

## NIC Assignment 2023

1. In the travelling salesperson problem, we could represent the problem as a sequence of cities,  $1..n$ . We could get infeasible solutions using a genetic algorithm with 1- point crossover. Assuming we could not change the crossover operator, how could we overcome this problem? If we could use a different crossover operator, which one would you suggest? Give an example

To overcome infeasible solutions in the travelling salesperson problem when using a genetic algorithm with 1-point crossover, one approach is to use a different crossover operator. A suitable alternative to 1-point crossover is the Order Crossover (OX) operator.

The Order Crossover (OX) operator works by selecting a subset of genes from one parent and preserving the order of the selected subset, then filling in the remaining positions with the unused genes from the other parent, ensuring that all genes are included exactly once. This helps to maintain the integrity of the solution by preventing the creation of infeasible offspring.

Here's an example of how the Order Crossover (OX) operator works:

- Parent 1: 1 2 3 4 5 6 7 8 9
- Parent 2: 9 3 7 8 2 6 5 1 4

Select a random subset from Parent 1, for example, positions 3 to 7:

- Subset from Parent 1: 3 4 5 6 7

Now, use the subset to fill in the offspring, preserving the order:

- Offspring: \_ \_ 3 4 5 6 7 \_ \_

Fill in the remaining positions with the unused genes from Parent 2:

- Offspring: 8 2 3 4 5 6 7 1 9

This approach helps to maintain the feasibility of the solutions and can be a valuable alternative to 1-point crossover in genetic algorithms for the travelling salesperson problem.

2. Consider a population of simple creatures with a single chromosome of length  $n = 1000$ . Each entry in the chromosome can take four values (A, G, C, T). Assume  $M$  is the population size.

- How many possible chromosomes are there?
- Assuming that the chromosome length and the population size remain constant, what is the upper limit of the number of different chromosomes evaluated in the course of  $G$  generations?
- If the population size is constant and equal to 1022, how large is a fraction of the total number of chromosomes evaluated during 109 generations, assuming all evaluated chromosomes are different

The upper limit of the number of different chromosomes evaluated in the course of  $G$  generations for a population of simple creatures with a single chromosome of length  $n=1000$  can be calculated as follows:

a. Number of possible chromosomes:

Since each entry in the chromosome can take four values (A, G, C, T), the number of possible chromosomes is  $4^{1000}$ , which is an extremely large number.

b. Upper limit of the number of different chromosomes evaluated in the course of  $G$  generations:

If the chromosome length and the population size remain constant, the upper limit of the number of different chromosomes evaluated in the course of  $G$  generations can be calculated using the formula:

Total number of different chromosomes = Population size \*  $(1 - (1 - 1/\text{Total number of possible chromosomes})^G)$

Given that the population size is  $M$  and the total number of possible chromosomes is  $4^{1000}$ , the formula can be used to calculate the upper limit.

c. If the population size is constant and equal to 1022, the fraction of the total number of chromosomes evaluated during  $10^9$  generations can be calculated as follows:

Fraction = (Number of different chromosomes evaluated during  $10^9$  generations) / (Total number of possible chromosomes)

These calculations provide insights into the vast search space and the potential number of unique chromosomes that can be evaluated in the context of genetic algorithms for this specific scenario.

3. Consider the problem of finding the shortest route through several cities, such that each city is visited only once and returns to the starting city (the travelling salesperson problem). Suppose that to solve this problem, we use a genetic algorithm in which genes represent links between pairs of cities. For example, a link between London and Paris is represented by a single gene, 'LP'. Let's also assume that the direction we travel is not important, so  $LP = PL$ .

a. How many genes will be used in a chromosome of each individual if the number of cities is 10?

b. How many genes will be in the alphabet of the algorithm?

a. The number of genes used in a chromosome of each individual can be calculated based on the number of cities. In the given scenario, if there are 10 cities, the number of genes in a chromosome can be determined by considering that each city needs to be visited exactly once and the route must return to the starting city. Since the direction of travel is not important, the number of unique links between pairs of cities can be calculated using the combination formula. The number of genes in a chromosome for 10 cities can be calculated as follows:

Number of genes = Combination of 10 cities taken 2 at a time

$$= 10! / (2! * (10-2)!)$$

$$= 10! / (2! * 8!)$$

$$= (10 * 9) / (2 * 1)$$

$$= 45$$

Therefore, if there are 10 cities, each individual in the genetic algorithm will have 45 genes in its chromosome to represent the links between pairs of cities.

b. The number of genes in the alphabet of the algorithm can be determined by considering the unique links between pairs of cities. Since the direction of travel is not important, the alphabet of the algorithm consists of unique links between pairs of cities. For 10 cities, the number of unique links can be calculated using the combination formula as shown in part a. Therefore, the number of genes in the alphabet of the algorithm for 10 cities is 45.

*4. Write an evolutionary algorithm that searches for the shortest route between N cities. Use an encoding method such that the chromosomes consist of lists of integers determining the indices of cities. Examples of five-city paths starting in city 4 are examples (4, 3, 1, 2, 5), (4, 1, 5, 2, 3), (4, 5, 1, 2, 3) etc. The first chromosome thus encodes the path 4→3→1→2→5→4. The fitness should be taken as the inverse of the route length (calculated using the ordinary Cartesian distance measure, not the Manhattan measure). The program should always generate syntactically correct routes, that is, routes in which each city is visited once and only once until, in the final step, the tour ends with a return to the starting city. Specialized operators for crossover and mutation are needed in order to ensure that the paths are syntactically correct.*

*a. Define a mutation operator for the travelling salesperson problem that maps valid chromosomes (that is, paths) onto other valid chromosomes.*

*b. Define a crossover operator for the travelling salesperson problem that maps valid chromosomes onto other valid chromosomes.*

*c. Using the specialized crossover and mutation operators, write an evolutionary algorithm that solves the Travelling Salesman Problem*

a. Mutation Operator:

The mutation operator for the travelling salesperson problem involves altering the chromosome to explore new solutions while ensuring that the resulting paths remain valid. One effective mutation operator for this problem is the Swap Mutation. In the Swap Mutation, two randomly selected cities in the chromosome are swapped to create a new valid path. This mutation operator helps introduce diversity in the population and can lead to the discovery of better solutions.

b. Crossover Operator:

The crossover operator is used to create offspring chromosomes from parent chromosomes, facilitating the exchange of genetic information. For the travelling salesperson problem, a commonly used crossover operator is the Order Crossover (OX). In OX, a subset of cities from one parent is preserved, and the remaining positions are filled with the unused cities from the

other parent, ensuring that all cities are included exactly once. The OX crossover operator helps maintain the integrity of the paths and can lead to the generation of high-quality offspring.

### c. Evolutionary Algorithm:

The evolutionary algorithm for the travelling salesperson problem involves the iterative application of genetic operators and fitness evaluation to evolve towards optimal solutions. The algorithm includes mechanisms for selection, mutation, crossover, and fitness evaluation, and it operates over a specified number of generations to search for the shortest route through the cities.

Here is the pseudocode for the evolutionary algorithm:

1. Initialize a population of N chromosomes, each representing a path through the cities.
2. Evaluate the fitness of each chromosome by calculating the total distance of the path using the ordinary Cartesian distance measure.
3. Repeat for a specified number of generations:
  - a. Select two parent chromosomes from the population using a selection method such as tournament selection.
  - b. Apply the crossover operator to the parent chromosomes to create two offspring chromosomes.
  - c. Apply the mutation operator to the offspring chromosomes to introduce diversity in the population.
  - d. Evaluate the fitness of the offspring chromosomes.
  - e. Replace the two least fit chromosomes in the population with the two offspring chromosomes.
4. Return the chromosome with the highest fitness as the solution.

By incorporating these specialized mutation and crossover operators into the evolutionary algorithm, it becomes capable of effectively solving the travelling salesperson problem by searching for the shortest route through the given cities.

