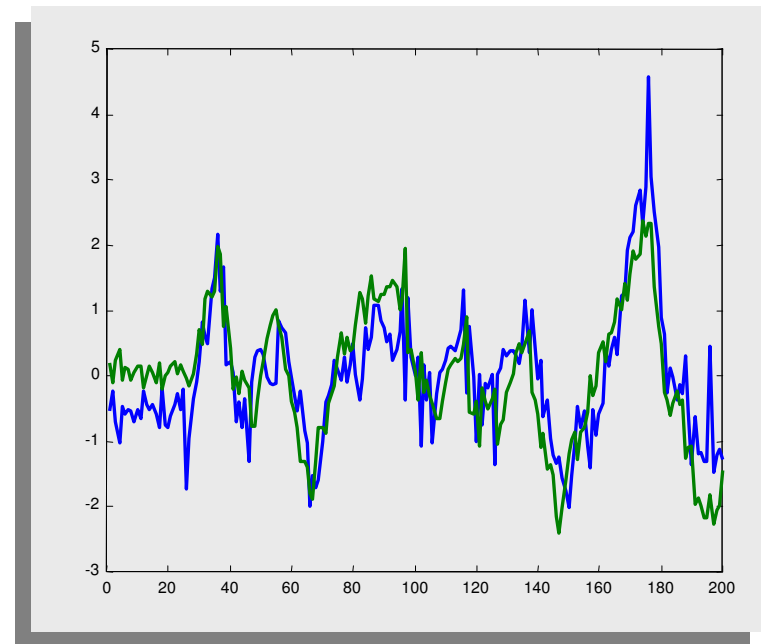
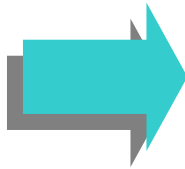
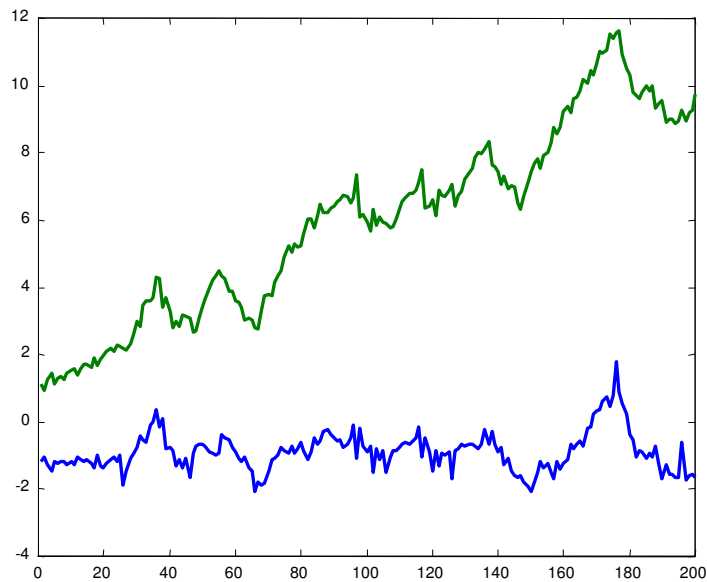


$$Q = (Q - \text{mean}(Q)) / \text{std}(Q)$$

$$C = (C - \text{mean}(C)) / \text{std}(C)$$

$$D(Q, C)$$

# Transformation III: Linear Trend



The intuition behind removing linear trend is...

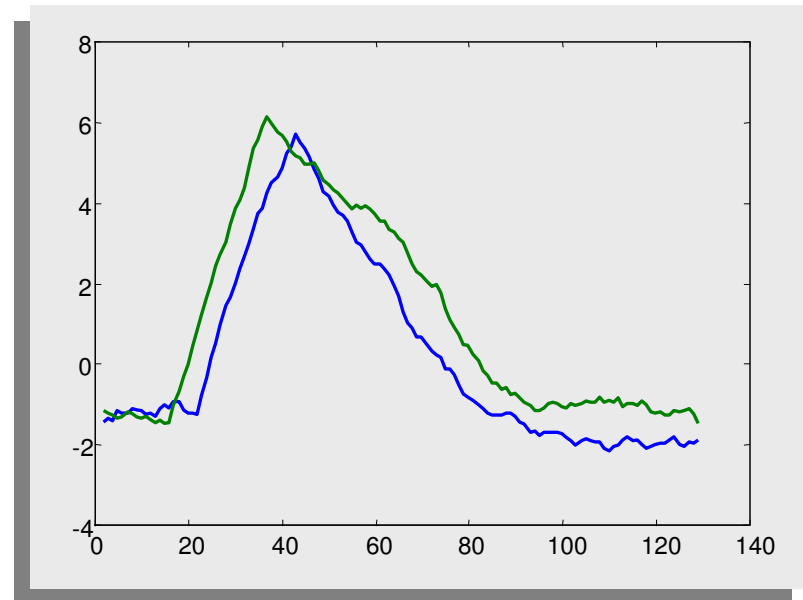
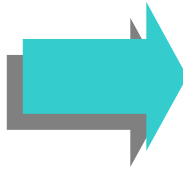
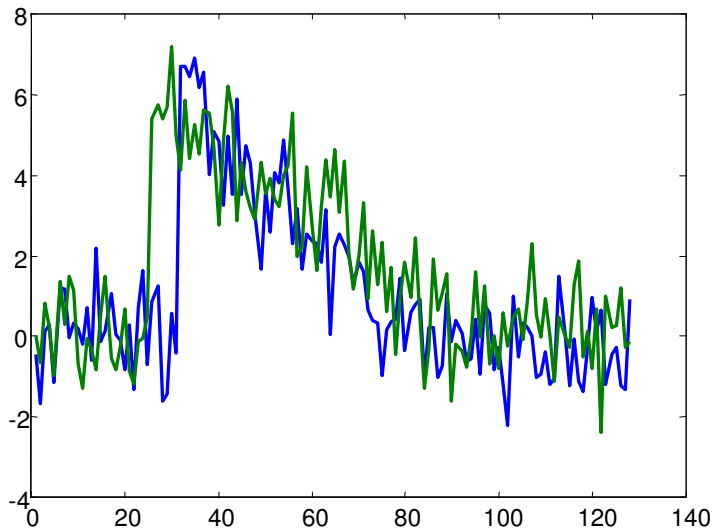
Fit the best fitting straight line to the time series, then subtract that line from the time series.

Removed **linear trend**

Removed offset translation

Removed amplitude scaling

# Transformation III: Noise



The intuition behind removing noise is...

Average each datapoints value with its neighbors.

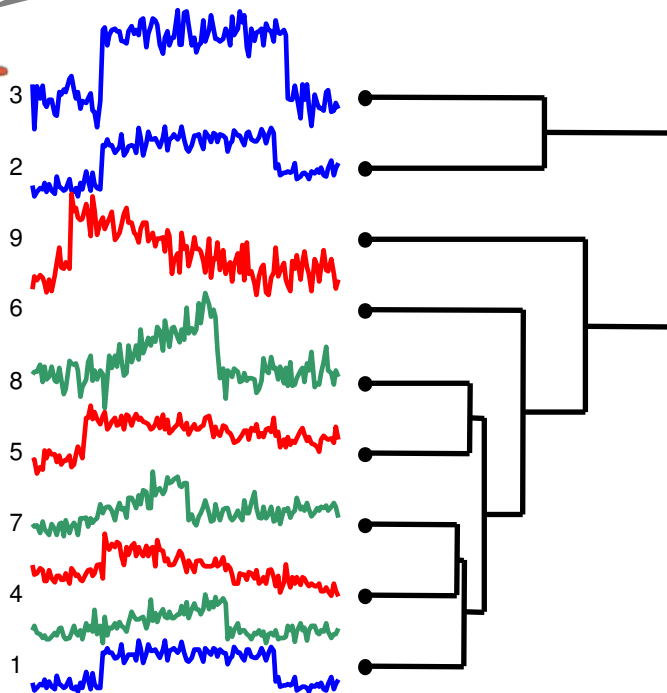
$$Q = \text{smooth}(Q)$$

$$C = \text{smooth}(C)$$

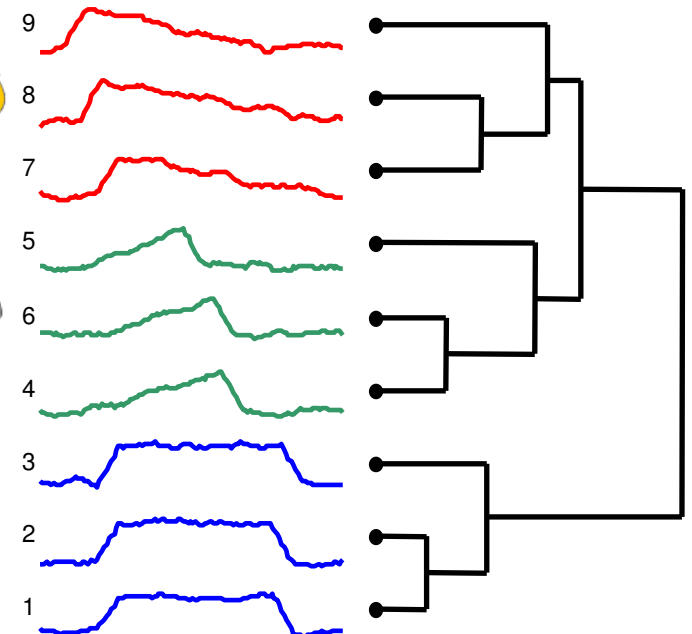
$$D(Q, C)$$

# A Quick Experiment to Demonstrate the Utility of Preprocessing the Data

Clustered using Euclidean distance on the raw data.



Clustered using Euclidean distance, after removing noise, linear trend, offset translation and amplitude scaling



# Summary of Preprocessing

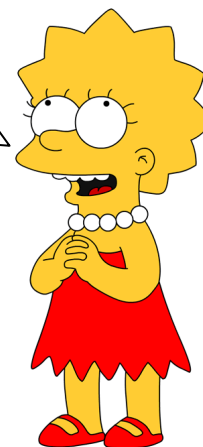
The "raw" time series may have distortions which we should remove before clustering, classification etc



Of course, sometimes the distortions are the most interesting thing about the data, the above is only a general rule

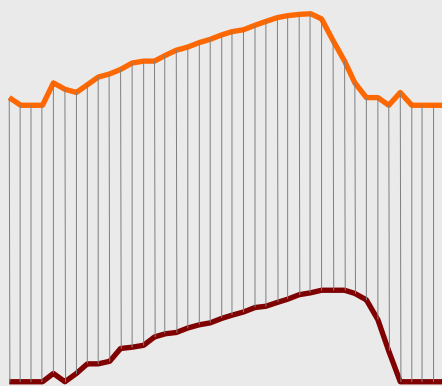
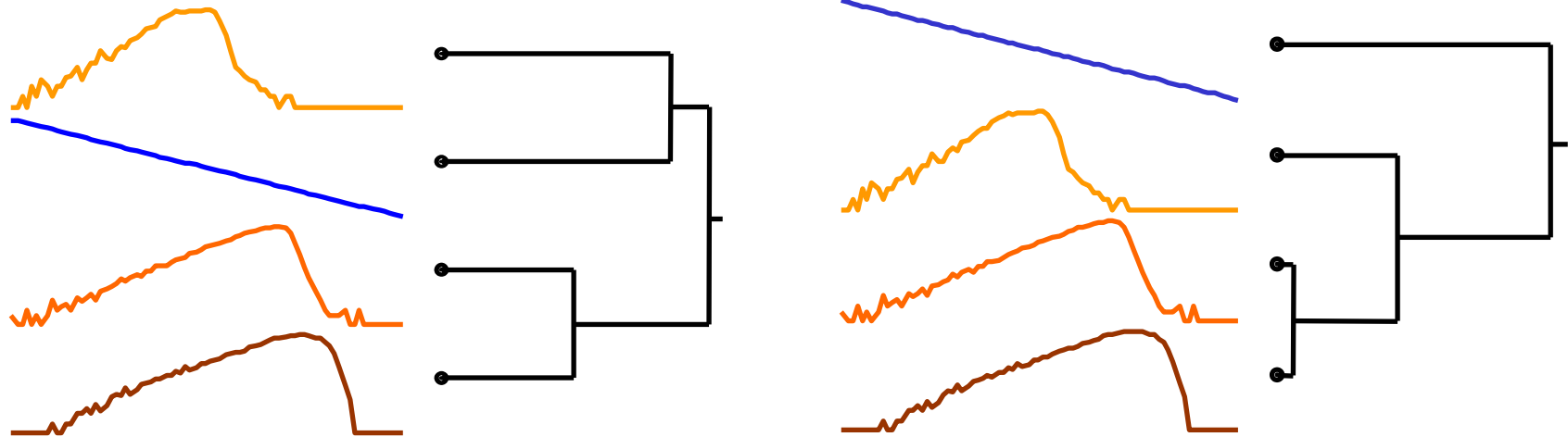


We should keep in mind these problems as we consider the high level representations of time series which we will encounter later (DFT, Wavelets etc). Since these representations often allow us to handle distortions in elegant ways



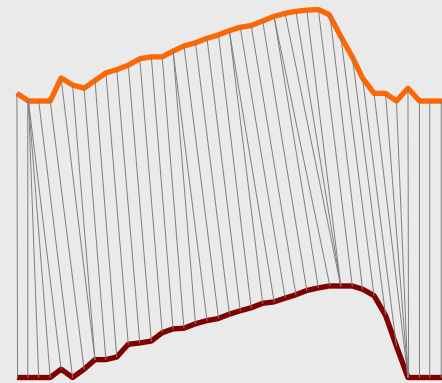


# Dynamic Time Warping



Fixed Time Axis

*Sequences are aligned "one to one".*



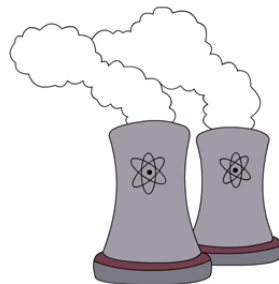
"Warped" Time Axis

*Nonlinear alignments are possible.*

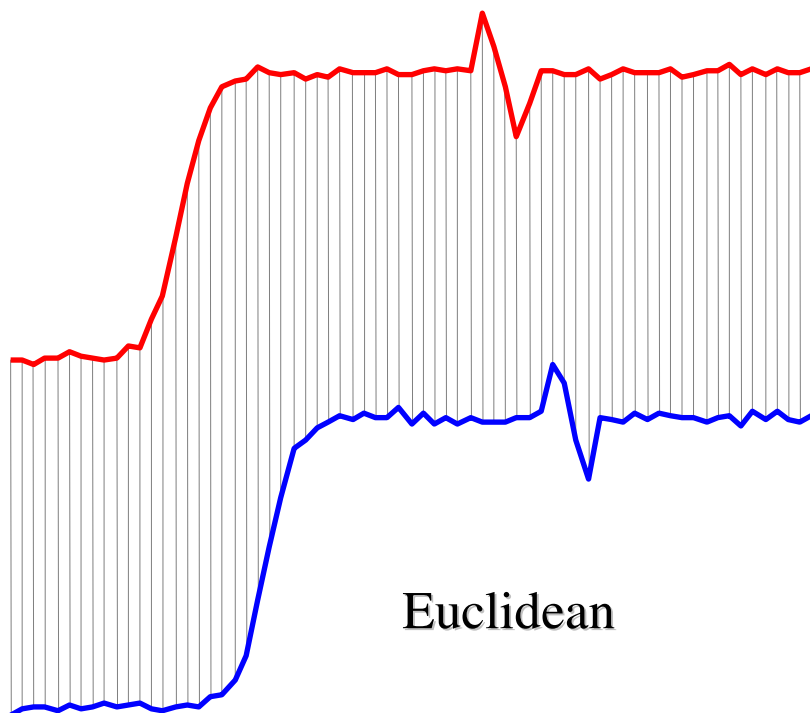
Note: We will first see the utility of DTW, then see how it is calculated.



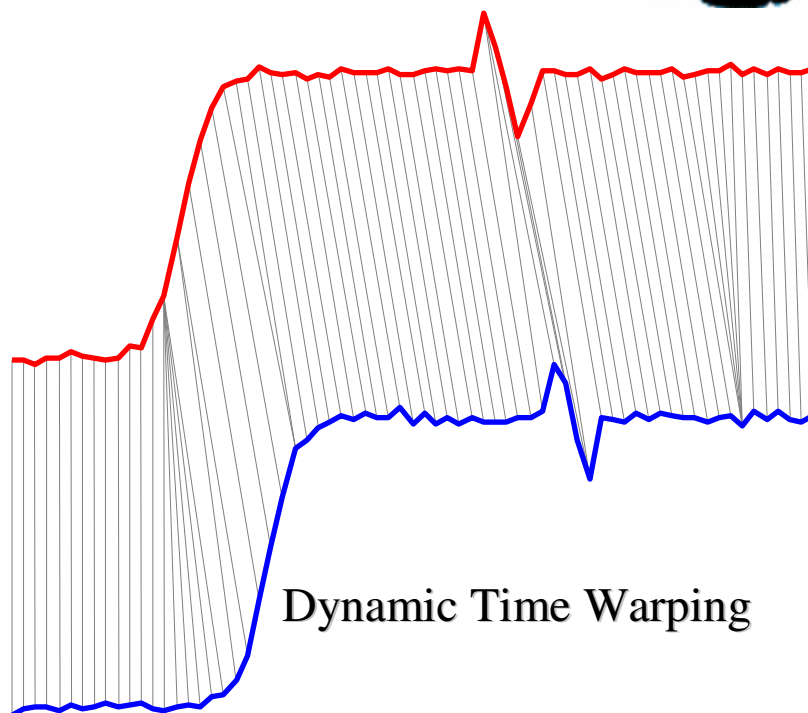
Here is another example on  
nuclear power plant trace  
data, to help you develop an  
intuition for DTW



Nuclear  
Power  
Excellent!

