

# Least Loss: A Simplified Filter Method for Feature Selection

Fadi Thabtah<sup>a,\*</sup>, Firuz Kamalov<sup>b</sup>, Suhel Hammoud<sup>c</sup>, Syed Reza Shahamiri<sup>d</sup>

<sup>a</sup>*Digital Technologies, Manukau Institute of Technology*

<sup>b</sup>*Mathematics department, Canadian University of Dubai, Dubai, UAE*

<sup>c</sup>*IT Department, University of Kalamoon, Syria*

<sup>d</sup>*Digital Technologies, Manukau Institute of Technology*

---

## Abstract

Identifying the relevant set of features in a dataset is an important part of data analytics. Discarding significant variables or keeping irrelevant variables has significant effects on the performance of the learning algorithm during knowledge discovery. In this paper, a feature selection method called Least Loss ( $L^2$ ) is proposed. Our method significantly reduces the dimensionality of data by disposing irrelevant variables in a robust manner without reducing the predictive performance of classifiers. The biggest strength of the proposed method is its simplicity and intuitiveness. It is based on quantifying the similarity between the observed and expected probabilities and generating scores for each independent variable. To evaluate the new method, we compared its performance against Information Gain (IG) and Chi Square (CHI) feature selection methods using 27 different datasets. We employ the Nave Bayes probabilistic classifier to conduct the numerical experiments. The results reveal that  $L^2$  is highly competitive with respect to error rate, precision, recall rates, and substantially reduces the number of selected variables in the datasets. Our study will be of high interest to data analysts, scholars and domain experts who deal with applications that include large numbers of features using statistical analysis methods.

**Keywords:** Classification, Data Mining, Dimensionality reduction, Feature

---

\*Corresponding author

Email address: `fadi.fayez@manukau.ac.nz` (Fadi Thabtah )

## 1. Introduction

Feature selection is an important pre-processing step in data analysis [1, 2]. In many classification problems, including text classification and microarray analysis, researchers must deal with a large number of features. It stands to  
 5 reason that many of these features ought to be redundant. A large number of variables can lead to increased classification error and difficulty in interpreting the resulting model. In addition, having too many features makes training classifiers computationally cumbersome [3]. Therefore, selecting the relevant features and reducing the dimension of the feature space is a critical part of the  
 10 classification process.

Feature selection algorithms can be broadly divided into three groups: filter, wrapper and embedded methods[4]. Filter methods use various metrics based on information theory and statistics to determine the strength of the relationship between a feature and the target variable [5]. These methods can be used to rank  
 15 the features and select the optimal subset based on a predetermined selection criteria. Furthermore, one can use these methods in the pre-processing phase with other algorithms, such as Correlation Feature Set (CFS) and Minimum Redundancy Maximum Relevance (mRMR), to determine the optimal subset of features [6, 7]. Despite their simplicity filter methods have been shown to  
 20 outperform other selection methods under certain conditions.

Wrapper methods determine the optimal subset of features by going through all possible subsets of features and testing their explanatory power with respect to the target variable using a classification algorithm [6]. Wrapper methods therefore require a) employing a classification algorithm to build classifiers dur-  
 25 ing feature selection process for each possible features set and b) testing all possible combinations of features sets in the dataset to choose the set that yields the best accuracy based on the results of the classification algorithm [8]. For instance, given a dataset with  $n$  features there will be  $2^n - 1$  possible combi-

nation of features that need to be processed by a classification algorithm during  
 30 feature selection process. Afterwards, the feature subset whose corresponding  
 classifier achieved the best results is selected as the optimal subset. Thus, the  
 wrapper approach is computationally burdensome, and researchers are therefore  
 constantly trying to identify ways to estimate the ideal feature subset by using  
 more efficient algorithms [9, 10, 11]. Lastly, embedded methods determine the  
 35 optimal feature subset as part of training a classifier [12, 13]. Common embed-  
 ded methods use regularization techniques to penalize irrelevant variables in the  
 model.

The advantage of using filter methods for feature selection is two-fold: effi-  
 ciency and relative robustness [14, 15, 16]. Filter methods are computationally  
 40 more efficient than wrapper and embedded methods. Wrapper and embedded  
 methods both require training the learning system in order to evaluate feature  
 importance. On the other hand, filter methods evaluate features directly thereby  
 saving on model training. Filter methods analyse general characteristics of the  
 data and evaluate features without involving a learning algorithm. Therefore,  
 45 their performance is less dependent on any particular classifier and is robust  
 against the issue of overfitting.

This paper focuses on analysis of filtering methods. We introduce a general  
 framework for viewing them and demonstrate that some of the most commonly  
 used filtering measures can be seen as special cases resulting from the proposed  
 50 framework. In addition, we propose a new feature selection measure which we  
 call  $L^2$ . Our methods forte is its simplicity and efficiency in classification tasks  
 which streamlines the process of feature selection and makes it more robust.

The motivation of the proposed  $L^2$  feature selection divergence is the measur-  
 ing of the  $L^2$  distance between the observed and expected probabilities. Recall  
 55 that a pair of random variables,  $X$  and  $Y$ , is independent if and only if the  
 expected probability is equal to the observed (joint) probability. Therefore, it  
 can be postulated that the further apart these probabilities are the more de-  
 pendent are the variables  $X$  and  $Y$ . In other words, the greater the value of the  
 $L^2$  the more relevant a feature is to the target class. In fact, the proposed  $L^2$

60 divergence is an example of a larger family of statistics that attempts to quantify the difference between the observed and expected probabilities in the data. Examples of popular divergences that belong to this larger family of methods include Information Gain and the  $L^2$  statistic. The main advantage of the  $L^2$  over these other methods used for feature selection is its simplicity, ease of understanding, and intuitiveness. It is also important to note that the subset of features selected using the  $L^2$  approach performs as well as, and at times better than, the subsets selected using other methods. A more detailed discussion of testing results is given in the following sections.

Finally, it is important to remember that despite many instances where feature selection has been shown effective it does not always perform well. One can easily devise situations where feature selection would fail [8]. For instance, in the classical XOR problem involving two features univariate selection methods would identify each individual feature as irrelevant. However, the two features jointly completely determine the target variable.

