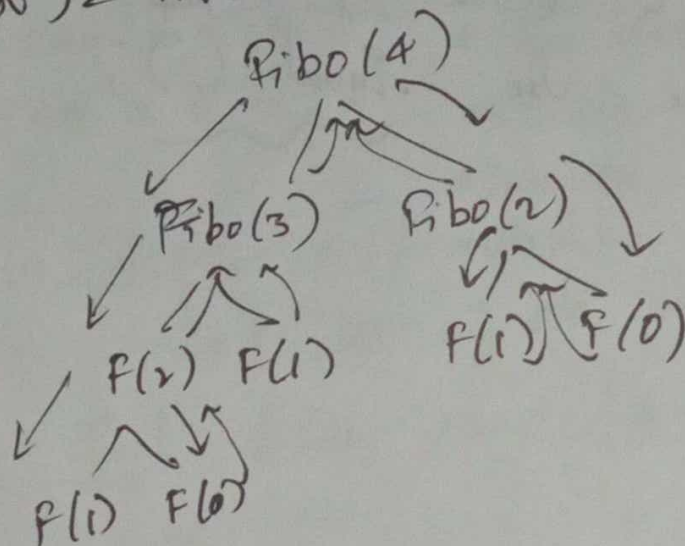


## Recursion:-

- \* All function calls go into stack memory.
  - After execution  $f^n$  is removed from stack and called to the place where called.
- \* Base condition is important to write.
- \* Without base condition —  $\infty$  no of calls created in stack
  - at a point stack overflows. so program error!!!
- \* Recursion  $\iff$  iteration.  
(loops).
- \* Space complexity  $\swarrow$   
not constant — due to calls.

## Fibonacci:-

$$\text{Fibo}(n) = \text{Fibo}(n-1) + \text{Fibo}(n-2) \quad \rightarrow \text{Recurrence relation}$$



Recursion tree.

```
* class Fibonacci {
    public:
```

```
    fiboc(n);
    public:
    int fiboc(int n) {
        if (n < 2) {
            return n;
        }
        return fiboc(n-1) + fiboc(n-2);
    }
}
```

\* At one rec  $f^n$  depend on the next  $f^n$  call then called  
"Tail recursion"  $\rightarrow$  not

## # Steps:

- (1) Write into small problems.
- (2) Write rec rel<sup>n</sup>.
- (3) Write rec tree.
- (4) Write the flow of function call.
  - Calls flow from left to right — tree calls.
- (5) Observe value returning.

## # Variables:-

- Arguments, return type.

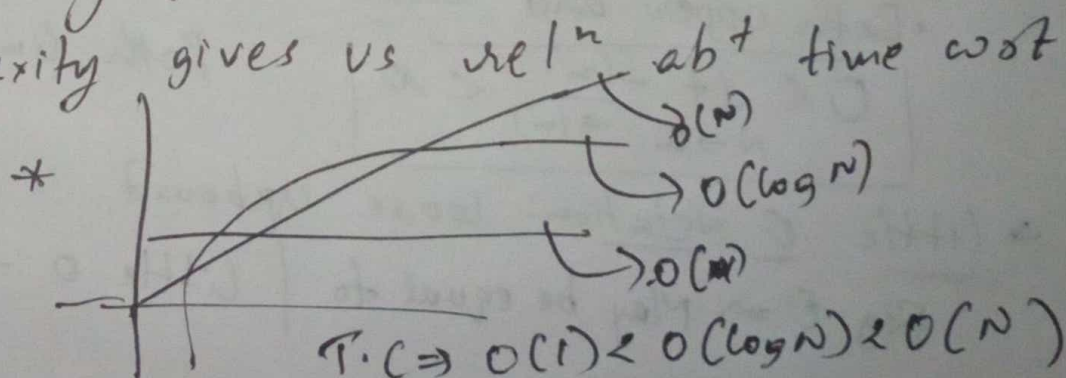
## \* Types of recurrences:-

- Linear rec rel<sup>n</sup> — Fibonacci
- Divide and conquer — Search space & such — reduces.
  - Binary Search.

## # Time & Space Complexity:-

- Time complexity  $\neq$  time taken.

- Time complexity gives us rel<sup>n</sup> abt time cost input.





# # Revision:-

## \* Factorial:

$$f(5) = f(4) \times 5 = f(3) \times 4 \times 5 = \dots$$

$$\begin{array}{c} \boxed{5} \\ \swarrow \\ \boxed{4} \times 5 \\ \swarrow \\ \boxed{3} \times 4 \times 5 \\ \swarrow \\ \boxed{2} \times 3 \times 4 \times 5 \\ \swarrow \\ \boxed{1} \times 2 \times 3 \times 4 \times 5 \end{array}$$

$$1 \Rightarrow 1$$

$$\text{if } (n == 1) \{ \\ \text{return } 1; \\ \}$$

$$\text{return } n \times \text{fact}(n-1);$$

Step wise:  $5 \times 4 \times 3 \times 2 \times \textcircled{1} \Rightarrow$  Main value or user given value.

## (8) Sum of digits:-

$$N = \boxed{342} \Rightarrow 1+3+4+2$$

$$\boxed{34} + 2 \quad \boxed{\phantom{00}} \Rightarrow$$

$$\boxed{13} + 4 + 2$$

$$\boxed{1} + 3 + 4 + 2$$

⑤ Stop;

## (9) Reversing number

$$N = \boxed{12345} \Rightarrow 54321$$

$$5 + \boxed{1234}$$

$$5 + 4 + \boxed{123}$$