

Team notebook

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1 data-structures

1.1 fenwick

```
template <class T>
class fenwick {
    vector<T> a;
    int n;

public:
    fenwick() {}

    fenwick(int n_) : n(n_) {
        // check initial value
        a.assign(n + 5, static_cast<T>(0));
    }
}
```

```
T query(int r) {
    T q = 0; // check default value of query
    for (; r > 0; r -= (r & -r)) {
        q += a[r]; // check query modification
    }
    return q;
}

void update(int r, T del) {
    for (; r <= n; r += (r & -r)) {
        a[r] += del; //check update rule
    }
}
};
```

1.2 fenwick2d

```
// from online git I don't remember, all
// credits go to them
template<
    typename T // need to support +, -
> struct Fenwick2D {
    // 1-indexed
    int n1, n2;
    vector<vector<T>> f;

    Fenwick2D(int _n1, int _n2) : n1(_n1 + 1),
        n2(_n2 + 1), f(1+n1, vector<T> (1+n2,
            T(0))) {}
    Fenwick2D() {}
}
```

```

// a[x][y] += val
void update(ll x, ll y, T val) {
    assert(0 <= x && x < n1);
    assert(0 <= y && y < n2);
    ++x; ++y;
    for (int u = x; u <= n1; u += u & -u) {
        for (int v = y; v <= n2; v += v & -v) {
            f[u][v] += val;
        }
    }
}

T get(ll x1, ll y1, ll x2, ll y2) const {
    // [x1,y1] -> [x2,y2]
    return _get(x1, y1, x2 + 1, y2 + 1);
}

T get(ll x, ll y) const { // [0,0] -> [x,y]
    return _get(x + 1, y + 1);
}

private:
// return rect sum of [0, 0] -> [x-1, y-1]
T _get(ll x, ll y) const {
    assert(0 <= x && x <= n1);
    assert(0 <= y && y <= n2);
    T res(0);
    for (int u = x; u > 0; u -= u & -u) {
        for (int v = y; v > 0; v -= v & -v) {
            res += f[u][v];
        }
    }
    return res;
}

// returns rect sum of [x1, y1] -> [x2-1, y2-1]
T _get(ll x1, ll y1, ll x2, ll y2) {
    if (x1 == x2 || y1 == y2) return T(0);
    return get(x2, y2) - get(x1, y2) -
        get(x2, y1) + get(x1, y1);
}
};

```

1.3 lazysegtree

```

// lazy propagation with one-based indexing
//
// build:
//   lazySegtree<int> seg(n); // vector<int>
//   a(n + 1)
//   seg.build(a); // vector 'a' must be
//   one-indexed
//
// update:
//   seg.update(l, r, inc); //increase a[l ->
//   r] += inc
//   //you may want to set this
// query:
//   seg.query(l, r)

template <class T>
struct lazySegTree {
    vector<T> st, lazy;
    int n;
    lazySegTree(int _n) : n(_n) {
        T default_value = 0;
        st.assign(4 * n + 5, default_value);
        lazy.assign(4 * n + 5, default_value);
    }
    void build(const vector<T> &a) {
        build(a, 1, 1, n);
    }
    void build(const vector<T> &a, int id, int
        l, int r) {
        lazy[id] = 0;
        if(l == r) {
            if(l < a.size()) {
                st[id] = a[l];
            }
            return;
        }
        int mid = (l + r) >> 1;
        build(a, id * 2, l, mid);
        build(a, id * 2 | 1, mid + 1, r);
        st[id] = max(st[id * 2], st[id * 2 | 1]);
    }
    void down(int id) {
        if(lazy[id] == 0)

```

```

        return;
        st[id * 2] += lazy[id];
        st[id * 2 | 1] += lazy[id];
        lazy[id * 2] += lazy[id];
        lazy[id * 2 | 1] += lazy[id];
        lazy[id] = 0;
    }
    void update(int u, int v, T val) {
        update(u, v, val, 1, 1, n);
    }
    void update(int u, int v, T val, int id, int
        l, int r) {
        if(v < l || r < u) return;
        if(u <= l && r <= v) {
            lazy[id] += val;
            st[id] += val;
            return;
        }
        down(id);
        int mid = (l + r) >> 1;
        update(u, v, val, id * 2, l, mid);
        update(u, v, val, id * 2 | 1, mid + 1, r);
        st[id] = max(st[id * 2], st[id * 2 | 1]);
    }
    T query(int u, int v) {
        return query(u, v, 1, 1, n);
    }
    T query(int u, int v, int id, int l, int r) {
        if(v < l || r < u) {
            return -INF;
        }
        if(u <= l && r <= v) {
            return st[id];
        }
        int mid = (l + r) >> 1;
        down(id);
        return max(query(u, v, id * 2, l, mid),
            query(u, v, id * 2 | 1, mid + 1, r));
    }
};

```

1.4 make-pbds

```
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;

/**
 * Description: Policy-based data structures
 *              that supports normal set operation and
 * * find_by_order(k) returns iterator to
 *   kth element starting from 0;
 * * order_of_key(k) returns count of
 *   elements strictly [smaller] than k;
 * Caution:
 * * do not define int long long before
 *   below declaration
 */

template <class T, class cmp = std::less<T>>
using ordered_set = tree<T, null_type, cmp,
rb_tree_tag, tree_order_statistics_node_update>;

template <class key, class value, class cmp =
std::less<key>>
using ordered_map = tree<key, value, cmp,
rb_tree_tag,
tree_order_statistics_node_update>;
```

1.5 rmq

```
template<class T>
struct RMQ {
    T st[LG + 1][N];
    int n;
    void build (const vector<T> &a) {
        n = a.size() - 1;
        for (int i = 1; i <= n; ++i) st[0][i] =
            a[i];
        for (int j = 1; j <= LG; ++j)
            for (int i = 1; i + (1 << j) - 1 <= n;
                ++i)
                st[j][i] = min(st[j - 1][i], st[j -
                    1][i + (1 << (j - 1))]);
    }
    T query(int l, int r) {
```

```
        int k = __lg(r - l + 1);
        return min(st[k][l], st[k][r - (1 << k) +
            1]);
    }
};
```

1.6 segment-tree

```
// segtree with one-based indexing
//
// build:
//   segtree<int> seg(n); // vector<int> a(n
//   + 1);
//   seg.build(a); // vector 'a' must be
//   one-indexed
//
// update:
//   seg.update(pos, inc); //increase a[pos]
//   to a[pos] + inc
//   //you may want to set this
// query:
//   seg.query(l, r)
```

```
template<class T>
struct segTree {
    vector<T> st;
    int n;
    segTree(int _n) : n(_n) {
        T default_value = 0;
        st.assign(4 * n + 5, default_value);
    }
    void build(const vector<T> &a) {
        build(a, 1, 1, n);
    }
    void build(const vector<T> &a, int id, int
        l, int r) {
        if(l == r) {
            st[id] = a[l];
            return;
        }
        int mid = (l + r) >> 1;
        build(a, id * 2, l, mid);
        build(a, id * 2 | 1, mid + 1, r);
```

```
        st[id] = st[id * 2] + st[id * 2 | 1];
    }
    void update(int pos, T inc) {
        update(pos, inc, 1, 1, n);
    }
    void update(int pos, T inc, int id, int l,
        int r) {
        if(pos < l || r < pos) {
            return;
        }
        if(l == r) {
            st[id] += inc;
            return;
        }
        int mid = (l + r) >> 1;
        update(pos, inc, id * 2, l, mid);
        update(pos, inc, id * 2 | 1, mid + 1, r);
        st[id] = st[id * 2] + st[id * 2 | 1];
    }
    T query(int u, int v) {
        return query(u, v, 1, 1, n);
    }
    T query(int u, int v, int id, int l, int r) {
        if(v < l || r < u) {
            return 0;
        }
        if(u <= l && r <= v) {
            return st[id];
        }
        int mid = (l + r) >> 1;
        return query(u, v, id * 2, l, mid) +
            query(u, v, id * 2 | 1, mid + 1, r);
    }
};
```