75 The paper is structured as follows. Section 2 presents an overview of the literature related to feature selection. Section 3 contains the details of the proposed  $L^2$  algorithm. In Section 4, we discuss the results of numerical experiments carried out to test the proposed method. Section 5 concludes the paper.

## 2. Related literature

80 The topic of feature selection has been covered extensively in the literature. There exists a plethora of selection techniques that attempt to identify the most suitable feature subset. Modern filter methods often combine several procedures to identify the optimal feature subset. Commonly used tactics include combining IG, correlation and other metrics to arrive at a cumulative metric to determine feature importance. More advanced techniques combine filter approaches with wrappers and genetic algorithms. Despite proliferation of fusion techniques methods relying on a single criterion continue to be used in the literature.

The common theme of the existing methods is to evaluate features based

on certain criteria and select the best performing feature subset. Authors often  
90 combine multiple criteria to arrive at a complex method for feature selection.  
However, it remains an open question whether the increased complexity in the  
selection algorithm is justified. The goal of this paper is to address the com-  
plexity of modern approaches by proposing a simple criterion to evaluate feature  
importance. Indeed, the biggest strength of the proposed  $L^2$  approach is its sim-  
95 plicity and intuitiveness without sacrificing accuracy.

### 2.1. Fusion Methods

Fusion methods have gained popularity over the last few years. Fusion meth-  
ods combine two or more metrics to compute a cumulative score of a feature  
or feature subset. Uuz proposed a two-stage feature selection procedure in the  
100 context of text classification [17]. In the first stage, each term within the doc-  
ument was ranked according to its IG score [18]. In the second stage, genetic  
algorithm and principal component analysis was applied to the ranked list of  
features/terms. This method has been applied to Reuters-21,578 and other  
datasets, achieving relatively good results. Akashdeep, et al. used IG and cor-  
105 relation to perform feature selection in the context of intrusion detection [19].  
In particular, the features were selected by combining the rankings from IG and  
correlation. The authors tested the performance of their method by using a feed  
forward neural network and several datasets, producing encouraging results [20].  
Kamalov and Thabtah proposed a new filtering method that initially integrates  
110 the scores of CHI and IG, then integrates a globally normalized score, called  
V\_Score, for each feature that is derived [5]. The aim was to reduce the number  
of chosen features, by discarding features with relatively low V\_Scores, without  
hindering the performance of the classification algorithms. The cut-off margin  
for a V\_Score is 50% or more above the maximum score obtained by the CSF  
115 features subset. For example, if the maximum V-score in the features set is 1.5  
then features with a V-score of 0.75 or above are selected. Evaluation using a  
large number of datasets has revealed that this approach minimizes the dimen-  
sionality of the datasets substantially when contrasted with results obtained

by IG, CFS, and CHI, without drastically impacting the classifiers predictive  
120 accuracies. Rajab investigated whether IG and CHI scores can be integrated together to reduce instability of the feature selection outcome on a cyber security application called phishing detection [21]. The author proposed a new filtering method based on unifying the CHI and IG computed scores that gets assigned to each website feature. Then, a ranking procedure is invoked to sort the features  
125 new scores which have been assigned to each phishing feature. The decision of which final features to choose prior model learning was given to the security expert. Empirical analysis using real security dataset revealed that unifying the scores of CHI and IG improved the performance of feature selection with respect to classification accuracy at least on the dataset considered. Wang, et al.  
130 proposed a modified model based on the popular mRMR method called Maximum Weight and Minimum Redundancy [22, 23]. In this embedded approach, the weight of each feature is determined based on its usefulness with respect to some predetermined task (e.g. classification) and the redundancy is calculated based on its correlation with other features. Experimental results, based on five  
135 datasets, have shown the benefits of this approach. An extended fusion method was proposed by the Yang and Mao [24]. The authors combined the rankings obtained from Fishers ratio, Relief, asymmetric dependency coefficient, and the absolute weight of support vector machine learning. By fusing the rankings of multiple criteria into a single ordering of features, the authors attempted  
140 to increase the robustness of their feature selection method. The method was tested on five gene expression datasets, and the experimental results showed a reasonable level of stability was achieved by the fusion technique.

#### *2.1.1. Advanced fusion methods*

Advanced fusion techniques combine filters with wrappers and genetic al-  
145 gorithms. Abedinia et al. proposed a new filter-wrapper method based on improving an information theoretic approach [19]. They applied their technique on forecasting load and prices data improving the efficiency of modelling non-linearity and interactions. The method reduced irrelevancy, redundancy and

increased efficiency through retaining meaningful interactions among features.

150 The proposed model is based on a hybrid filter-wrapper paradigm. First, the filtering portion selects a set of maximizing relevancy features. Second, the wrapper part refines the subset’s composite index. The combined approach is said to have a wide range of applications across contexts. Kunasekaran and Sugumaran investigated Genetic Algorithm and Greedy Stepwise on a medical  
155 images dataset in order to reduce the search space for variables and to discover how this reduction may impact the performance of classifiers [25]. Results obtained with the medical dataset showed that when merging Genetic Algorithm with Greedy Stepwise this may yield smaller yet influential features. Min and Xu consider the problem of feature selection with hypothesis tests [26]. The  
160 authors present a three-step semi-greedy filtering heuristic method that creates a set of candidate solutions. First, the heuristic function is designed. In the second step, a feature is iteratively chosen at random based on the current bestk-features. Finally,pcandidate solutions are obtained and the best one is selected. Experimental results show that this new approach is capable of producing better  
165 solutions.

