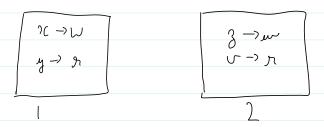
3.1. Urn 1 contains x white and y red balls. Urn 2 contains z white and v red balls. A ball is chosen at random from urn 1 and put into urn 2. Then a ball is chosen at random from urn 2. What is the probability that this ball is white?



$$P(w \text{ from 2}) = P(w \text{ from 1}) \times P(w \text{ from new 2}) + P(x \text{ from 1}) \times P(w \text{ from new 2})$$

$$= \frac{x}{x + y + 1} + \frac{y}{x + y + 1} \times \frac{3}{x + y + 1}$$

$$= \frac{x(3+1) + 3y}{(x+y)(3+y+1)} + \frac{3y}{x + y + 1}$$

- 3.2. Two defective tubes get mixed up with two good ones. The tubes are tested, one by one, until both defectives are found.
- (a) What is the probability that the last defective tube is obtained on the second test?
 - (b) What is the probability that the last defective tube is obtained on the third test?
 - (c) What is the probability that the last defective tube is obtained on the fourth test?
 - (d) Add the numbers obtained for (a), (b), and (c) above. Is the result surprising?

(a) That means both first and second tubes are defective

$$P(firrt defective) = 2/4 = 1/2$$

$$P(recond defective) = \frac{1}{2} \times \frac{1}{3} = \frac{1}{6}$$

(D) Last defective found on 3rd test

This means that in 1st and 2nd texts we have already found one defective and one non defective tibe.

We can have following cores possible

(ant defective found on 4th test

Following wares we possible

$$= \frac{3}{6} = \frac{1}{2} Am$$

(a) On adding results of a, b and a we get

$$\frac{1}{3} + \frac{1}{2} + \frac{1}{4} = \frac{2+3+1}{4} = 1$$

$$\frac{1}{3} + \frac{1}{2} + \frac{1}{6} = \frac{2+3+1}{6} = 1$$

3.3. A box contains 4 bad and 6 good tubes. Two are drawn out together. One of them is tested and found to be good. What is the probability that the other one is also good?

- 3.4. In the above problem the tubes are checked by drawing a tube at random, testing it and repeating the process until all 4 bad tubes are located. What is the probability that the fourth bad tube will be located
 - (a) on the fifth test?
 - (b) on the tenth test?

6 B B B B 6/10
$$\times$$
 4/4 \times 3/8 \times 2/7 \times 1/6
B B B B 4/10 \times 6/4 \times 3/8 \times 2/7 \times 1/6
B B B G B B 4/10 \times 3/4 \times 6/5 \times 1/6
B B B G B 4/10 \times 3/4 \times 1/6
B B B G B 4/10 \times 3/4 \times 1/6

A \times 4 \times 4 \times 2 \times 2 \times 1 - 2

105 Ams

3.5. Suppose that A and B are independent events associated with an experiment. If the probability that A or B occurs equals 0.6, while the probability that A occurs equals 0.4, determine the probability that B occurs.