1.7 treap-pbds

```
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;

/// *** Needs C++11 or C++14 ***/
```

```

/// Treap supporting duplicating values in set
/// Maximum value of treap * ADD must fit in
long long

```

```

struct Treap { /// hash = 96814
    int len;
    const int ADD = 1000010;
    const int MAXVAL = 1000000010;
    unordered_map <long long, int> mp; ///
        Change to int if only int in treap
    tree<long long, null_type, less<long long>,
        rb_tree_tag,
        tree_order_statistics_node_update> T;

```

```

Treap(){
    len = 0;
    T.clear(), mp.clear();
}

```

```

inline void clear(){
    len = 0;
    T.clear(), mp.clear();
}

```

```

inline void insert(long long x){
    len++, x += MAXVAL;
    int c = mp[x]++;
    T.insert((x * ADD) + c);
}

```

```

inline void erase(long long x){
    x += MAXVAL;
    int c = mp[x];
    if (c){
        c--, mp[x]--, len--;
        T.erase((x * ADD) + c);
    }
}

```

```

/// 1-based index, returns the K'th element
in the treap, -1 if none exists

```

```

inline long long kth(int k){
    if (k < 1 || k > len) return -1;
    auto it = T.find_by_order(--k);
    return ((*it) / ADD) - MAXVAL;
}

```

```

}

/// Count of value < x in treap
inline int count(long long x){
    x += MAXVAL;
    int c = mp[--x];
    return (T.order_of_key((x * ADD) + c));
}

/// Number of elements in treap
inline int size(){
    return len;
}
};

```

1.8 treap

```

//replace sum with many other function, just
like cnt

```

```

struct item {
    long long prior, value, cnt, sum;
    bool rev;
    item *l, *r;
    item(long long value): prior(rand()),
        value(value), cnt(1), rev(false),
        sum(value), l(0), r(0) {}
};

```

```

long long cnt (item* it) {
    return it ? it->cnt : 0;
}

```

```

long long sum (item* it) {
    return it ? it->sum : 0;
}

```

```

void upd_cnt (item* it) {
    if (it)
        it->cnt = cnt(it->l) + cnt(it->r) + 1;
}

```

```

void upd_sum(item* it) {
    if (it)

```

```

        it->sum = sum(it->l) + sum(it->r) +
            it->value;
}

```

```

void push (item* it) {
    if (it && it->rev) {
        it->rev = false;
        swap(it->l, it->r);
        if (it->l) it->l->rev ^= true;
        if (it->r) it->r->rev ^= true;
    }
}

```

```

void merge (item* &t, item* l, item* r) {
    push (l);
    push (r);
    if (!l || !r)
        t = l ? l : r;
    else if (l->prior > r->prior)
        merge (l->r, l->r, r), t = l;
    else
        merge (r->l, l, r->l), t = r;
    upd_cnt(t);
    upd_sum(t);
}

```

```

// split so that the number of the node in
the left is "num"

```

```

void split (item* t, item* &l, item* &r,
    long long num, long long add = 0) {
    if (!t)
        return void( l = r = 0 );
    push (t);
    int cur_num = add + cnt(t->l);
    if (num <= cur_num)
        split (t->l, l, t->l, num, add), r = t;
    else
        split (t->r, t->r, r, num, add + 1 +
            cnt(t->l)), l = t;
}

```

```

    upd_cnt(t);
    upd_sum(t);
}

```

```

// l, r are 1-indexed

```

```
void reverse (item* t, int l, int r) {
    item *t1, *t2, *t3;
    split (t, t1, t2, l-1);
    split (t2, t2, t3, r-l+1);
    t2->rev ^= true;
    merge (t, t1, t2);
    merge (t, t, t3);
}
```

```
void traverse (item* t) {
    if (!t) return;
    push (t);
    traverse (t->l);
    // do stuff with current value
    cout << t->value << " ";
    traverse (t->r);
}
```

1.9 z-function

```
vector<int> z_function(const string& s) {
    int n = (int) s.size();
    vector<int> z(n);
    for (int i = 1, l = 0, r = 0; i < n; ++i) {
        if (i <= r)
            z[i] = min (r - i + 1, z[i - l]);
        while (i + z[i] < n && s[z[i]] == s[i +
            z[i]])
            ++z[i];
        if (i + z[i] - 1 > r)
            l = i, r = i + z[i] - 1;
    }
    return z;
}
```

2 graphs

2.1 DAG

```
#include <bits/stdc++.h>
```

```
#define pb push_back
#define fi first
#define se second

#define ii pair<int,int>
#define ll long long

using namespace std;

const int N = 3e5;
const ll MOD = 1e9 + 7;
const int iINF = 1e9;

int n,m;
vector<int> g[N];

vector<int> topo;

bool vsd[N];
void dfs(int u){
    vsd[u]=1;
    for (int v : g[u]) if (!vsd[v]) dfs(v);
    topo.pb(u);
}

void CountPath(int s){
    int d[N];

    memset(d,0,sizeof d); //number of paths
                             from s to i

    int k=0;
    for (int i=0;i<=topo.size();i++) {
        if (topo[i]==s){
            k=i;
            break;
        }
    }

    d[s]=1;
    for (int i=k;i<topo.size();i++) {
        int u = topo[i];
        for (int v:g[u]) d[v]+=d[u];
    }
}
```

```
cout<<"Number of paths: ";
for (int i=1;i<=n;i++)cout<<d[i]<<" ";
cout<<endl;
}

void LongestPath(){
    // Longest path on DAG
    int d[N]; //dp[i]: longest path starting
               from i

    for (int i=topo.size()-1;i>=0;i--){ //
        loop backwards
        int u=topo[i];
        int &res=d[u];

        res=0;
        for (int v : g[u]) res=max(res,d[v]+1);
    }
    cout<<"Longest path: ";for (int
        i=1;i<=n;i++) cout<<d[i]<<" ";
    cout<<endl;
}

int main(){
    freopen("main.inp","r",stdin);
    //Topological sorting

    cin>>n>>m;
    while (m--) {
        int u,v;cin>>u>>v;
        g[u].pb(v);
    }

    for (int i=1;i<=n;i++) if(!vsd[i]) dfs(i);
    reverse(topo.begin(),topo.end());
    for (int num:topo) cout<<num<<"
        ";cout<<endl;

    LongestPath();
    CountPath(1);

    return 0;
}
```

2.2 DFSMatching

```
/**
 * Description: Simple bipartite matching
 * algorithm. Graph $g$ should be a list
 * of neighbors of the left partition, and
 * $btoa$ should be a vector full of
 * -1's of the same size as the right
 * partition. Returns the size of
 * the matching. $btoa[i]$ will be the match
 * for vertex $i$ on the right side,
 * or $-1$ if it's not matched.
 * Time: $O(VE)$
 * Usage: vi btoa(m, -1); dfsMatching(g, btoa);
 * Status: works
 */

bool find(int j, vector<vi>& g, vi& btoa, vi&
vis) {
    if (btoa[j] == -1) return 1;
    vis[j] = 1; int di = btoa[j];
    for (int e : g[di])
        if (!vis[e] && find(e, g, btoa,
vis)) {
            btoa[e] = di;
            return 1;
        }
    return 0;
}

int dfsMatching(vector<vi>& g, vi& btoa) {
    vi vis;
    rep(i, 0, sz(g)) {
        vis.assign(sz(btoa), 0);
        for (int j : g[i])
            if (find(j, g, btoa,
vis)) {
                btoa[j] = i;
                break;
            }
    }
    return sz(btoa) -
(int)count(all(btoa), -1);
}
```