## 2.2. Basic filter methods

Although fusion methods have gained popularity in the literature basic filter methods remain robust performers. Speed and efficiency are the main advantages of using a single metric in feature evaluation. Li and Oh have investigated  
170 a number of filtering methods in relation to the problem of sentiment analysis, and while doing so developed the Expansion Ranking (ER) filtering technique [27]. The ER technique receives results based on a query and allocates weights to each variable in the dataset. Results generated by using a probabilistic classifier, called Nave Bayes, against four datasets related to Turkish consumer behaviour  
175 have shown that ER was able to choose a subset of variables that yields an acceptable error rate when compared with the results obtained by the CHI filtering method and using the same probabilistic classifier. Yuan, et al. proposed a new feature selection method called maximum information correlation [28]. In

this method features are ranked according to correlation information between  
the feature and the class coding spaces. Then, recursive feature elimination is  
180 used to select the features. Experimental results based on the proposed method,  
performed on highly dimensional protein data, have shown very promising signs.  
Another IG based selection method was proposed by Lefakis and Fleuret [29].  
The authors proposed two novel criteria for characterizing the informative value  
185 of a set of features in a classification context by using their mutual information  
with the class under a Gaussian model of the features given in the class. The  
first approach uses the entropy of a single Gaussian of the same expectation  
and variance as the mixture in order to obtain an upper bound on, and subse-  
quently an approximation of, the true entropy. The second approach is based  
190 on a decomposition of the mutual information, in the binary class case, using a  
sum of the Kullback-Leibler divergence terms which can be efficiently approx-  
imated. Empirical results have shown that the methods are competitive with  
currently leading ones with respect to prediction accuracy. One of the most  
popular use cases for feature selection is microarray analysis. Yousef, et al.  
195 tested the effect of filtering methods on MicroRNAs dataset in order to check  
whether reduction of data dimensionality results in higher predictive power [22].  
MicroRNAs dataset contains 700 data instances and represents RNA sequences  
with posttranscriptional gene regulation. Results obtained from pre-processing  
of the dataset revealed that when correlated features are grouped together this  
200 improves the classifiers predictive performance.

### 3. Proposed Feature Selection Method ( $L^2$ )

Among current scholarship there exist multiple feature selection criteria,  
including Information Gain (IG<sup>1</sup>), Chi Squared statistic (CHI) [30, 31] , the  
weight of SVM coefficients, Fishers ratio, and Relief [32]. Many of these meth-  
205 ods are based on measuring the difference between the expected and observed

---

<sup>1</sup>We will use abbreviation IG to refer to information gain between the target and feature variables. Similarly, CHI will refer to the  $\chi^2$  statistic between the target and feature variables.



probabilities. This description fits particularly well to the IG and CHI metrics. Therefore, let us investigate IG and CHI in more detail in order to illustrate our view of feature selection being a statistic of the difference between the expected and observed probabilities. Based on this analysis, we will then introduce our  
210 own method,  $L^2$ , for feature selection.

Throughout this paper  $Y$  and  $X$  will denote categorical variables. In the context of classification,  $Y$  represents the target class and  $X$  represents an independent feature class. In addition, let  $p(y)$  and  $p(x)$  represent the theoretical (population) marginal distributions of  $X$  and  $Y$  respectively. Similarly, let  $p(y, x)$  represent the theoretical joint probability distribution, i.e.  
215  $p(y_i, x_j) = Pr(Y = y_i, X = x_j)$ . Recall that if  $Y$  and  $X$  are independent then  $p(y, x) = p(y)p(x)$ . Thus, we can view  $p(y).p(x)$  as an approximation of  $p(y, x)$  to the extent that  $Y$  and  $X$  are dependent. In practice, we rarely have knowledge of the true theoretical distributions and instead we substitute them  
220 with estimated probabilities based on sample observations (frequencies). Let  $\hat{p}(x)$ ,  $\hat{p}(y)$  and  $\hat{p}(y, x)$  be the frequency distributions based on sample data, i.e.

$$\hat{p}(x) = \frac{\hat{x}}{N}, \hat{p}(y) = \frac{\hat{y}}{N}, \hat{p}(x, y) = \frac{(\hat{y}, \hat{x})}{N}$$

where  $\hat{y}$ ,  $\hat{x}$  and  $(\hat{y}, \hat{x})$  are the number of times the values of  $x$ ,  $y$  and  $(y, x)$  occur in the sample respectively,  $N$  is the sample size. We will refer to the quantity  $\hat{p}(y).\hat{p}(x)$  as the expected probability and refer to  $\hat{p}(x, y)$  as the observed  
225 probability.

Information gain is computed based on Shannon entropy, and calculates the amount of entropy that is removed from the target variable by having the knowledge about the feature variable (Shannon, 1948). In particular, the information gain between  $Y$  and  $X$  is given by the following equation

$$IG(Y, X) = \sum_{i,j} p(y_i, x_j) \log \frac{p(y_i, x_j)}{p(y_i)p(x_j)} \quad (1)$$

230 In practice, the theoretical distributions are replaced with sample frequency

distributions, i. e.

$$IG(Y, X) = \sum_{i,j} \hat{p}(y_i, x_j) \log \frac{\hat{p}(y_i, x_j)}{\hat{p}(y_i)\hat{p}(x_j)}$$

Equation 1 can be restated as

$$IG(Y, X) = H(Y) - H(Y|X) \quad (2)$$

where  $H(Y)$  is the entropy of the target variable and  $H(Y|X)$  is the conditional entropy. We can see from Equation 1 that as the observed probability,  $\hat{p}(x, y)$ , approaches the expected probability  $\hat{p}(y)\hat{p}(x)$ , the value of  $IG(Y, X)$  approaches 0. In particular, note that  $\hat{p}(x, y) = \hat{p}(y)\hat{p}(x)$  if and only if  $IG(Y, X) = 0$  in which case  $Y$  and  $X$  are statistically independent. Therefore, we can conclude that it evaluates the dependence between  $Y$  and  $X$  by measuring the proximity between the observed and expected probabilities.

The chi squared statistic is a popular method used in statistical hypothesis testing to determine if a pair of variables are independent. It is given by the following equation:

$$CHI(Y, X) = \sum_{i,j} \frac{[\hat{p}(x, y) - \hat{p}(y)\hat{p}(x)]^2}{\hat{p}(y)\hat{p}(x)} \quad (3)$$

Similar to  $IG$ , we can see from Equation 3 that as the observed probability approaches the expected probability the  $CHI(Y, X)$  approaches 0. So  $CHI$  measures the dependence between  $Y$  and  $X$  by measuring the proximity between the observed and expected probabilities. These observations lead to the following generalization. Let  $f(p, q)$  be a continuous, convex, function of two variables such that

$$f(p, q) = 0, \text{ whenever } p = q$$

Then we define the generalized relation divergences between variables  $Y$  and  $X$  by

$$F(Y, X) = \sum_{i,j} f(\hat{p}(y_i, x_j), \hat{p}(y_i)\hat{p}(x_j)) \quad (4)$$