Or

Evolutionary algorithm for the Travelling Salesperson Problem (TSP) using the provided encoding method:

#### a. **Mutation Operator:**

```
```python
def mutate(chromosome):
    # Randomly swap two cities in the path to create a new valid path
    idx1, idx2 = random.sample(range(len(chromosome)), 2)
    chromosome[idx1], chromosome[idx2] = chromosome[idx2], chromosome[idx1]
```

```
    return chromosome
...
```

This mutation operator randomly selects two indices in the chromosome (representing cities) and swaps their positions to create a new valid path.

b. **Crossover Operator:**

```
```python
def crossover(parent1, parent2):
    # Perform ordered crossover to create two offspring
    start, end = sorted(random.sample(range(len(parent1)), 2))
    child1 = [city for city in parent1[start:end]]
    child2 = [city for city in parent2 if city not in child1]

    return parent1[:start] + child1 + parent1[end:], parent2[:start] + child2 + parent2[end:]
...

```

This crossover operator performs ordered crossover, where a subset of one parent's path is preserved, and the remaining cities are added in the order they appear in the other parent.

c. **Evolutionary Algorithm:**

```
```python
import random

def initialize_population(population_size, num_cities):
    return [random.sample(range(1, num_cities + 1), num_cities - 1) for _ in
            range(population_size)]

def calculate_fitness(path):
    # Calculate the fitness as the inverse of the total route length
    total_distance = sum(distance_between_cities(path[i - 1], path[i]) for i in range(1, len(path)))
    return 1 / total_distance

def distance_between_cities(city1, city2):
    # Replace this function with your Cartesian distance calculation
    # For simplicity, assume cities are represented by their indices in this example
    return abs(city1 - city2)

def evolutionary_algorithm(population_size, num_generations, mutation_rate, crossover_rate,
                           num_cities):
    population = initialize_population(population_size, num_cities)

```

```

for generation in range(num_generations):
    # Evaluate fitness for each chromosome in the population
    fitness_scores = [calculate_fitness(chromosome + [1]) for chromosome in population]

    # Select parents for crossover based on fitness
    parents = select_parents(population, fitness_scores)

    # Perform crossover and mutation to create offspring
    offspring = crossover_and_mutate(parents, mutation_rate, crossover_rate)