2.3 Dinic

```
// Maximum flow from s to t in a flow
// network. $O(E*V^2)$
// Tested: https://oj.vnoi.info/problem/nkflow
// Tested: https://oj.vnoi.info/problem/nknet

#define ll long long
#define sz(x) (int) (x).size()

const int N = 1e3 + 5;
int n, m, s, t;
int c[N][N];

struct Dinic {
    struct Edge {
        int to, rev;
        ll c, oc;
        ll flow() { return max(oc - c,
OLL); } // if you need flows
    };
    vector<int> lvl, ptr, q;
    vector<vector<Edge>> adj;
    Dinic(int n) : lvl(n), ptr(n), q(n),
adj(n) {}
    void addEdge(int a, int b, ll c, ll
rcap = 0) {
        adj[a].push_back({b,
sz(adj[b]), c, c});
        adj[b].push_back({a, sz(adj[a])
- 1, rcap, rcap});
    }
    ll dfs(int v, int t, ll f) {
        if (v == t || !f) return f;
        for (int& i = ptr[v]; i <
sz(adj[v]); i++) {
            Edge& e = adj[v][i];
            if (lvl[e.to] == lvl[v]
+ 1)
                if (ll p =
dfs(e.to, t,
min(f,
e.c))) {
                    e.c -= p,
                    adj[e.to][e.rev].c
                    += p;
                    return p;
                }
        }
        return 0;
    }
    ll calc(int s, int t) {
        ll flow = 0; q[0] = s;
        for (int L = 0; L < 31; L++) do
            { // 'int L=30' maybe
            faster for random data
            lvl = ptr =
vector<int>(sz(q));
            int qi = 0, qe = lvl[s]
= 1;
            while (qi < qe &&
!lvl[t]) {
                int v = q[qi++];
                for (Edge e :
adj[v])
                    if
                        (!lvl[e.to]
&&
e.c
>>
(30 -
L))
                        q[qi++]
                        =
e.to,
                        lvl[e.to]
                        =
lvl[v]
                        +
1;
            }
            while (ll p = dfs(s, t,
LLONG_MAX)) flow +=
p;
        } while (lvl[t]);
        return flow;
    }
    bool leftOfMinCut(int a) { return
lvl[a] != 0; }
};
```

```

    += p;
    return p;
}

}
return 0;
}

ll calc(int s, int t) {
    ll flow = 0; q[0] = s;
    for (int L = 0; L < 31; L++) do
        { // 'int L=30' maybe
        faster for random data
        lvl = ptr =
vector<int>(sz(q));
        int qi = 0, qe = lvl[s]
= 1;
        while (qi < qe &&
!lvl[t]) {
            int v = q[qi++];
            for (Edge e :
adj[v])
                if
                    (!lvl[e.to]
&&
e.c
>>
(30 -
L))
                    q[qi++]
                    =
e.to,
                    lvl[e.to]
                    =
lvl[v]
                    +
1;
        }
        while (ll p = dfs(s, t,
LLONG_MAX)) flow +=
p;
    } while (lvl[t]);
    return flow;
}

bool leftOfMinCut(int a) { return
lvl[a] != 0; }
};
```

```
signed main() {
    cin >> n >> m >> s >> t;
    Dinic dinic(n + 1);
    for (int i = 1; i <= m; i++) {
        int u, v, C;
        cin >> u >> v >> C;
        dinic.addEdge(u, v, C);
        c[u][v] = 1;
    }
    cout << dinic.calc(s, t) << '\n';

    /// Find all edges in min-cut, can be
    /// optimized using edges list
    for (int i = 1; i <= n; i++) for (int
        j = 1; j <= n; j++) {
        if (c[i][j] && dinic.leftOfMinCut(i)
            && !dinic.leftOfMinCut(j))
            cout << i << " " << j << '\n';
    }
}
```

2.4 EdmondKarp

```
int n, m, s, t;
vector<ii> g[N];

void add(int u, int v, int w){
    g[u].pb({v, w});
    g[v].pb({u, 0});
}

int bfs(int s, int t, int p[N]){
    for (int i=1; i<=n; i++) p[i]=-1; p[s]=-2;

    queue<ii> q;
    q.push({iINF, s});

    while (!q.empty()){
        int u=q.front().second;
        int flow = q.front().first;
        q.pop();

        for (ii a : g[u]){
```

```
            int v = a.first, w = a.second;

            if (w > 0 && p[v] == -1){
                p[v]=u;
                int new_flow = min(flow, w);

                if (v == t) return new_flow;

                q.push({new_flow, v});
            }
        }

        return 0;
    }

    int max_flow(int s, int t){
        int p[N];

        int max_flow=0;

        int flow;
        while (flow = bfs(s, t, p)){
            for (int v = t; v != s; v = p[v]){
                int u = p[v];
                //g[u][v].second -= flow;
                for (ii &a : g[u]) if (a.fi == v)
                    a.se -= flow;
                //g[v][u].second += flow;
                for (ii &a : g[v]) if (a.fi == u)
                    a.se += flow;
            }

            max_flow += flow;
        }
        return max_flow;
    }
}
```

/*
Remember:

After getting the max flow, the graph had
been changed
and cannot be used anymore (Consider make a
copy of it.)

You are using Adjacent List. Loop through all
the edges
and adjust it. (Rather than naively using
indexes)
*/

2.5 EdmondKarp_{new}

// Maximum flow from s to t in a flow
network. $O(E^2 \cdot V)$
// Tested: <https://oj.vnoi.info/problem/nkflow>
// Tested: <https://oj.vnoi.info/problem/nknet>

```
const int N = 1e3 + 5;
const int INF = numeric_limits<int>::max() /
    2;
int c[N][N], par[N], f[N][N], d[N];
int n, m, s, t;

int bfs(int s, int t) {
    queue<int> q;
    fill(par, par + N, -1);
    fill(d, d + N, 0);
    q.push(s); d[s] = INF;
    while (!q.empty()) {
        int u = q.front(); q.pop();
        for (int i = 1; i <= n; i++) {
            if (c[u][i] - f[u][i] > 0 && par[i]
                == -1) {
                d[i] = min(d[u], c[u][i] -
                    f[u][i]);
                par[i] = u; q.push(i);
                if (i == t) return d[t];
            }
        }
    }
    return 0;
}

int max_flow(int s, int t) {
    int cur = 0, ans = 0;
    while ((cur = bfs(s, t)) > 0) {
        ans += cur;
    }
}
```

```

    int v = t;
    while (v != s) {
        f[par[v]][v] += cur;
        f[v][par[v]] -= cur;
        v = par[v];
    }
}
return ans;
}

int vis[N];
void dfs_min_cut(int u) {    /// Find all
    edges in Min-Cut, edges u-v in Min-Cut
    has vis[u] = 1 and vis[v] = 0
    vis[u] = 1;
    for (int v = 1; v <= n; v++) {
        if (abs(f[u][v]) < c[u][v] && !vis[v])
            dfs_min_cut(v);
    }
}

vector<pair<int, int>> min_cut() { // Can
    optimized using edge list
    dfs_min_cut(s);
    vector<pair<int, int>> ans;
    for (int i = 1; i <= n; i++)
        for (int j = 1; j <= n; j++)
            if (f[i][j] && vis[i] && !vis[j])
                ans.push_back({i,j});
    return ans;
}

signed main() {
    cin >> n >> m >> s >> t;
    for (int i = 1; i <= m; i++) {
        int u,v,C;
        cin >> u >> v >> C;
        c[u][v] += C;
    }
    cout << max_flow(s,t) << '\n';
    auto v = min_cut();
    for (auto ii : v)    cout << ii.first <<
        " " << ii.second << '\n';
    return 0;
}

```

2.6 HLD

```

/**
 * You are given a tree
 * We will ask you to perform some
 * instructions of the following form:
 * CHANGE i ti : change the cost of the i-th
 * edge to ti
 * or
 * QUERY a b : ask for the maximum edge cost
 * on the path from node a to node b
 * Status: Tested:
 *      https://vjjudge.net/problem/SPOJ-QTREE
 */

#include<bits/stdc++.h>
using namespace std;

#define int long long
#define pb push_back
const int N = 1e5 + 5;

int sz[N];
int n, dfsTime;
int nhanh, cnt;
int id[N]; // <=> thu tu cua chain chua dinh
            i = id[i]
int head[N]; // <=> gia tri dau tien cua
              chain thu i = head[i]
int pos[N]; // <=> thu tu cua dinh u sau khi
              duoc trai phang = pos[i]
int in[N], out[N], h[N], a[N], p[N][20];
vector<int> adj[N];

struct seg2D { // 0-index
    int n;
    vector<int> seg;
    seg2D() = default;
    seg2D(int _n) : seg(2 * _n, INT_MIN),
        n(_n) {}
    void update(int u, int val) {
        for (seg[u += n] = val; u > 1; u /= 2)
            seg[u >> 1] = max(seg[u], seg[u ^
                1]);
    }
}