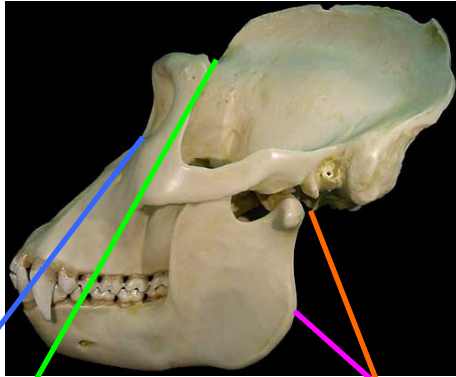


Euclidean

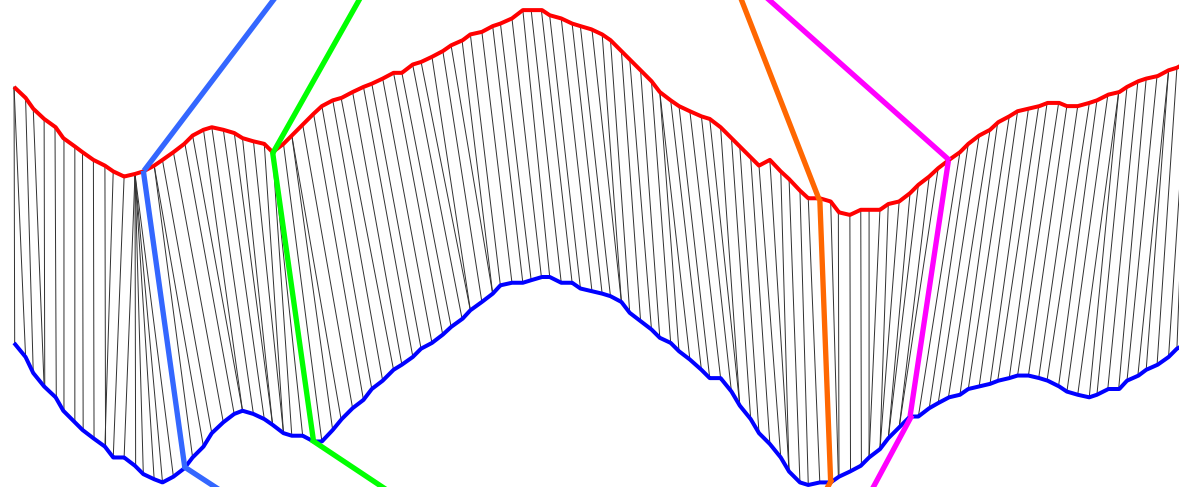


Dynamic Time Warping

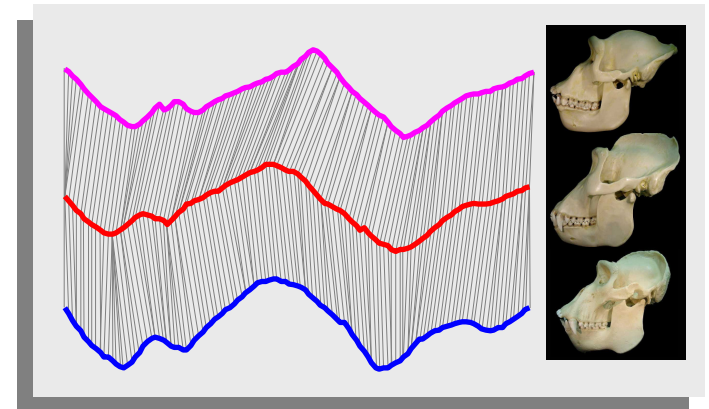
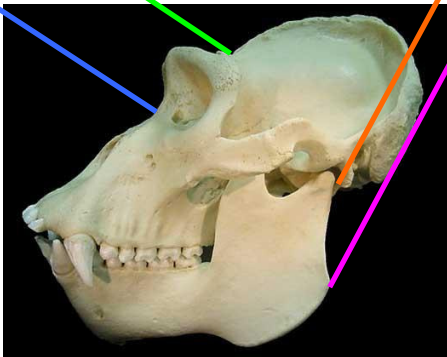
Lowland Gorilla  
*Gorilla gorilla gorilla*



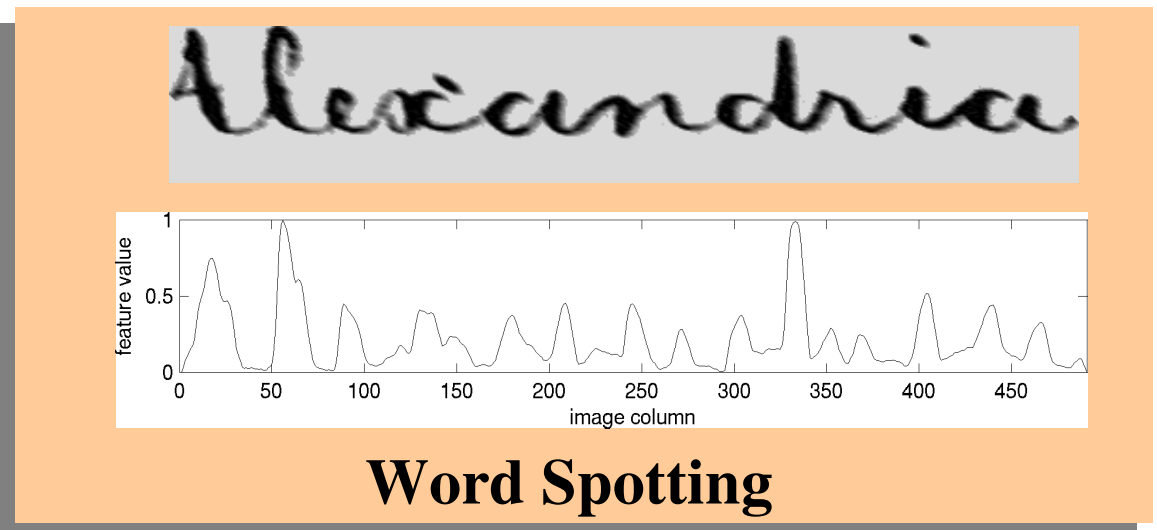
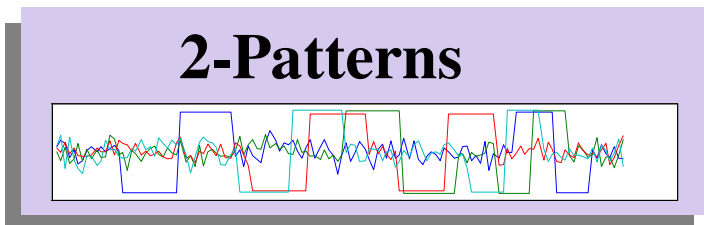
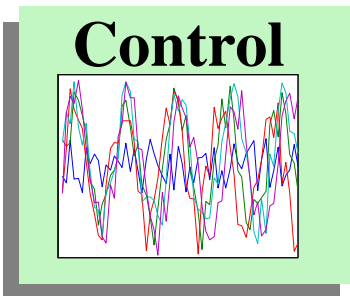
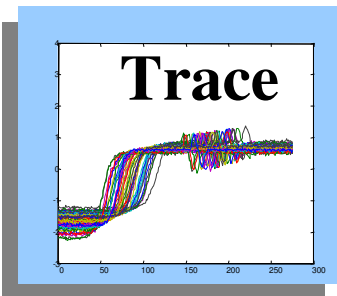
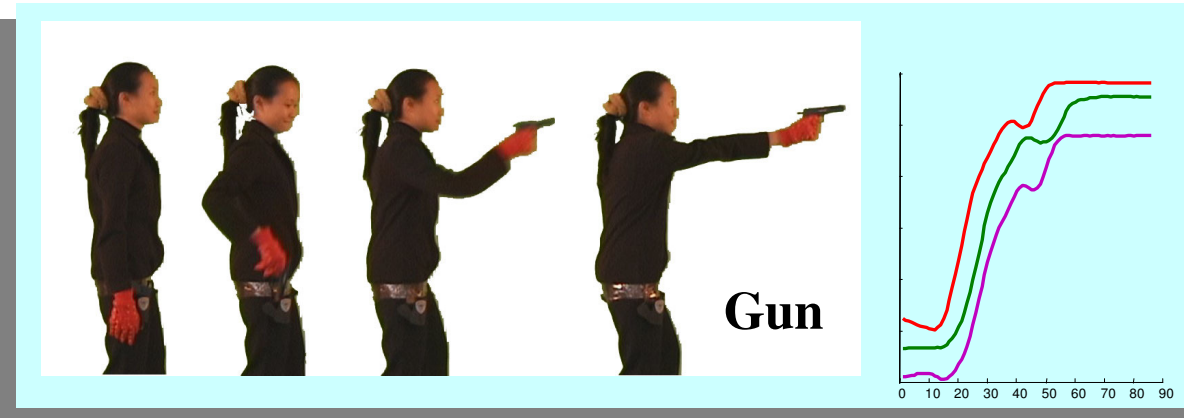
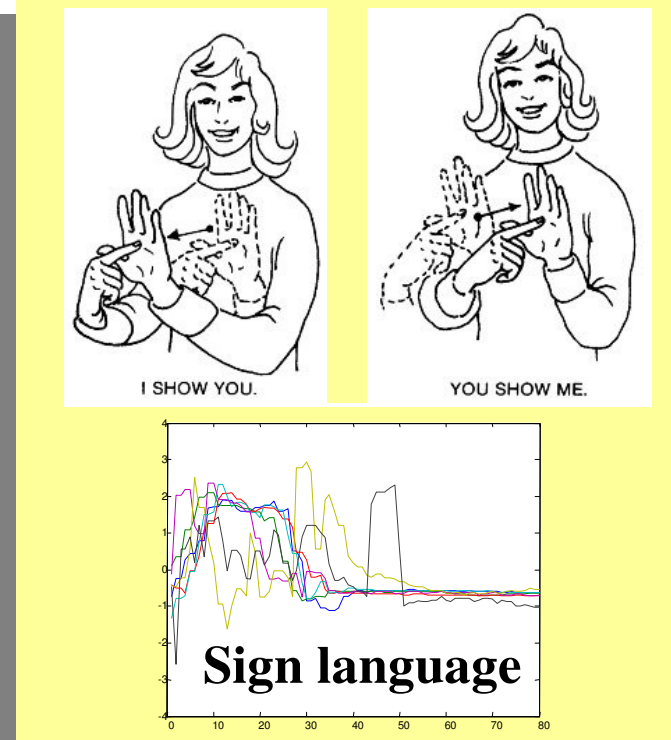
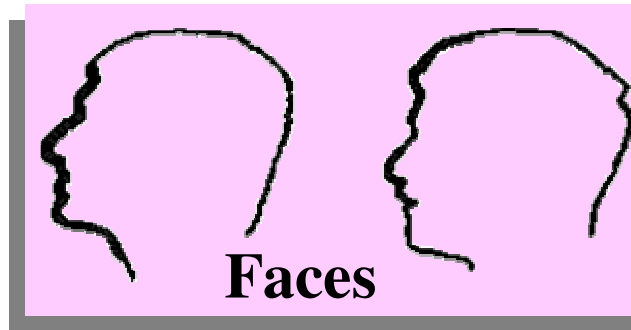
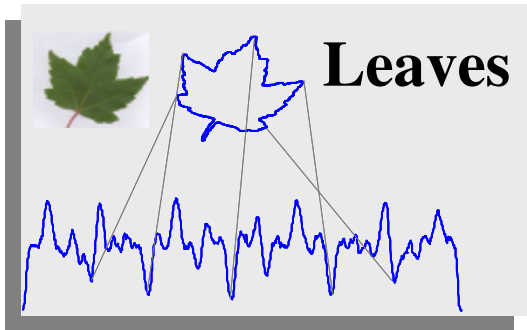
DTW is needed  
for most natural  
objects...



Mountain Gorilla  
*Gorilla gorilla beringei*



# Let us compare Euclidean Distance and DTW on some problems



# Results: Error Rate

Dataset	Euclidean	DTW
Word Spotting	4.78	1.10
Sign language	28.70	25.93
GUN	5.50	1.00
Nuclear Trace	11.00	0.00
Leaves <sup>#</sup>	33.26	4.07
(4) Faces	6.25	2.68
Control Chart*	7.5	0.33
2-Patterns	1.04	0.00

Using 1-nearest-neighbor, leaving-one-out evaluation!



# Results: Time (msec )

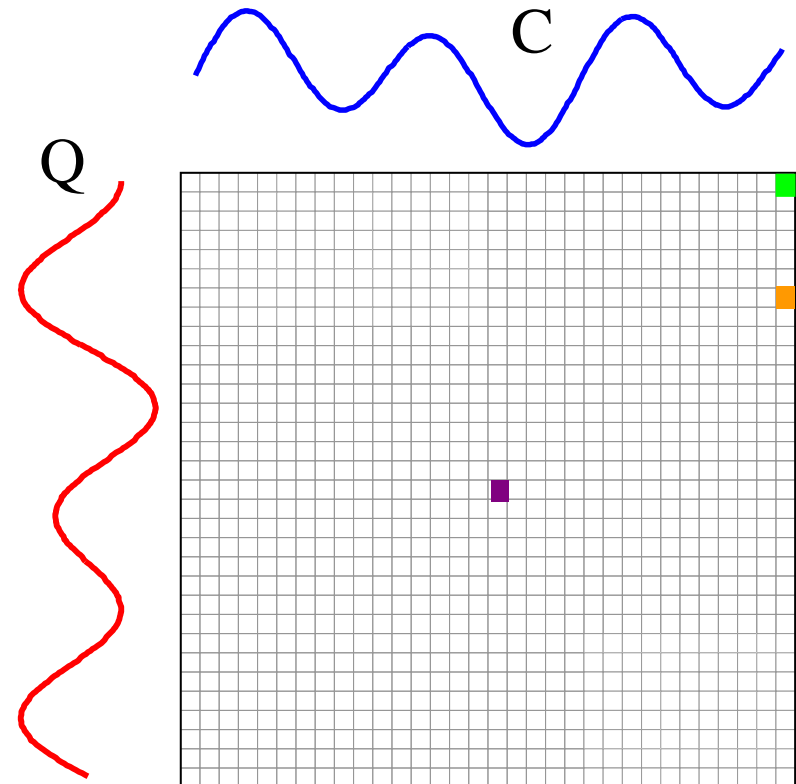
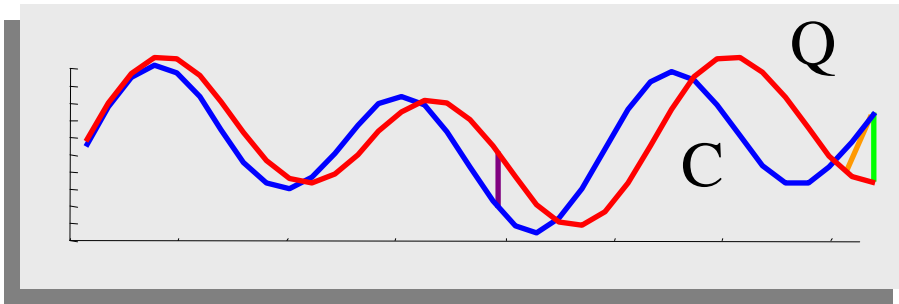
Dataset	Euclidean	DTW	
Word Spotting	40	8,600	215
Sign language	10	1,110	110
GUN	60	11,820	197
Nuclear Trace	210	144,470	687
Leaves	150	51,830	345
(4) Faces	50	45,080	901
Control Chart	110	21,900	199
2-Patterns	16,890	545,123	32

DTW is  
two to  
three  
orders of  
magnitude  
slower  
than  
Euclidean  
distance



# How is DTW Calculated? I

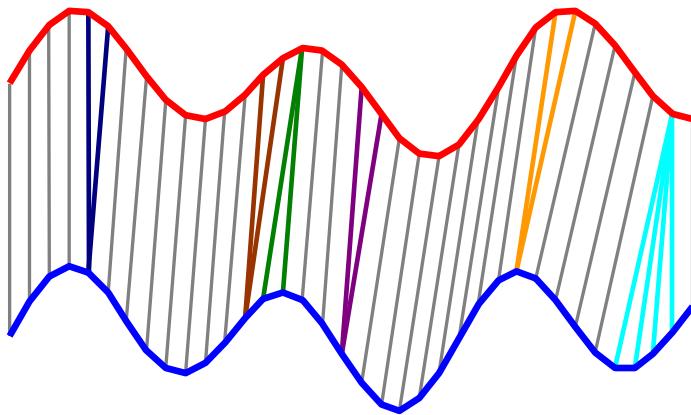
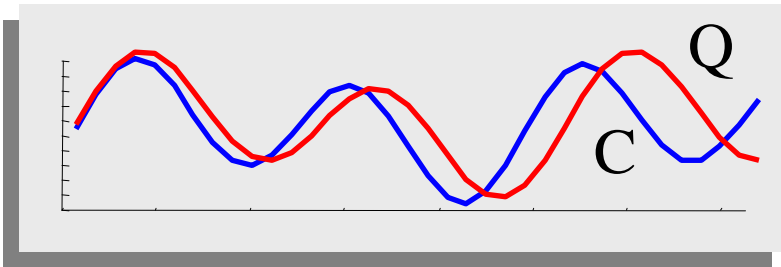
We create a matrix the size of  $|Q|$  by  $|C|$ , then fill it in with the distance between every pair of point in our two time series.