It is not hard to see that  $IG$  and  $CHI$  are special cases of the generalized divergence  $F$ . In particular, the  $IG$  can be obtained by taking  $(p, q) = p \log \frac{p}{q}$ . Then,  $f(p, q)$  is continuous, convex, and  $f(p, p) = 0$ . Similarly, the  $CHI$  can be obtained by taking  $f(p, q) = \frac{(p-q)^2}{p}$ . Recall that the family  $\{I^\lambda : \lambda \in R\}$  of power divergence statistics is defined by 34

$$2nI^\lambda = \frac{2}{\lambda(\lambda+1)} \sum_{i=1}^k X_i \left( \frac{X_i^\lambda}{E_i^\lambda} - 1 \right)$$

where  $X_i$  is the observed frequency and  $E_i$  is the expected frequency. It is easy to see, by taking  $f_\lambda(p, q) = p[(\frac{p}{q})^\lambda - 1]$ , that any member of the power divergence statistics is also a special case of divergences defined in Equation 4. Indeed,  $f_\lambda$  is a continuous, convex and  $f_\lambda(p, q) = 0$  whenever  $p = q$ . Note that the set of functions defined by Equation 4 is larger than  $\{I^\lambda : \lambda \in R\}$ . For instance, the  $L^2$  based divergence that we will describe below (see Eq. 5) does not belong to the family of power divergence statistics.

One can come up with multiple functions that would fit the definition of the generalized statistics and use them for feature selection. However, the simplest function would be

$$f(p, q) = (p - q)^2 \quad (5)$$

It is not hard to check that the function defined in Equation 5 satisfies all the necessary requirements. In particular, it is easy to see that the function is continuous and zero when  $p = q$ . To check that the function  $f(p, q) = (p - q)^2$  is convex we can show that its Hessian matrix is positively definite. In particular, the Hessian matrix is given by  $H = \begin{bmatrix} 2 & -2 \\ -2 & 2 \end{bmatrix}$ . So given a vector  $v = [a, b]$ , the product  $v^T H v = 2(a - b)^2$  is nonnegative. It follows that  $f(x, y)$  is a convex function. Therefore, a relation method can be created based on the function. This resulting method will be called the  $L^2$  divergence, which is given by

$$L^2(Y, X) = \sum_{i,j} [\hat{p}(y_i, x_j) - p(y_i)p(x_j)]^2 \quad (6)$$

Note that despite the resemblance between the equation of the  $L^2$  and  $CHI$ ,  
 275 in theory, they are different functions. Nevertheless, in practice, the two often  
 move in the same direction i.e. if  $CHI(Y, X_1) < CHI(Y, X_2)$ , then often times  
 $L^2(Y, X_1) < L^2(Y, X_2)$ . The relationship between  $CHI$  and  $L^2$  arises from the  
 fact that they both measure the similarity between the observed and expected  
 probabilities. This behaviour will be evident when the experimental results are  
 280 examined in the next section. That feature rankings based on  $CHI$  and  $L^2$  are  
 often very similar will be clearly seen. However, it is important to note that  
 there are also cases, such as the lymph dataset, where feature rankings differ  
 substantially. This subject will be addressed in more detail in the next section.

The most distinguishing characteristic that makes the  $L^2$  method an attrac-  
 285 tive alternative is its simplicity and ease of understanding and interpretation.  
 As can be seen in Eq. 6, the  $L^2$  metric simply measures the squared distance  
 between the joint and expected distributions of the variables. Recall that a pair  
 of random variables,  $Y$  and  $X$ , are independent if and only if the observed (joint)  
 probability is equal to the expected probability. It follows that the larger the  
 290 difference between the observed and expected probabilities the more dependent  
 are the variables. The new method is the most direct way of calculating the  
 difference between the probabilities. Therefore,  $L^2$  allows one to delve straight  
 into the heart of the relationship between random variables. On the other hand,  
 the more established measures of the dependence between a pair of variables,  
 295 such as IG and CHI, try to calculate the strength of the relationship via an elab-  
 orate formula that is not very intuitive. Indeed, the formula for calculating IG  
 (Eq. 1) is a complex probability weighted log difference between the observed  
 and expected probabilities. The formula for CHI (Eq. 3) is similar to  $L^2$ , but  
 inversely weighted by the expected probability. Since all three metrics IG, CHI,  
 300 and  $L^2$  measure the similarity between the observed and expected probabilities  
 it is logical to prefer the simplest metric. Given that in mathematics the sim-  
 plest and the most popular distance measure is the  $l^2$  metric we establish the  
 theoretical preference of the proposed  $L^2$  measure.

Figure 1 below illustrates the complete cycle of feature selection based on

305 the  $L^2$  criterion.

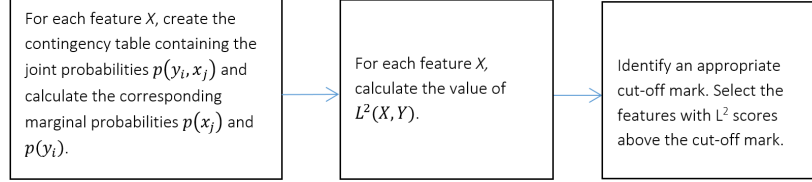


Figure 1: The steps of performing the  $L^2$  based feature selection

The main advantages of this method are summarized below:

- Easy and efficient to compute
- Simple to interpret
- 310 • Reduces data dimensionality when compared to existing filtering methods (i.e. IG, CHI)

Also note that the generalized relation statistic,  $F$ , can be applied to continuous variables by replacing the summation with integration. However, in practice continuous variables are often discretized due to the lack of data. There are two categories of discretization methods: supervised and unsupervised. Supervised discretization uses the class labels to determine the optimal partitioning of the continuous feature. These methods give quality results although they require relatively large datasets since the data used to determine the partition cannot be used to also test the classifier and avoid bias. Unsupervised methods include equal width interval and equal frequency interval. Each method has its strengths and weaknesses. In this paper a hybrid approach to discretizing continuous data is used. In particular, equal width binning is applied to the intervals  $[min, median]$  and  $(median, max]$ . The choice of the median incorporates the equal frequency concept to some extent. The use of median allows the mitigation of the discretization problems inherent in unbalanced data. Therefore, even if the data contains extreme values the bins would contain a representative

amount of data. In Section 4, we show the sensitivity analysis and specifically how the results obtained by  $L^2$  method may differ using different cut-off values.