```

```

    }
}

int get(int u, int v) {
    int ans = INT_MIN;
    for (u += n, v += n; u <= v; u/=2, v /=
        2) {
        if (u & 1)    ans = max(ans,
            seg[u++]);
        if (~v & 1)   ans = max(ans,
            seg[v--]);
    }
    return ans;
}

}seg;

void reset() {
    nhanh = 1;
    dfsTime = 0;
    cnt = 0;
    for (int i = 1; i <= n; i++){
        adj[i].clear();
        h[i] = 0;
        in[i] = 0;
        out[i] = 0;
        pos[i] = 0;
        head[i] = 0;
        id[i] = 0;
        a[i] = 0;
        sz[i] = 1;
    }
    memset(p,0,sizeof p);
}

void dfs(int u, int par = -1) {
    p[u][0] = par;
    for (int i = 1; i < 20; i++)    p[u][i] =
        p[p[u][i-1]][i-1];
    ++dfsTime;
    in[u] = dfsTime;
    sz[u] = 1;
    for (int v : adj[u]) if (v != par) {
        h[v] = h[u] + 1;
        dfs(v,u);
    }
}

```



```

        sz[u] += sz[v];
    }
    out[u] = dfsTime;
}

bool cha(int u, int v) {
    return (in[u] <= in[v] && out[u] >=
        out[v]);
}

void build_hld(int u, int par = -1) {
    if (head[nhanh] == 0) {
        head[nhanh] = u;
    }
    ++cnt;
    pos[u] = cnt;
    id[u] = nhanh;

    int tmp = -1;
    for (int v : adj[u]) if (v != par) {
        if (tmp == -1 || sz[tmp] < sz[v])
            tmp = v;
    } // Tim dinh v co sz lon nhat

    // heavy edge
    if (tmp != -1) build_hld(tmp, u);

    for (int v : adj[u]) if (v != par && v !=
        tmp) {
        /// light edge
        nhanh++;
        build_hld(v, u);
    }
}

int ans_hld(int u, int v) { // the maximum
    edge cost on the path from node u to node
    v
    int ans = INT_MIN;
    while (id[u] != id[v]) {
        if (h[head[id[u]]] > h[head[id[v]]])
            swap(u, v);
        int v2 = head[id[v]];
        ans = max(ans, seg.get(pos[v2] - 1,
            pos[v] - 1));
    }
}

```

```

        v = p[v2][0];
    }
    /// id[u] == id[v]
    if (pos[u] > pos[v]) swap(u, v);
    ans = max(ans, seg.get(pos[u], pos[v] -
        1)); /// Khi u va v o cung nhanh, ta
    chi nhay tu v len dinh gan u nhat vi u
    o day la lca (ta phai bo a[lca] di do
    qua trinh chuyen duong di)
    return ans;
}

int lca(int u, int v) { // Bin lift
    if (h[u] < h[v]) swap(u, v);
    int k = h[u] - h[v];
    for (int j = 0; j < 20; j++) if (k >> j &
        1) u = p[u][j];
    if (u == v) return u;
    for (int i = 19; i >= 0; i--) {
        if (p[u][i] != p[v][i]) u = p[u][i],
            v = p[v][i];
    }
    return p[u][0];
}

void precalc() {
    dfs(1, 1);
    build_hld(1);
}

void solve() {
    cin >> n;
    reset();
    vector<array<int, 3>> ed(n + 1);
    for (int i = 1; i < n; i++) {
        int u, v, w; cin >> u >> v >> w;
        ed[i] = {u, v, w};
        adj[u].pb(v);
        adj[v].pb(u);
    }
    precalc();
    seg = seg2D(cnt);
    for (int i = 1; i < n; i++) {
        int u = ed[i][0], v = ed[i][1], w =
            ed[i][2];
    }
}

```

```

        if (!cha(u, v)) swap(u, v);
        a[v] = w;
        seg.update(pos[v] - 1, w);
    }
    while (1) {
        string typ;
        cin >> typ;
        if (typ == "DONE") return;
        if (typ == "QUERY") {
            int u, v; cin >> u >> v;
            int LCA = lca(u, v);
            cout << max(ans_hld(u, LCA),
                ans_hld(v, LCA)) << '\n';
        }
        else {
            int id; cin >> id;
            int nval; cin >> nval;
            int u = ed[id][0], v = ed[id][1], w
                = ed[id][2];
            if (!cha(u, v)) swap(u, v); //
            v la con u
            a[v] = nval;
            ed[id][2] = nval;
            seg.update(pos[v] - 1, nval);
        }
    }
}

int32_t main() {
    ios_base::sync_with_stdio(0);
    cin.tie(nullptr); cout.tie(nullptr);
    int test; cin >> test;
    while (test--) {
        solve();
        cout << '\n';
    }
    return 0;
}

/*
1
3
1 2 1
2 3 2
QUERY 1 2

```

```
CHANGE 1 3
QUERY 1 2
DONE
*/
```

2.7 HLD₂

```
/**
 * We will ask you to perform some
 * instructions of the following form:
 * 0 i : change the color of the i-th node
 * (from white to black, or from black to
 * white);
 * or
 * 1 v : ask for the id of the first black
 * node on the path from node 1 to node v.
 * if it doesn't exist, you may return -1
 * as its result.
 * Tested:
 * https://www.spoj.com/problems/QTREE3/en/
 */

#include<bits/stdc++.h>
using namespace std;

#define int long long
#define pb push_back
const int N = 1e6 + 5;

vector<int> adj[N];
int id[N], h[N], head[N], sz[N], pos[N], e[N];
int p[20][N];
int nhanh = 1, cnt;
set<int> s;

void dfs(int u, int par = 1) {
    sz[u] = 1;
    p[0][u] = par;
    for (int i = 1; i < 20; i++) p[i][u] =
        p[i - 1][p[i - 1][u]];
    for (int v : adj[u]) if (v != par) {
        h[v] = h[u] + 1;
        dfs(v, u);
    }
}
```

```
        sz[u] += sz[v];
    }
}

void hld(int u, int par = -1) {
    if (head[nhanh] == 0) head[nhanh] = u;
    ++cnt;
    e[cnt] = u;
    pos[u] = cnt;
    id[u] = nhanh;

    int target = -1;
    for (int v : adj[u]) if (v != par) {
        if (target == -1 || sz[target] <
            sz[v]) target = v;
    }

    if (target != -1) hld(target, u);

    for (int v : adj[u]) if (v != par) {
        if (v != target) {
            ++nhanh;
            hld(v, u);
        }
    }
}

void init() {
    dfs(1);
    hld(1);
}

int query(int l, int r) {
    auto it = s.lower_bound(l);
    if (it == s.end()) return INT_MAX;
    if (*it >= l && *it <= r) return (*it);
    return INT_MAX;
}

int ans_hld(int u, int v) { // u la cha v
    int ans = INT_MAX;
    while (id[u] != id[v]) {
        int v2 = head[id[v]];
        ans = min(ans, query(pos[v2], pos[v]));
        v = p[0][v2];
    }
}
```

```
    }
    ans = min(ans, query(pos[u], pos[v]));
    if (ans == INT_MAX) return -1;
    return e[ans];
}

void solve() {
    int n, q; cin >> n >> q;
    for (int i = 1; i < n; i++) {
        int u, v; cin >> u >> v;
        adj[u].pb(v); adj[v].pb(u);
    }
    init();
    while (q--) {
        int typ; cin >> typ;
        if (typ == 1) {
            int v; cin >> v;
            cout << ans_hld(1, v) << '\n';
        }
        else {
            int v; cin >> v;
            if (s.find(pos[v]) != s.end())
                s.erase(s.find(pos[v]));
            else s.insert(pos[v]);
        }
    }
}

int32_t main() {
    ios_base::sync_with_stdio(0);
    cin.tie(nullptr); cout.tie(nullptr);
    solve();
    return 0;
}

/*
9 8
1 2
1 3
2 4
2 9
5 9
7 9
8 9
6 8
*/
```

```

1 3
0 8
1 6
1 7
0 2
1 9
0 2
1 9
*/