# How is DTW Calculated? II

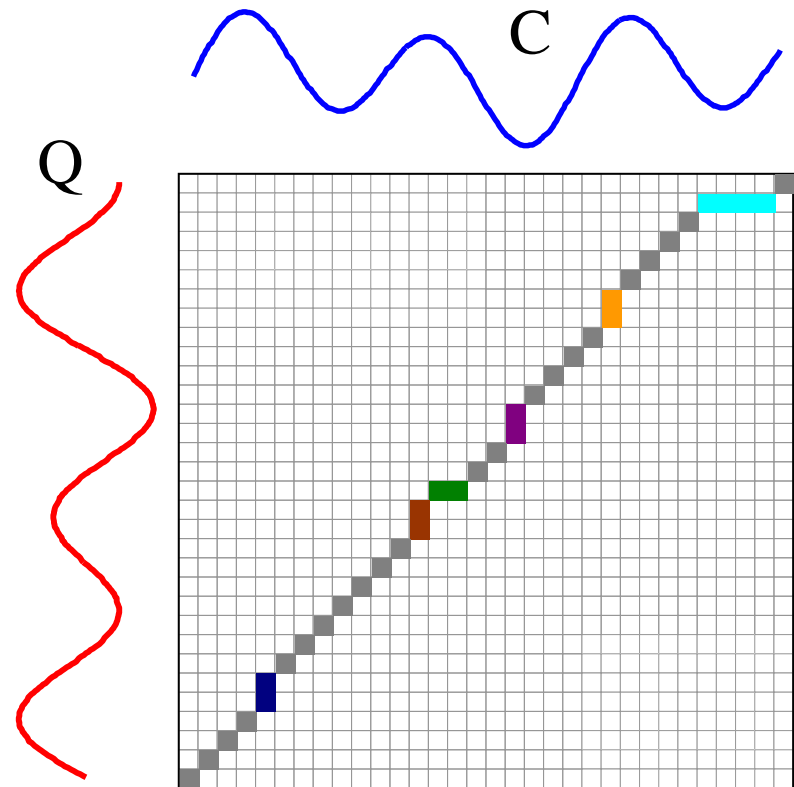
Every possible warping between two time series, is a path through the matrix. We want the best one...

$$DTW(Q, C) = \min \left\{ \sqrt{\sum_{k=1}^K w_k} / K \right\}$$



This recursive function gives us the minimum cost path

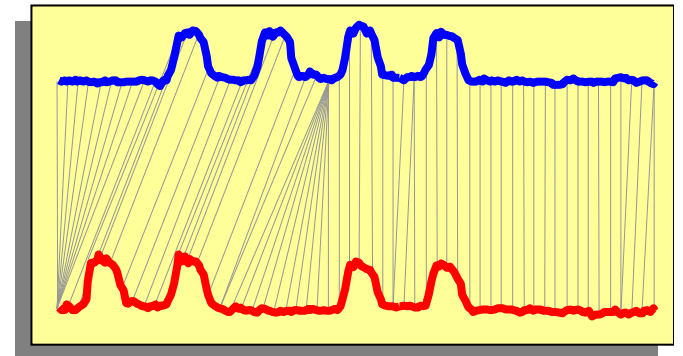
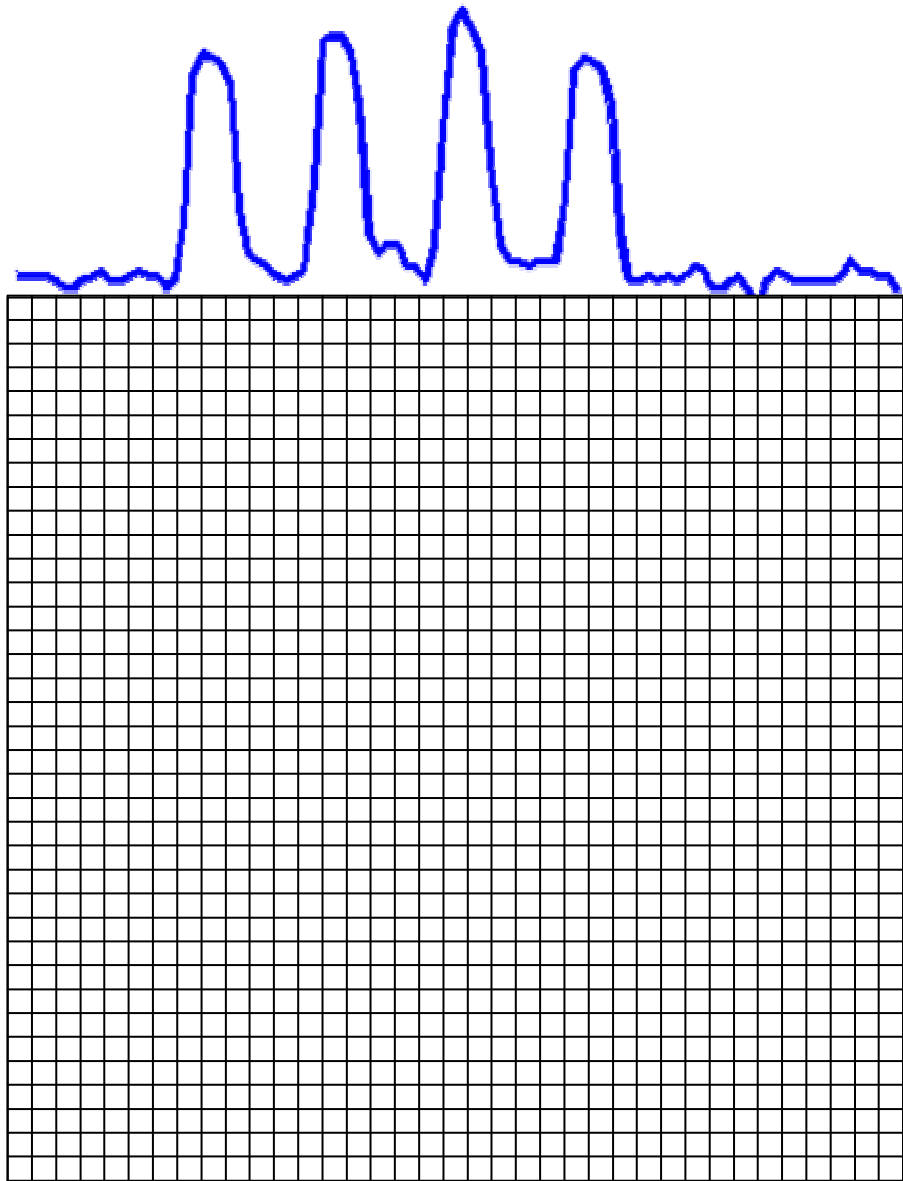
$$\gamma(i, j) = d(q_i, c_j) + \min \{ \gamma(i-1, j-1), \gamma(i-1, j), \gamma(i, j-1) \}$$



Warping path  $w$



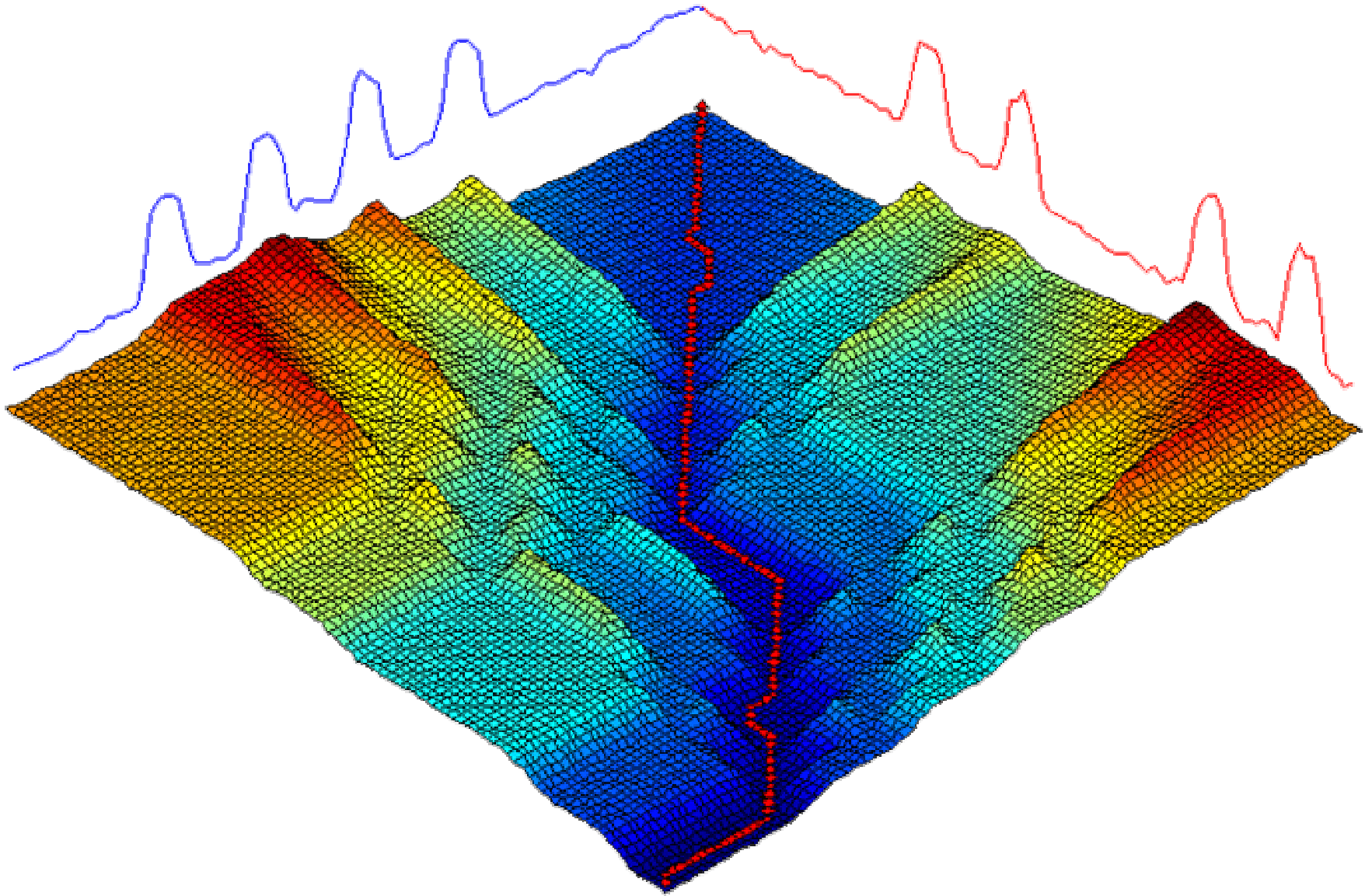
# Let us visualize the cumulative matrix on a real world problem I



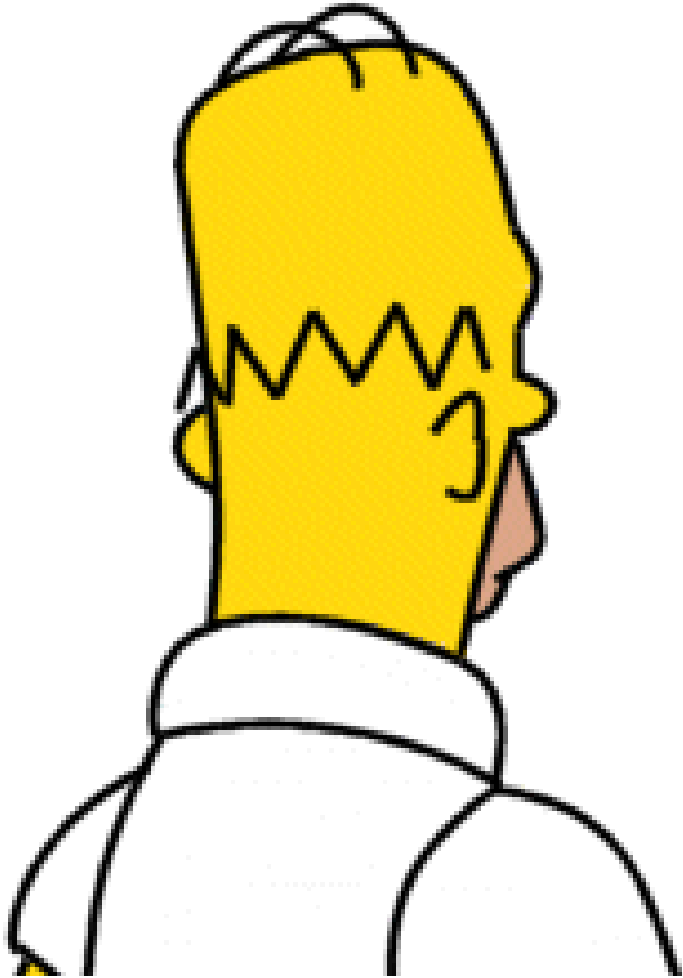
This example shows 2 one-week periods from the power demand time series.

Note that although they both describe 4-day work weeks, the blue sequence had Monday as a holiday, and the red sequence had Wednesday as a holiday.

Let us visualize the cumulative matrix on a real world problem II



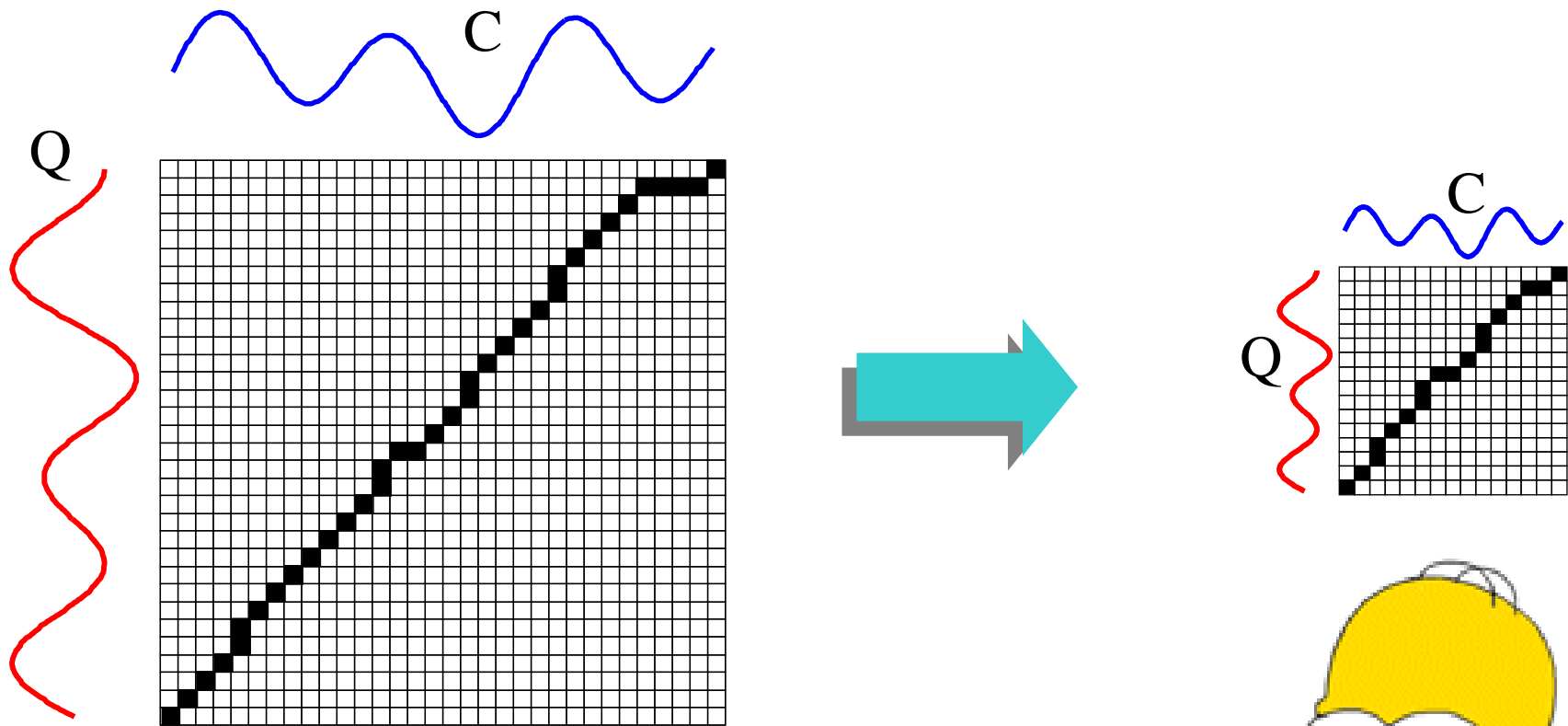
# What we have seen so far...



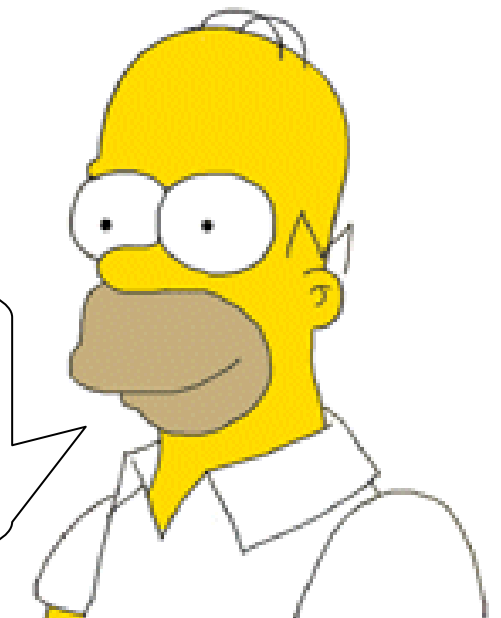
- Dynamic Time Warping gives **much better** results than Euclidean distance on virtually all problems.
- Dynamic Time Warping is very very slow to calculate!

Is there anything we can do to speed up similarity search under DTW?

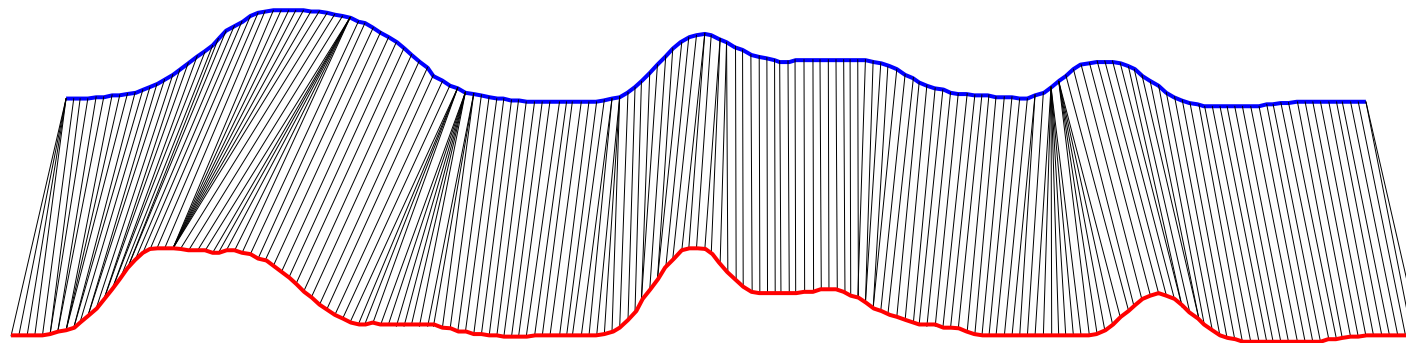
# Fast Approximations to Dynamic Time Warp Distance I



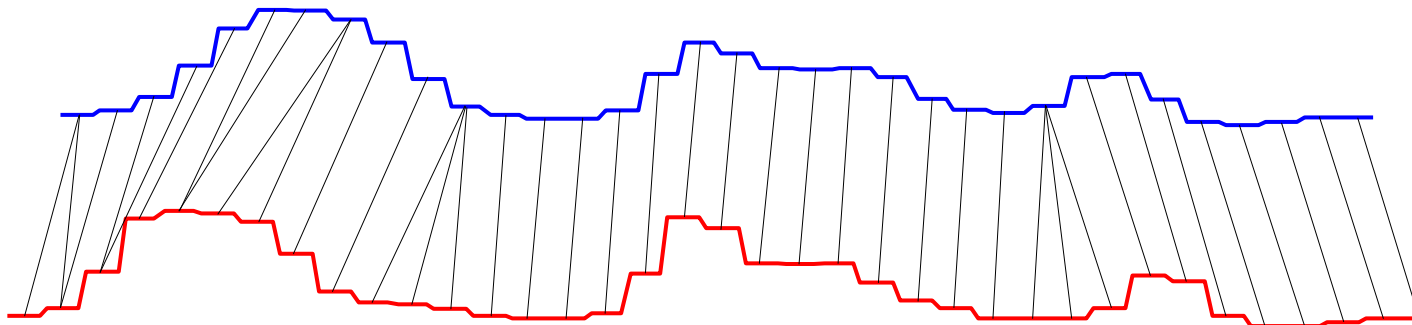
Simple Idea: Approximate the time series with some compressed or downsampled representation, and do DTW on the new representation. How well does this work...



