

FACULTY OF ENGINEERING

B.E. 3/4 (CSE) I – Semester (Main & Backlog) Examination, December 2017

Subject: Automata Languages and Computation

Time: 3 Hours

Max.Marks: 75

Note: Answer all questions from Part A and any five questions from Part B.

PART – A (25 Marks)

- 1 Distinguish between NFA and DFA. 3
- 2 What are regular expressions? 2
- 3 Compare right linear grammar and left line grammar. 3
- 4 What do you mean by ambiguous grammar? 2
- 5 State the general form of transition function for NPDA. 2
- 6 State pumping lemma for CFG. 3
- 7 What is restricted turing machine? 3
- 8 Mention ID format for TM. 2
- 9 What do you mean by post correspondence problem? 3
- 10 State church's hypothesis. 2

PART – B (5x10 = 50 Marks)

- 11 a) Construct a DFA 6

	0	1
$\rightarrow \gamma_0$	$q_0 q_1$	q_0
q_1	ϕ	q_2
q_2	ϕ	q_3
αq_3	q_3	q_3

- b) Minimize the following DFA 4

	0	1
$\rightarrow A$	B	E
B	C	F
*C	D	H
D	E	H
E	F	I
*F	G	B
G	H	B
H	I	C
*I	A	C

- 12 a) Explain algebraic laws for regular expressions. 5
- b) Write short note on "equivalence and minimization of automata". 5
- 13 Convert the following PDA $P = \{[p, q], \{0,1\}, \{x, z_0\}, \delta, q, z_0\}$ to context for grammar if δ is given by 10
- $\delta(q, 1, z_0) = (q, xz_0)$
 $\delta(q, 1, x) = (q, xx)$
 $\delta(q, 0, x) = (p, x)$
 $\delta(q, \epsilon, x) = (q, \epsilon)$
 $\delta(p, 1, x) = (p, \epsilon)$
 $\delta(q, 0, z_0) = (q, z_0)$
- 14 Explain about the programming techniques of TM with example. 10
- 15 a) Explain post correspondence problem. 5
- b) Explain about universal language. 5
- 16 a) Given grammar C with production 5
- $S \rightarrow aB \mid bA$
 $A \rightarrow a \mid aS \mid bAA$
 $B \rightarrow b \mid bS \mid aBB$ for a string 'aaabbabbba'.
 Find the right most and left most derivation parse tree.
- b) Using pumping lemma prove $L = \{ww \mid w \in \{0,1\}^*\}$ is not CFL. 5
- 17 a) Explain the classes of P, NP and explain the terms NP – Bhard and NP – complete. 5
- b) Give the regular grammar for the language $L = \{0^n \mid n \geq 1\}$. 5

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B.E. 3/4 (CSE) I – Semester (New) (Suppl.) Examination, May/June 2017

Subject: Automata Languages and Computation

Time: 3 Hours

Max.Marks: 75

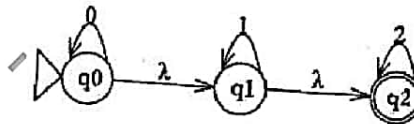
Note: Answer all questions from Part A. Answer any five questions from Part B.

PART – A (25 Marks)

- 1 Define deterministic finite automata. 2
- 2 Design a finite automaton that accepts all the strings starting with '0' and ending with '11' over the alphabet $\Sigma = \{0, 1\}$. 3
- 3 Mention the decision properties of regular languages. 2
- 4 Define context free grammar. 3
- 5 Differentiate between FA and PDA. 2
- 6 Define Greibach Normal Form with an example. 3
- 7 Define TM. 3
- 8 Mention the Extensions to the Turing Machine. 3
- 9 Define Post-Corresponding problem. 2
- 10 What is meant by Restricted Satisfiability Problem? 2

PART – B (5x10 = 50 Marks)

- 11 a) Construct DFA for the language $L = \{W \mid W \text{ does not contain the substring } 110\}$. 5
- b) Convert the following automata to regular expression. 5



- 12 a) Using Pumping lemma prove whether the following language is regular or not?