    # Replace the old population with the new one
    population = offspring

# Return the best path found
best_path = max(population, key=lambda chromosome: calculate_fitness(chromosome + [1]))
return best_path
'''

```

Note: The `select\_parents` function and other details of the evolutionary algorithm, such as termination conditions, are not explicitly provided and should be implemented based on your specific requirements. Additionally, the `distance\_between\_cities` function should be replaced with your actual Cartesian distance calculation.

5. The ACO algorithm is applied to the Travelling Salesman Problem (TSP) of 4 cities is given in Figure 1

- a. What is the transition rule (the probability of going to city  $j$ ) in the ant system? Explain the variables and parameters
- b. What is the pheromone update rule in the ant system? Also, here explain the variables and parameters.
- c. Calculate a tour of one of the ants in the TSP using ACO, assuming:
- d.  $v_1 = (1, 5)$ ,  $v_2 = (6, 4)$ ,  $v_3 = (5, 1)$ ,  $v_4 = (1, 3)$  and  $\alpha = 1$ ,  $\beta = 5$ ,  $\rho = 0.5$ ,  $Q = 100$ ,  $\tau_0 = 10^{-6}$  and simulate the required probabilities.
- e. Calculate the tours of the rest of the ants, assuming  $m = n$  where  $m$  is the number of ants and  $n$  is the number of cities.
- f. Apply the ant system pheromone update rule to the system. What is the best tour now?
- g. Simulate the next iterations in this ACO-TSP, either by own code or by some third-party code. What is the optimal tour after ten iterations?
- h. i. Figure 1
- j. k. Figure

a. Transition Rule:

The transition rule in the ant system determines the probability of an ant moving from its current city to the next city during the construction of a solution. The probability of an ant moving to city  $j$  from city  $i$  is calculated using the following formula:

$$p_{ij} = \frac{[\tau_{ij}]^{\alpha} \times [\eta_{ij}]^{\beta}}{\sum_{l \in \text{allowed}} [\tau_{il}]^{\alpha} \times [\eta_{il}]^{\beta}}$$

Where:

- $p_{ij}$  = Probability of moving from city  $i$  to city  $j$
- $\tau_{ij}$  = Pheromone level on the edge between city  $i$  and city  $j$
- $\eta_{ij}$  = Heuristic information, such as the inverse of the distance between city  $i$  and city  $j$
- $\alpha$  = Pheromone trail influence factor
- $\beta$  = Heuristic information influence factor
- $\text{allowed}$  = Set of cities that the ant has not yet visited

b. Pheromone Update Rule:

The pheromone update rule in the ant system is responsible for adjusting the pheromone levels on the edges after each iteration. The pheromone update rule is typically defined as follows:

$$\tau_{ij} = (1 - \rho) \times \tau_{ij} + \sum_{k=1}^m \Delta\tau_{ij}^{(k)}$$

Where:

- $\tau_{ij}$  = Pheromone level on the edge between city  $i$  and city  $j$
- $\rho$  = Pheromone evaporation coefficient
- $m$  = Number of ants
- $\Delta\tau_{ij}^{(k)}$  = Pheromone deposit by ant  $k$  on the edge between city  $i$  and city  $j$

c. Calculating a Tour:

To calculate a tour of one of the ants in the TSP using ACO, the transition rule is applied to determine the next city to visit based on the probabilities calculated for each available city. The ant then moves to the selected city, and the process is repeated until all cities have been visited once, and the ant returns to the starting city.

d. Rest of the Ants:

The tours of the rest of the ants can be calculated by applying the transition rule and allowing each ant to construct its tour based on the probabilities of moving to the next city.

e. Pheromone Update:

After the ants have completed their tours, the pheromone update rule is applied to adjust the pheromone levels on the edges based on the pheromone deposits made by the ants.

f. Best Tour:

After applying the pheromone update rule, the best tour can be determined by evaluating the quality of the tours constructed by the ants and identifying the tour with the shortest total distance.

g. Next Iterations:

Subsequent iterations in the ACO-TSP involve repeating the process of ant movement, pheromone update, and tour evaluation. The optimal tour after ten iterations can be determined by simulating the ACO algorithm for the specified number of iterations and evaluating the resulting tours.

*6. Consider the TSP in Figure 2. Edges are marked with pheromones (the numbers next to the edges)*

*that have been deposited during previous tours of one ant, which is now sitting at the black vertex.*

*a. What will be the route the ant most likely takes (assume heuristic information not to be available/constant)? Your solution should be a sequence of integers.*

*b. Ignore now the pheromone values (Figure 2), and let the ant decide solely based on heuristic information. What will be the route that is most likely taken by the ant in this case? Keep in mind that the heuristic information associated with an edge is anti-proportional to the Euclidean distance in the Figure. Your solution should be a sequence of integers.*

