

1) Genetic Algorithm for optimization problems:-

Genetic Algorithm (GA) is an optimization technique inspired by the process of natural selection & genetics. It is part of evolutionary computation & is used to find approximate solutions to complex problems by simulating evolution. GAs work with a population of potential solutions, evolving them over generations through selection, crossover & mutation.

Key components of genetic algorithm

1. population: A set of potential solutions to the problem
2. chromosome: A representation of a solution. Often in the form of strings, array, or other data structures.
3. fitness Function: A function that evaluates how good a solution is relative to others.
4. Selection: The process of choosing the best solutions to create the next generation.
5. crossover: The process of combining two parent solutions to create offspring.
6. mutation: Random alterations to offspring to maintain diversity in population.

Application of genetic algorithm for optimisation problems

1. Travelling Salesman problem(TSP)

- * Description: The goal is to find the shortest possible route that visits each city exactly once & returning to the origin city
- * Application: GAs can generate feasible routes by selecting shorter paths applying crossover to combine segments of different routes & using mutation to introduce variations

2. knapsack problem

- * Description: Given a set of items with weight & values, the task is to maximize the total value without exceeding a weight limit
- * Application: GAs can encode item selection as chromosomes using fitness functions to evaluate total values while adhering to weight constraints

3. job scheduling

- * Description: Assigning jobs to resource in a way that optimizes objectives like minimizing total completion time
⑥ minimize resource utilization

* Application:- GA's can create schedules as potential solutions, applying selection & crossover to find optimal arrangements using mutation to explore new configurations.

- Travelling Salesman Problem

Algorithm for Travelling Salesman problem:-

function GeneticAlgorithm(population-size, gene
-rotation, distance-matrix)

 Initialize population with random tour (permutations of cities)

 For generation from 1 to generations Do
 calculate fitness for each tour in
 population

$$\text{fitness} = 1 / (\text{total distance of the tour})$$

 Create empty list next-generation

 While next-generation is not full Do

 Parent1 = Selection(Population, fitness scores)

 Parent2 = Selection(Population, fitness scores)

 child = crossover(Parent1, Parent2)

 child = mutate(child)

ADD child to next-generation

SET Population = next-generation

best-tour = find the tour with the best
fitness in population

best-distance = 1 / best-fitness

Return best-tour, best-distance

Function crossover(parent1, parent2)

Select two crossover points

Create child by combining segments from
parent1 & parent2 while maintaining
order

Return child

Function Mutate(tour)

If random-value < mutation_rate then

Select 2 positions in the tour

Swap cities at those 2 positions

Return tour

function Selection(population, fitness_scores)

Select a candidate based on fitness scores.

Between Selected candidate

Enter Number of cities to visit in tour

Particle Swarm Optimization for function Optimization

Particle Swarm optimization is a powerful & versatile optimization technique inspired by collective behaviour of nature particularly in the movement of birds in flocks & fish in schools. This algorithm uses the principle of social collaboration & individual learning to explore complex Solution Spaces & converge towards optimal solution.

Define the problem

Mathematical function: we will create a mathematical function to optimize for example let's define the function $f(x) = x^2$. The goal is to find the value of x that minimizes the function which known to be at $x=0$.

Initialize parameters

Number of Particles: choose an appropriate number of particles for the swarm

inertia weight: Set inertia weight to control the impact of the previous velocity.

cognitive coefficient: which influences how much particle is influenced by its own best position

Social co-efficient: which influences how much particle is influenced by the best position found by the Swarm

Generate initial population:-

Create initial population of particles. For each particle

Randomly initialize its position within a defined range

Randomly initialize its velocity, within

Set its best position = initial position

Evaluate its initial best fitness

Evaluate fitness! -

For each particle, calculate its current fitness using the defined mathematical function, update its best-position & best-fitness

If the current fitness is better than its previous

Pseudo code

function PSO(fitness-function, num-particles, num-iterations, inertial-weight, cognitive-coeff, social-weight, social-coefficient)

Create an array of particles with size num-particles

For i from 0 to num-particles -1;

 Particles[i].Position = Randomly initialize
 Position in range [-5, 5]

 Particles[i].Velocity = Randomly initialize
 Velocity in range [-1, 1]

 Particles[i].best-position = particles[i].Position

 Particles[i].best-fitness = fitness-function(
 Particles[i].Position)

Global-best-position = particles[0].best-position

Global-best-fitness = particles[0].best-fitness

for iteration from 1 to num_iterations:

For each particle in particles:

current_fitness = fitness.function

(particle.position)

if current_fitness < particle.best_fitness:

particle.best_position = particle.position

Particle.best_fitness = current_fitness

if current_fitness < global_best_fitness:

global_best_position = particle.position

global_best_fitness = current_fitness

~~$r_1 = \text{random value in range } [0, 1]$~~

~~$r_2 = \text{random value in range } [0, 1]$~~

particle.velocity = inertia_weight * parti-

-cle. velocity + cognitive_coeff * $r_1 * ($

particle.best_position - particle.posi-

-tion) + social_coefficient * $r_2 * ($

$\star (\text{global-best-position} - \text{particle}$

$\cdot \text{position}))$

particle.position = particle.position + particle.velocity.

between global-best-position, global-best-fitness

global-best-position = $[1.8777 \pm 640e^{+4}]$

but position: $[-1.8777 \pm 640e^{+4}] - 1.8777 \pm 640e^{-13}$

best value: $-5.80651522055670e-25$

global-best-fitness

global-best-fitness = $1.8777 \pm 640e^{+4}$

global-best-fitness

global-best-fitness = $1.8777 \pm 640e^{+4}$

global-best-fitness

global-best-fitness = $1.8777 \pm 640e^{+4}$

~~global-best-fitness~~
2010-24

global-best-fitness = $1.8777 \pm 640e^{+4}$

global-best-fitness

global-best-fitness = $1.8777 \pm 640e^{+4}$

7/11/24

Lab - 3

Ant colony optimization for Travelling Salesman problem

ACO is inspired by the behaviour of real ants when they forage for food. Ant explore their environment & deposit a chemical substance called pheromone on the ground, the pheromone trail is stronger on paths that are shorter & more frequently used by ant. This leads other ants to favour these paths thus creating a positive feedback loop, over time shortest path will accumulate the most phero-mone & be chosen by more ant

Define problem:

In this we define the cities as a dictionary where each key represents a city ID & the cor-responding value is a tuple of its (x, y) co-ordinate in 2D plane. The n-cities variable stores the total no of cities to be visited in the TSP

Initialize parameters

no. number of Ants (n-ants): Number of ants in the colony

pheromone Importance (α): Preference of pheromone on decision

Heuristic Importance (β): Influence of ~~pheromone~~ the distance

Evaporation Rate (ρ): Rate at which pheromone evaporates

Initial pheromone: Set initial pheromone value for each edge

Construct Solution:

Ant path construction: Each ant starts at a random city & probabilistically chooses the next city based on pheromones & heuristic information

'Transition probability': Ants are more likely to visit cities with higher pheromone levels & shorter distance

Repeat for 3 to 4 steps for a fixed no. of iterations

Applications of ACO

Travelling Salesman
Vehicle routing

Network Routing

Robotics

Pseudocode:

initialize parameters: n_ants, n_iterations, alpha
beta, rho, d_cities

calculate distance matrix for all cities

Initialize pheromone matrix (small values)

for iteration=1 to n_iterations:

for each ant:

- Initialize the tour of the ant (start city)
- while ant not visited all cities
 - calculate probability next choosing city on pheromone level & distance using alpha, beta

