



Rethinking Adversarial Examples

Master's Thesis

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This thesis comes from working on a problem that truly matters to me, in an environment where curiosity and passion were shared, and I felt a sense of belonging. The topic of adversarial examples reflects my journey well, highlighting how subtle differences in perspective can lead to vastly different interpretations and outcomes.

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I hope to continue this journey with the same spirit that brought me here.

Abstract

...

 $\textbf{Keywords:} \ \ \textbf{Robustness}, \ \textbf{Alignment}, \ \textbf{Interpretability}, \ \textbf{Algorithmic Models}$

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We have two goals in writing this document. One: fulfilling the requirements for a master's degree by presenting and extending our original research [1] in thesis form. Two: offering a fresh and cohesive perspective on the rapidly evolving and, in our view, really exciting field of adversarial machine learning to a broader audience, with fewer technical prerequisites. We hope it will be valuable to those interested.

1.1 Definition

Adversarial examples are closely related to the concept of perturbation methods¹.

The origin of perturbations can be traced back to the early days of computational geometry by Seidel et al. in 1998 [2]. Perturbation techniques in computational geometry address a fundamental challenge: handling "degeneracies" in geometric algorithms. These are special cases that occur when geometric primitives align in ways that break the general position assumptions the algorithms rely on.

Example: Perturbation scheme for a linear classifier.

Consider a simple case of determining whether a point lies above or below a line [3]. While this classification appears straightforward, numerical issues arise when the point lies exactly on the line. Such degeneracies can cascade into algorithm failures or inconsistent results. The elegant solution is to imagine slightly moving (perturbing) the geometric objects to eliminate these special cases. Formally, we can express symbolic perturbation as $p_{\varepsilon}(x) = x + \varepsilon \cdot \delta(x)$ where x is the original input, ε is an infinitesimally small positive number the exact value of which is unimportant, and $\delta(x)$ is the perturbation function to break degeneracies.

¹Thanks to Prof. Wattenhofer for sharing this piece of unorthodox history.

A perturbation scheme should be (1) consistent, meaning that the same input always produces the same perturbed output (2) infinitesimal, such that perturbations are small enough not to affect non-degenerate cases and (3) effective, in breaking all possible degeneracies.

One powerful perturbation approach is Simulation of Simplicity (SoS) [4, 5, 6, 7, 8, 9]. SoS systematically perturbs input coordinates using powers of a symbolic infinitesimal. For a point $p_i = (x_i, y_i)$, the perturbed coordinates become:

$$(\tilde{x_i}, \tilde{y_i}) = (x_i + \varepsilon^{2i}, y_i + \varepsilon^{2i+1}) = p_i + \varepsilon^{2i} \cdot (1, \varepsilon)$$

This scheme ensures that no two perturbed points share any coordinate, effectively eliminating collinearity and other degeneracies.

The beauty of perturbation methods lies in their ability to handle degeneracies without explicitly detecting them, making geometric algorithms both simpler and more robust.

Adversarial examples on the other hand, first introduced by Szegedy et al. in 2014 [10], follow the same principles as perturbation methods, but with the opposite objective. Instead of seeking to eliminate degeneracies (brittleness in the decision boundary), they exploit them to cause targeted misclassifications. Intuitively they can be understood as seeking the closest point in the input space that lies on the "wrong side" of a decision boundary relative to the original input. This shift, applied to the original input, creates an adversarial example.

Example: Fast Gradient Sign Method (FGSM)

FGSM is one of the earliest and most widely recognized adversarial attack techniques, introduced by Goodfellow et al. [11] in the context of visual recognition tasks. Given an input image x, FGSM generates an adversarial example x' by perturbing the input in the direction of the gradient of the loss function with respect to the input.

The perturbation is controlled by a parameter $\varepsilon > 0^a$, which determines the magnitude of the change based on the direction of change for each pixel or feature in the input x. The model's loss function denoted by J, θ represents the model's parameters, and y is the true target label.

It works by calculating the gradient of the loss function with respect to the input, $\nabla_x J(\theta, x, y)$, and then adjusting the input in the direction of this gradient. The sign of the gradient, $\operatorname{sign}(\nabla_x J(\theta, x, y))$,

is used to ensure that the perturbation is small, while the ℓ_{∞} -norm constraint ensures that the change to the input remains "imperceptible" to human observers [11, 12]. More on the concept of imperceptibility later.

The process for generating an adversarial example with FGSM can be expressed as:

$$x' = x + \varepsilon \cdot \operatorname{sign}(\nabla_x J(\theta, x, y))$$
Perturbation

In the untargeted version, the perturbation is designed to increase the loss for the correct class. In the targeted version the perturbation is designed to minimize the loss with respect to the adversary's chosen target class, making the model predict it deliberately.

^aCommonly $\varepsilon=8/255$ for 8-bit images, so it stays within the precision constraints of the pixel values.

While initially discovered in computer vision applications, the attack can be crafted for any domain or data type, even graphs [13]. Natural language processing models can be attacked by circumventing the discrete nature of text data [14, 15, 16]. One particularly entertaining example is the subversion of the conference paper-reviewer assignment model by Eisenhofer et al. [17], where authors preselect reviewers to gain a competitive advantage. Speech recognition systems are vulnerable to audio-based attacks, where crafted noise can cause system failure [18]. Deep reinforcement learning applications, including pathfinding and robot control, have also shown susceptibility to adversarial manipulations that can compromise their decision-making capabilities [19].