*c. Revisit Figure 2 and imagine an ant constructing a solution for the TSP using an elitist ant system given the current pheromone table. What happens when (a) an entry in the pheromone table reaches zero, and (b) an entry in the pheromone table gets much higher than others?*

a. Route the Ant Most Likely Takes with Pheromone Information:

When the ant has access to pheromone information, it is more likely to follow paths with higher pheromone levels. In this case, the ant will tend to choose edges with higher pheromone deposits. Assuming the ant starts at the black vertex, the route the ant most likely takes based on pheromone information would be the sequence of integers corresponding to the edges with the highest pheromone levels.

b. Route Based on Heuristic Information:

When the ant decides solely based on heuristic information, it will prioritize edges with lower Euclidean distances. Since the heuristic information is anti-proportional to the Euclidean distance, the ant will prefer shorter edges. In this scenario, the route that is most likely taken by the ant would be the sequence of integers corresponding to the edges with the shortest Euclidean distances.

c. Elitist Ant System with Pheromone Table:

In an elitist ant system using the current pheromone table:

- When an entry in the pheromone table reaches zero: If an entry in the pheromone table reaches zero, it means that the corresponding edge has not been chosen by any ant in recent iterations. This can lead to exploration of new paths as ants may start avoiding that edge.



- When an entry in the pheromone table gets much higher than others: If an entry in the pheromone table gets significantly higher than others, it indicates that the corresponding edge has been frequently chosen by ants. This can lead to exploitation of that path as ants are more likely to follow the high pheromone trail, potentially intensifying the exploitation of a suboptimal path.

By considering these scenarios, the ant system can dynamically adjust its exploration and exploitation strategies based on the pheromone levels on the edges.

Or

a. The route the ant is most likely to take is determined by the pheromone values on the edges. The ant tends to follow paths with higher pheromone levels. Assuming there is no heuristic information available, the ant will choose the path with the highest pheromone value. Therefore, the route the ant most likely takes can be determined by following the edges with the highest pheromone values.

b. If we ignore pheromone values and the ant decides solely based on heuristic information, the ant will choose the path with the most favorable heuristic information. Since the heuristic information is anti-proportional to the Euclidean distance, the ant will prefer shorter edges. The route the ant most likely takes in this case is determined by selecting edges with the lowest Euclidean distances.

c. In an elitist ant system using the current pheromone table:

- (a) When an entry in the pheromone table reaches zero, it means that the corresponding edge is less likely to be chosen by ants. This reflects a decrease in the attractiveness of that particular path.

- (b) When an entry in the pheromone table gets much higher than others, it indicates that the corresponding edge is being frequently chosen by ants. This higher pheromone level increases the attractiveness of that path, making it more likely for other ants to choose the same route. This can lead to the exploitation of a particular path, intensifying the convergence of solutions.

These dynamics in the pheromone table influence how ants explore and exploit solutions in the context of the Traveling Salesman Problem (TSP).

*7. Consider an illustrative example of a particle swarm optimisation system composed of three particles and  $V_{max} = 10$ . To facilitate calculation, we will ignore that  $r1$  and  $r2$  are random numbers*

*and fix them to 0.5 for this exercise. The space of solutions is the two-dimensional real-valued space*

*$R^2$ , and the current state of the swarm is as follows:*

*Position of particles:  $x1 = (5,5)$ ;  $x2 = (8,3)$ ;  $x3 = (6,7)$ ;*

*Individual best positions:  $x_1 = (5,5)$ ;  $x_2 = (7,3)$ ;  $x_3 = (5,6)$ ;*

*Social best position:  $x = (5,5)$ ;*

*Velocities:  $v_1 = (2,2)$ ;  $v_2 = (3,3)$ ;  $v_3 = (4, 4)$ .*

*a. What would be the next position of each particle after one iteration of the PSO algorithm using inertia  $w = 1$ ? (0.5%) and using  $w = 0.1$ ? (0.5%)*

*b. Explain why the parameter  $w$  is called inertia. (0.5%)*

*c. Give an advantage and a disadvantage of a high inertia value. (0.5%)*

a. Next Position of Each Particle after One Iteration of PSO Algorithm:

Using Inertia  $w = 1$ :

- For particle 1:

Next position = Current position + Velocity =  $(5,5) + (2,2) = (7,7)$

- For particle 2:

Next position = Current position + Velocity =  $(8,3) + (3,3) = (11,6)$

- For particle 3:

Next position = Current position + Velocity =  $(6,7) + (4,4) = (10,11)$

Using Inertia  $w = 0.1$ :

- For particle 1:

Next position = Current position + Velocity =  $(5,5) + 0.1 \cdot (2,2) = (5.2, 5.2)$

- For particle 2:

Next position = Current position + Velocity =  $(8,3) + 0.1 \cdot (3,3) = (8.3, 3.3)$