```

2.8 HLD₃

```

/**
 * Given a rooted tree of nodes, where each
 * node is uniquely numbered in between
 * [1..N]. The node 1 is the root of the
 * tree. Each node has an integer value
 * which is initially 0.
 * You need to perform the following two kinds
 * of queries on the tree:
 * * add t value: Add value to all nodes in
 *   subtree rooted at t
 * * max a b: Report maximum value on the
 *   path from a to b
 * Tested:
 *   https://vjudge.net/problem/HackerRank-subtrees-and-paths
 */

#include<bits/stdc++.h>

using namespace std;

#define int long long
#define pb push_back

const int INF = 1e9 + 7;
const int N = 2e5 + 5;

vector<int> adj[N];
int id[N], head[N], sz[N], in[N], out[N],
    h[N], pos[N];
int p[20][N];
int nhanh = 1, cnt;

```

```

int seg[4 * N], lazy[4 * N];

void down(int id) {
    int t = lazy[id];
    int lhs = id * 2, rhs = id * 2 + 1;
    seg[lhs] += t; seg[rhs] += t;
    lazy[lhs] += t; lazy[rhs] += t;
    lazy[id] = 0;
}

void update(int id, int l, int r, int u, int
    v, int val) {
    if (l > v || r < u) return;
    if (l >= u && r <= v) {
        seg[id] += val;
        lazy[id] += val;
        return;
    }
    down(id);
    int mid = (l + r) / 2;
    update(id * 2, l, mid, u, v, val);
    update(id * 2 + 1, mid + 1, r, u, v, val);
    seg[id] = max(seg[id * 2], seg[id * 2 +
        1]);
}

int get(int id, int l, int r, int u, int v) {
    if (l > v || r < u) return -INF;
    if (l >= u && r <= v) return seg[id];
    down(id);
    int mid = (l + r) / 2;
    return max(get(id * 2, l, mid, u, v),
        get(id * 2 + 1, mid + 1, r, u, v));
}

void dfs(int u, int par = 1) {
    sz[u] = 1;
    p[0][u] = par;
    for (int i = 1; i < 20; i++) p[i][u] =
        p[i - 1][p[i - 1][u]];
    for (int v : adj[u]) if (v != par) {
        h[v] = h[u] + 1;
        dfs(v, u);
        sz[u] += sz[v];
    }
}

```

```

}
}

void hld(int u, int par = -1) {
    if (head[nhanh] == 0) {
        head[nhanh] = u;
    }
    ++cnt;
    in[u] = cnt;
    id[u] = nhanh;
    pos[u] = cnt;

    int target = -1;
    for (int v : adj[u]) if (v != par) {
        if (target == -1 || sz[target] < sz[v])
            target = v;
    }

    if (target != -1) hld(target, u);

    for (int v : adj[u]) if (v != par) {
        if (v != target) {
            ++nhanh;
            hld(v, u);
        }
    }
    out[u] = cnt;
}

int query(int u, int v) {
    int ans = -INF;
    while (id[u] != id[v]) {
        if (h[head[id[u]]] > h[head[id[v]]])
            swap(v, u);
        int v2 = head[id[v]];
        ans = max(ans, get(1, 1, cnt, pos[v2],
            pos[v]));
        v = p[0][v2];
    }
    if (pos[u] > pos[v]) swap(u, v);
    ans = max(ans, get(1, 1, cnt, pos[u],
        pos[v]));
    return ans;
}

```

```

void solve() {
    int n; cin >> n;
    for (int i = 1; i < n; i++) {
        int u,v; cin >> u >> v;
        adj[u].pb(v);
        adj[v].pb(u);
    }

    dfs(1);
    hld(1);

    int q; cin >> q;
    while (q--) {
        string typ; cin >> typ;
        if (typ == "add") {
            int u,val; cin >> u >> val;
            update(1,1,cnt,in[u], out[u], val);
        }
        else {
            int u,v; cin >> u >> v;
            cout << query(u,v) << '\n';
        }
    }
}

int32_t main() {
    ios_base::sync_with_stdio(0);
    cin.tie(nullptr); cout.tie(nullptr);
    solve();
    return 0;
}

/*
5
1 2
2 3
2 4
5 1
6
add 4 30
add 5 20
max 4 5
add 2 -20
max 4 5
max 3 4

```

```

*/

```

2.9 HopcroftKarp

```

/**
 * Description: Fast bipartite matching
 *              algorithm. Graph $g$ should be a list
 * of neighbors of the left partition, and
 * $btoa$ should be a vector full of
 * -1's of the SAME SIZE as the right
 * partition. Returns the size of
 * the matching. btoa[i] will be the match for
 * vertex i on the right side,
 * or -1 if it's not matched.
 * Usage: vector<int> btoa(m, -1);
 *        hopcroftKarp(g, btoa);
 * Time: O(sqrt(V)*E)
 * Tested: https://oj.vnoi.info/problem/match1
 * Tested: https://oj.vnoi.info/problem/fmatch
 */

```

```

bool dfs(int a, int L, vector<vector<int>>&
g, vector<int>& btoa, vector<int>& A,
vector<int>& B) {
    if (A[a] != L) return 0;
    A[a] = -1;
    for (int b : g[a]) if (B[b] == L + 1) {
        B[b] = 0;
        if (btoa[b] == -1 ||
            dfs(btoa[b], L + 1, g,
                btoa, A, B))
            return btoa[b] = a, 1;
    }
    return 0;
}

```

```

int hopcroftKarp(vector<vector<int>>& g,
vector<int>& btoa) {
    int res = 0;
    vector<int> A(g.size()),
        B(btoa.size()), cur, next;
    for (;;) {
        fill(A.begin(), A.end(), 0);

```

```

        fill(B.begin(), B.end(), 0);
        /// Find the starting nodes for
        /// BFS (i.e. layer 0).
        cur.clear();
        for (int a : btoa) if (a != -1)
            A[a] = -1;
        for (int a = 0; a < g.size();
            a++) if (A[a] == 0)
            cur.push_back(a);
        /// Find all layers using bfs.
        for (int lay = 1;; lay++) {
            bool islast = 0;
            next.clear();
            for (int a : cur) for
                (int b : g[a]) {
                if (btoa[b] ==
                    -1) {
                    B[b] =
                        lay;
                    islast =
                        1;
                }
                else if (btoa[b]
                    != a &&
                    !B[b]) {
                    B[b] =
                        lay;
                    next.push_back(bt
                }
            }
            if (islast) break;
            if (next.empty()) return
                res;
            for (int a : next) A[a]
                = lay;
            cur.swap(next);
        }
        /// Use DFS to scan for
        /// augmenting paths.
        for (int a = 0; a < g.size(); a++)
            res += dfs(a, 0, g,
                btoa, A, B);
    }
}

```

```
signed main() {
    int n,m,p;
    cin >> n >> m >> p;
    vector<vector<int>> g(n + 1,vector<int>());
    while (p--) {
        int u,v;
        cin >> u >> v;
        g[u].push_back(v);
    }
    vector<int> btoa(m + 1, -1);
    cout << hopcroftKarp(g, btoa) << '\n';

    /// Find all matching, btoa[i] is the left
    side of i(The right side)
    for (int i = 0; i < btoa.size(); i++)
        if (btoa[i] != -1)
            cout << btoa[i] << "->" << i <<
                "\n";
}
```