#### 4. Experimental Analysis

330 In this section, the experiments setting, data, feature selection, and machine learning methods considered to generate the results are discussed. The ultimate purpose of this is to answer the question raised in Section 1: a new generalized filtering method produce comparable features results while maintaining accuracy and improving efficiency?

335 This research question can be clarified experimentally by implementing the  $L^2$  feature selection method and comparing its performance with other common methods such as Chi-square and IG. The performance can be measured by applying supervised learning algorithms to the results obtained from  $L^2$  and other considered filtering methods. In other words, the distinctive sets of features chosen by the Chi-Square, IG, and  $L^2$  methods will be thoroughly tested against  
340 a large number of datasets and with respect to different evaluation metrics will include error rate, recall, and precision among others [32, 33]. These evaluation metrics are generated based on the outcomes of the supervised learning algorithms and will reveal the true performance of the  $L^2$  method when compared  
345 to its counterparts.

##### 4.1. Data and Experimental Setting

The newly proposed feature selection method has been implemented in Java and embedded within the Waikato Environment for Knowledge Analysis tool (WEKA) Attribute-Selection package for comparison purposes, thus, all experiments have been conducted in the WEKA 3.8 environment [34]. WEKA is an  
350 open source Java tool that contains varying implementations of feature selection, data mining, visualization, and machine learning techniques. This tool has been successfully utilized by students, faculty members, researchers, and managers for data analysis and model development. The experiments were performed on  
355 a personal computer with 2.0 Ghz processor and 8 GB RAM.

Deriving the classification models of the supervised learning algorithms, the 10-fold cross validation testing technique was employed. By using 10-fold-cross validation, [35] the training dataset is partitioned into ten subsets and the learning algorithms use nine subsets to generate the classification model before evaluating the models predictive performance on the remaining subset. The same procedure gets repeated ten times in order to average the error rates of the ten runs.

Twenty seven datasets, published at the University of California Irvine data repository (UCI) and belonging to varying domains, have been utilized in the experimental runs [36]. Small, medium, and large datasets (with respect to the number of variables) are present. Different criteria have been used to choose the datasets, including the type of application, number of instances, number of variables, and variable types. Table 1 shows the datasets along with their general characteristics. For fair results analysis, datasets with noise (such as missing values) and with continuous variables have been chosen. As shown in Table 1 most of the datasets are imbalanced with respect to class labels.

In order to reveal the true performance of the proposed feature selection method, particularly in regard to the predictive power of the classification systems, a Nave Bayes (NB) classifier has been adopted [37]. Primary use for a NB classifier is to construct classifiers from the chosen variables of the filtering methods considered. This algorithm is highly efficient since it employs simple calculations based on the Bayes Theorem for deriving class likelihoods. The choice of NB was primarily based on its efficiency in the way it builds classifiers from the distinctive sets of features that we intend to derive by applying feature selection methods on different datasets. The NB implementation utilizes multinomial distributional assumption. Performance of  $L^2$  has been compared with two well-known filtering methods that have proven their merits in different classification applications: IG and CHI. Main reasons for selecting IG and CHI in the comparison are as follows:

- (a) they produce scores per variables as  $L^2$

- (b) they rank variables as  $L^2$
- (c) they have been successfully applied in the classification domain

Cut-off points for CHI and IG have been set to 10.83 and 0.01 respectively [5, 31]. These cut-off points were set in the experimental runs of CHI and IG in order to discard variables with scores below these thresholds (otherwise the variable will be selected). For the  $L^2$ , quartiles have been used as a threshold to differentiate variables based on their scores. To be precise, the calculated 50% and 75% thresholds were used, based on the variables scores assigned by  $L^2$  for a dataset. In the first round of experiments, any variable with a score above the 50% cutoff of all scores was selected, and in the second set of experiments, a 75% cutoff was utilized.

The results obtained by  $L^2$  method have been investigated using different cut-off values in order to identify the ones that can be utilized by novice users. We derive sets of features from different datasets by  $L^2$  when the cut-off value varies. This extensive experimental analysis step is carried out on different datasets in which the cutoff values were set to an equispaced grid 5%, 10%, , 95%. We show for presentation purposes the results obtained on six datasets (Figures 2) in which we plotted the cut-off values (X-Axis) and the error rates derived using Bayes Net probabilistic classifier (Y-Axis). Based on the results obtained, it is clear from the Anneal dataset figures that the error rate was stable when the cut-off was set between 10% and 36%. The error rate started to slightly increase when the cut-off values were between 36% and 50%. Continuing, the error rate had clearly increased when the cut-off value becomes larger than 50%. The same pattern was observed in the results obtained on the Audiology dataset in which when the cut-off values were around 50% and 75% respectively sudden changes in error rate values were obvious. Lastly, the Car and Cleved datasets show a clear increase in error rate when the cut-off values were around 25% and 50% respectively. There was one notable result on the Anneal dataset when the cut-off value reached 85% in which the error derived by Bayes Net was dropped to 10%.



Table 1: The datasets description and results of # of selected variables by the filter methods