# Fast Approximations to Dynamic Time Warp Distance II



1.03 sec



0.07 sec

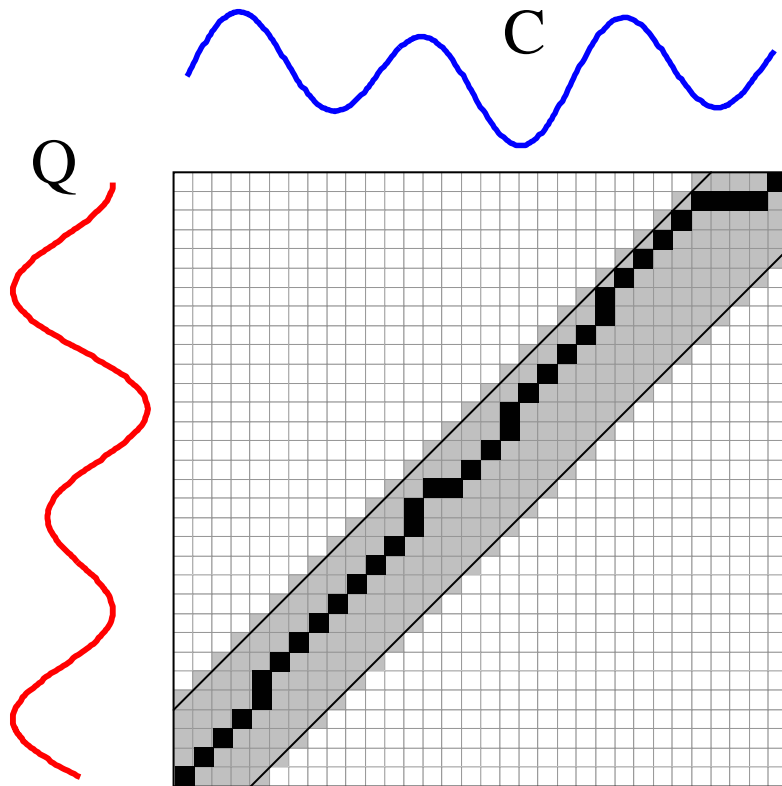
... there is strong visual evidence to suggest it works well

There is good experimental evidence for the utility of the approach on clustering, classification, etc

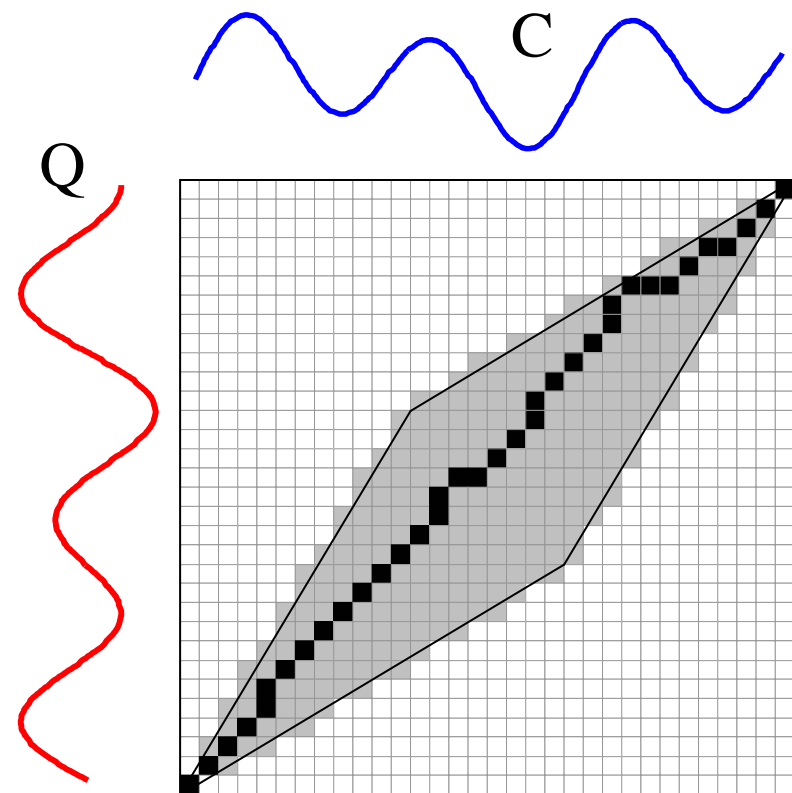


# Global Constraints

- Slightly speed up the calculations
- Prevent pathological warpings

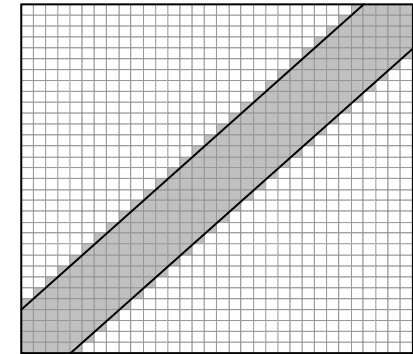
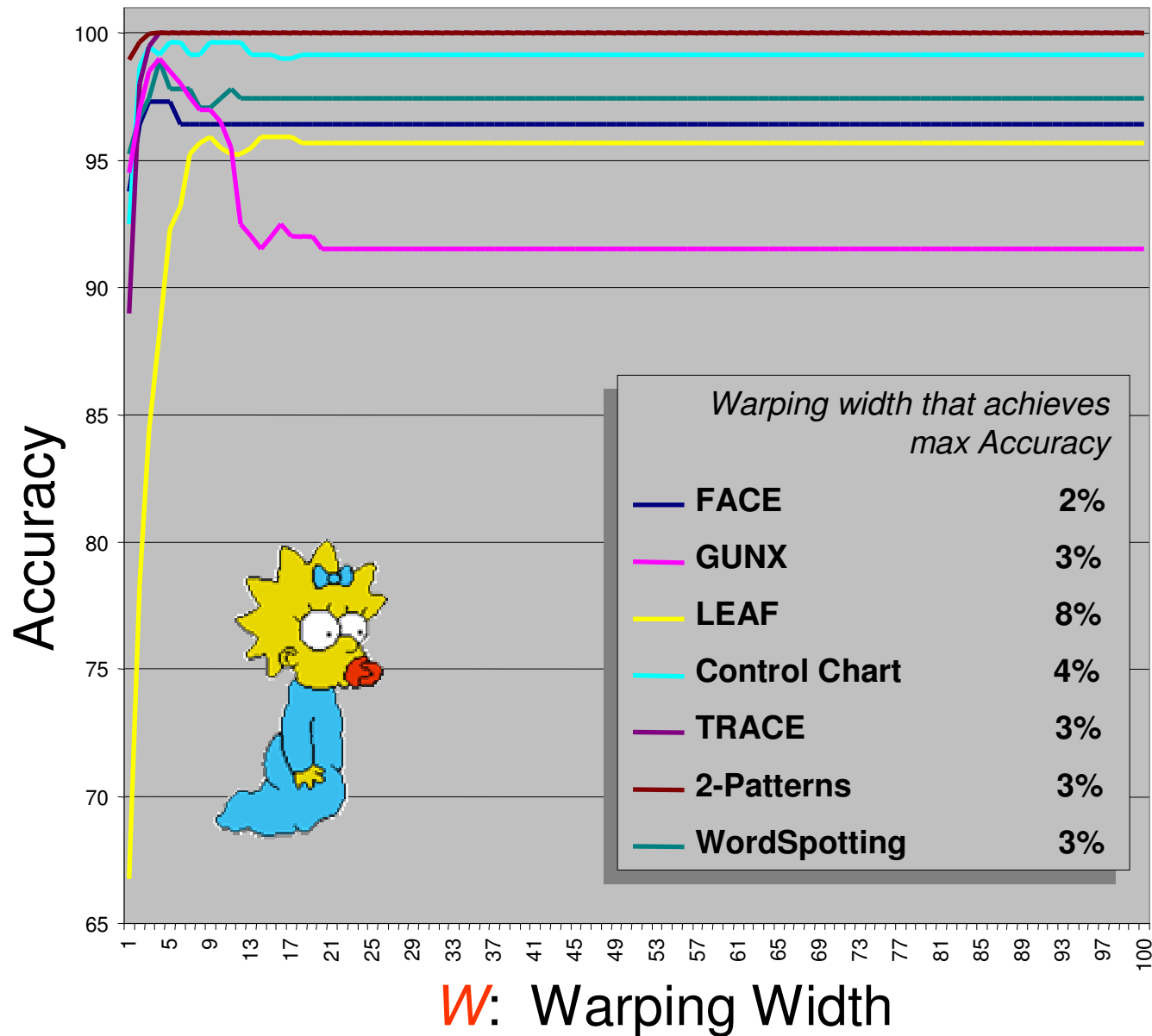


Sakoe-Chiba Band



Itakura Parallelogram

# Accuracy vs. Width of Warping Window

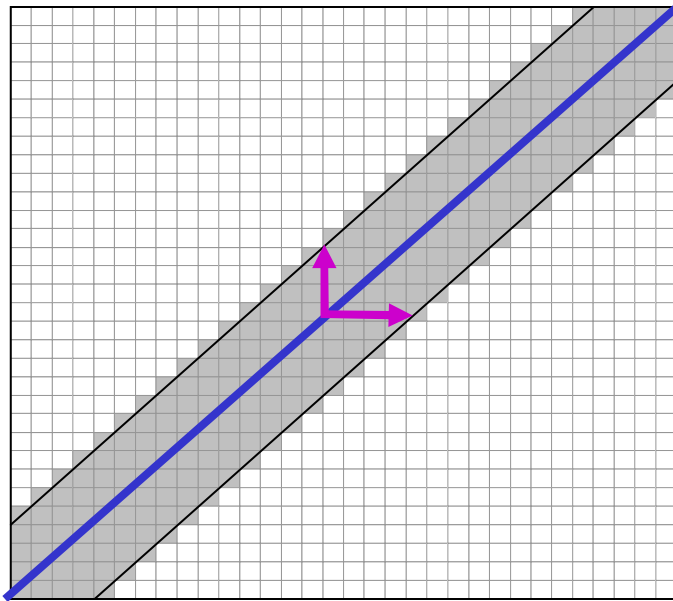


**W**



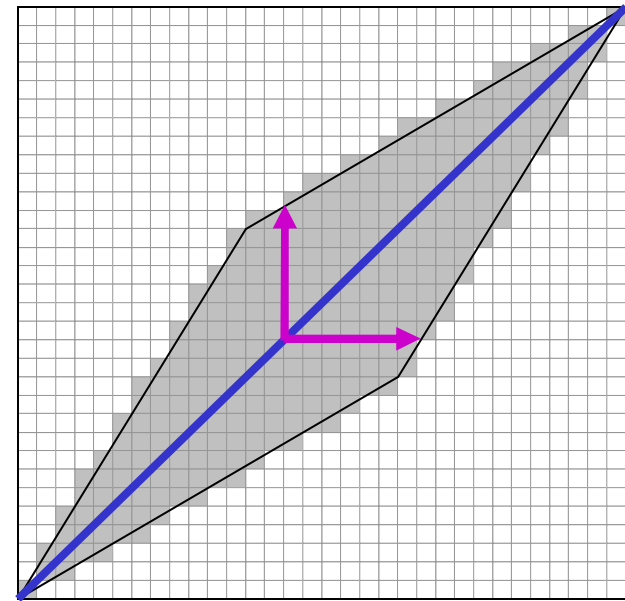
A global constraint constrains the indices of the warping path  $w_k = (i, j)_k$  such that  $j-r \leq i \leq j+r$

Where  $r$  is a term defining allowed range of warping for a given point in a sequence.



Sakoe-Chiba Band

$r_i$



Itakura Parallelogram



In general, it's hard to speed up a single DTW calculation



However, if we have to make many DTW calculations (which is almost always the case), we can potentially speed up the whole process by *lowerbounding*.



Keep in mind that the *lowerbounding* trick works for any situation where you have an expensive calculation that can be *lowerbounded* (string edit distance, graph edit distance etc)



I will explain how *lowerbounding* works in a generic fashion in the next two slides, then show concretely how *lowerbounding* makes dealing with massive time series under DTW possible...




# Lower Bounding I


Assume that we have two functions:

- $\text{DTW}(A,B)$
- $\text{lower\_bound\_distance}(A,B)$

The true DTW  
function is very  
slow...



The *lower  
bound* function  
is very fast...



By definition, for all  $A, B$ , we have

$$\text{lower\_bound\_distance}(A,B) \leq \text{DTW}(A,B)$$

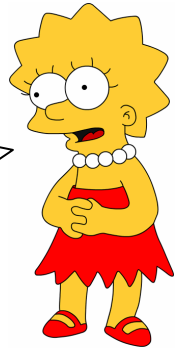
# Lower Bounding II

We can speed up similarity search under DTW by using a lower bounding function

## Algorithm Lower\_Bounding\_Sequential\_Scan(Q)

```
1.  best_so_far = infinity;
2.  for all sequences in database
3.    LB_dist = lower_bound_distance( $C_i$ , Q);
4.    if LB_dist < best_so_far
5.      true_dist = DTW( $C_i$ , Q);
6.      if true_dist < best_so_far
7.        best_so_far = true_dist;
8.        index_of_best_match = i;
9.      endif
10.   endif
11. endfor
```

Try to use a cheap lower bounding calculation as often as possible.

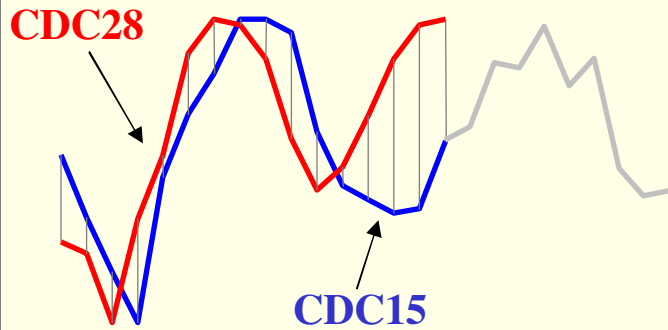


Only do the expensive, full calculations when it is absolutely necessary

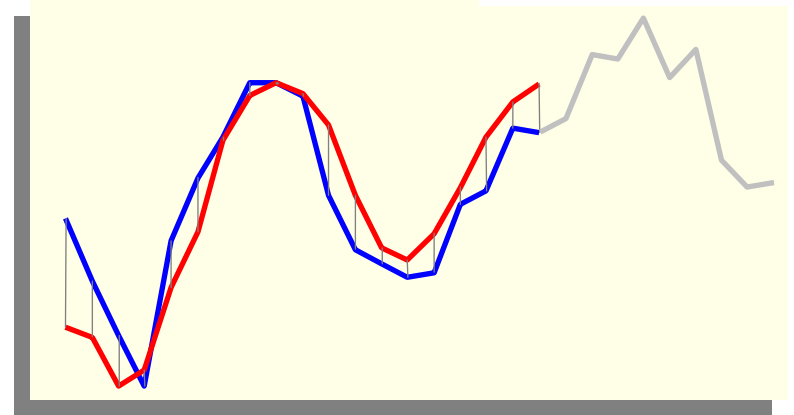
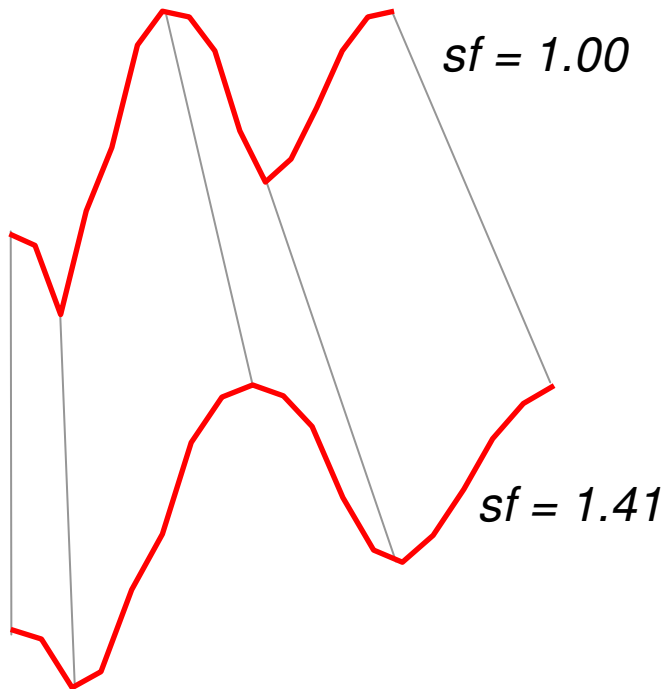


# Uniform Scaling I

Two genes that are known to be functionally related...