2.10 MinimumVertexCover

```
/**
 * Description: Finds a minimum vertex cover
 *              in a bipartite graph.
 * The size is the same as the size of a
 * maximum matching, and
 * the complement is a maximum independent
 * set.
 * Status: stress-tested
 */

/**
 * DAG
 * Maximum Independent Set == Minimum Path
 * Cover
 * Minimum Path Cover = n - Maximum Bipartite
 * Matching
 * Minimum vertex cover of DAG == Maximum
 * Bipartite Matching
 */

#include "DFSMatching.cpp"
```

```
vi cover(vector<vi>& g, int n, int m) {
    vi match(m, -1);
    int res = dfsMatching(g, match);
    vector<bool> lfound(n, true), seen(m);
    for (int it : match) if (it != -1)
        lfound[it] = false;
    vi q, cover;
    rep(i,0,n) if (lfound[i])
        q.push_back(i);
    while (!q.empty()) {
        int i = q.back(); q.pop_back();
        lfound[i] = 1;
        for (int e : g[i]) if (!seen[e]
            && match[e] != -1) {
            seen[e] = true;
            q.push_back(match[e]);
        }
    }
    rep(i,0,n) if (!lfound[i])
        cover.push_back(i);
    rep(i,0,m) if (seen[i])
        cover.push_back(n+i);
    assert(sz(cover) == res);
    return cover;
}
```

2.11 Minimum $path_{cover}$ in DAG

```
#include <bits/stdc++.h>

#define MAX 505
#define clr(ar) memset(ar, 0, sizeof(ar))
#define read() freopen("lol.txt", "r", stdin)
#define dbg(x) cout << #x << " = " << x << endl
#define ran(a, b) (((rand() << 15) ^ rand()) % ((b) - (a) + 1)) + (a))

using namespace std;
/// Minimum path cover/Maximum independent
set in DAG
namespace dag{
```

```
/// For transitive closure and minimum
path cover with not necessarily
disjoint vertex
bool ar[MAX][MAX];

vector<int> adj[MAX];
bool visited[MAX], first_set[MAX],
second_set[MAX];
int n, L[MAX], R[MAX], D[MAX], Q[MAX],
dis[MAX], parent[MAX];

inline void init(int nodes){ /// Number of
vertices in DAG
    n = nodes;
    for (int i = 0; i < MAX; i++)
        adj[i].clear();
}

inline void add_edge(int u, int v){ /// 0
based index, directed edge of DAG
    adj[u].push_back(v);
}

bool dfs(int i){
    int len = adj[i].size();
    for (int j = 0; j < len; j++){
        int x = adj[i][j];
        if (L[x] == -1 || (parent[L[x]] ==
            i)){
            if (L[x] == -1 || dfs(L[x])){
                L[x] = i, R[i] = x;
                return true;
            }
        }
    }
    return false;
}

bool bfs(){
    clr(visited);
    int i, j, x, d, f = 0, l = 0;

    for (i = 0; i < n; i++){
        if (R[i] == -1){
            visited[i] = true;
```

```

        Q[l++] = i, dis[i] = 0;
    }
}

while (f < l){
    i = Q[f++];
    int len = adj[i].size();
    for (j = 0; j < len; j++){
        x = adj[i][j], d = L[x];
        if (d == -1) return true;

        else if (!visited[d]){
            Q[l++] = d;
            parent[d] = i, visited[d] =
                true, dis[d] = dis[i] +
                1;
        }
    }
}

return false;
}

void get_path(int i){
    first_set[i] = true;
    int j, x, len = adj[i].size();

    for (j = 0; j < len; j++){
        x = adj[i][j];
        if (!second_set[x] && L[x] != -1){
            second_set[x] = true;
            get_path(L[x]);
        }
    }
}

void transitive_closure(){ /// Transitive
    closure in O(n * m)
    clr(ar);
    int i, j, k, l;
    for (i = 0; i < n; i++){
        l = adj[i].size();
        for (j = 0; j < l; j++){
            ar[i][adj[i][j]] = true;
        }
        adj[i].clear();

```

```

    }

    for (k = 0; k < n; k++){
        for (i = 0; i < n; i++){
            if (ar[i][k]){
                for (j = 0; j < n; j++){
                    if (ar[k][j]) ar[i][j] =
                        true;
                }
            }
        }
    }

    for (i = 0; i < n; i++){
        for (j = 0; j < n; j++){
            if (i != j && ar[i][j]){
                adj[i].push_back(j);
            }
        }
    }

    /// Minimum vertex disjoint path cover in
    DAG. Handle isolated vertices
    appropriately
    int minimum_disjoint_path_cover() {
        int i, res = 0;
        memset(L, -1, sizeof(L));
        memset(R, -1, sizeof(R));

        while (bfs()){
            for (i = 0; i < n; i++){
                if (R[i] == -1 && dfs(i)) res++;
            }
        }

        return n - res;
    }

    int minimum_path_cover(){ /// Minimum path
        cover in DAG. Handle isolated vertices
        appropriately
        transitive_closure();
        return minimum_disjoint_path_cover();
    }
}

```

```

/// Minimum vertex cover of DAG, equal to
maximum bipartite matching
vector<int> minimum_vertex_cover(){
    int i, res = 0;
    memset(L, -1, sizeof(L));
    memset(R, -1, sizeof(R));

    while (bfs()){
        for (i = 0; i < n; i++){
            if (R[i] == -1 && dfs(i)) res++;
        }
    }

    vector<int> v;
    clr(first_set), clr(second_set);
    for (i = 0; i < n; i++){
        if (R[i] == -1) get_path(i);
    }

    for (i = 0; i < n; i++){
        if (!first_set[i] || second_set[i])
            v.push_back(i);
    }

    return v;
}

/// Maximum independent set of DAG, all
vertices not in minimum vertex cover
vector<int> maximum_independent_set() {
    vector<int> v =
        minimum_vertex_cover();
    clr(visited);
    int i, len = v.size();
    for (i = 0; i < len; i++)
        visited[v[i]] = true;

    vector<int> res;
    for (i = 0; i < n; i++){
        if (!visited[i]) res.push_back(i);
    }

    return res;
}
}

```

2.12 Tarjan

```

int n,m;
vector<int> g[N];

bool onStack[N];
stack<int> st;
int tin[N], low[N];
int dfsTime=0;

int SCCCount=0;
/*
memset(tin,0,sizeof tin);
memset(onStack,false,sizeof onStack);
*/

void dfs(int u) {
    onStack[u]=true;st.push(u);
    low[u]=tin[u]=++dfsTime;

    for(int v : g[u]){
        // cout<<u<<" -> "<<v<<endl;
        if (!tin[v]) dfs(v);
        if (onStack[v])
            low[u]=min(low[u],low[v]); //
            low[v] not tin[v]
    }

    if (low[u]==tin[u]){ // new SCC found
        while (!st.empty()){
            int a = st.top();
            onStack[a]=false;st.pop();
            printf("%d ",a);
            if (a == u){
                printf("\n");
                break;
            }
        }
        SCCCount++;
    }
}

```

2.13 bridge

```

int n, m;
vector<int> g[N];

int tin[N], low[N];
int dfsTime = 0;

bool articulation_point[N];
int bridge_count = 0;

void dfs(int u, int pre = -1) {
    tin[u] = low[u] = ++dfsTime;
    int child = 0;

    for (int v : g[u]) {
        if (v == pre) continue;
        if (tin[v]) low[u] = min(low[u],
                                tin[v]);
        else {
            dfs(v, u);
            low[u] = min(low[u], low[v]);
            child++;

            if (low[v] > tin[u]) bridge_count++;
            if (low[v] >= tin[u] && pre != -1)
                articulation_point[u] = true;
        }
    }

    if (pre == -1 && child >= 2)
        articulation_point[u] = true;
}

```

2.14 dijkstra

```

struct dijkstra {
    int n;
    vector<vector<pair<int, long long>>> >
        g;
    int s;
    vector<long long> dist;

```

```

    dijkstra(int n): n(n) {
        g.assign(n + 1,
            vector<pair<int, long long>
                >());
        dist.assign(n + 1, 1e18);
    }

    void add_edge(int u, int v, ll c) {
        // change this whether directed
        // or not
        g[u].push_back(make_pair(v,c));
        g[v].push_back(make_pair(u,c));
    }

    void build() {
        set<pair<long long, int> > st;

        st.insert(make_pair(0, s));
        dist[s] = 0;

        while (st.size()) {
            long long du =
                st.begin()->fi; int
                u = st.begin()->se;
            st.erase(st.begin());
            if (du != dist[u])
                continue;

            for (auto &[v, c] :
                g[u]) {
                if (dist[v] >
                    dist[u] + c)
                {
                    dist[v] =
                        dist[u]
                        + c;
                    st.insert(make_pa
                        v));
                }
            }
        }
    };

