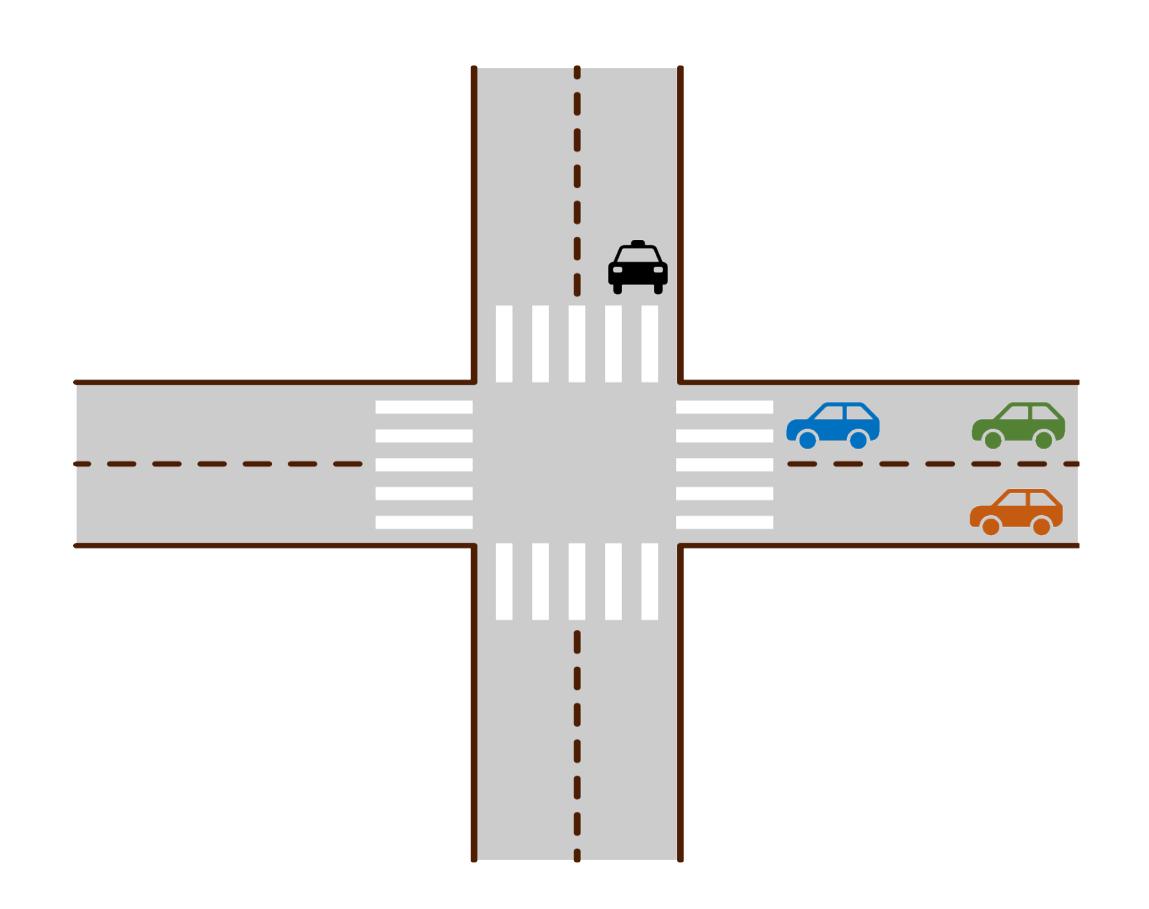
Specification-Guided Learning of Nash Equilibria with High Social Welfare

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Multi-agent System

- n agents and finite state space S.
- Action space A_i for agent i.
- Transition probability P(s' | s, a) for $s, s' \in S$ and $a \in \prod_i A_i$.

User Input

- A specification ϕ_i for each agent i.
- A method to sample from $P(\cdot | s, a)$.

Problem Statement

Given a joint policy π , score of agent i is $J_i(\pi) = \Pr_{\zeta \sim D(\pi)} [\zeta \vDash \phi_i]$. Solve