1.2 Types of Adversarial Examples

Having established the general concept of adversarial examples, we can now explore the various ways they can be categorized. Our system is not exhaustive: The field continues to evolve, with new attack vectors emerging regularly [20].

We can differentiate between white-box and black-box attacks. White-box attacks assume complete knowledge of and access to the target model, while black-box attacks operate with limited or no access to the model's internal workings [21]. Interestingly, research has shown that in some cases, black-box attacks can be more effective than white-box approaches at compromising model security [21].

An attack can be targeted or untargeted. Targeted attacks aim to manipulate the model into producing a specific, predetermined output, whereas untargeted

attacks simply seek to cause any misclassification or erroneous output [21, 13]. This distinction is particularly relevant in security-critical applications, where the attacker's goals may vary from causing general disruption to achieving specific malicious outcomes.

The method used to generate adversarial examples can be gradient-based, optimization-based or search-based strategies. For example, some text-based attacks leverage language models to generate alternatives for masked tokens, ensuring grammatical correctness and semantic coherence [22].

The extent to which adversarial examples are transferable – meaning their ability to fool multiple different models – is another way to differentiate them. Some adversarial examples demonstrate high transferability across various model architectures, while others are more model-specific in their effectiveness [23, 24]. Recent research has shown that adversarial examples are more readily transferable between vanilla neural networks than between defended ones [25, 26].

Finally, the attacks can be either focused on preserving the semantic meaning of inputs or exploit the mathematical properties of models without regard for semantic interpretation provides [27].

1.3 Imperceptible \neq Semantics Preserving

Adversarial examples are traditionally expected to have two key properties: (1) they should successfully cause misclassification in machine learning models while (2) remaining imperceptible to human observers [28].

However, the concept of "imperceptibility [to humans]" as originally proposed by Szegedy et al. [10] by limiting pixel-space perturbations through an ε -bounded constraint is fundamentally flawed. This is because the human visual system is not solely reliant on pixel-space information to interpret images [29]:

- 1. Changing many pixels doesn't necessarily change semantics: For instance, changes in lighting, exposure, sharpness, angle, shadow, field of view, or even the the orientation of an animal's fur does not necessarily alter the semantic content of an image, despite involving many pixel-space changes [30]. The figure 1.1 serves to illustrate this point, assuming that the latent representations are perfectly aligned with the human judgement function.
- 2. Changing few pixels doesn't necessarily preserve semantics: The assumption that minimal pixel-space changes ensure semantic preservation is also flawed. This is because small ε -bounded adversarial perturbations are proven to cause misclassification in time-constrained humans [31]. Even more interestingly, humans detect forged low- ε adversarial examples with

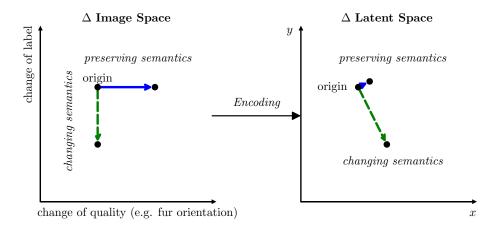


Figure 1.1: Semantics preserving/changing perturbations in pixel/latent-space.

high accuracy in the visual (85.4%) [32] and textual $(\geq 70\%)$ [33] domain. This raises the question of whether our current understanding of the human-machine vision gap is accurate enough to guide the development of adversarial examples.

If imperceptibility is not a reliable indicator of semantic preservation, then what are the true properties of adversarial examples?

Recent research has shifted towards more nuanced concepts like "semantic preservation" acknowledging that the relationship between perturbation size and semantic change is not straightforward [34]. This shift has led to the development of new methods for generating adversarial examples that focus on preserving semantic information rather than relying on pixel-space constraints [35].

The challenge of defining semantics remains central to this discussion. Without perfect representations that align with human judgment functions, we must rely on the best available encoders as proxies for semantic preservation [33]. This pragmatic approach acknowledges the limitations of current technology while striving for more meaningful adversarial examples.

1.4 Counterintuitive Properties

1.5 Mental Models

Chapter 2

Methodology

Chapter 3

Results

Chapter 4

Stuff

4. Stuff 9



Figure 4.1: This is an example graphic.

"The stuff is what the stuff is, brother. Okay. We don't ask questions about the weights. We just wake up, we go to work, we use the weights, we go back home. Okay. If we change the weights, the predictions would be different and less good, probably... depending on the weather... so we don't ask about the weights."

— James Mickens, USENIX Security 18 [36]

4.1 First Section Title

Lorem ipsum dolor sit amet, consetetur sadipscing elitr, sed diam nonumy eirmod tempor invidunt ut labore et dolore magna aliquyam erat, sed diam voluptua.

4.1.1 First Subsection Title

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Theorem 4.1 (First Theorem). This is our first theorem.

Proof. And this is the proof of the first theorem with a complicated formula and a reference to Theorem 4.1. Lorem ipsum dolor sit amet, consetetur sadipscing elitr, sed diam nonumy eirmod tempor invidunt ut labore et dolore magna aliquyam erat, sed diam voluptua. Lorem ipsum dolor sit amet, consetetur sadipscing elitr, sed diam nonumy eirmod tempor invidunt ut labore et dolore magna aliquyam erat, sed diam voluptua.

$$\frac{d}{dx}\arctan(\sin(x^2)) = -2 \cdot \frac{\cos(x^2)x}{-2 + (\cos(x^2))^2}$$
(4.1)

And here we cite some external documents [37, 38]. An example of an included graphic can be found in Figure 4.1. Note that in LaTeX, "quotes" do not use the usual double quote characters.

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First Appendix Chapter Title