ϵ gamma

update tour by adding next cities

calculate total length for ant

update pheromone matrix

Evaluate pheromone using probabilistic function

Deposit pheromone on the edge of each
ants tour on the edges it visited

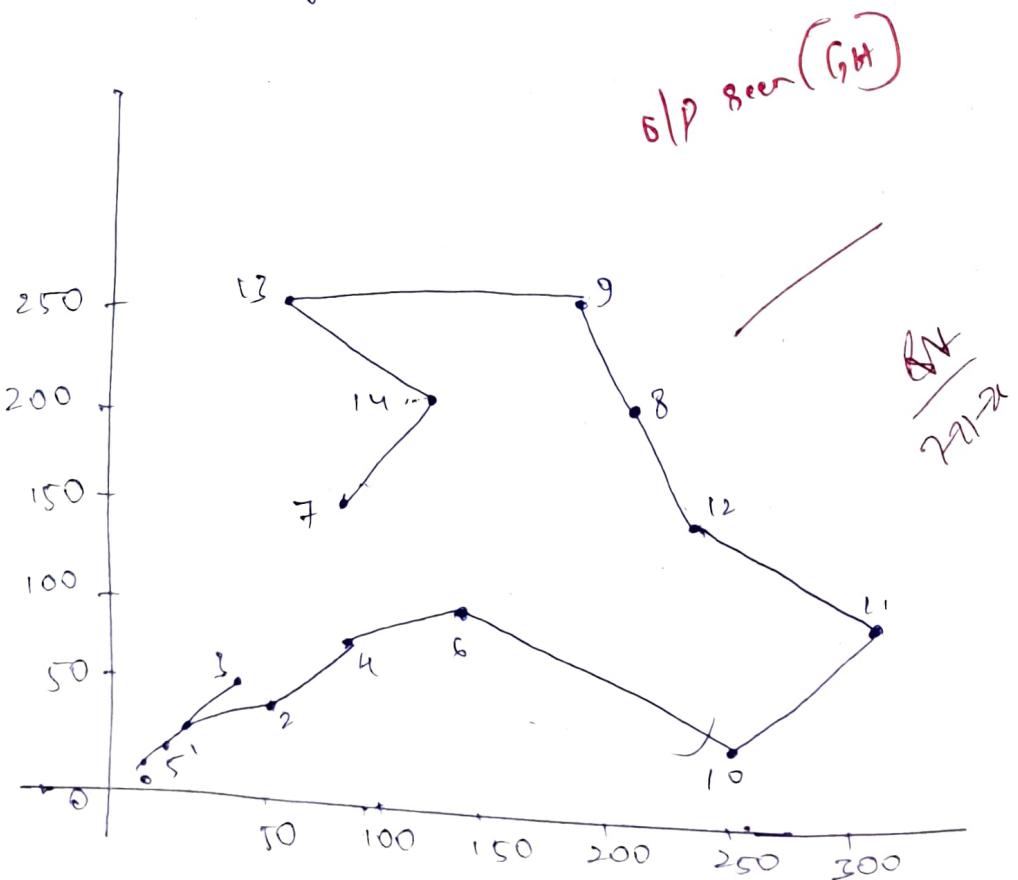
update the best solution found

If any stopping condition is met end for

Return the best solution found

Output:

Best tour length: 986.30



cuckoo search(cs)

cuckoo search is a nature-inspired optimization algorithm based on brood parasitism of some cuckoo species. This behaviour involves laying eggs in the nests of other birds, leading to optimization of survival strategies. CS uses Levy flight to generate new solutions promoting global search capabilities & avoiding local minima.

Algorithm

Initialize nests randomly within in solution space

best-nest = nest with best fitness

bgr-fitnes = fitness of best nest

for iteration = 1 to max-ites

for each nest i

~~new-nest-i = nest-i + alpha * levy-flight (lambda)~~

~~new-nest-i = clip(new-nest-i,
lower-bound, upper
bound.)~~

new-fitness_i = objective-function(<sub>new
nest-i</sub>)

if new-fitness_i < fitness_i:

nest_{-i} = new-nest_{-i}

fitness_{-i} = new-fitness_{-i}

for i in range(num-nests):

if random() < beta:

nest_{-i} = random-solution()

current-best-fitness = min(fitness)

if current-best-fitness < best-fitness

best-fitness = current-best-fitness

best-nest = nest with best fitness

return best-nest, best-fitness

Parameters:

Levy flight: A random walk where the step size follows a heavy tailed distribution

Alpha(α): Scaling factor that controls the

size in Levy flight

Beta(β): probability of abandoning nest

Lambda(λ): Defines characteristics of Levy distribution

Applications:

transportation (vehicle routing, traffic control tools)

manufacturing (job scheduling, resource allocation).

VR
20/12/24

Grey wolf optimizer (GWO)

The grey wolf optimizer algorithm is a swarm intelligence algorithm inspired by the social hierarchy & hunting behaviour of grey wolves. It mimics the leadership structure of alpha, beta, delta & omega wolves & their collaborative hunting strategies. The GWO algorithm uses these social hierarchical to model the optimization process where alpha wolves guide the search process while beta & delta wolves assist in refining the search direction.