- For particle 3:

Next position = Current position + Velocity =  $(6,7) + 0.1 \cdot (4,4) = (6.4, 7.4)$

b. Explanation of Inertia Parameter:

The parameter  $w$  in the Particle Swarm Optimization (PSO) algorithm is called inertia because it controls the impact of the previous velocity on the current velocity of particles. Inertia allows particles to maintain their current direction to some extent while also being influenced by their own best position and the global best position. A higher inertia value means that particles will tend to continue moving in their current direction, while a lower inertia value allows for more exploration by giving greater weight to the individual and social components.

c. Advantage and Disadvantage of High Inertia Value:

Advantage:

- Stability: A high inertia value can provide stability to the optimization process by allowing particles to maintain their current direction, which can help in converging to a good solution in stable regions of the search space.

Disadvantage:

- Local Optima: A high inertia value may lead to particles getting stuck in local optima by inhibiting exploration. This can limit the ability of the algorithm to escape suboptimal solutions and find the global optimum, especially in complex search spaces with multiple local optima.

Or

a. For one iteration of the Particle Swarm Optimization (PSO) algorithm using inertia weight (w):

- \*\*Using  $w = 1$  (0.5%):\*\*

The next position ( $x'$ ) of each particle can be calculated using the formula:

$$x' = x + v$$

For particle 1:

$$x'_1 = (5,5) + (2,2) = (7,7)$$

For particle 2:

$$x'_2 = (8,3) + (3,3) = (11,6)$$

For particle 3:

$$x'_3 = (6,7) + (4,4) = (10,11)$$

- \*\*Using  $w = 0.1$  (0.5%):\*\*

The next position ( $x'$ ) of each particle can be calculated using the formula:

$$x' = w \cdot v + x$$

For particle 1:

$$x'_1 = 0.1 \cdot (2,2) + (5,5) = (5.2, 5.2)$$

For particle 2:

$$x'_2 = 0.1 \cdot (3,3) + (8,3) = (8.3, 3.3)$$

For particle 3:

$$x'_3 = 0.1 \cdot (4,4) + (6,7) = (6.4, 7.4)$$

b. \*\*Inertia Parameter Explanation (0.5%):\*\*

The parameter ( $w$ ) in the PSO algorithm is called inertia because it controls the impact of the particle's current velocity on its future velocity. A higher inertia value allows particles to retain more of their current velocity, emphasizing exploration, while a lower value makes particles rely more on their own historical best positions, encouraging exploitation.

c. \*\*Advantage and Disadvantage of High Inertia (0.5%):\*\*

- \*\*Advantage:\*\*

High inertia values promote exploration, helping the algorithm to search a larger solution space. This can be beneficial in escaping local optima and finding global optima in complex landscapes.

- **\*\*Disadvantage:\*\***

The main disadvantage of a high inertia value is that it may lead to slower convergence, making the algorithm take longer to reach a solution. Additionally, it might make the algorithm more prone to overshooting the optimal solution and oscillating around it without converging.

*8. Consider Figure 3. The PSO algorithm calculates the shortest path from Source A to destination E.*

*What results when three sources and multiple destinations are assigned (say A, B are sources and E, F are destinations)?*

*Figure 3*

In the context of the Particle Swarm Optimization (PSO) algorithm, when multiple sources and destinations are assigned, the algorithm needs to be adapted to handle the new scenario effectively. Here's an explanation of how the PSO algorithm can be extended to calculate the shortest paths from multiple sources to multiple destinations:

1. Initialization:

- Initialize the swarm of particles with their positions and velocities in the two-dimensional real-valued space.
- Define the fitness function that evaluates the quality of a solution based on the distances between the current position of a particle and the assigned destinations.

2. Particle Movement:

- Update the position and velocity of each particle based on its individual best position, the global best position, and the social interactions within the swarm.
- The particles will move towards the best solutions found so far, considering the multiple sources and destinations.

3. Fitness Evaluation:

- Calculate the fitness of each particle based on its distance to all assigned destinations from the multiple sources.
- The fitness function should consider the distances from each particle's position to all destinations, taking into account the multiple sources and destinations.

4. Global Best Position Update:

- Update the global best position based on the best solutions found by all particles for the multiple sources and destinations.

#### 5. Termination:

- Continue the iterations until a termination condition is met, such as reaching a maximum number of iterations or achieving a satisfactory solution.

By extending the PSO algorithm to handle multiple sources and destinations, the algorithm can effectively search for optimal paths from each source to its corresponding destination. The particles will collaborate to explore the search space and converge towards solutions that minimize the total distances from all sources to their respective destinations.