$C = \{w \mid w \text{ has an equal number of 0's and 1's}\}$. 5

- b) Given a CFG. 5

$E \rightarrow E + T / T$

$T \rightarrow T \times F / F$

$F \rightarrow (E) / a$

Give parse Tree and derivation (both LMD and RMD) for a data. Verify whether grammar is ambiguous / not.

- 13 a) Construct PDA that recognize the language $\{0^n 1^n \mid n \geq 0\}$. 5
- b) Reduce the following grammar to CNF. 5

$S \rightarrow aB / ab$

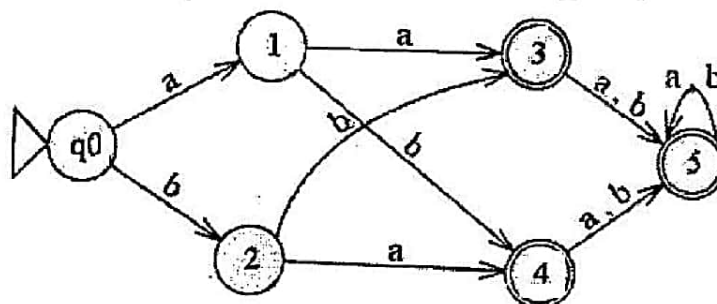
$A \rightarrow aAB / a$

$B \rightarrow ABb / b$

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- 14 a) What are the various programming techniques for Turing Machine. 5
- b) Construct a TM for multiplication of two numbers $M \times N$. 5
- 15 a) Distinguish between Recursive and Recursively Enumerable language. Give an example for each. 5
- b) Write short note on the universal Turing Machine. 5
- 16 Give the DFA accepting the set of strings over alphabet $\Sigma = \{0, 1\}$ such that in each string number of 0's is divisible by five and number of 1's is divisible by 3. Justify it with an example. 10
- 17 a) Minimize the following DFA and draw the minimized DFA. 6



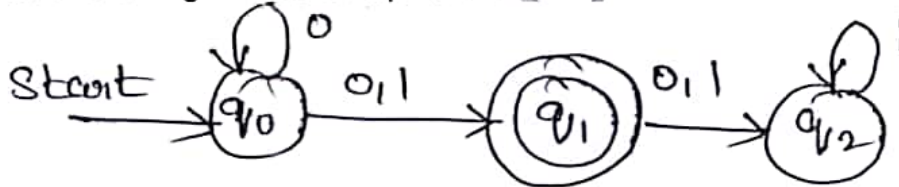
- b) Explain Chomsky classification of languages. 4

FACULTY OF ENGINEERING**B.E. 3/4 (CSE) I - Semester (Old) Examination, May / June 2017****Subject : Automata Languages and Computation****Time : 3 Hours****Max. Marks: 75****Note: Answer all questions from Part-A and answer any five questions from Part-B.****PART – A (25 Marks)**

- 1 Define Finite Automata. (2)
- 2 Determine DFA accepting all strings over $\{0, 1\}$ which begins with and ends with 01. (3)
- 3 Write down the applications of Pumping lemma of RL. (3)
- 4 Define Ambiguous grammar. (2)
- 5 Define 'δ' function of push down Automata. (3)
- 6 Define context free grammar. (2)
- 7 What do you mean by Undecidability? (2)
- 8 What is Restricted satisfiability problem? (3)
- 9 Mention the programming techniques for TM's. (2)
- 10 Define Turing machine. (3)

PART – B (50 Marks)

- 11 (a) Distinguish between DFA and NFA. (4)
- (b) Convert the following NFA to its equivalent DFA. (6)