Algorithm:-

Step 1:- Randomly initialize Grey wolf population of N particles x_i ($i = 1 \dots n$)

Calculate the fitness value of each individuals

Sort grey wolf population based on fitness values

alpha-wolf = wolf with best fitness value

beta-wolf = wolf with second best fit
- ness value

gamma-wolf = wolf with third best fit
- ness value

for i in range(max_iter):

calculate the value of α

$$\alpha = 2^{\frac{1}{\star}} \left(1 - \frac{i}{\text{max_iter}} \right)$$

for i in range(N):

a. compute the value of $A_1, A_2,$

$$A_3 \in C_1, C_2 \in C_3$$

$$A_1 = \alpha^{\star} (2^{\star} r_1 - 1), A_2 = \alpha^{\star} (2^{\star} r_2 - 1)$$

$$A_3 = \alpha^{\star} (2^{\star} r_3 + 1)$$

~~$$C_1 = 2^{\star} r_1, C_2 = 2^{\star} r_2, C_3 = 2^{\star} r_3$$~~

Compute x_1, x_2, x_3

$$x_1 = \text{alpha_wolf.position} -$$

$$A_1^{\star} \text{abs}(C_1^{\star} \text{alpha_wolf-} \\ \text{posith} - i^{\text{th}} \text{.wolf.position})$$

$$x_2 = \text{beta_wolf.position} -$$

$$A_2^{\star} \text{abs}(C_2^{\star} \text{beta_wolf - posith} \\ - i^{\text{th}} \cdot \text{wolf.position})$$

$$x_3 = \text{gamma_wolf.position} -$$

$$A_3^{\star} \text{abs}(C_3^{\star} \text{gamma_wolf.POSI-} \\ \text{TION} - i^{\text{th}} \cdot \text{wolf.position})$$

$$- n)$$

compute new solution & fitx fitness

$$x_{\text{new}} = (x_1 + x_2 + \dots + x_s)/3$$

$$f_{\text{new}} = \text{fitness}(x_{\text{new}})$$

if ($f_{\text{new}} < \text{ith-wolf.fitness}$)

$$\text{ith-wolf-position} = x_{\text{new}}$$

$$\text{ith-wolf.fitness} = f_{\text{new}}$$

Sort grey wolf population based on fitness value

alpha-wolf = wolf with best fitness value

beta-wolf = wolf with second best fitness value

gamma-wolf = wolf third best fitness value

Return the best wolf in the population

AB
mult

parallel cellular Algorithms & programs

parallel cellular algorithms are inspired by functioning of biological cells that operate in a highly parallel & distributed manner. These algorithms leverage the principles of cellular automata & parallel computing to solve complex optimization problems efficiently. Each cell represents a potential solution & interacts with its neighbours to update its state based on predefined rules. This interaction models the diffusion of information in an array cellular grid.

Algorithm

```
function initialize_grid(width, height):
    grid = create_grid(width, height)
    for each cell in grid:
        grid[cell.x][cell.y] = random_state()
```

return grid

```
function count_alive_neighbors(grid, x, y):
```

count = 0

```
for each neighbor(dx, dy) in [-1, 0, 1]:
```

```
    if (dx, dy) != (0, 0):
```

```
        neighbor_x = (x + dx * width).width
```

$\text{neighbor_y} = (\text{y} + \text{dy}) \bmod \text{height}$

$\text{count} += \text{grid}[\text{neighbor_x}][\text{neighbor_y}]$

return count

function next_state(grid, x, y):

alive_neighbors = count_alive_neighbors(grid, x, y)

if $\text{grid}[\text{x}][\text{y}] == 1$:

return 1 if alive_neighbors == 2

or alive_neighbors == 3 else 0

else:

return 1 if alive_neighbors == 3 else 0

function parallel_update(grid):

next_grid = create_grid(width, height)

parallel_for each cell(x, y) in grid

~~next-grid[x][y] = next_state(grid, x, y)~~

return next_grid

~~for~~
~~do~~

function run_simulation(width, height, num_steps):

grid = initialize_grid(width, height)

for step in 1 to num_steps:

~~grid = parallel_update(grid)~~

display_grid(grid).

Gene Expression optimization

Gene Expression optimization is a bio inspired optimization algorithm - that mimics gene expression in biological systems & it is designed to solve complex optimization problems by finding optimal solution through iterative improvement using principles such as expression, mutation & natural selection

Parameters:

Population size - P

Max Iteration T

Mutation rate - m

Crossover rate - c

fitness function F

population = InitializePopulation(population size)

fitness value = evaluate_fitness(population, fitness function)

for t in range(maxIterations):

Selected parents = Selection(population - on, fitness value)

offspring = crossover (selected-parents,
crossover rate)

offspring = mutation (offspring,
mutation rate)

offspring-fitness = evaluate fitness
(offspring, fitness
function)

population combine & select (population,

offspring-fitness-values, offspring-fitness

fitness-values = evaluate fitness (population,
fitness function)

best-solution = get-best-solution (population,
fitness-values)

Print("Best solution found", best solution,