

# 5. Shift Reduce Parser 2

Monday, March 1, 2021

8:28 AM

Augmented Grammar

$E' \rightarrow E$   
 $E \rightarrow E + T$   
 $E \rightarrow T$   
 $T \rightarrow T * F$   
 $T \rightarrow F$   
 $F \rightarrow id \mid (E)$

$I_1 \text{ closure}(I_0, E)$

$E' \rightarrow E.$   
 $E \rightarrow E. + T$

$I_2 \text{ closure}(I_0, T)$

$E \rightarrow T.$   
 $T \rightarrow T. * F$

$I_5 \text{ closure}(I_0, '(')$

$F \rightarrow (. E)$   
 $E \rightarrow . E + T$   
 $E \rightarrow . T$   
 $T \rightarrow . T * F$   
 $T \rightarrow . F$   
 $F \rightarrow . id$   
 $F \rightarrow . (E)$

$I_0 \text{ closure}(E' \rightarrow E)$

$E' \rightarrow . E$   
 $E \rightarrow . E + T$   
 $E \rightarrow . T$   
 $T \rightarrow . T * F$   
 $T \rightarrow . F$   
 $F \rightarrow . id$   
 $F \rightarrow . (E)$

$I_3 \text{ closure}(I_0, F)$

$T \rightarrow F.$

$I_4 \text{ closure}(I_0, id)$

$F \rightarrow id.$

$\text{goto}(I_0, F) \rightarrow I_1$

$E' \rightarrow E.$   
 $E \rightarrow E. + T$

$\text{goto}(I_0, T) \rightarrow I_2$

$E \rightarrow T.$   
 $T \rightarrow T. * F$

$\text{goto}(I_0, id) \rightarrow I_5$

$F \rightarrow id.$

$\text{goto}(I_0, F) \rightarrow I_3$

$T \rightarrow F.$

$\text{goto}(I_0, '(') \rightarrow I_4$

$F \rightarrow (. E)$   
 $E \rightarrow . E + T$   
 $E \rightarrow . T$   
 $T \rightarrow . T * F$   
 $T \rightarrow . F$   
 $F \rightarrow . (E)$   
 $F \rightarrow . id$

\* till you cannot move to a new item set

$\text{goto}(I_1, +) \rightarrow I_6$

$E \rightarrow E + . T$   
 $T \rightarrow . T * F$   
 $T \rightarrow . F$   
 $F \rightarrow . (E)$   
 $F \rightarrow . id$

$\text{goto}(I_4, E) \rightarrow I_8$

$F \rightarrow (E.)$   
 $E \rightarrow E. + T$   
 $E \rightarrow . E + T$

$\text{goto}(I_2, *) \rightarrow I_7$

$T \rightarrow T * . F$   
 $F \rightarrow . (E)$   
 $F \rightarrow . id$

$\text{goto}(I_4, T)$

$E \rightarrow T.$   
 $T \rightarrow T. * F$  }  $I_2$   
 $E \rightarrow . E + T$

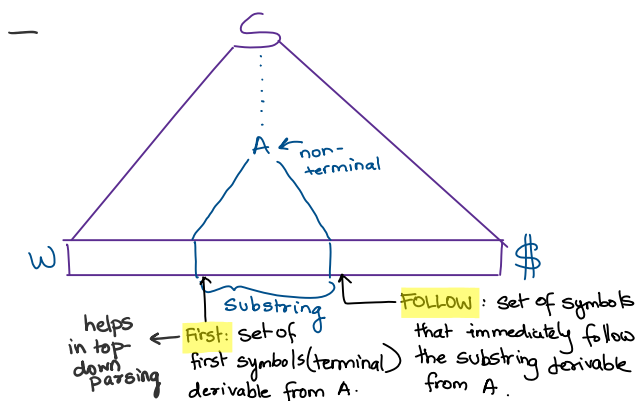
$F \rightarrow (E.)$   
 $E \rightarrow E.*T$   
 $\text{goto}(I_4, id) \rightarrow I_5$   
 $F \rightarrow id. \} I_5$   
 $\text{goto}(I_5, T) \rightarrow I_3$   
 $E \rightarrow E.*T.$   
 $T \rightarrow T.*F$   
 $\text{goto}(I_6, F) \rightarrow I_3$   
 $T \rightarrow F. \} I_3$   
 $\text{goto}(I_6, id) \rightarrow I_5$   
 $F \rightarrow id. \} I_5$   
 $\text{goto}(I_7, F) \rightarrow I_{10}$   
 $T = T.*F.$   
 $\text{goto}(I_8, T) \rightarrow I_6$   
 $\text{goto}(I_9, *) \rightarrow I_7$

$T \rightarrow T.*F \} I_2$   
 $\text{goto}(I_4, F) \rightarrow I_3$   
 $T \rightarrow F. \} I_3$   
 $\text{goto}(I_4, '(') \rightarrow I_4$   
 $F \rightarrow (.E) \} I_4$   
 $E \rightarrow$   
 $T \rightarrow$   
 $F \rightarrow$   
 $\text{goto}(I_6, '(') \rightarrow I_4$   
 $F \rightarrow (.E) \} I_4$   
 $E \rightarrow$   
 $T \rightarrow$   
 $F \rightarrow$   
 $\text{goto}(I_8, '(') \rightarrow I_4$   
 $\text{goto}(I_7, id) \rightarrow I_5$   
 $\text{goto}(I_8, ')') \rightarrow I_1$   
 $F \rightarrow (E).$

\*DFA of goto function  $\rightarrow$  DFA

## Parse Table

### (1) FIRST & FOLLOWS



(1)  $\text{First}(x) = \{x\}$   
 $x \rightarrow y_1 y_2 \dots y_n$

Example tree structure:  
 $x \rightarrow y_1 y_2 y_3$   
 $y_1 \rightarrow \epsilon$ ,  $y_2 \rightarrow \epsilon$ ,  $y_3 \rightarrow a$   
 $\rightarrow \text{First}(x) = a$

Example:

(1)  $S \rightarrow Az$   
 $A \rightarrow a$

$\text{First}(A) = \{a\}$   
 $\text{First}(S) = \{a\}$

(2)  $S \rightarrow Az$   
 $A \rightarrow \epsilon$

$\text{First}(A) = \{\epsilon\}$   
 $\text{First}(S) = \{z\}$

$$(1) \text{First}(X) = \{X\}$$

$$X \rightarrow Y_1 Y_2 \dots Y_n$$

$$\begin{array}{ccc} Y_1 & Y_2 & Y_3 \\ | & | & | \\ \epsilon & \epsilon & a \end{array}$$

$$A \rightarrow \epsilon$$

$$\text{First}(\epsilon) = \{\epsilon\}$$

$$(2) \text{First}(X) \rightarrow \text{First}(Y_1) \text{ except } \epsilon \text{ (empty string)} \cup \\ \text{First}(Y_2) \text{ except } \epsilon \cup \\ \vdots \\ \text{First}(Y_n) \text{ except } \epsilon$$

$$(3) X \rightarrow \epsilon ; \text{First}(X) = \{\epsilon\}$$