- 12 (a) Give CFG $G = \{(A, B), \{0, 1\}, P, A\}$ where P consists of
 $A \rightarrow 0BA / 0$
 $B \rightarrow A1B / AA / 10$
 Give the RMD, LMD and parse tree for the string "001100". (5)
- (b) Obtain context free grammar to generate string consisting of any number of a's and b's with atleast one a. (5)
- 13 Obtain a PDA to accept the language $L = \{a^n b^n / n \geq 1\}$ by a final state. (10)
- 14 (a) Describe briefly about problems that computers cannot solve. (5)
- (b) Explain about Extensions to the Turing machines. (5)
- 15 Obtain a TM to accept a palindrome consisting of a's and b's of any length. (10)
- 16 (a) Define Chomsky hierarchy. (3)
- (b) What are recursively enumerable languages? Give example. (3)
- (c) Explain undecidability. (4)
- 17 (a) Write about Post correspondence problem. (5)
- (b) Give an Instance of PCP, show that this instance has no solution. (5)

i	List A	List B
1	011	101
2	11	011
3	1101	110

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B.E. 3/4 (CSE) I-Semester (New) (Main) Examination, Nov./Dec. 2016

Subject : Automata Languages and Computation

Time : 3 hours

Max. Marks : 75

Note: Answer all questions from Part-A. Answer any FIVE questions from Part-B.

PART – A (25 Marks)

- 1 Define strings, alphabets, and languages. 3
- 2 Write any two applications of finite automata. 2
- 3 Write a regular expression which accepts set of all strings whose $\Sigma = \{0, 1\}$. 2
- 4 Define pumping lemma for regular languages. 2
- 5 What do you mean by equivalence states? 3
- 6 Define Ambiguous grammar. 2
- 7 Write about Chomsky normal form. 3
- 8 Define 's' of turing machine with an example. 3
- 9 Write about classes P and NP. 3
- 10 Define undecidability. 2

PART – B (50 Marks)

- 11 a) Construct DFA for $\{W \mid W \text{ is any string except } 11 \text{ and } 111\}$ where $\Sigma = \{0, 1\}$. 5
- b) Construct DFA equivalent to the NFA's $\{(p, q, r, s), \{0, 1\}, \delta, p, \{s\}\}$. Where δ is defined as follows : 5

δ	0	1
p	{p, q}	p
q	r	r
r	s	-
s	s	s

- 12 Minimize the given below DFA. Draw the minimized resultant FA. 10

Q\S	a	b
$\rightarrow A$	B	E
B	C	D
*C	H	I
*D	I	H
E	F	G
*F	H	I
*G	H	I
H	H	H
I	I	I

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δ	0	1
p	{p, q}	p
q	r	r
r	s	-
s	s	s

- 12 Minimize the given below DFA. Draw the minimized resultant FA. 10

Q\S	a	b
$\rightarrow A$	B	E
B	C	D
*C	H	I
*D	I	H
E	F	G
*F	H	I
*G	H	I
H	H	H
I	I	I

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- 13 a) Use Pumping lemma theorem to prove whether the following languages is CFG or not. $L = \{0^n 1^n 0^n 1^n \mid n \geq 0\}$. 5
- b) Construct PDA that recognize the language $L = \{WW^R \mid W \in \{0, 1\}^*\}$. 5
- 14 Design a TM for the language. 10
- $B = \{WW \mid W \in \{0, 1\}^*\}$.
- 15 a) What is the difference between PCP and MPCP? 5
- b) Given the following list A and B of words. Is it having a solution? 5
- If so, give the sequence

	List A	List B
i	W_i	X_i
1	1	111
2	10111	10
3	10	0

- 16 a) Convert CFG which is given below into CNF form. 5
- $S \rightarrow bA/aB$
- $A \rightarrow bAA/as/a$
- $B \rightarrow aBB/bs/b$
- b) Write the FA for the regular expression $a.(a+b)^*b.b$ 5
- 17 a) What is Halting problem and its significance in automata languages? 5
- b) Explain the Chomsky's hierarchy of language. 5

FACULTY OF ENGINEERING**B.E. 3/4 (CSE) I-Semester (Old) Examination, November / December 2016****Subject : Automata Languages and Computation****Time : 3 hours****Max. Marks : 75****Note: Answer all questions from Part-A. Answer any FIVE questions from Part-B.****PART – A (25 Marks)**