Datasets Description							Variables Selected			
Dataset	instances	variables	classes	Missing values	Cont. vars.	Class Weights %	IG	CHI	$L^2$ 50% cut-off	$L^2$ 75% cut-off
Anneal	898	38	6	Yes	Yes	76, 11, 7, 5, 1, 0	29	29	19	10
arrhythmia	452	279	16	Yes	Yes	54,9,3,3,3,5, 0.5,0.5,2,11,0,0,0.8,0.8,4	124	117	140	70
Audiology	226	69	24	Yes	No	25,21,9,9,8,3,3,2,1,1,1,1, 0.9,0.9,0.9,0.9,0.9,0.9, 0.9,0.4,0.4,0.4,0.4,0.4	58	51	35	18
Autos	205	25	7	Yes	Yes	Risk factor 33,26,15 ,13,11,1,0	23	23	13	7
Breast-cancer	286	10	2	Yes	No	70.28, 29.72	6	4	5	3
Car	1728	6	4	No	No	70, 22, 4, 4	5	5	3	2
Cleve	303	11	2	Yes	No	54.45, 45.55	10	9	6	3
CMC	1473	9	3	No	Yes	42.70, 34.70, 22.61	7	8	5	3
Colic	368	22	2	Yes	Yes	63.04, 36.06	16	13	11	6
Credit-a	690	15	2	Yes	Yes	55.50, 44.50	13	12	9	4
Credit-g	1000	20	2	No	Yes	70, 30	10	11	10	5
Cylinder-bands	540	39	2	Yes	Yes	57.78, 42.22	21	20	20	10
Dermatology	366	34	6	Yes	Yes	30, 20, 17, 14, 14, 5	34	34	17	9
Diabetes	768	8	2	No	Yes	65.10, 34.90	8	8	4	2
Ecoli	336	7	8	No	Yes	42,23,15,10,6,1,0.6,0.	6	6	4	2
Flags	194	29	8	No	Yes	35,24,20,8,5,5,1,0.5	26	21	15	8
Glass	214	9	7	No	Yes	35,33,13,8,6,4,0	8	8	5	3
Heart-c	303	13	5	Yes	Yes	54,18,12,12,4	10	9	7	4
Hepatitis	155	19	2	Yes	Yes	79.35, 20.65	15	9	10	5
Hypothyroid	3772	29	4	Yes	Yes	92, 5, 2.5, 0.5	6	10	15	8
Ionosphere	351	34	2	No	Yes	64.10, 35.90	33	33	15	9
Labor	57	16	2	Yes	Yes	64.91, 35.08	14	3	8	4
Lymphography	148	18	4	No	Yes	55, 41, 3, 1	18	10	9	5
Mushroom	8124	22	2	Yes	No	51.80, 48.20	20	21	11	6
Optdigits	5620	64	10	No	Yes	10, 10, 10, 10, 10, 9.93, 9.93, 9.91, 9.86, 9.86	56	58	32	16
Segment	2310	19	7	No	Yes	14.28 each	18	18	10	5
Wave	5000	40	3	No	Yes	33.84, 33.1 , 33.06	19	19	19	10

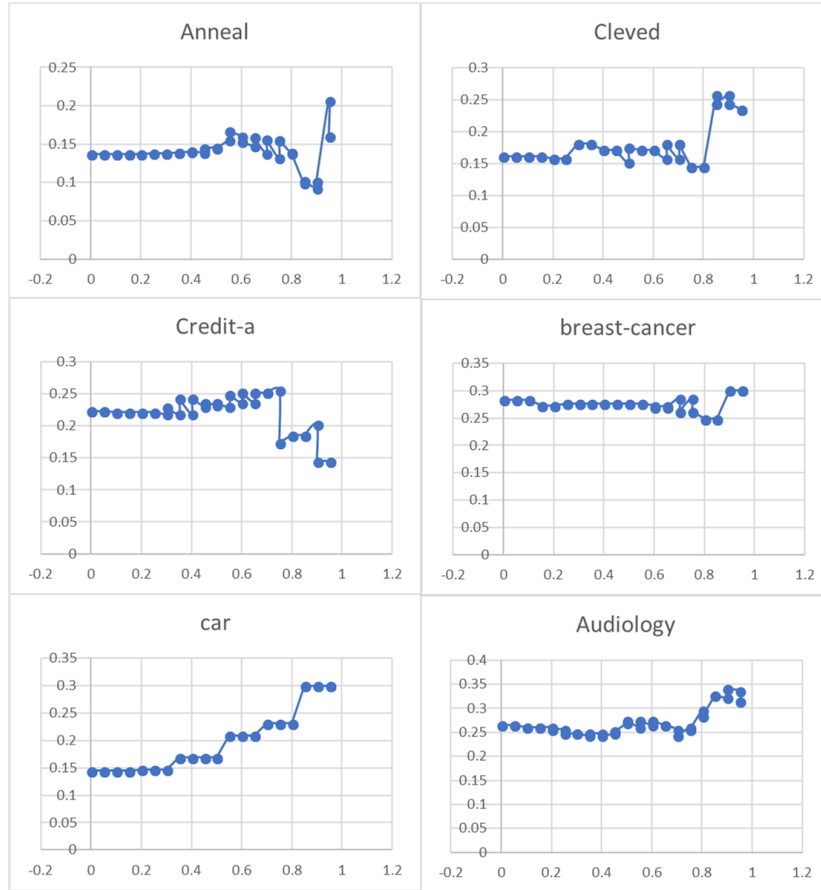


Figure 2: Sample of sensitivity analysis using the Median and error rate using the 6 datasets

These examples if limited show one feasible way to identify potential cut-off points for the  $L^2$  method, that is to consider the balance of the number of variables remaining and the predictive accuracy obtained. In this context, if the cut-off is set too high, such as  $> 75\%$ , the expected number of variables detected by  $L^2$  will be limited and may cause a reduction in predictive accuracy. On the other hand, if the  $L^2$  cut-off is set to a smaller value, i.e.  $10\%$ , larger numbers of variables can be selected and this may enhance the predictive power of the models, but this also may overfit the model. There should be a trade-off between the number of variables which remain and the expected predictive accuracy of

the models, thus the warming up sensitivity analysis results revealed that 50% cut-off value can balance the accuracy and number of variables selected by  $L^2$ . In addition, we empirically demonstrate that when the cut-off values are larger than 75% or 25%, these cases may also produce good sets of features in some cases. Therefore, for fair comparison we have considered 50% to be the default cut-off value of  $L^2$  in addition to testing the other two cut-off values of 25% and 75% respectively in Section 4.2. We omitted using very low cut-off values since these may create overfitted models.

## 4.2. Results Analysis

### 4.2.1. Dimensionality Reduction Results

The number of variables selected by  $L^2$  and the other filtering methods are shown in Table 1.  $L^2$  was able to significantly reduce data dimensionality for the majority of the datasets when contrasted with the IG and CHI methods. With a 50% cutoff,  $L^2$  was able to select a fewer number of variables than both IG and CHI on 19 out of 27 datasets. When  $L^2$  was compared to CHI and IG individually, it produced a lower number of variables on 21 and 22 datasets respectively. When a cutoff threshold of 75% was used, the method consistently retained fewer numbers of variables for all datasets considered (except the Hypothyroid dataset in which IG generated fewer variables). One notable result of  $L^2$  was the arrhythmia dataset, which originally contained 280 variables. More variables than IG and CHI were selected by  $L^2$  with a 50% cutoff since many variables in this dataset have similar scores, which can be an issue that  $L^2$  needs to consider going forward. Overall, dimensionality reduction results of the data clearly demonstrate that  $L^2$ , both with 50% and 75% cutoffs, was able to cut down the search space of variables and thus improve efficiency of the learning algorithm.

