

Q10 Code

October 22, 2021

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[1]: import numpy as np
      from tensorflow.keras.datasets import mnist
      from typing import List
      import seaborn as sns
      import matplotlib.pyplot as plt
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[2]: def load_data():
      (x_train, y_train), (x_test, y_test) = mnist.load_data()

      x_train = x_train / 255
      x_test = x_test / 255
      x_train = x_train.reshape(x_train.shape[0], -1)
      x_test = x_test.reshape(x_test.shape[0], -1)

      digits = []
      targets = []
      for i in range(10):
          images = x_train[y_train == i]
          digits.append(images[np.random.choice(
              len(images), 1000, replace=False)])
          targets.append(np.full((1000,), i))

      x_train = np.vstack(digits)
      y_train = np.hstack(targets)

      permutation = np.random.permutation(x_train.shape[0])
      x_train = x_train[permutation]
      y_train = y_train[permutation]

      test_indices = np.random.choice(x_test.shape[0], 1000)
      x_test = x_test[test_indices]
      y_test = y_test[test_indices]
      return (x_train, y_train), (x_test, y_test)
```

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[3]: def LeastSquares(A, b, reg=1.0):
      return np.linalg.inv((A.T @ A) + reg * np.eye(A.shape[1])) @ (A.T @ b)
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[4]: def confusion_matrix(y_true, y_pred, labels: List = []):
    matrix = np.zeros((len(labels), len(labels)), dtype=int)
    for i in range(len(y_pred)):
        matrix[y_true[i], y_pred[i]] += 1
    return matrix

[5]: def main():
    (x_train, y_train), (x_test, y_test) = load_data()
    classifier = np.zeros((x_train.shape[1], 10))
    for i in range(10):
        b = 2*(y_train == i) - 1
        classifier[:, i] = LeastSquares(x_train, b, reg=1.0)
    y_pred = np.argmax(x_test @ classifier, axis=1).astype(int)
    print(f"Accuracy : {np.mean(y_pred == y_test)}")

    cnf_matrix = confusion_matrix(y_test, y_pred, labels=range(10))
    sns.heatmap(cnf_matrix, annot=True, cmap="Blues", fmt="d")
    plt.title("Confusion Matrix")
    plt.xlabel("Predicted Label")
    plt.ylabel("True Label")
    plt.show()

if __name__ == "__main__":
    main()
```

Accuracy : 0.847