- 1 Define deterministic finite automata. 2
- 2 Determine an NFA accepting all strings over $\{0, 1\}$ which end in 1, but do not contain the substring 00. 3
- 3 Write any three decision properties of regular languages. 3
- 4 Draw parse tree of an example string of a grammar. 2
- 5 Define push down automata. 2
- 6 Define left recursion. 2
- 7 Eliminate unit productions from the grammar
 $S \rightarrow A0|B, B \rightarrow A|11, A \rightarrow 0|2|B.$ 3
- 8 Write about GNF. 3
- 9 Distinguish between classes P and NP. 3
- 10 Define PCP. 2

PART – B (50 Marks)

- 11 a) Write about informal picture of finite automata. 5
 - b) Obtain a DFA to accept strings of a's and b's having even number of a's and b's. 5
 - 12 a) State and prove pumping lemma for regular languages. 5
 - b) Show that $L = \{a^n b^n | n \geq 0\}$ is not regular. 5
 - 13 Obtain a PDA to accept the language $L(M) = \{WCW^R | W \in (a+b)^*\}$ where W^R is reverse of W by a final state. 10
 - 14 a) Write in detail about programming techniques for T/M. 5
 - b) Explain briefly about ID's of TM. 5
 - 15 Prove that for every nondeterministic TM (NTM) there exists a determine TM (DTM) such that $L(NTM) = L(DTM)$. 10
 - 16 a) Write about CNF and GNF. 4
 - b) Convert the following grammar into GNF. 6
- $$S \rightarrow AA | 0$$
- $$A \rightarrow SS | 1$$
- 17 a) Explain a restricted satisfiability problem. 5
 - b) Explain the terms NP-complete and NP-hard. 5

FACULTY OF ENGINEERING**B.E. 3/4 (CSE) I - Semester (Main) Examination, December 2015****Subject : Automata Languages and Computation****Time : 3 hours****Max. Marks : 75****Note: Answer all questions from Part-A. Answer any FIVE questions from Part-B.****PART – A (25 Marks)**

- 1 Define the term 'Automata' with an example. 3
- 2 What are regular expressions? 2
- 3 Compare right-linear grammar with left-linear grammar. 3
- 4 What do you mean by inherently ambiguous language? 2
- 5 State the general form of transition function for NPDA. 2
- 6 State the pumping lemma for CFG. 3
- 7 What are the reasons for a TM not accepting its input? 3
- 8 What are the types of Turing machines? 2
- 9 What do you mean by Post's correspondence problem? 3
- 10 What do you mean by Recursively enumerable languages? 2

PART – B (50 Marks)

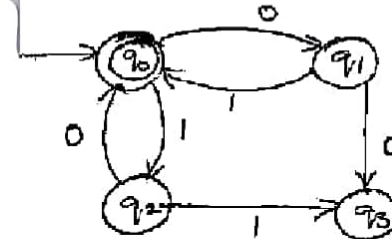
- 11 a) Determine the DFA that accepts the language $L(ab(a+ab^*(a+aa)))$. 5
b) Construct a finite-state machine that delays an input string two bits, given 00 as the first two bits of output. 5
- 12 a) Given grammar G with productions $S \rightarrow aB|bA, A \rightarrow a|aS|bAA, B \rightarrow b|bs|aBB$. For the string aaabbabbba, find a rightmost derivation, leftmost derivation and parse tree. 5
b) Obtain a CFG for generating all integers. 5
- 13 a) Construct a PDA equivalent to the CFG. 5
 $S \rightarrow 0BB, B \rightarrow 0S, B \rightarrow 1S, B \rightarrow 0$
b) Using pumping lemma prove that the language $L = \{ww|w \in \{0,1\}^*\}$ is not a CFL. 5
- 14 a) Design a TM that recognizes the set of all bit strings that contain an even number of 1s. 5
b) Construct a Turing machine which computer the function $f(n) = n \bmod 5$. 5
- 15 a) Find a regular expression for the language of the set of all strings of 0's and 1's whose number of 0's is divisible by 5 and whose number of 1's is even. 5
b) Compute ϵ -NFA for the following, regular expression : $1(1+10)^* + 10(0+01)^*$. 5
- 16 a) Show that the CFG with following production is Unambiguous. 5
 $S \rightarrow S(S)|\epsilon$
b) Is the following grammar ambiguous. Justify 5
 $S \rightarrow AB, A \rightarrow aA|\epsilon, B \rightarrow ab|bB|\epsilon$.
- 17 a) Explain undecidability with an example. 5
b) Explain the classes of P, NP and explain the terms NP-completed and NP-hard. 5