Figures 3, 4, and 5 illustrate the reduction in percentage (%) per dataset when  $L^2$  is applied compared to All-variables, CHI, and IG results. The figures clearly demonstrate a large reduction of the dataset dimensionalities in terms of percentage. Based on the distinctive features sets, results obtained with  $L^2$

455 and a 50% cutoff were able to, on average, reduce 48%, 14%, and 25% of the  
 datasets dimensionality. For example, the reduction in % on the Anneal, Autos,  
 and Car datasets were 34%, 43%, and 40% by  $L^2$  when compared to CHI and  
 IG respectively. For the same datasets,  $L^2$  reduced the search space of the  
 original datasets by 74%, 72%, and 67%. These results reveal the significance  
 460 of the proposed filtering method. In addition, when  $L^2$  is used with a cutoff  
 of 75% the dimensionalities of all datasets were further minimized as shown in  
 Figure 4. An exception was the Hypothyroid dataset in which  $L^2$  selected more  
 variables than the IG and CHI filtering methods when a 50% threshold was  
 set. One probable reason could be that this dataset is significantly unbalanced  
 465 with respect to class labels. More specifically, the class labels Hypothyroid and  
 Secondary- Hypothyroid respectively.

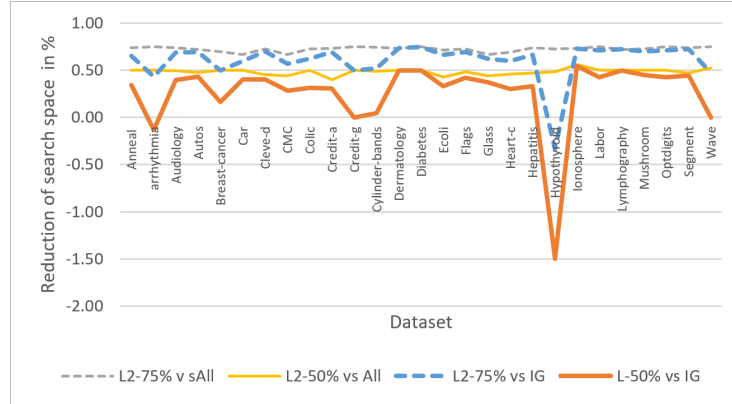


Figure 3: The dimensionality reduction difference between  $L^2$  and the original dataset

For this dataset, the majority of the variable scores produced by all filtering  
 methods are somehow close to each other. To be exact, aside from the highest  
 3 variable scores (TSH, TT4, and FTI) the remaining 26 variables have slightly  
 470 different low scores. In other words, there were three variables with significant  
 scores, and all remaining variables have very small scores without significant  
 differences. This forces  $L^2$  to retain more variables since 26 of them with low  
 scores contribute in computing the median, and many may in fact be associated  
 with scores larger than the 50% threshold. This issue is still under investigation

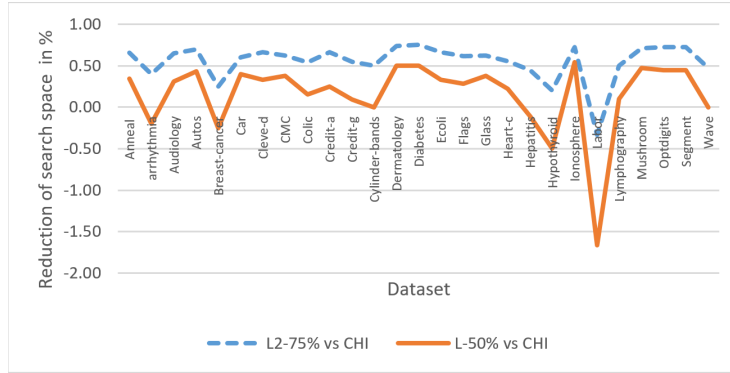


Figure 4: The dimensionality reduction difference between L2 and CHI

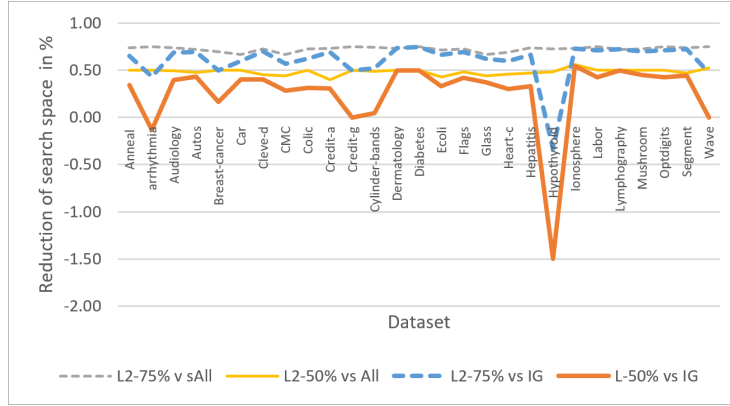


Figure 5: The dimensionality reduction difference between L2 and IG

475 by scholars specializing in feature selection. In fact, even IG and CHI have  
no single threshold that can differentiate between acceptable and unacceptable  
variables, and often this is left to the domain expert to set. However, one feasible  
way to overcome the cutoff value in  $L^2$  is to employ a new search method aside  
from ranking search.