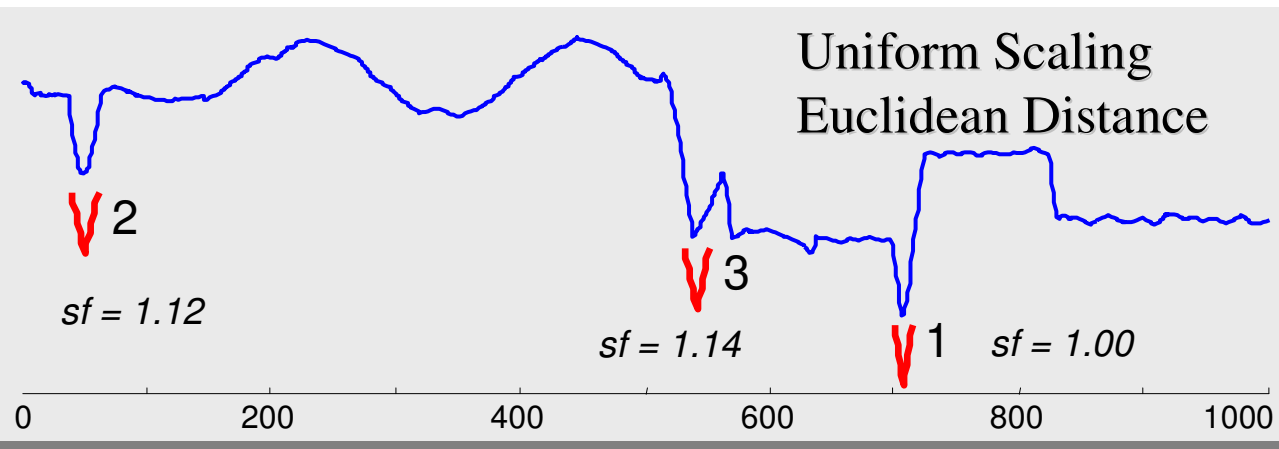
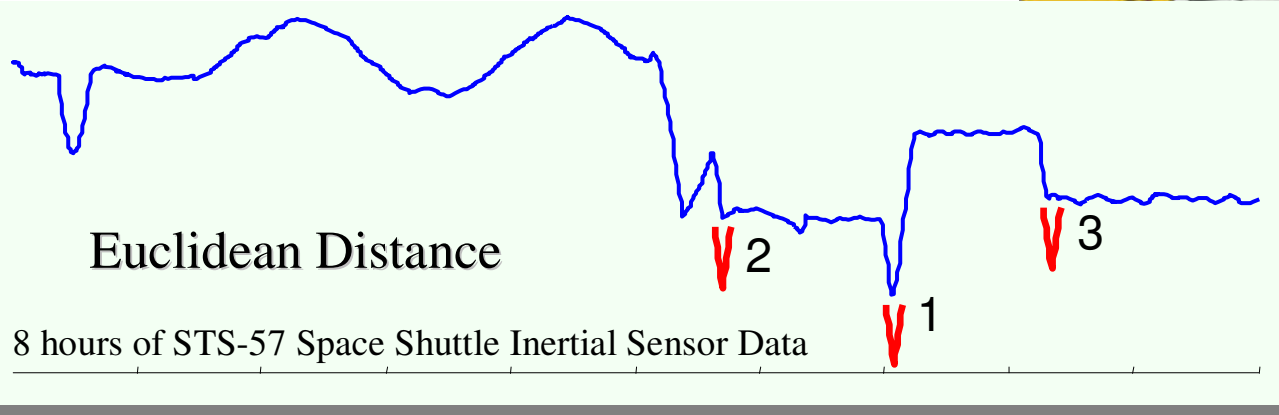


Sometimes  
global or  
*uniform scaling*  
is as important  
as DTW

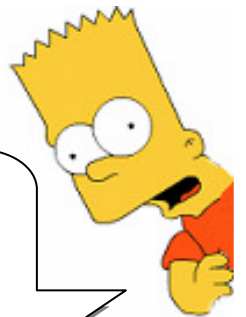


# Uniform Scaling II

Without scaling, matches 2 and 3 seem unintuitive



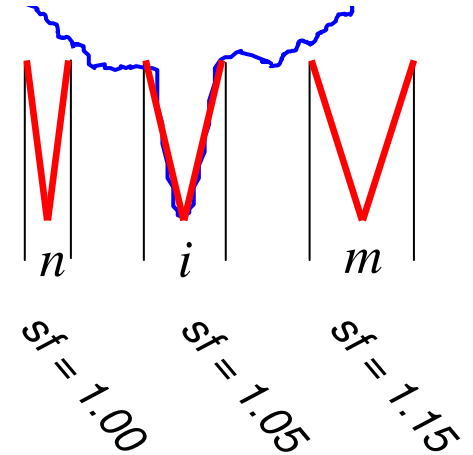
We need to test all scalings!



V ... V ... V  
 $sf = 1.00$   $sf = 1.01$   $sf = 1.10$



Here is some notation, the shortest scaling we consider is length  $n$ , and the largest is length  $m$ . The *scaling factor* ( $sf$ ) is the ratio  $i/n$ ,  $n \leq i \leq m$



**Algorithm:** **Test\_All\_Scalings**(Q,C)

```
best_match_val      = inf;
best_scaling_factor = null;
for  $p = n$  to  $m$ 
  QP = rescale(Q,p);
  distance = squared_Euclidean_distance(QP, C[1..p])
  if distance < best_match_val
    best_match_val = distance;
    best_scaling_factor =  $p/n$ ;
  end;
end;
return(best_match_val, best_scaling_factor)
```

Here is the code to **Test\_All\_Scalings**, the time complexity is only  $O((m-n) * n)$ , but we may have to do this many times...



# Only Euclidean and DTW Distance are Useful

**Stop!**

What about the dozens of other techniques for measuring time series shape similarity?



Unfortunately, none of them appear to be useful!



# Classification Error Rates on two publicly available datasets



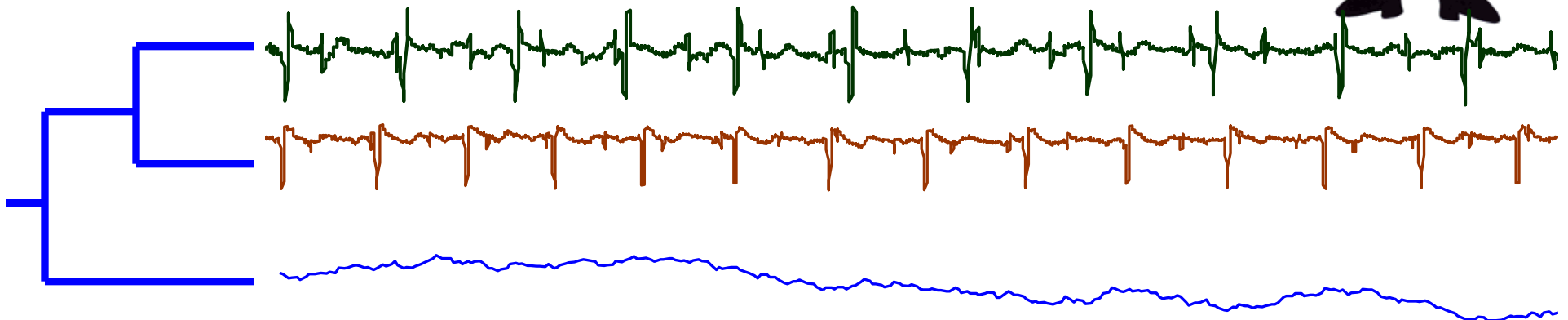
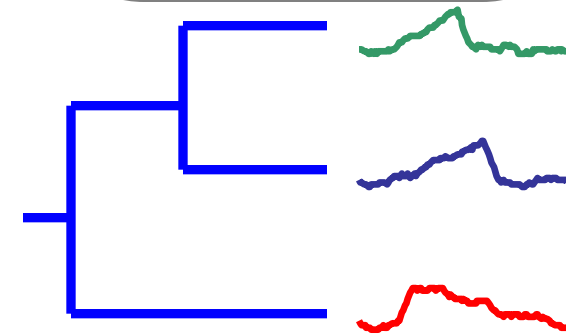
Approach	Cylinder-Bell-F'	Control-Chart
<i><b>Euclidean Distance</b></i>	<i><b>0.003</b></i>	<i><b>0.013</b></i>
Aligned Subsequence	<b>0.451</b>	<b>0.623</b>
Piecewise Normalization	<b>0.130</b>	<b>0.321</b>
Autocorrelation Functions	<b>0.380</b>	<b>0.116</b>
Cepstrum	<b>0.570</b>	<b>0.458</b>
String (Suffix Tree)	<b>0.206</b>	<b>0.578</b>
Important Points	<b>0.387</b>	<b>0.478</b>
Edit Distance	<b>0.603</b>	<b>0.622</b>
String Signature	<b>0.444</b>	<b>0.695</b>
Cosine Wavelets	<b>0.130</b>	<b>0.371</b>
Hölder	<b>0.331</b>	<b>0.593</b>
Piecewise Probabilistic	<b>0.202</b>	<b>0.321</b>



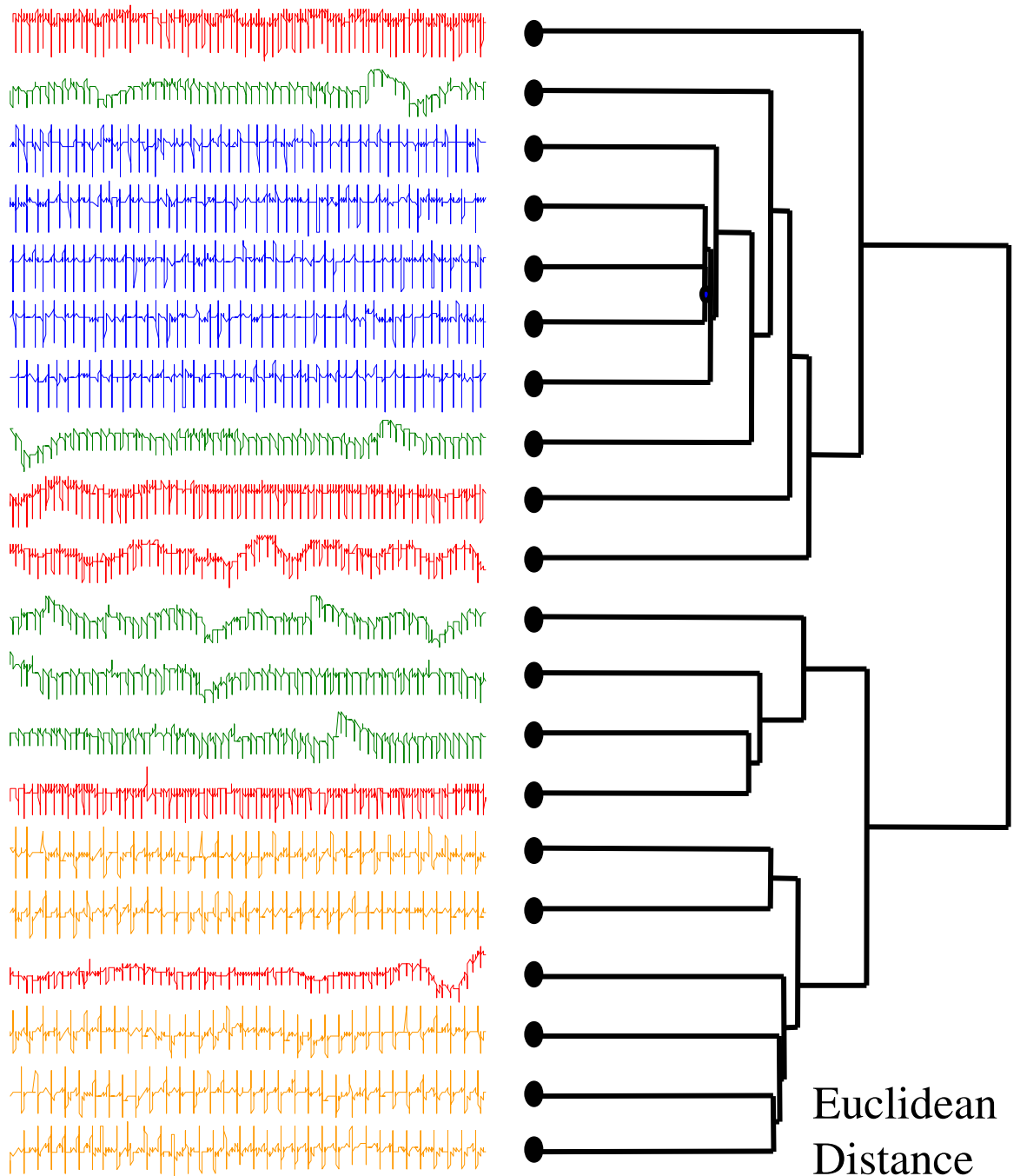
# Two Kinds of Similarity

We are  
done with  
*shape*  
similarity

Let us consider  
similarity at  
the *structural*  
level for the  
next 10 minutes

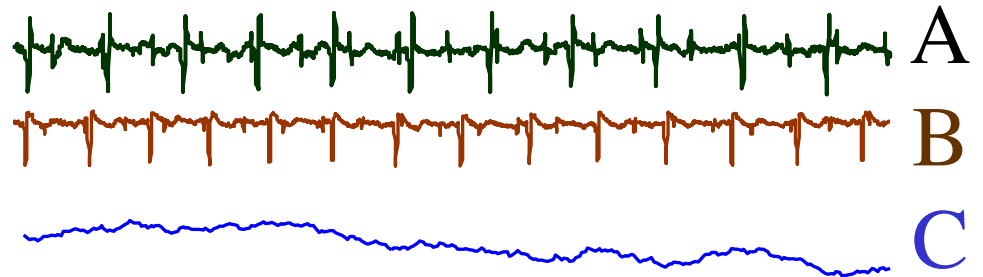


For long time series, *shape* based similarity will give very poor results. We need to measure similarity based on high level *structure*



# Structure or Model Based Similarity

The basic idea is to extract *global* features from the time series, create a feature vector, and use these feature vectors to measure similarity and/or classify



Feature \ Time Series			
	A	B	C
Max Value	11	12	19
Autocorrelation	0.2	0.3	0.5
Zero Crossings	98	82	13
ARIMA	0.3	0.4	0.1
...	...	...	...



But which

- **features?**
- **distance measure/learning algorithm?**

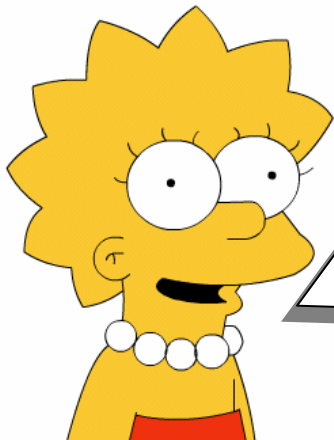
# Feature-based Classification of Time-series Data

Nanopoulos, Alcock, and Manolopoulos

- features?
- distance measure/  
learning algorithm?

## Learning Algorithm

multi-layer perceptron neural network



Makes sense, but when  
we looked at the *same*  
dataset, we found we  
could be better  
classification accuracy  
with Euclidean  
distance!

## Features

mean

variance

skewness

kurtosis

mean (1<sup>st</sup> derivative)

variance (1<sup>st</sup> derivative)

skewness (1<sup>st</sup> derivative)

kurtosis (1<sup>st</sup> derivative)

# Learning to Recognize Time Series: Combining ARMA Models with Memory-Based Learning

Deng, Moore and Nechyba

- features?
- distance measure/  
learning algorithm?

## Distance Measure

Euclidean distance (between coefficients)

- Use to detect drunk drivers!
- Independently rediscovered and generalized by Kalpakis et. al. and expanded by Xiong and Yeung

## Features

The parameters of the Box Jenkins model.

More concretely, the coefficients of the ARMA model.

*“Time series must be invertible and stationary”*

# Deformable Markov Model Templates for Time Series Pattern Matching

Ge and Smyth

## Part 1

- features?
- distance measure/  
learning algorithm?

## Distance Measure

“Viterbi-Like” Algorithm



Variations independently developed by Li and Biswas, Ge and Smyth, Lin, Orgun and Williams etc

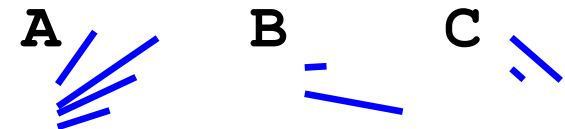
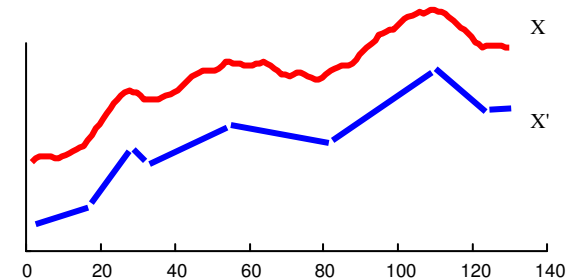
There tends to be lots of parameters to tune...

	A	B	C
A	0.1	0.4	0.5
B	0.4	0.2	0.2
C	0.5	0.2	0.3

## Features

The parameters of a Markov Model

The time series is first converted to a piecewise linear model

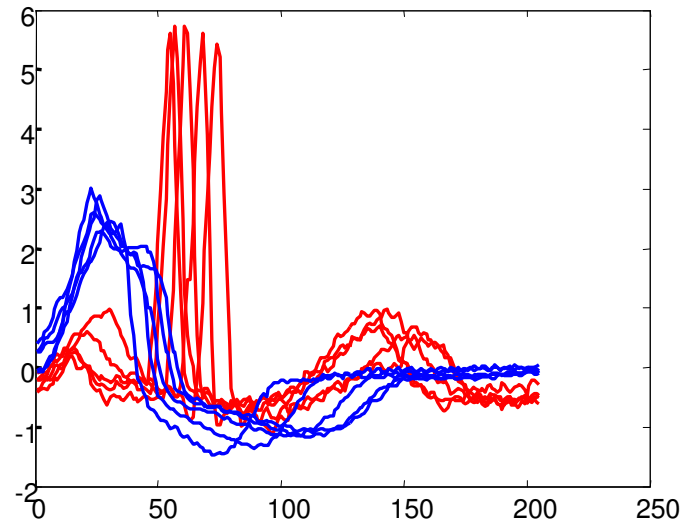


# Deformable Markov Model Templates for Time Series Pattern Matching

Ge and Smyth

## Part 2

On this problem  
the approach  
gets 98%  
classification  
accuracy\*...



## Features

The parameters of a  
Markov Model

The time series is first  
converted to a piecewise  
linear model

But Euclidean distance  
gets 100%! And has no  
parameters to tune, and  
is tens of thousands  
times faster...