FACULTY OF ENGINEERING**B.E. 3/4 (CSE) I - Semester (Supplementary) Examination, June / July 2015****Subject : Automata Languages and Computation****Time : 3 hours****Max. Marks : 75****Note: Answer all questions from Part-A. Answer any FIVE questions from Part-B.****PART – A (25 Marks)**

- 1 Give grammar for the language $L(G) = 0^n \mid n \geq 1$. 3
- 2 Mention closure properties of regular languages. 3
- 3 What is a derivation tree? Explain. 3
- 4 State Church's hypothesis. 2
- 5 Give the formal definition of PDA. 2
- 6 What is universal language? 2
- 7 Explain SAT problem. 3
- 8 Give 2 applications of CFG's. 2
- 9 What is undecidability? 3
- 10 Define inherent ambiguity. 2

PART – B (50 Marks)

- 11 a) Obtain a regular expression for the finite automata. 6



- b) Define ϵ -closure of a state and explain with a suitable example. 4
- 12 a) Convert the following grammar to CNF. 6
- $S \rightarrow aAa \mid aBC$
 $A \rightarrow aS \mid bD \mid \epsilon$
 $B \rightarrow aBa \mid C \mid b$
 $C \rightarrow abb \mid DD$
 $D \rightarrow aDa$
- b) State pumping Lemma for CFL's. What are its applications? 4

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- 13 How can a PDA be converted to a grammar? Explain the methodology with the help of an example. 10
- 14 a) Construct a TM to accept the language of palindromes over the alphabet $\{a, b\}$. 6
- b) Explain Halting problem of a TM. 4
- 15 a) Find whether the given instance of PCP has a solution or not. 5

	List A	List B
1	10	101
2	011	11
3	101	011

- b) State and explain the properties of recursively enumerable languages. 5
- 16 Consider the CFG : $S \rightarrow A_1A_2 \mid A_2A_3$; $A_1 \rightarrow A_2A_1 \mid 0$; $A_2 \rightarrow A_3A_3 \mid 1$;
 $A_3 \rightarrow A_1A_2 \mid 0$ 10
- Test if "10010" is a member or not using CYK algorithm.
- 17 Give short notes on : 5
- a) CHOMSKY hierarchy 5
- b) LBA

FACULTY OF ENGINEERING
B.E. 3/4 (CSE) I-Semester (Suppl.) Examination, July 2014

Subject : Automata Languages and Computation

Time : 3 Hours

Max. Marks: 75

Note: Answer all questions of Part - A and answer any five questions from Part-B.

PART – A (25 Marks)

- 1 Define δ in a TM. (2)
- 2 State pumping lemma for CFL's. (2)
- 3 Define Church's hypothesis. (2)
- 4 Define the term LBA and explain. (2)
- 5 Prove that $(0+1)^* 100$ regular or not. (3)
- 6 State the closure properties of Regular Languages. (2)
- 7 Define PCP and MPCP. (2)
- 8 Construct a right linear grammar for $(0+1)^* 00(0+1)^*$. (3)
- 9 Convert to CNF. (3)

$S \rightarrow aB \mid bA$
 $A \rightarrow a \mid aS \mid bAA$
 $B \rightarrow b \mid bS \mid aBB$
- 10 What are intractable problem ? Explain. (3)

PART – B (50 Marks)