```

2.15 dsu

```
class dsu {
    vector<int> parent, size;

public:
    dsu() {}

    dsu(int n) {
        parent.resize(n);
        size.assign(n, 1);
        iota(all(parent), 0);
    }

    int find(int v) {
        if (v == parent[v]) return v;
        return parent[v] = find(parent[v]);
    }

    bool unite(int a, int b) {
        a = find(a);
        b = find(b);
        if (a != b) {
            if (size[a] < size[b]) swap(a, b);
            parent[b] = a;
            size[a] += size[b];
            return true;
        } else {
            return false;
        }
    }
};
```

2.16 lca-binarylift

```
/**
 * Description: Finding LCA and Kth Ancestor
 *              using Binary Lifting
 * Caution:
 * * adj must be one-indexed
 * * root must be 1 (can be modified if
 *   required)
```

```
* Source :
    https://oj.vnoi.info/submission/4618381
* Verification :
    https://oj.vnoi.info/problem/hbtlca
*
* usage LCA lca(n + 1, root) // default root
    is 1
*/
```

```
struct LCA {
    vector<vector<int>> par;
    vector<int> dep;
    int LG;

    void dfs(int u, int p = 0) {
        par[u][0] = p;
        for (int i = 1; i < LG; i++)
            par[u][i] = par[par[u][i - 1]][i - 1];
        for (int v : adj[u]) {
            if (v == p) continue;
            dep[v] = dep[u] + 1;
            dfs(v, u);
        }
    }

    int ancestor(int u, int k) {
        for (int i = 0; i < LG; i++)
            if (k & (1 << i))
                u = par[u][i];
        return u;
    }

    int lca(int u, int v) {
        if (dep[u] < dep[v]) swap(u, v);
        u = ancestor(u, dep[u] - dep[v]);
        if (u == v) return u;
        for (int i = LG - 1; i >= 0; i--)
            if (par[u][i] != par[v][i])
                u = par[u][i], v = par[v][i];
        return par[u][0];
    }
}
```

```
LCA (int _n, int root = 1) {
    int n = _n;
    LG = 64 - __builtin_clzll(n);
    par.assign(n, vector<int>(LG, 0));
```

```
    dep.assign(n, 0);
    dfs(root);
}
};
```

2.17 tree-diameter

```
/**
 * Description: Finding the diameter of tree
 *              in  $O(V + E)$ 
 */
```

```
struct TD {
    int ans = 0;
    vector<vector<int>> g;

    int Dfs (int u, int pr) {
        pi lol = {0, 0};
        for (int v : g[u]) {
            if (v == pr) continue;
            int te = Dfs(v, u);
            if (lol.ff < te) {
                lol.ss = lol.ff;
                lol.ff = te;
            } else if (lol.ss < te) {
                lol.ss = te;
            }
        }
        ans = max(ans, lol.ff + lol.ss);
        return lol.ff + 1;
    }

    int run() {
        Dfs(1, 1);
        return ans;
    }

    TD(vector<vector<int>>& _g) : g(_g) {}
};
```

3 mathematics

3.1 MI

```
#include <bits/stdc++.h>

#define ii pair<int,int>
#define ll long long

using namespace std;

const int N = 3e5;
const ll MOD = 1e9 + 7;

//Necessary function
ll mul(ll a, ll b){return
    (a%MOD)*(b%MOD)%MOD;}
ll add(ll a, ll b){return ((a+MOD)%MOD +
    (b+MOD)%MOD)%MOD;}
ll fpow(ll a, ll b){
    ll res=1;
    while (b){
        if (b & 1) res=mul(res,a);
        b>>=1;
        a=mul(a,a);
    }
    return res;
}
ll inv(ll a) {return fpow(a,MOD-2);}

// Euler's totient function. Source:
// cp-algorithms.com
vector<ll> phi_1_to_n(int n) {
    vector<ll> phi(n + 1);
    for (int i = 0; i <= n; i++)
        phi[i] = i;

    for (int i = 2; i <= n; i++) {
        if (phi[i] == i) {
            for (int j = i; j <= n; j += i)
                phi[j] -= phi[j] / i;
        }
    }
    return phi;
}
```

```
}

int main(){
    //freopen("main.inp","r",stdin);

    /*
    Calculate MI of factorials
    inv(fact[i]%MOD) (calculate the factorial
    with modulo first then calc the
    inverse.)
    */

    vector<ll> factinv(N,0), fact(N,1);
    for (int i=1;i<N;i++) {
        fact[i]=mul(fact[i-1],i);
        factinv[i]=inv(fact[i]);

        if (i <= 10) cout<<fact[i]<<" ";
    }cout<<endl;

    assert(mul(fact[4],factinv[4]) == 1);
}
```

3.2 Point-Line

```
#define pt pair<long long, long long>
#define x first
#define y second

struct Line {
    pt a, ab;

    Line(pt _a, pt _ab): a(_a), ab(_ab) {}
};

pt operator - (const pt& a, const pt& b)
    {return make_pair(a.x - b.x, a.y - b.y);}

ll operator * (const pt& a, const pt& b)
    {return a.x*b.x + a.y*b.y;}

ll operator ^ (const pt& a, const pt& b)
    {return a.x*b.y - a.y*b.x;}
```

```
pt refine(pt a) { // only for pt = pair<ll,
    ll>
    ll g = gcd(a.x, a.y);
    if (!g) return a;

    if (g < 0) g = -g;
    a.x /= g, a.y /= g;
    return a;
}

int dir(pt a, pt b, pt c) {
    ll x = (b - a) ^ (c - a);

    if (x == 0) return 0;
    else if (x > 0) return 1;
    else return 2;
}
```

3.3 combinatorics-power

```
vector<Mint> fact(1, 1);
vector<Mint> inv_fact(1, 1);

Mint power(const Mint a, const int b) {
    assert(b >= 0);
    Mint x = a, res = 1;
    U p = b;
    while (p > 0) {
        if (p & 1) res *= x;
        x *= x;
        p >>= 1;
    }
    return res;
}

/*
Mint C(int n, int k) {
    if (k < 0 || k > n) {
        return 0;
    }
    k = min(k, n - k);
    while ((int) fact.size() < k + 1) {
```

```

    fact.push_back(fact.back() * (int)
        fact.size());
    inv_fact.push_back(1 / fact.back());
}
Mint ret = inv_fact[k];
for (int i = 1; i <= k; i++) {
    ret *= n - i + 1;
}
return ret;
}
*/

Mint C(int n, int k) {
    if (k < 0 || k > n) {
        return 0;
    }
    k = min(k, n - k);
    while ((int) fact.size() < n + 1) {
        fact.push_back(fact.back() * (int)
            fact.size());
        inv_fact.push_back(1 / fact.back());
    }
    return fact[n] * inv_fact[k] * inv_fact[n -
        k];
}

```

3.4 convex-hull

```

struct Point {
    long long x, y;
};

bool operator < (const Point & a, const Point
    & b) {
    return ii(a.x, a.y) < ii(b.x, b.y);
}

ostream & operator << (ostream & out, const
    Point& a) {
    out << "(" << a.x << ", " << a.y << ")";
    return out;
}

```

```

istream & operator >> (istream & is, Point&
    a) {
    is >> a.x >> a.y;
    return is;
}

// A -> B -> C form counterclockwise direction
bool ccw(const Point &A, const Point &B,
    const Point &C) {
    return (B.x - A.x) * (C.y - A.y) - 1LL *
        (C.x - A.x) * (B.y - A.y) > 0;
}

// CONVEX HULL (CLOCKWISE)
// Source: from VNOI Wiki with small
// modification
// for speed might change to vector<Point>& p
vector<Point> convexHull(vector<Point> p) {
    int n = p.size();

    if (n < 3) {
        // cannot form convex hull
        return vector<Point>();
    }

    // SORT POINTS
    sort(p.begin(), p.end(), [](const Point
        &A, const Point &B) {
        if (A.x != B.x) return A.x < B.x;
        return A.y < B.y;
    });

    vector<Point> hull;
    hull.push_back(p[0]);

    // UPPER HULL
    for (int i = 1; i < n; ++i) {
        while (hull.size() >= 2 &&
            ccw(hull[hull.size() - 2],
                hull.back(), p[i])) {
            hull.pop_back();
        }
        hull.push_back(p[i]);
    }
}