# Compression Based Dissimilarity

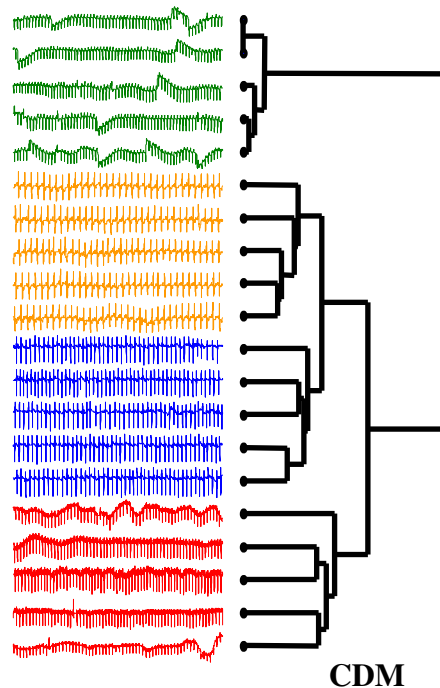
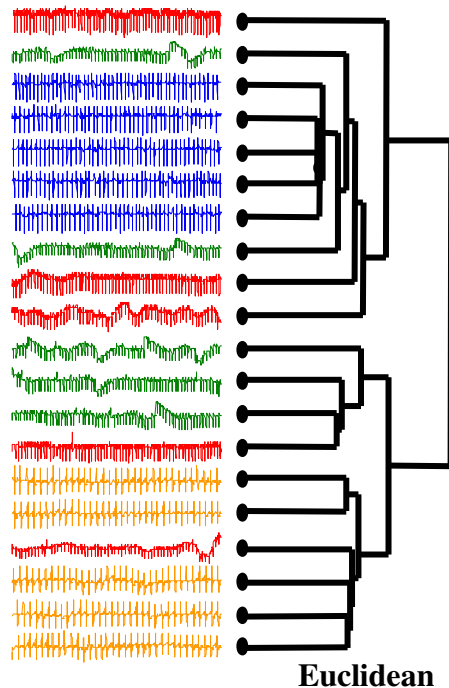
(In general) Li, Chen, Li, Ma, and Vitányi: (For time series) Keogh, Lonardi and Ratanamahatana

- features?
- distance measure/  
learning algorithm?

## Distance Measure

Co-Compressibility

$$CDM(x, y) = \frac{C(xy)}{C(x) + C(y)}$$



## Features

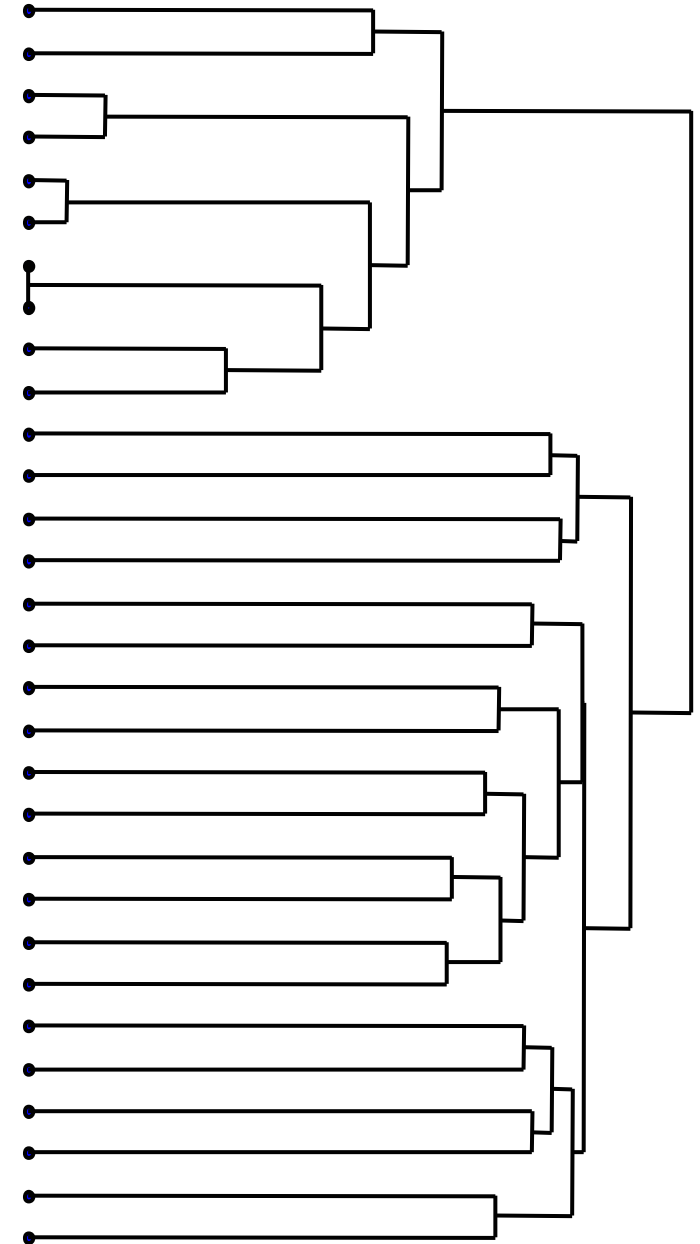
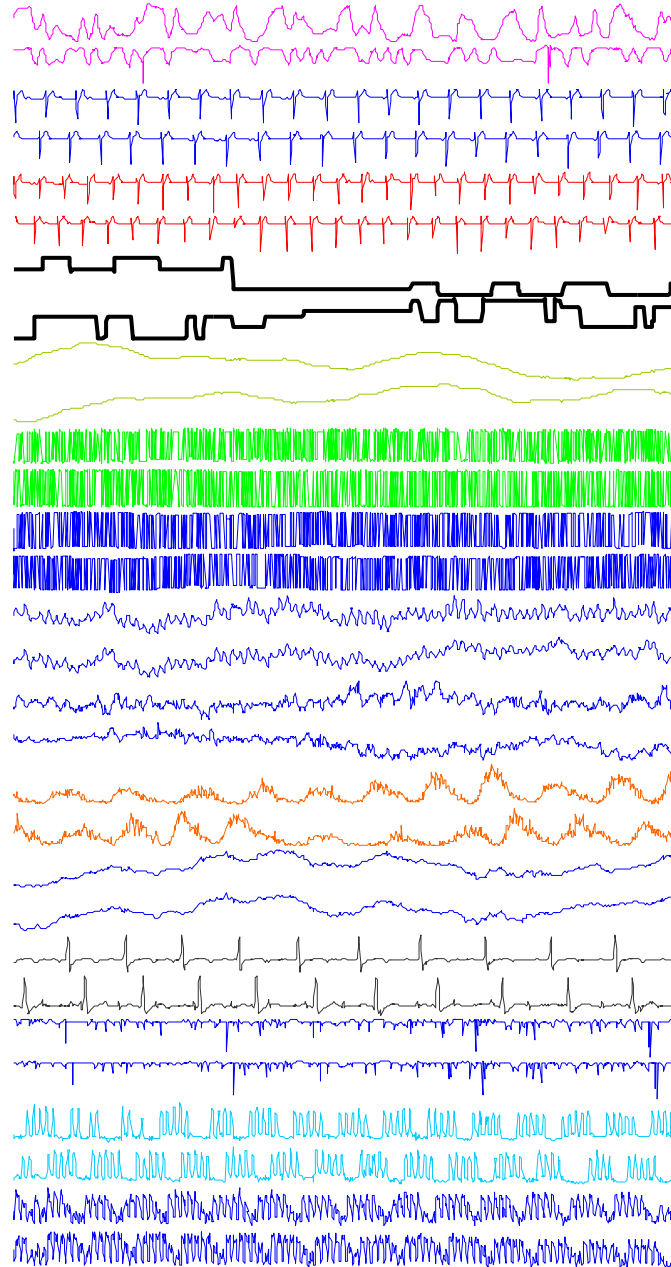
Whatever structure  
the compression  
algorithm finds...

The time series is first converted  
to the SAX symbolic  
representation\*



# Compression Based Dissimilarity

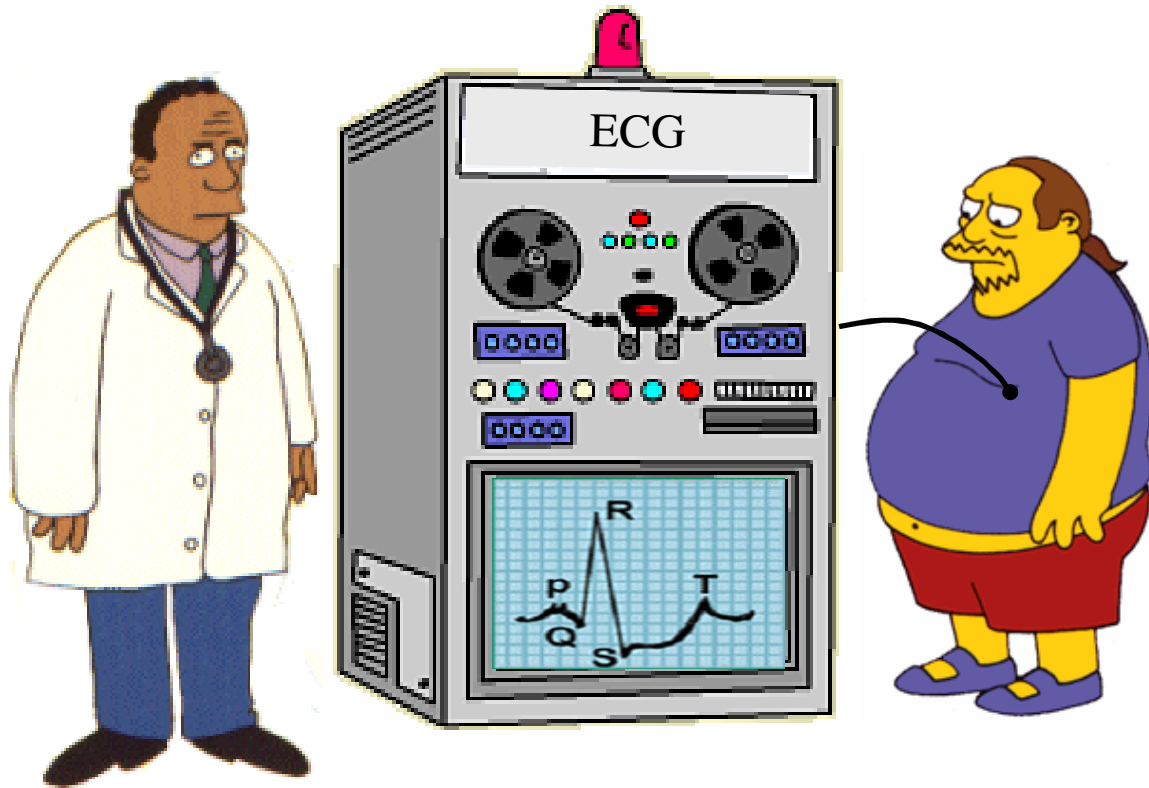
Reel 2: Tension  
 Reel 2: Angular speed  
 Koski ECG: Fast 2  
 Koski ECG: Fast 1  
 Koski ECG: Slow 2  
 Koski ECG: Slow 1  
 Dryer hot gas exhaust  
 Dryer fuel flow rate  
 Ocean 2  
 Ocean 1  
 Evaporator: vapor flow  
 Evaporator: feed flow  
 Furnace: cooling input  
 Furnace: heating input  
 Great Lakes (Ontario)  
 Great Lakes (Erie)  
 Buoy Sensor: East Salinity  
 Buoy Sensor: North Salinity  
 Sunspots: 1869 to 1990  
 Sunspots: 1749 to 1869  
 Exchange Rate: German Mark  
 Exchange Rate: Swiss Franc  
 Foetal ECG thoracic  
 Foetal ECG abdominal  
 Balloon2 (lagged)  
 Balloon1  
 Power : April-June (Dutch)  
 Power : Jan-March (Dutch)  
 Power : April-June (Italian)  
 Power : Jan-March (Italian)



# Summary of Time Series Similarity

- If you have *short* time series, use DTW after searching over the warping window size<sup>1</sup> (and shape<sup>2</sup>)
- Then use envelope based lower bounds to speed things up<sup>3</sup>.
- If you have *long* time series, and you know nothing about your data, try compression based dissimilarity.
- If you do know something about your data, try to leverage of this knowledge to extract features.

## Motivating example revisited...



You go to the doctor because of chest pains. Your ECG looks strange...

Your doctor wants to search a database to find **similar** ECGs, in the hope that they will offer clues about your condition...

Two questions:

- How do we define similar?
- How do we search quickly?**

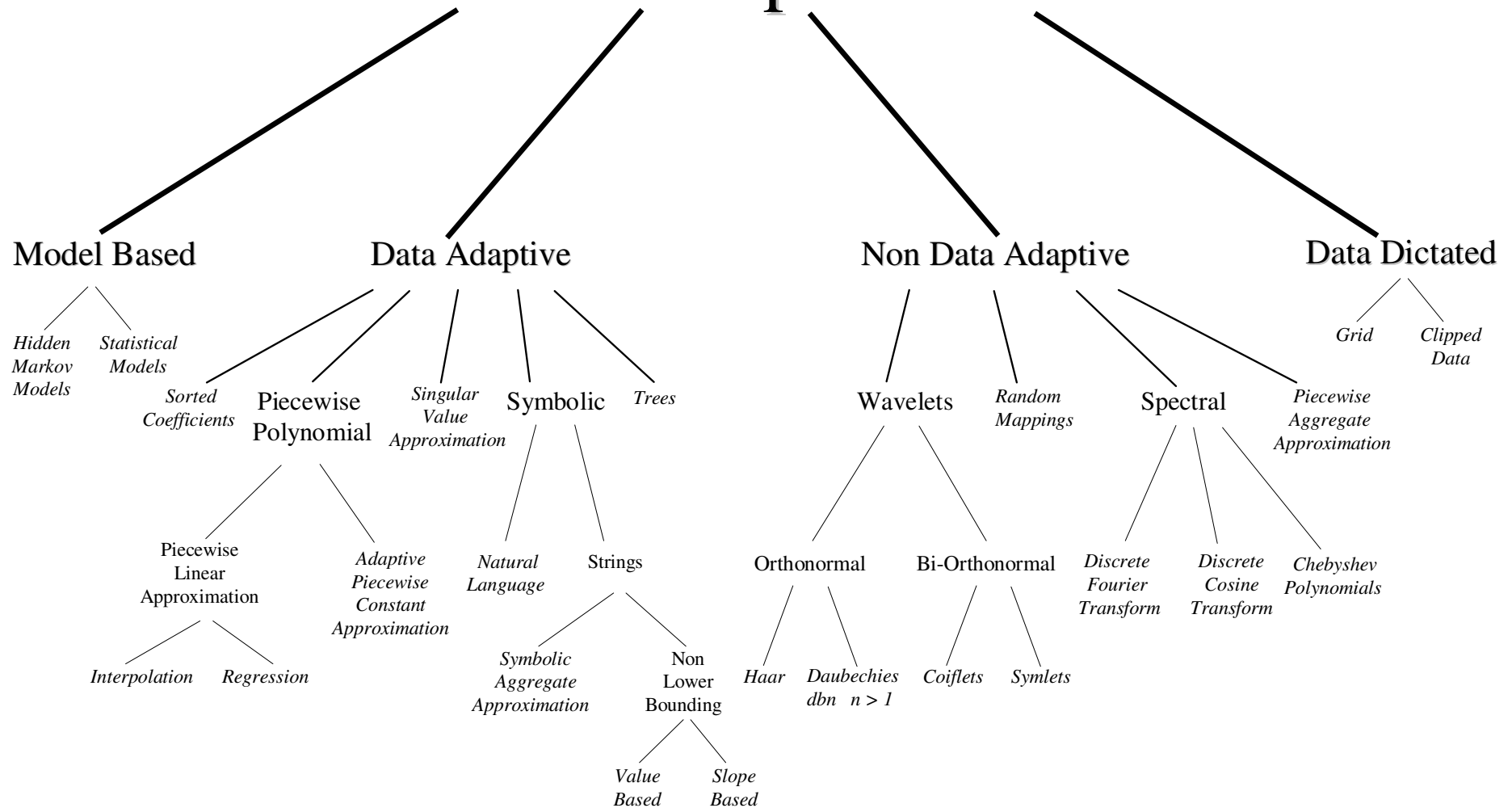
# The Generic Data Mining Algorithm

- Create an *approximation* of the data, which will fit in main memory, yet retains the essential features of interest
- Approximately solve the problem at hand in main memory
- Make (hopefully very few) accesses to the original data on disk to confirm the solution obtained in Step 2, or to modify the solution so it agrees with the solution we would have obtained on the original data

But which *approximation* should we use?



# Time Series Representations



# The Generic Data Mining Algorithm (revisited)

- Create an *approximation* of the data, which will fit in main memory, yet retains the essential features of interest
- Approximately solve the problem at hand in main memory
- Make (hopefully very few) accesses to the original data on disk to confirm the solution obtained in Step 2, or to modify the solution so it agrees with the solution we would have obtained on the original data

This *only* works if the approximation allows **lower bounding**



Lets take a tour of other time series problems

- Before we do, let us briefly revisit SAX, since it has some implications for the other problems...

# Exploiting Symbolic Representations of Time Series

- One central theme of this tutorial is that *lowerbounding* is a very useful property. (recall the *lower bounds* of DTW /uniform scaling, also recall the importance of lower bounding dimensionality reduction techniques).
- Another central theme is that dimensionality reduction is very important. That's why we spend so long discussing DFT, DWT, SVD, PAA etc.
- Until last year there was no lowerbounding, dimensionality reducing representation of time series. In the next slide, let us think about what it means to have such a representation...



