(4)=) (ode, results, Confusion matrix and regions of classification in IR2 plane are clearly shown in the poly attached below. (a and b parts) Regions of dassification are marked by red (when y = 1) and blue (when y = -1). (c) yes polynomial $g = x_1x_2$ dassifies the generated points with zero error: Obtained boly no mial: f(x) = 0.0338 + 0.0197x, + 0.020 x2 + 0.649 x1x2 + 0.0068 x,2 - * 0.0032 nz As un can see n, n_2 has by a go big maryin the biggest coefficient while other terms have non-zoro small coefficients.

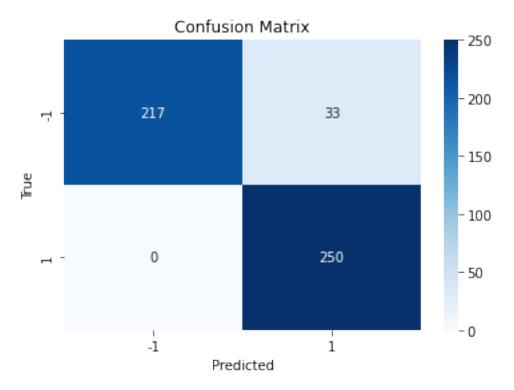
October 21, 2021

[1]: import numpy as np

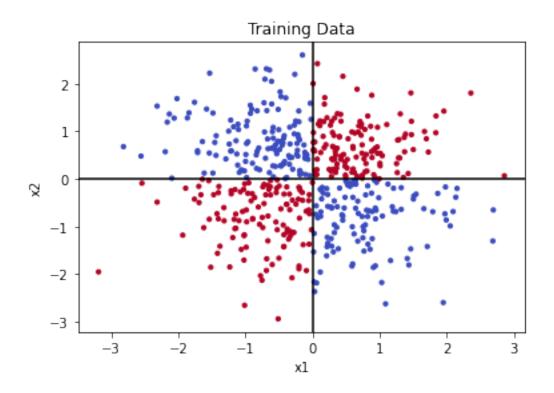
```
import matplotlib.pyplot as plt
     import seaborn as sns
[2]: N = 500
     def load_data():
         x_train = np.random.randn(N, 2)
         y_train = (x_train[:, 0]*x_train[:, 1] >= 0.) * 2 - 1
         return x_train, y_train
     def least_squares(A, b, reg=1.0):
         return np.linalg.inv((A.T @ A) + reg * np.eye(A.shape[1])) @ (A.T @ b)
[3]: def confusion_matrix(y_true, y_pred, labels=[]):
         matrix = np.zeros((len(labels), len(labels)), dtype=int)
         for i in range(len(y_pred)):
             x = labels.index(y_true[i])
             y = labels.index(y_pred[i])
             matrix[x, y] += 1
         return matrix
[4]: def preprocess_data(x_train):
         a = np.empty((x_train.shape[0],6))
         a[:,0] = 1
         a[:,1:3] = x_train
         a[:,3] = x_train[:,0]*x_train[:,1]
         a[:,4:6] = x_train**2
         return a
[5]: x_train, y_train = load_data()
     A = preprocess_data(x_train)
     x_hat = least_squares(A, y_train)
     y_pred = A @ x_hat
     y_pred = np.sign(y_pred).astype(np.int32)
```

```
[6]: err = np.mean(y_pred != y_train)
print(f"Error: {err*100:.2f}%")
```

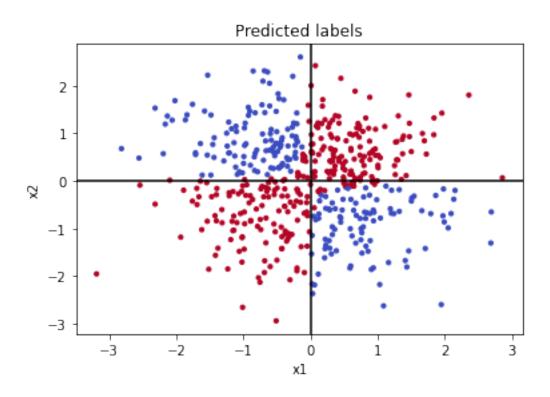
Error: 6.60%



```
[8]: fig,ax = plt.subplots()
    ax.scatter(x_train[:,0], x_train[:,1], c=y_train, s=10, cmap='coolwarm')
# ax.grid(True,which = 'both')
    ax.axhline(y=0, color='k')
    ax.axvline(x=0, color='k')
    ax.set_title("Training Data")
    ax.set_xlabel("x1")
    ax.set_ylabel("x2")
    plt.show()
```



```
[9]: fig,ax = plt.subplots()
   ax.scatter(x_train[:,0], x_train[:,1], c=y_pred, s=10, cmap='coolwarm')
   # ax.grid(True,which = 'both')
   ax.axhline(y=0, color='k')
   ax.axvline(x=0, color='k')
   ax.set_title("Predicted labels")
   ax.set_xlabel("x1")
   ax.set_ylabel("x2")
   plt.show()
```



```
[10]: POINTS = 100000
    x_test = np.random.randn(POINTS, 2)
    y_test = (x_test[:, 0]*x_test[:, 1] >= 0.) * 2 - 1
    A_test = preprocess_data(x_test)
    y_hat = A_test @ x_hat
    y_hat = np.sign(y_hat).astype(np.int32)

[11]: fig,ax = plt.subplots()
    ax.scatter(x_test[:,0], x_test[:,1], c=y_hat, s=10, cmap='coolwarm')
    # ax.grid(True,which = 'both')
    ax.axhline(y=0, color='k')
    ax.axvline(x=0, color='k')
    ax.set_title("Test data labels")
    ax.set_xlabel("x1")
    ax.set_ylabel("x2")
    plt.show()
```