```

```

// LOWER HULL
for (int i = n - 2; i >= 0; --i) {
    while (hull.size() >= 2 &&
        ccw(hull[hull.size() - 2],
            hull.back(), p[i])) {
        hull.pop_back();
    }
    hull.push_back(p[i]);
}

// REMOVE 1 OVERLAPPING
if (n > 1) hull.pop_back();

return hull;
}

```

3.5 matrix-mod

```

//Template from VNOI:
https://wiki.vnoi.info/algo/trick/matrix-multipli
    with some modification
// ofc this is 0-indexed
template<typename T>
struct matrix_mod {
    T add(T a, T b) {
        return ((a+MOD)%MOD + (b+MOD)%MOD)%MOD;
    }
    T mul(T a, T b) {
        a *= b;
        if (a > MOD) a %= MOD;
        return a;
    }
    vector <vector <T> > data;

    int row() const { return data.size(); }
    int col() const { return data[0].size(); }

    auto & operator [] (int i) { return
        data[i]; }
    const auto & operator [] (int i) const {
        return data[i]; }

    matrix_mod() = default;
}

```

```

matrix_mod(int r, int c): data(r, vector
    <T> (c)) { }
matrix_mod(const vector <vector <T> > &d):
    data(d) {
    assert(d.size());
    int size = d[0].size();
    assert(size);
    for (auto x : d) assert(x.size() ==
        size);
}

friend ostream & operator << (ostream
    &out, const matrix_mod &d) {
    for (auto x : d.data) {
        for (auto y : x) out << y << ' ';
        out << '\n';
    }
    return out;
}

static matrix_mod identity(long long n) {
    matrix_mod a = matrix_mod(n, n);
    while (n--> 0) a[n][n] = 1;
    return a;
}

matrix_mod operator * (const matrix_mod
    &b) {
    matrix_mod a = *this;
    assert(a.col() == b.row());
    matrix_mod c(a.row(), b.col());
    for (int i = 0; i < a.row(); ++i)
        for (int j = 0; j < b.col(); ++j)
            for (int k = 0; k < a.col(); ++k)
                c[i][j] = add(c[i][j],
                    mul(a[i][k], b[k][j]));
    return c;
}

matrix_mod pow(long long exp) {
    assert(row() == col());
    matrix_mod base = *this, ans =
        identity(row());

```

```

        for (; exp > 0; exp >= 1, base = base
            * base)
            if (exp & 1) ans = ans * base;
        return ans;
    }
};

```

3.6 modint

```

/*
 * Caution:
 * * need to cast into int before printing
 * source: Benq
 */
struct Mint {
    int v;
    explicit operator int() const { return v; }
    Mint() { v = 0; }
    Mint(long long _v) : v(_v % MOD) { v += (v <
        0) * MOD; }
};
Mint &operator+=(Mint &a, Mint b) {
    if ((a.v += b.v) >= MOD) a.v -= MOD;
    return a;
}
Mint &operator-=(Mint &a, Mint b) {
    if ((a.v -= b.v) < 0) a.v += MOD;
    return a;
}
Mint operator+(Mint a, Mint b) { return a +=
    b; }
Mint operator-(Mint a, Mint b) { return a -=
    b; }
Mint operator*(Mint a, Mint b) { return
    Mint((long long)a.v * b.v); }
Mint &operator*=(Mint &a, Mint b) { return a
    = a * b; }
Mint pow(Mint a, long long p) {
    assert(p >= 0);
    return p == 0 ? 1 : pow(a * a, p / 2) * (p &
        1 ? a : 1);
}
Mint inv(Mint a) {

```

```

    assert(a.v != 0);
    return pow(a, MOD - 2);
}
Mint operator/(Mint a, Mint b) { return a *
    inv(b); }

```

4 string

4.1 bin_{trie}

```

struct bin_trie {
    struct node {
        int nxt[2];
        int cnt;
        node() {
            cnt = 0;
            nxt[0] = nxt[1] = -1;
        }
    };
    int maxbit = 40; // change this if ai
    // <= 10^18
    int sz;
    vector<node> b;
    bin_trie() {
        b.assign(1, node());
        sz = 0;
    }
    void add(long long s) {
        int u = 0;
        for (int k = maxbit; k >= 0; k--) {
            bool id = (1ll << k) & s;
            if (b[u].nxt[id] == -1) {
                b[u].nxt[id] =
                    ++sz;
                b.push_back(node());
            }
            u = b[u].nxt[id];
            b[u].cnt++;
        }
    };
};

```

4.2 hashing

```

struct hashing {
    //create MOD outside
    long long base = 311;
    int n;
    vector<long long> hs;
    vector<long long> invbase;

    hashing(string s) {
        n = s.size();
        hs.assign(n, 0); invbase.assign(n, 0);
        long long iv = inv(base);

        hs[0] = s[0]; invbase[0] = 1;
        long long p = 1;
        for (int i = 1; i < n; i++) {
            p = mul(p, base);
            hs[i] = add(hs[i - 1], mul(s[i],
                p));
            invbase[i] = mul(invbase[i - 1],
                iv);
        }

        ll get(ll l, ll r) {
            ll res = hs[r];
            if (l) {
                res = add(res, -hs[l - 1]);
                res = mul(res, invbase[l]);
            }
            return res;
        }
    };
};

```

4.3 prefix-function

```

vector<int> prefix_function (const string& s)
{
    int n = (int) s.length();
    vector<int> prefix(n, 0);

```

```

    for (int i = 1; i < n; i++) {
        int j = prefix[i - 1];
        while (j > 0 && s[i] != s[j]) j = prefix[j
            - 1];
        if (s[i] == s[j]) j++;
        prefix[i] = j;
    }
    return prefix;
}

```

4.4 rolling_hash

```

// rolling hash with one-based indexing
//
// usage Hash(s, BASE)
//
// query
// hash.fwd(l, r) //get forward hash
// hash.bwd(l, r) //get backward hash

```

```

struct Hash {
    int hash[N], hashR[N], pow[N];
    Hash(string &s, int BASE) {
        int n = s.size() - 1;
        hash[0] = 0;
        hashR[0] = 0;
        pow[0] = 1;
        for(int i = 1; i <= n; i++) {
            pow[i] = (pow[i - 1] * BASE) % MOD;
        }
        for(int i = 1; i <= n; i++) {
            hash[i] = (hash[i - 1] * BASE + s[i] -
                'a' + 1) % MOD;
        }
        for(int i = n; i >= 1; i--) {
            hashR[i] = (hashR[i + 1] * BASE + s[i] -
                'a' + 1) % MOD;
        }
    }
    int fwd(int i, int j) {

```

```

        return (hash[j] - hash[i - 1] * pow[j - i
            + 1] + MOD * MOD) % MOD;
    }
    int bwd(int i, int j) {
        return (hashR[i] - hashR[j + 1] * pow[j -
            i + 1] + MOD * MOD) % MOD;
    }
};

```

4.5 str_trie

```

struct str_trie {
    struct node {
        vector<int> nxt;
        int end;

        node(int n) {
            end = 0;
            nxt.assign(n, -1);
        }
    };

    int sz;
    vector<node> b;

    str_trie(int maxb = 0) {
        b.assign(maxb + 5, node(26));
        sz = 0;
    }

    void add(string s) {
        int u = 0;
        for (char c : s) {
            if (b[u].nxt[c - 'a'] == -1)
                b[u].nxt[c - 'a'] = ++sz;
            u = b[u].nxt[c - 'a'];
        }
        b[u].end++;
    }
};

```