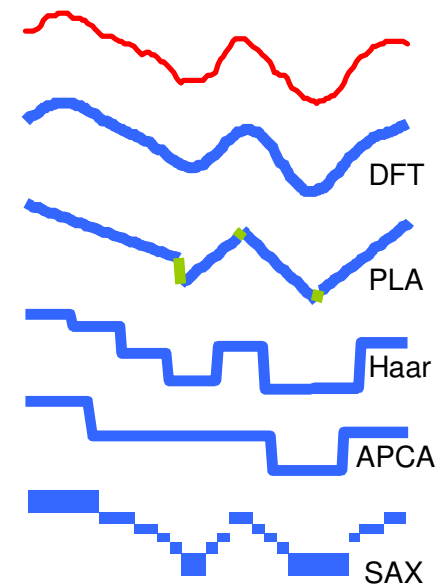
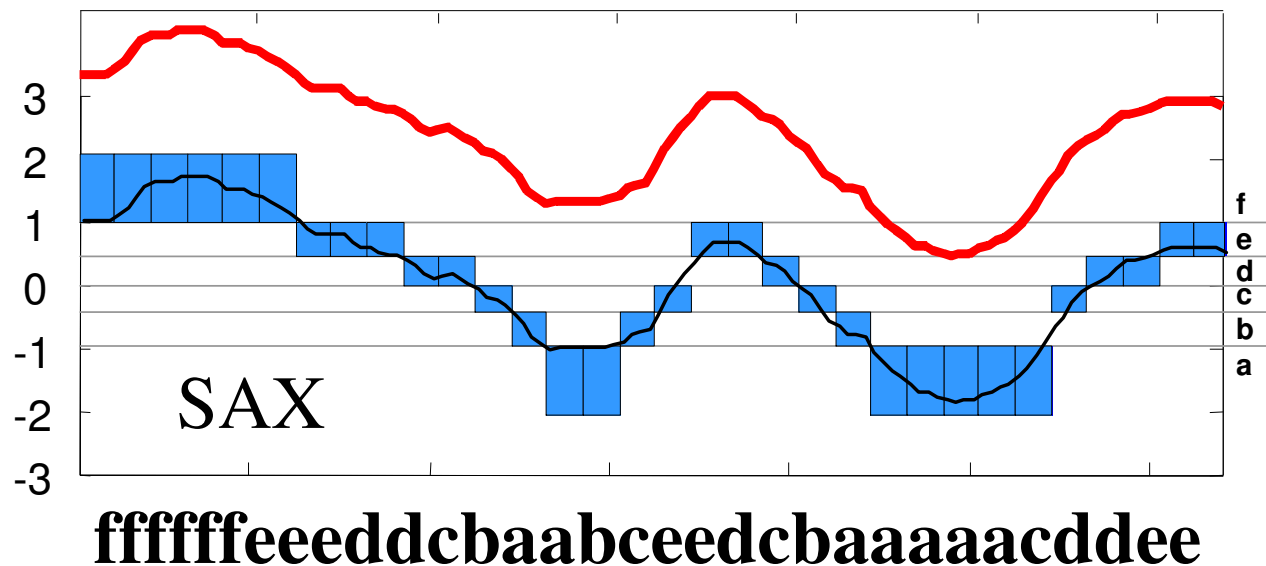
# Exploiting Symbolic Representations of Time Series

- If we had a lowerbounding, dimensionality reducing representation of time series, we could...
- Use data structures that are only defined for discrete data, such as suffix trees.
- Use algorithms that are only defined for discrete data, such as hashing, association rules etc
- Use definitions that are only defined for discrete data, such as Markov models, probability theory
- More generally, we could utilize the vast body of research in text processing and bioinformatics

# Exploiting Symbolic Representations of Time Series

There is now a lower bounding dimensionality reducing time series representation! It is called **SAX** (Symbolic Aggregate ApproXimation)

I expect SAX to have a major impact on time series data mining in the coming years...



# Anomaly (interestingness) detection

We would like to be able to discover surprising (unusual, interesting, anomalous) patterns in time series.

Note that we don't know in advance in what way the time series might be surprising

Also note that “surprising” is very context dependent, application dependent, subjective etc.



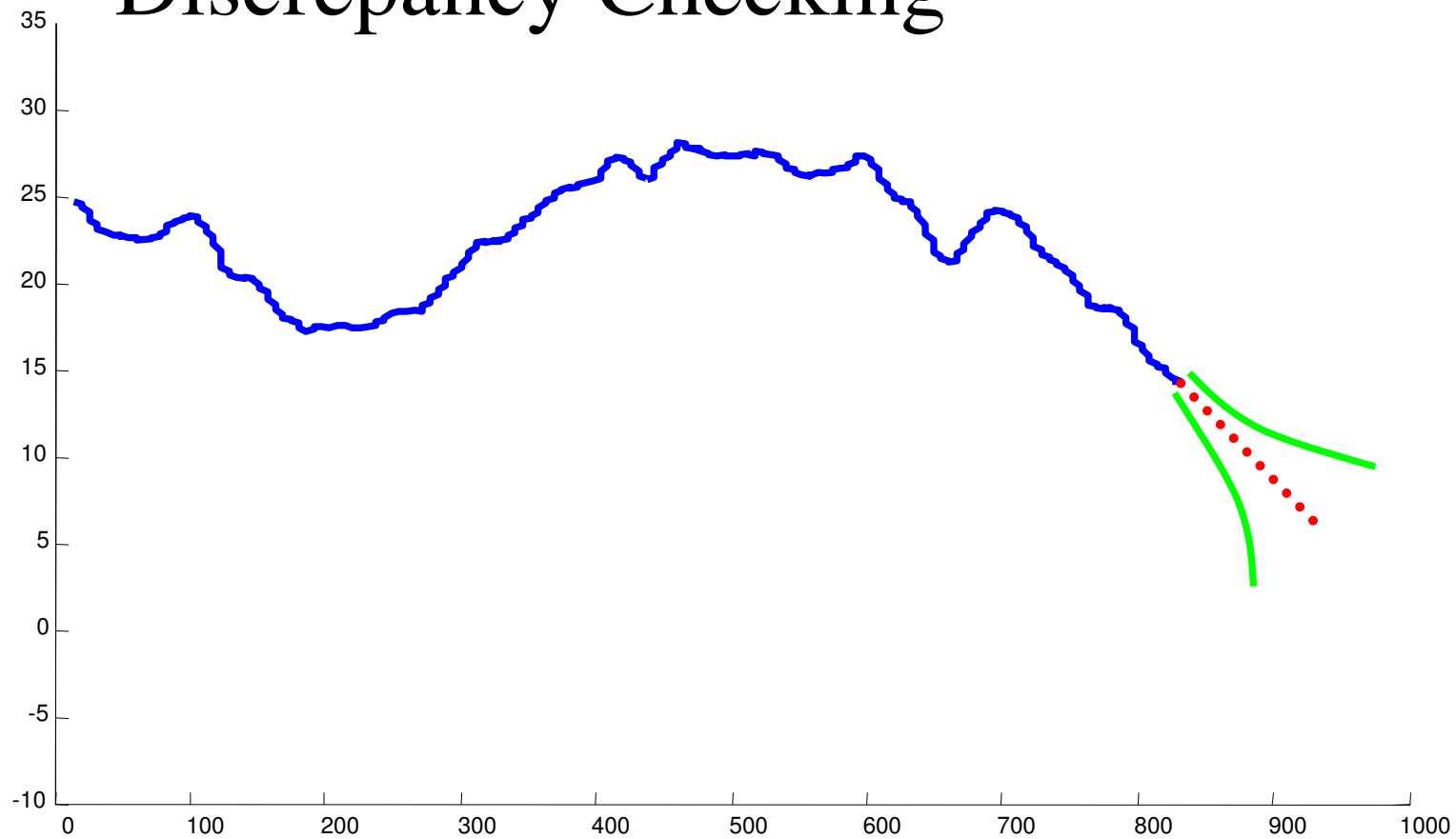
# Simple Approaches I

## Limit Checking



# Simple Approaches II

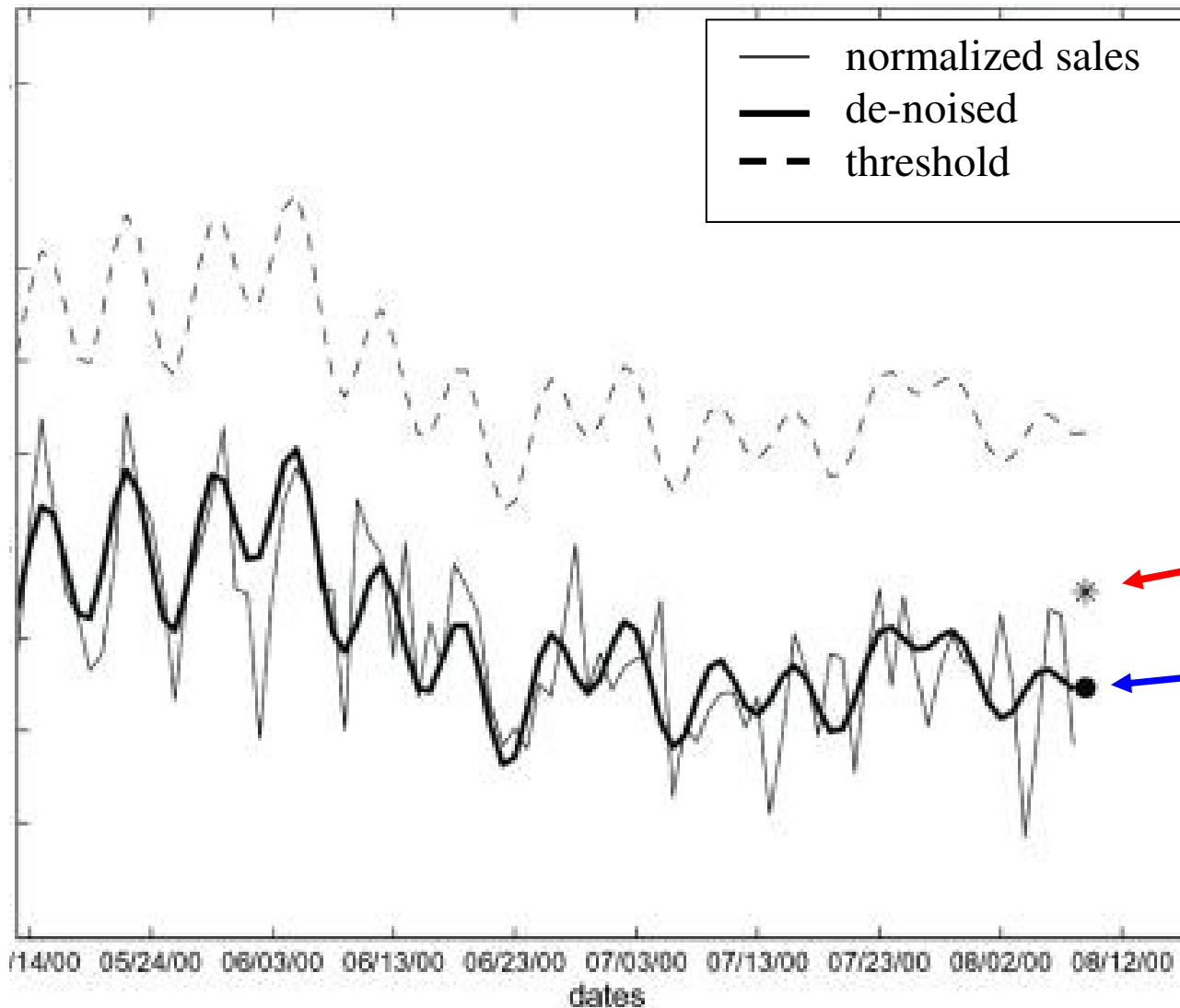
## Discrepancy Checking



# Discrepancy Checking: Example

Early statistical detection of anthrax outbreaks by tracking over-the-counter medication sales

Goldenberg, Shmueli, Caruana, and Fienberg

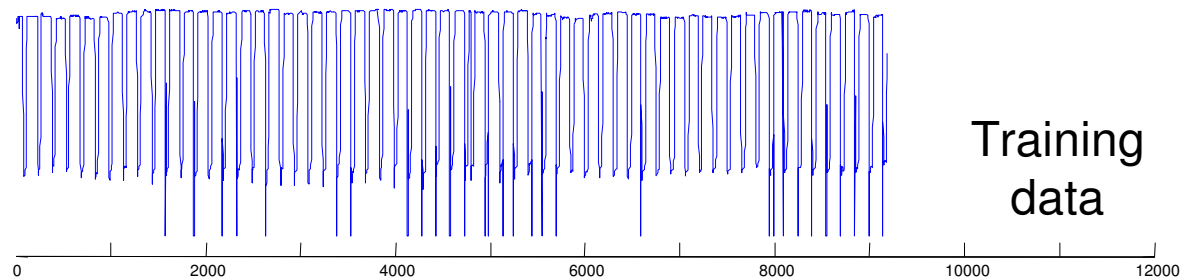


**Actual value**

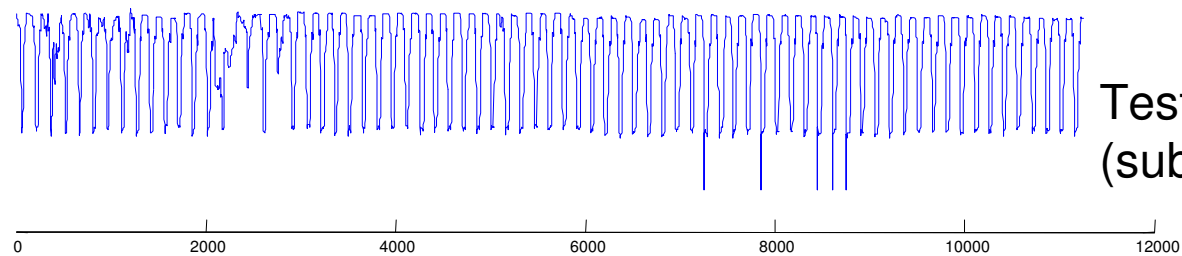
**Predicted value**

The **actual value** is greater than the **predicted value**, but still less than the threshold, so no alarm is sounded.

- Note that this problem has been solved for text strings
- You take a set of text which has been labeled “normal”, you learn a Markov model for it.
- Then, any future data that is not modeled well by the Markov model you annotate as *surprising*.
- Since we have just seen that we can convert time series to text (i.e SAX). Lets us quickly see if we can use Markov models to find surprises in time series...



Training data



Test data  
(subset)

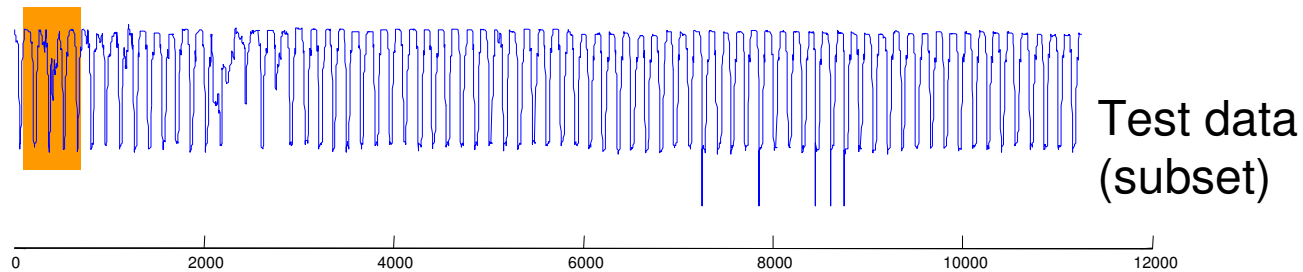
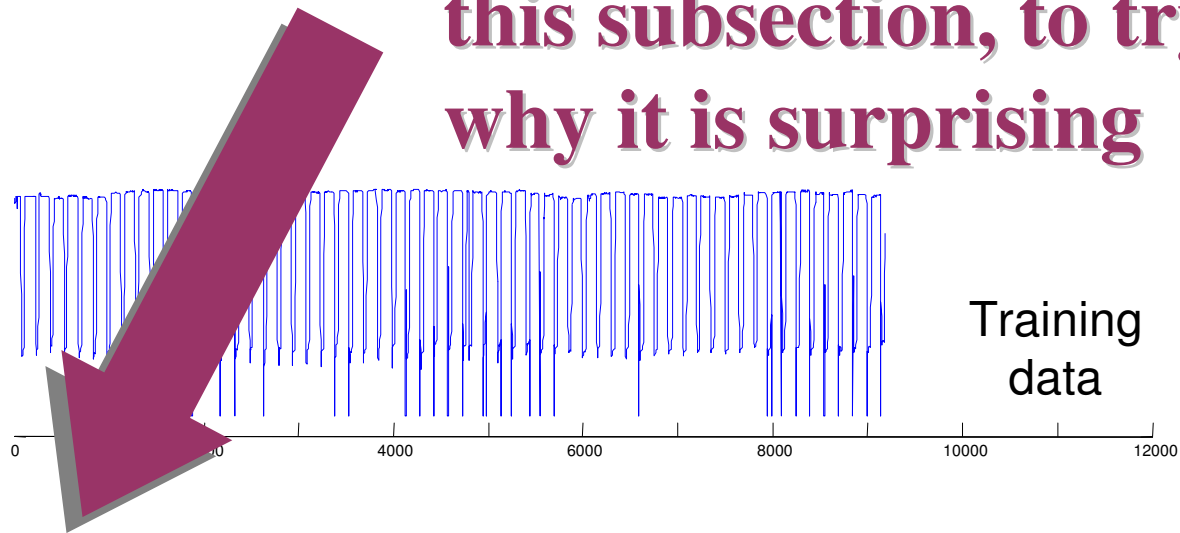
These were converted to the symbolic representation. I am showing the original data for simplicity



Markov model  
surprise



**In the next slide we will zoom in on  
this subsection, to try to understand  
why it is surprising**

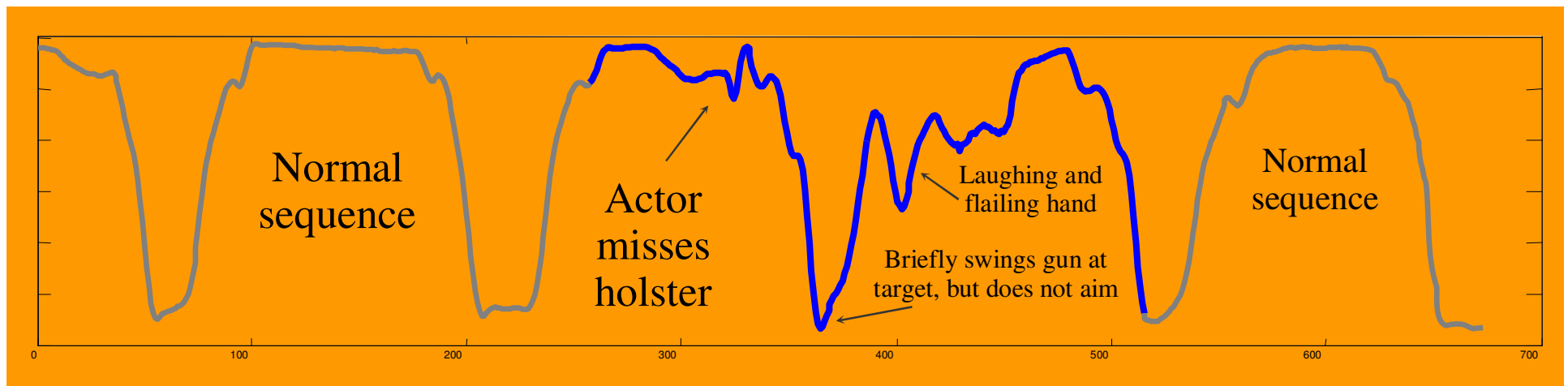




Normal  
Time Series



Surprising  
Time Series



# Anomaly (interestingness) detection

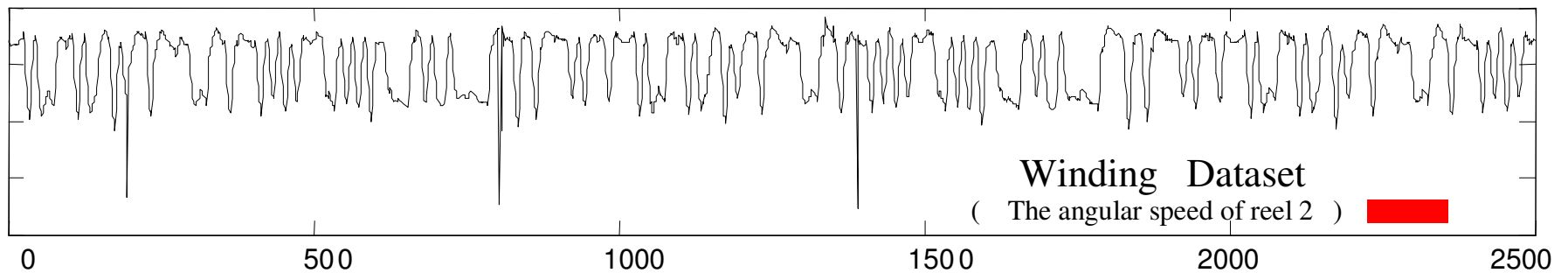
In spite of the nice example in the previous slide, the anomaly detection problem is wide open.