$$\underset{\pi}{\operatorname{arg\,max}} \sum_{i} J_{i}(\pi)$$

s.t. π is ϵ -Nash equilibrium

Our Framework

Phase I: Prioritized Enumeration

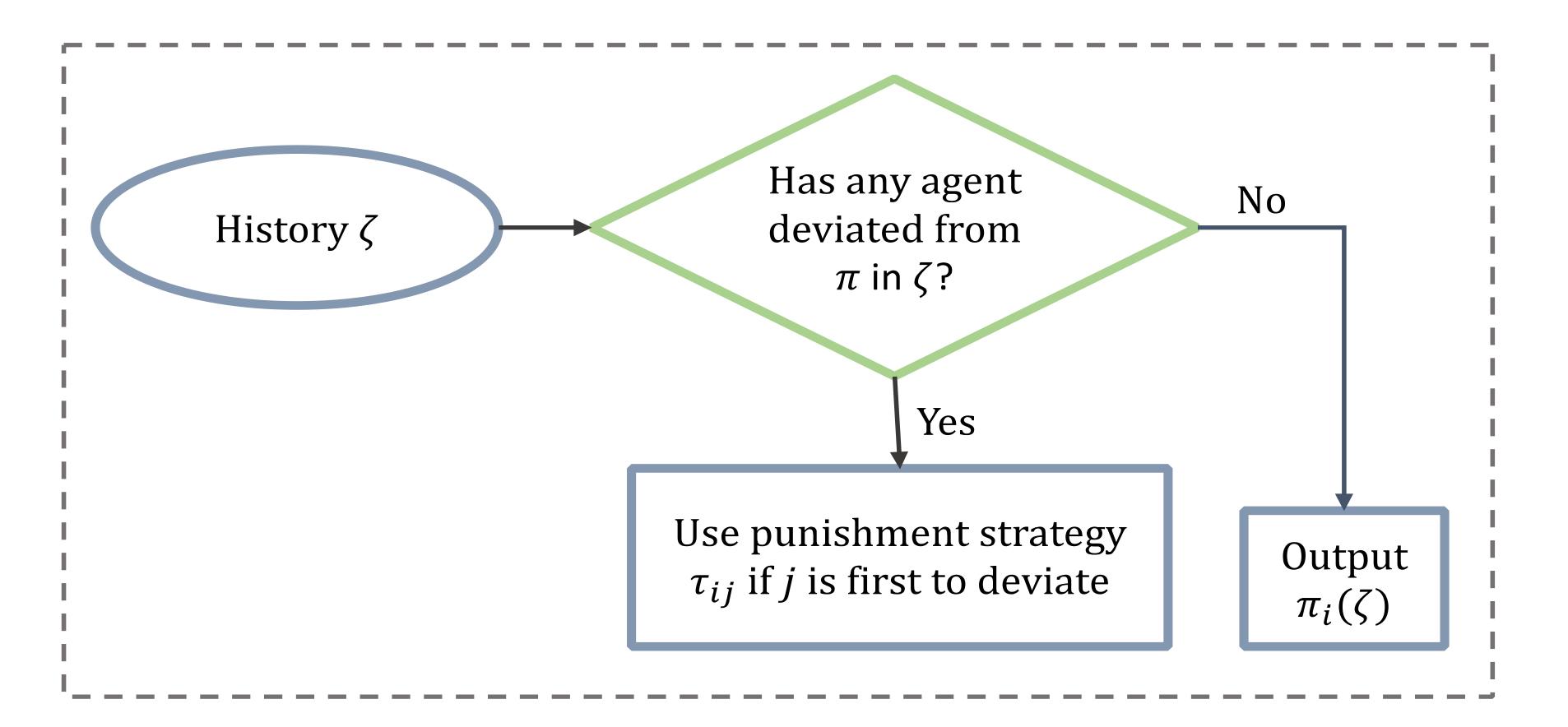
Use the specification of each agent to enumerate *finite-state deterministic* joint policies.

- Uses the specifications to construct multiple abstract graphs whose edges denote joint subtasks.
- Uses *single-agent RL* to learn joint policies for edges in the abstract graphs.
- Each *path* in the abstract graphs corresponds to a finite state joint policy (applies the edge policies in order).
- The policies are ordered in decreasing value of social welfare.

Phase II: Nash Verification

Checks if a joint policy can be **modified** to get an ϵ -Nash equilibrium **without affecting social welfare**.

- Modifications are restricted to *adding punishment strategies* which trigger when some agent deviates.
- Uses a *self-play RL algorithm* to compute the best punishment strategies.
- Return the first joint policy (from Phase I) which can be converted to ϵ -Nash equilibrium this way.



Experiments on Intersection Environment						
Spec.	Num. of agents	Algorithm	$\begin{array}{c} \mathtt{welfare}(\pi) \\ (\mathtt{avg} \pm \ \mathtt{std}) \end{array}$	$\epsilon_{\min}(\pi)$ (avg ± std)	Num. of runs terminated	Avg. num. of sample steps (in millions)
ϕ^1	3	HIGHNASH NVI MAQRM	0.33 ± 0.00 0.32 ± 0.00 0.18 ± 0.01	0.00 ± 0.00 0.00 ± 0.00 0.51 ± 0.01	10 10 10	1.78 1.92 2.00
ϕ^2	4	HIGHNASH NVI MAQRM	0.55 ± 0.10 0.04 ± 0.01 0.12 ± 0.01	0.01 ± 0.02 0.02 ± 0.01 0.20 ± 0.03	10 10 10	11.53 12.60 15.00
ϕ^3	4	HIGHNASH NVI MAQRM	0.49 ± 0.01 0.45 ± 0.01 0.11 ± 0.01	0.00 ± 0.01 0.00 ± 0.01 0.22 ± 0.02	10 10 10	11.26 12.60 15.00
ϕ^4	3	HIGHNASH NVI MAQRM	0.90 ± 0.15 0.98 ± 0.00 0.23 ± 0.01	0.00 ± 0.00 0.00 ± 0.00 0.39 ± 0.04	10 4 10	2.16 2.18 2.00
ϕ^5	5	HIGHNASH NVI MAQRM	0.58 ± 0.02 0.05 ± 0.01 Timeout	0.00 ± 0.00 0.01 ± 0.01 Timeout	10 7 0	62.17 80.64 Timeout





Code

Paper