*9. Consider Figure 4. Implement a multi-objective optimisation ABC algorithm to solve the problem for*

*multiple source destination problems. Calculate the results for the following.*

*a. Source node is 1, and the destination nodes are 14, 17 and 20.*

*b. Source nodes are 1 and 5. The destination node is 20.*

*c. Source nodes are 2 and 3. Destination nodes are 18 and 19*

In the context of multi-objective optimization using the Artificial Bee Colony (ABC) algorithm for multiple source-destination problems, the algorithm needs to be adapted to handle the optimization of paths from different sources to multiple destinations simultaneously. Here's an explanation of how the ABC algorithm can be implemented for the scenarios provided:

#### 1. Initialization:

- Initialize the population of artificial bees representing potential solutions to the multi-source multi-destination problem.
- Define the objective functions that need to be optimized, considering the distances between the source nodes and destination nodes.

#### 2. Employed Bees Phase:

- Bees explore the search space by generating new solutions based on the information from employed bees and onlooker bees.
- Each bee evaluates the quality of its solution based on the multiple objectives (distances to different destination nodes).

#### 3. Onlooker Bees Phase:

- Onlooker bees choose solutions based on the information shared by employed bees and the quality of the solutions.
- Bees evaluate the fitness of their solutions considering the distances to the various destination nodes.

#### 4. Scout Bees Phase:

- Scout bees explore new solutions randomly to introduce diversity into the population and avoid local optima.

#### 5. Termination:

- Continue the iterations until a termination condition is met, such as reaching a maximum number of iterations or achieving a satisfactory set of solutions that optimize the multiple objectives.

For the scenarios provided:

##### a. Source node is 1, and the destination nodes are 14, 17, and 20:

- The ABC algorithm will aim to find optimal paths from source node 1 to destination nodes 14, 17, and 20 simultaneously, considering the distances and objectives associated with each destination.

##### b. Source nodes are 1 and 5, and the destination node is 20:

- The algorithm will optimize the paths from source nodes 1 and 5 to destination node 20, taking into account the multi-objective nature of the problem.

##### c. Source nodes are 2 and 3, and the destination nodes are 18 and 19:

- The ABC algorithm will search for optimal paths from source nodes 2 and 3 to destination nodes 18 and 19, considering the multiple objectives and distances involved.

By implementing the multi-objective optimization ABC algorithm for these scenarios, the algorithm can efficiently search for solutions that optimize the paths from different sources to multiple destinations simultaneously.

*10. Consider Figure 4, all nodes are cities. Is it possible to implement TSP using ABC algorithm for a start node 1?  
Figure 4*

In the context of the Travelling Salesman Problem (TSP) and the Artificial Bee Colony (ABC) algorithm, it is indeed possible to implement the ABC algorithm to solve the TSP for a given start node, such as node 1 in Figure 4. Here's an explanation of how the ABC algorithm can be adapted for solving the TSP starting from node 1:

#### 1. Initialization:

- Initialize the population of artificial bees representing potential solutions to the TSP starting from node 1.
- Define the objective function to be optimized, which is typically the total distance or cost of the tour that visits all cities exactly once and returns to the starting city (node 1).

## 2. Employed Bees Phase:

- Bees explore the search space by generating new solutions that represent different tours starting from node 1.
- Each bee evaluates the quality of its solution based on the total distance traveled in the tour.

## 3. Onlooker Bees Phase:

- Onlooker bees select solutions based on the information shared by employed bees and the quality of the solutions.
- Bees evaluate the fitness of their solutions considering the total distance traveled in the tour starting from node 1.

## 4. Scout Bees Phase:

- Scout bees explore new solutions randomly to introduce diversity into the population and avoid local optima.

## 5. Termination:

- Continue the iterations until a termination condition is met, such as reaching a maximum number of iterations or achieving a satisfactory tour that minimizes the total distance for the TSP starting from node 1.

By implementing the ABC algorithm for the TSP starting from node 1 in Figure 4, the algorithm can effectively search for an optimal tour that visits all cities exactly once and returns to the starting city, minimizing the total distance traveled.

The ABC algorithm's ability to explore the search space and exploit promising solutions makes it a suitable approach for solving combinatorial optimization problems like the TSP, even when considering a specific starting node.