How can we find interesting patterns...

- Without (or with very few) false positives...
- In truly massive datasets...
- In the face of concept drift...
- With human input/feedback...
- With annotated data...

# Time Series Motif Discovery

(finding repeated patterns)

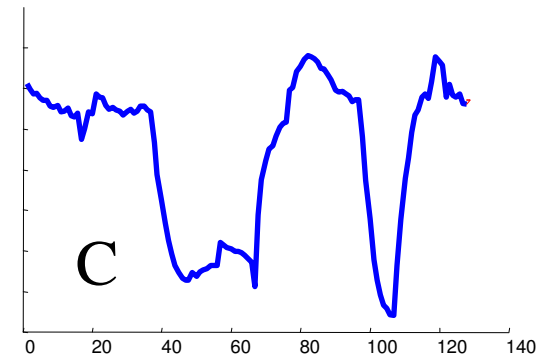
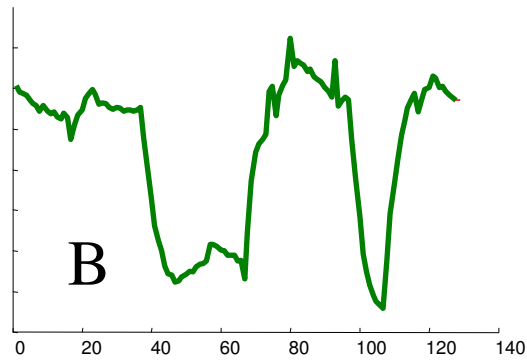
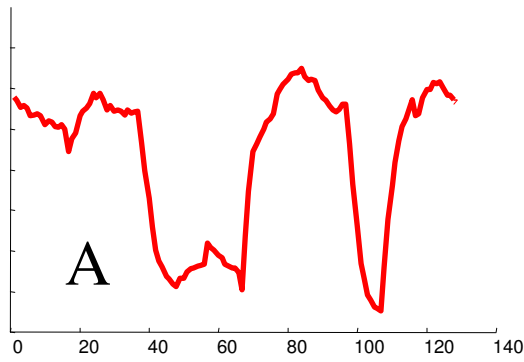
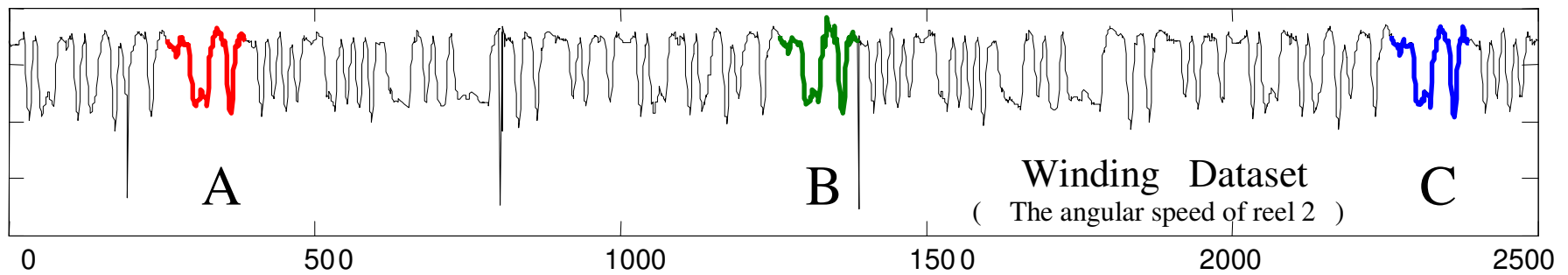


Are there any repeated patterns, of about this length  in the above time series?



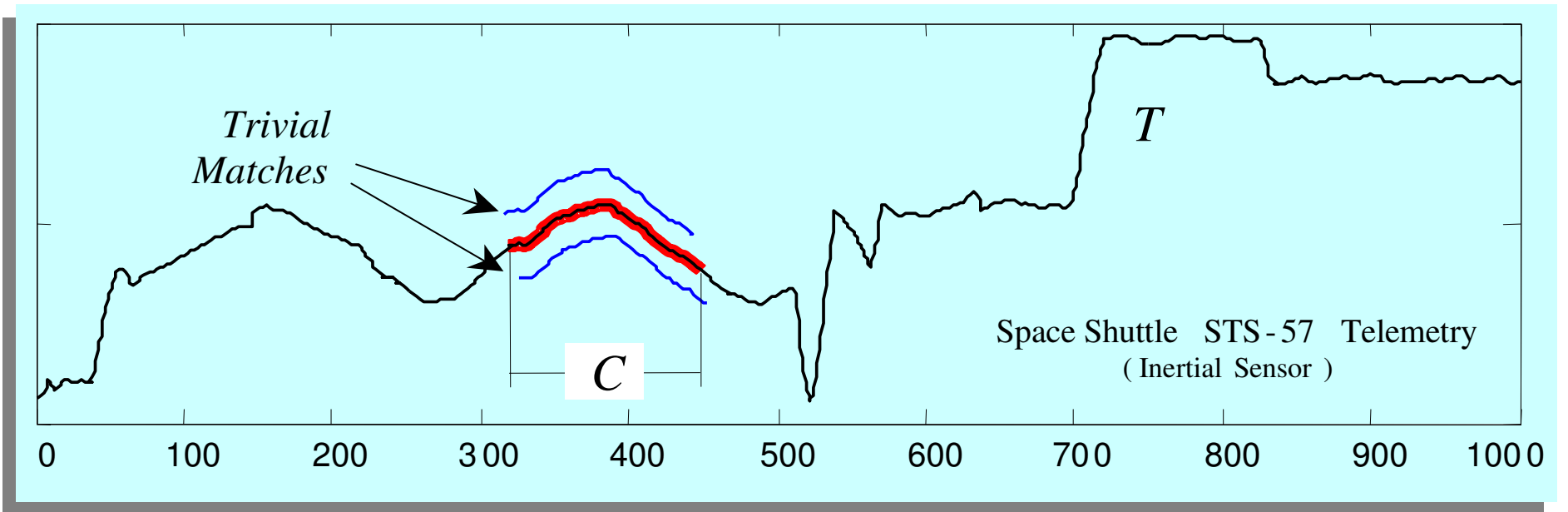
# Time Series Motif Discovery

(finding repeated patterns)



# Why Find Motifs?

- Mining **association rules** in time series requires the discovery of motifs. These are referred to as *primitive shapes* and *frequent patterns*.
- Several time series **classification algorithms** work by constructing typical prototypes of each class. These prototypes may be considered motifs.
- Many time series **anomaly/interestingness detection** algorithms essentially consist of modeling normal behavior with a set of typical shapes (which we see as motifs), and detecting future patterns that are dissimilar to all typical shapes.
- In **robotics**, Oates et al., have introduced a method to allow an autonomous agent to generalize from a set of qualitatively different *experiences* gleaned from sensors. We see these “*experiences*” as motifs.
- In **medical data mining**, Caraca-Valente and Lopez-Chavarrias have introduced a method for characterizing a physiotherapy patient’s recovery based of the discovery of *similar patterns*. Once again, we see these “*similar patterns*” as motifs.
- **Animation and video capture...** (Tanaka and Uehara, Zordan and Celly)



**Definition 1. Match:** Given a positive real number  $R$  (called *range*) and a time series  $T$  containing a subsequence  $C$  beginning at position  $p$  and a subsequence  $M$  beginning at  $q$ , if  $D(C, M) \leq R$ , then  $M$  is called a *matching* subsequence of  $C$ .

**Definition 2. Trivial Match:** Given a time series  $T$ , containing a subsequence  $C$  beginning at position  $p$  and a matching subsequence  $M$  beginning at  $q$ , we say that  $M$  is a *trivial match* to  $C$  if either  $p = q$  or there does not exist a subsequence  $M'$  beginning at  $q'$  such that  $D(C, M') > R$ , and either  $q < q' < p$  or  $p < q' < q$ .

**Definition 3.  $K$ -Motif( $n, R$ ):** Given a time series  $T$ , a subsequence length  $n$  and a range  $R$ , the most significant motif in  $T$  (hereafter called the *1-Motif*( $n, R$ )) is the subsequence  $C_1$  that has highest count of non-trivial matches (ties are broken by choosing the motif whose matches have the lower variance). The  $K^{\text{th}}$  most significant motif in  $T$  (hereafter called the  *$K$ -Motif*( $n, R$ )) is the subsequence  $C_K$  that has the highest count of non-trivial matches, and satisfies  $D(C_K, C_i) > 2R$ , for all  $1 \leq i < K$ .

# OK, we can define motifs, but how do we find them?

The obvious brute force search algorithm is just too slow...

The most reference algorithm is based on a *hot* idea from bioinformatics, *random projection*\* and the fact that SAX allows use to lower bound discrete representations of time series.

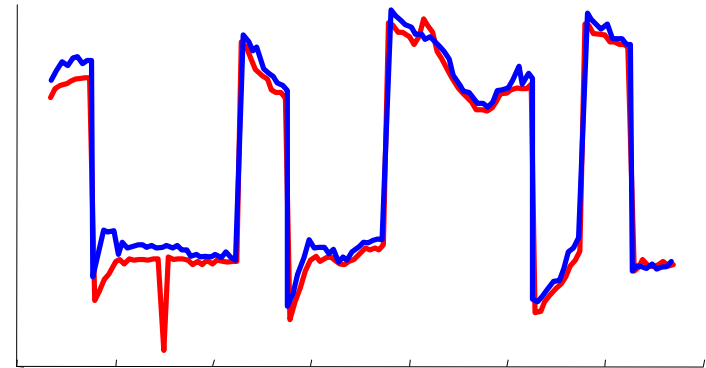
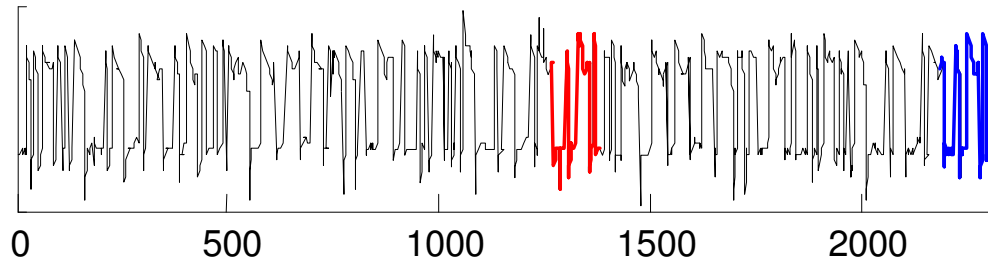
\* J Buhler and M Tompa. *Finding motifs using random projections*. In RECOMB'01. 2001.



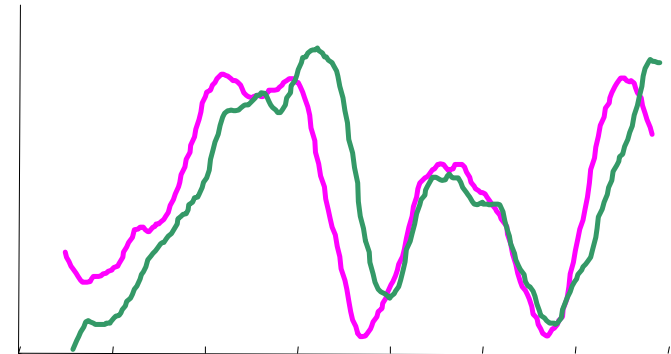
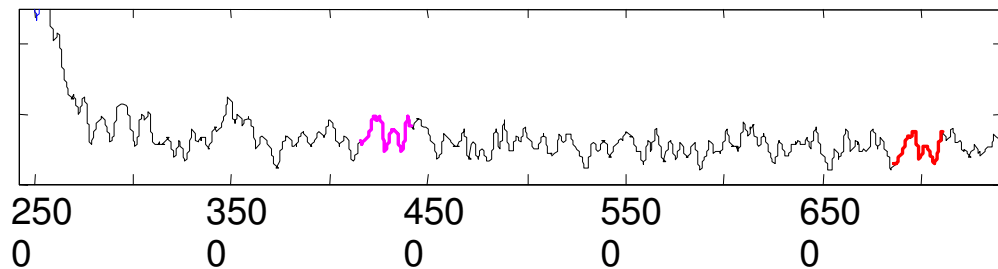


# Some Examples of Real Motifs

Motor 1 (DC Current)



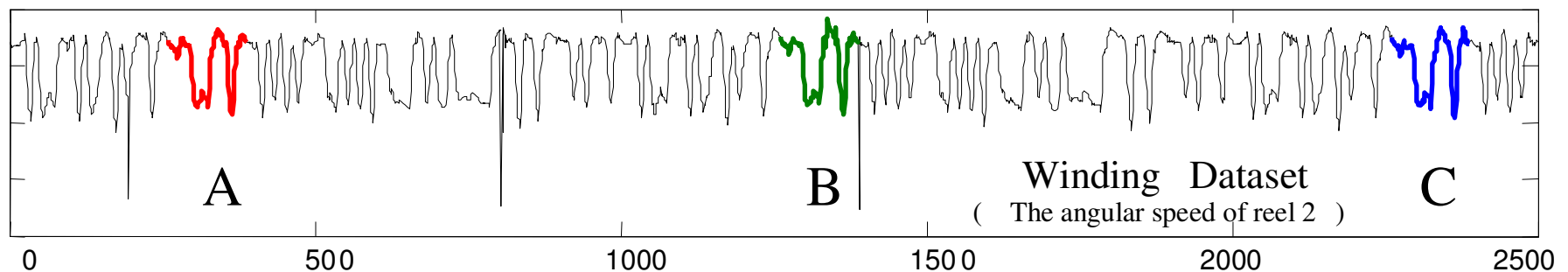
Astrophysics (Photon Count)



# Motifs Discovery Challenges

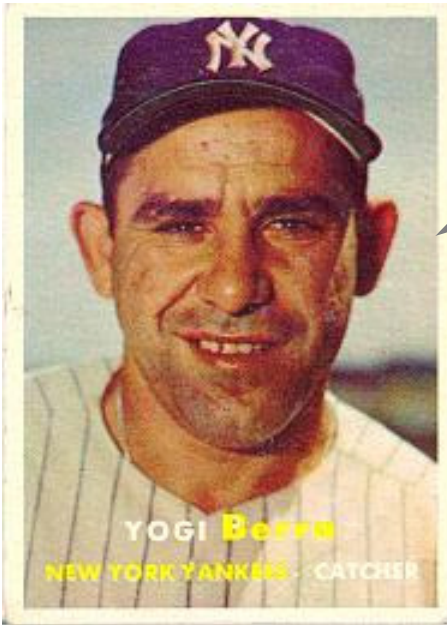
How can we find motifs...

- Without having to specify the length/other parameters
- In massive datasets
- While ignoring “background” motifs (ECG example)
- Under time warping, or uniform scaling
- While assessing their significance



Finding these 3 motifs requires about 6,250,000 calls to the Euclidean distance function

# Time Series Prediction



Yogi Berra  
1925 -

Prediction is hard, especially about the future

There are two kinds of time series prediction

- **Black Box:** Predict tomorrow's electricity demand, given *only* the last ten years electricity demand.
- **White Box (side information ):** Predict tomorrow's electricity demand, given the last ten years electricity demand *and* the weather report, *and* the fact that the world cup final is on and...

# Black Box Time Series Prediction

- A paper in SIGMOD 04 claims to be able to get better than 60% accuracy on black box prediction of financial data (random guessing should give about 50%). The authors agreed to test blind on a dataset which I gave them, they again got more than 60%. But I gave them quantum-mechanical random walk data!
- A paper in SIGKDD in 1998 did black box prediction using association rules, more than twelve papers extended the work... but then it was proved that the approach *could* not work\*!

Nothing I have seen suggests to me that any non-trivial contributions have been made to this problem. (To be fair, it is a *very* hard problem)