

## 4. CFG 2

Wednesday, February 24, 2021

1:40 PM

### Shift reduce parser

- bottom-up

- L-R  $\rightarrow$  rightmost derivation

$\downarrow$   
left to right scanning

- \* uses stack
- \* buffer that holds input string
- \* \$ denotes bottom of stack and end of input buffer

### Parsing Algorithm

- \* holds rules for parsing: **parsing table**
- \* parses sees input symbol in buffer and

a  $\rightarrow$  **Shifts**: shift input symbol to the stack

b  $\rightarrow$  **reduces**: takes the handle from the stack and reduces it w/ the help of a production.

**Input buffer**

holds tokens

### Example

$w = id_1 * id_2$

parser gives parsing rule through parsing table

Stack  
\$ a X Y Z  
\$ a A

$A \rightarrow XYZ$   $\rightarrow$  Reduction

c  $\rightarrow$  Error situations  
cannot decide shift or reduce

d  $\rightarrow$  accept

Stack  
\$ S

input \$  $\rightarrow$  accept State

Stack	input	action
\$	$id_1 * id_2$ \$	Shift
\$ $id_1$	$* id_2$ \$	reduce $F \rightarrow id$
\$ F	$* id_2$ \$	reduce $T \rightarrow F$
\$ T	$* id_2$ \$	Shift
\$ T *	$id_2$ \$	Shift
\$ T * $id_2$	\$	reduce $F \rightarrow id$
\$ T * F	\$	reduce $T \rightarrow T * F$
\$ T	\$	reduce $E \rightarrow T$
\$ E	\$	accept

$E \rightarrow E + T$      $F \rightarrow id$   
 $E \rightarrow T$          $F \rightarrow (E)$   
 $T \rightarrow T * F$       $T \rightarrow F$

How does the parser make parsing decisions

$\rightarrow$  CFG

### LR(K) Parsing Algorithm

(number of symbols used for lookahead)

$\rightarrow$  Simple L-R parses (**SLR**) [shift/reduce bottom up]

\* maintain a set of **states**

$\rightarrow$  number of **L-R(0) items**

L-R(0) item of a Grammar G

is a production of the grammar with a  $\cdot$

L-R(0) item of a Grammar G  
is a production of the grammar with a  $\cdot$   
at any position in the body of the production

$A \rightarrow XYZ$   
 $A \rightarrow \cdot XYZ$   
 $A \rightarrow X \cdot YZ$   
 $A \rightarrow XY \cdot Z$   
 $A \rightarrow XYZ \cdot$

$\cdot$  represents how much of a production we have seen

$A \rightarrow \cdot XYZ$  // not seen this production  
 $A \rightarrow XYZ \cdot$  // seen this production entirely

## Collection of states

### canonical L-R(0) collection

↳ construct an L-R automata (Deterministic)  
that helps the parser make decisions

### 1- Augmented Grammar

2- Closure function:  $\text{closure}(I)$  // generates L-R(0) items

3- Goto function:  $\text{goto}(I, X)$  // defines transitions

functions

### Augmented Grammar $G'$

→ grammar G with an additional production

$S' \rightarrow S$

\* parser needs to have a specific production to announce that the string is in an accepting state

Example:

$E \rightarrow E + T \mid T$   
 $T \rightarrow T * F \mid F$   
 $F \rightarrow (E) \mid id$

Augmented Grammar:

$E' \rightarrow E$   
 $E \rightarrow E + T \mid T$   
 $T \rightarrow T * F \mid F$   
 $F \rightarrow (E) \mid id$

### Closure

→ Assume I is a set of L-R(0) items  
then the closure of I is formed by using the two items:

- 1- add all items of I to  $\text{closure}(I)$
- 2- If you have a production of the form

$A \rightarrow \alpha \cdot \beta$  in I

and  $B \rightarrow \gamma$

this item also must be added to closure of I

Example:

L-R(0) item:  $E' \rightarrow \cdot E$

Closure ( $E' \rightarrow \cdot E$ ) =

$E \rightarrow \cdot E$   
 $E \rightarrow \cdot E + T$   
 $F \rightarrow \cdot T$   
 $T \rightarrow \cdot T * F$   
 $T \rightarrow \cdot F$   
 $F \rightarrow \cdot id$   
 $F \rightarrow \cdot (E)$

initial state  
 $I_0$

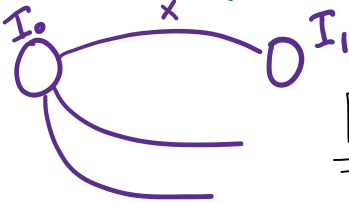
### Goto ( $X, I$ )

- defines transitions
- move the symbol  $\cdot$

in  $I_0$

$A \rightarrow \alpha \cdot X \beta$

$\text{goto}(X, I) \Rightarrow \text{closure}(A \rightarrow \alpha X \cdot \beta)$



### Example

$\text{goto}(I_0, X)$   
 $\text{goto}(I_0, E)$   
 $\text{goto}(I_0, T)$   
 $\text{goto}(I_0, F)$   
 $\text{goto}(I_0, id)$   
 $\text{goto}(I_0, '(')$

$E' \rightarrow E$   
 $E \rightarrow E + T$

cannot be further derived

## Building the L-R(0) automaton

...

$T. \text{closure}(E' \rightarrow E)$

## Building the LR(0) automaton

Augmented Grammar

$E' \rightarrow E$        $T \rightarrow F$   
 $E \rightarrow E + T$      $F \rightarrow id \mid (E)$   
 $E \rightarrow T$   
 $T \rightarrow T * F$

$I_0 \text{ closure}(I_0, E)$

$E' \rightarrow E.$   
 $E \rightarrow E. + T$

$I_2 \text{ closure}(I_0, T)$

$E \rightarrow T.$   
 $T \rightarrow T. * F$

$I_5 \text{ closure}(I_0, '(')$

$F \rightarrow (. E)$   
 $E \rightarrow . E + T$   
 $E \rightarrow . T$   
 $T \rightarrow . T * F$   
 $T \rightarrow . F$   
 $F \rightarrow . id$   
 $F \rightarrow . (E)$

$I_0 \text{ closure}(E' \rightarrow E)$

$E' \rightarrow . E$   
 $E \rightarrow . E + T$   
 $E \rightarrow . T$   
 $T \rightarrow . T * F$   
 $T \rightarrow . F$   
 $F \rightarrow . id$   
 $F \rightarrow . (E)$

$I_3 \text{ closure}(I_0, F)$

$T \rightarrow F.$

$I_4 \text{ closure}(I_0, id)$

$F \rightarrow id.$