- 11 (a) Construct a DFA equivalent to the regular expression $10+(0+11)0^*1$. (6)
- (b) Differentiate between NFA and DFA. (4)
- 12 (a) Given CFG $G = (\{S, A\}, \{a, b\}, P, S)$ where
 P consists of $S \rightarrow aAS \mid a$
 $A \rightarrow SbA \mid SS \mid ba$
 Give the LMD, RMD and parse tree for "aabbaa" (5)
- (b) What are ambiguous grammars ? Give examples. Is the above grammar ambiguous. (5)
- 13 Design a PDA to accept equal no of a's and b's over the alphabet $(a+b)^*$. (10)
- 14 (a) Write short notes on Universal TM . (5)
- (b) Design a TM for $L \{WW^R \mid W \in (0+1)^*, R \text{ stands for Reverse}\}$. (5)
- 15 Reduce to GNF
 $S \rightarrow AA \mid O$
 $A \rightarrow SS \mid 1$ (10)
- 16 (a) Define Chomsky hierarchy. (3)
- (b) What are recursively enumerable languages? Give example. (3)
- (c) Explain undecidability. (4)
- 17 (a) Explain a restricted satisfiability problem. (5)
- (b) Explain the classes of P, NP and explain the terms NP - complete and NP-hard. (5)

FACULTY OF ENGINEERING

B.E. 3/4 (CSE) I – Semester (Main) Examination, November 2013

Subject : Automata Languages and Computation

Time : 3 hours

Max. Marks : 75

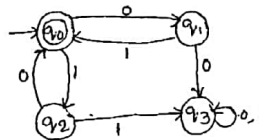
Note: Answer all questions from Part-A. Answer any FIVE questions from Part-B.

PART – A (25 Marks)

1. Obtain a DFA to accept strings of 0's, 1's and 2's beginning with a '0' followed by odd no. of 1's and ending with a '2'. 3
2. Obtain a regular expression to accept strings of a's and b's whose length is either even or multiples of 3 or both. 2
3. If $\Sigma = \{0,1\}$, $\Gamma = \{1,2,3\}$, $h(0) = 3122$, $h(1) = 132$
What is $(0+1)^*(00)^*$? 2
4. Consider the following grammar 3
 $S \rightarrow aCa$
 $C \rightarrow aCa|b$
 What is the language generated by this grammar?
5. Define Chomsky Normal Form (CNF). 2
6. Prove that reversal of a CFL is also an CFL. 3
7. What do you understand by the term LBA? 3
8. Define turning machine. How a TM accepts a language? 3
9. Define MPCP. 2
10. What is universal language? 2

PART – B (50 Marks)

- 11.a) Construct a DFA to accept decimal strings divisible by 3. 5
- b) Convert the FA to regular expression. 5



- 12.a) Prove that $(00^*1)^*1 = 1+0(0+10)^*11$. 5
- b) State and prove pumping lemma for CFL. 5

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13. Obtain a TM to accept a palindrome consisting of a's and b's of any length. 10
- 14.a) Convert the following grammar into GNF. 5
 $A \rightarrow BC$ $B \rightarrow CA/b$ $C \rightarrow AB/a$
- b) Obtain a CFG for the following PDA. 5
 $\delta(q_0, a, z) = (q_0, AZ)$, $\delta(q_0, a, A) = (q_0, A)$
 $\delta(q_0, b, A) = (q_1, \epsilon)$, $\delta(q_1, \epsilon, z) = (q_2, \epsilon)$
- 15.a) Prove that PCP is undecidable. 5
- b) State PCP and find whether given instances of PCP has solution or not. 5

	List A	List B
1	10	101
2	011	11
3	101	011

- 16.a) Obtain a TM to multiply two unary no's separated by the delimiter '1'. 6
- b) Consider the CFG $S \rightarrow A_1A_2|A_2A_3$, $A_1 \rightarrow A_2A_1|0$
 $A_2 \rightarrow A_3A_3|1$, $A_3 \rightarrow A_1A_2|0$ 4
 Test 10010 is a member or not using CYK algorithm
17. Minimize the following DFA : 10

	0	1
→ A	B	A
B	A	C
C	D	B
* D	D	A
E	D	F
F	D	E
G	F	G
H	G	D