#### 480 4.2.2. Error Rate, Recall and Precision Results

Since the adopted datasets are either binary (two class labels) or multi-  
class classification, evaluation metrics that go along with the nature of these  
problems were used. Common metrics, generated from the confusion matrix

Table 2: Confusion matrix for a binary classification problem

Actual Class Value	Predicted Class Value	
	Yes	No
Yes	True Positive (TP)	False Positive (FP)
No	False Negative (FN)	True Negative (TN)

(Table 2), including error rate, precision, and recall, have been used to evaluate  
485 the performance of the variables chosen by the considered methods. In Table 2  
the possible predictions for test data during a classification process are shown.  
Error rate (equation 7) is one of the popular metric utilized in such supervised  
learning problems. Using this metric, the number of test cases that have been  
assigned the correct class label by the learning algorithm from the total number  
490 of test cases is calculated. Recall, or sometimes named sensitivity (equation  
9), denotes the percentage of the test cases that are classified correctly (yes or  
true positive rate) from the total of cases that are associated with yes, while  
precision is the percentage of correctly classified positive cases in relation to the  
predicted total of positive cases (equation 10). In the below equations, TP, TN,  
495 FP and FN stands for True Positive, True Negative, False Positive and False  
Negative respectively.

$$error\_rate(\%) = 1 - Accuracy \quad (7)$$

$$Accuracy(\%) = \frac{|TP + TN|}{|TP + TN + FP + FN|} \quad (8)$$

$$Recall(\%) = \frac{|TP|}{|TP + FN|} \quad (9)$$

$$Precision(\%) = \frac{|TP|}{|TP + FP|} \quad (10)$$

Figures 6 and 7 display the error rates of the classifiers generated by the NB  
algorithm on the data subsets, both with and without feature selection. The

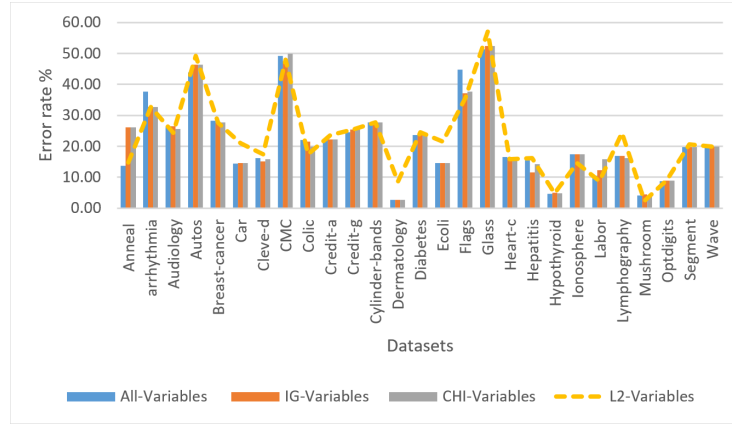


Figure 6: Error rate figures of  $L^2$ -50% cutoff, CHI, IG, and no feature selection

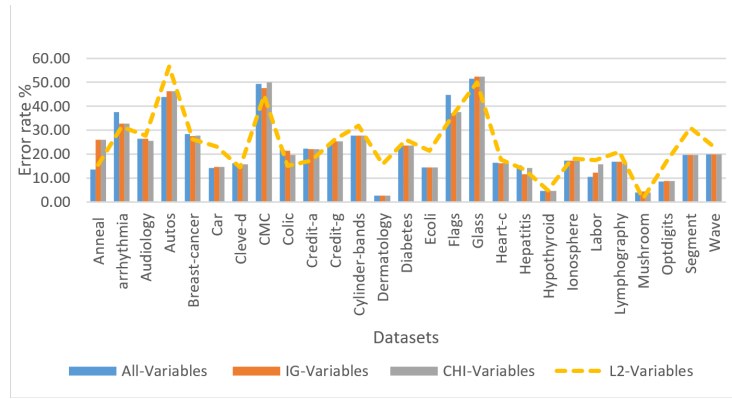


Figure 7: Error rate figures of  $L^2$ -75% , CHI, IG, and no feature selection

results obviously show that the proposed method was able to produce distinctive  
500 sets of variables when processed by NB and competitive classifiers are formed.  
In Figure 6, the NB algorithm derived more accurate classifiers on 10 datasets  
from the  $L^2$  features sets when compared with those of IG and CHI. On the  
other hand, NB derived more accurate classifiers from 13 of the CHI and IG  
features sets when compared with  $L^2$ . Nevertheless,  $L^2$  maintained consistently  
505 fewer numbers of variables for most datasets when compared with those of IG  
and CHI. The win-lost-tie records of  $L^2$  when compared to the CHI and IG  
methods for the classifiers derived by NB with a 50% cutoff were 10-13-4 and

10-13-4 respectively. These results revealed that  $L^2$  discarded more variables when contrasted with common filtering methods such as CHI and IG without  
510 drastically increasing the error rate of the NB classifiers. In Figure 7, for the Car dataset,  $L^2$  showed a higher error rate. After a careful investigation it was revealed that this particular dataset is small, with 7 variables from which 3 were picked by  $L^2$ . However, there were two additional common variables selected by IG and CHI (maint, log\_boot) that contributed to the increase of their classifiers  
515 accuracies but were discarded by  $L^2$ . The  $L^2$  method discarded these two since they had lower scores than the 50% cutoff of all seven variables in the dataset.

Surprisingly, when the 75% cutoff was set in  $L^2$ , it not only substantially minimized the number of variables but also showed higher quantities of predictive classifiers, especially for the larger datasets. In particular, for the arrhythmia,  
520 Anneal, Cylinder-bands, and Optdigits datasets, with 280, 64, 39, and 69 variables respectively,  $L^2$  minimized the number of variables to 70, 16, 10, and 16 while IG and CHI selected 124, 29, 21, 56 and 117, 29,20, 58 variable sets from the same data. Despite the large reduction in the number of variables by the new method on these datasets, NB derived higher predictive models from  $L^2$   
525 subsets when compared with the larger IG and CHI subsets. This shows the competitiveness of  $L^2$  when it comes to feature selection. The proposed method balances the dimensionality of the dataset and the predictive performance by allowing, in some cases, a slight decrease in accuracy for an exchange of more efficient data processing and smaller feature sets.

530 In Figure 7 the proposed method shows a slightly higher error rate on the Lymphography and Autos datasets when compared with results produced by NB from IG and CHI features sets. For the Autos case, this dataset contains a small number of training instances and imbalanced class labels. When  $L^2$  was applied, the scores assigned to the variables of this dataset were very close  
535 and forced  $L^2$  to choose 7 of the 25 total variables. In other words, there were variables ignored by  $L^2$  which have close scores to some selected variables and therefore some knowledge was tossed out. This explains the 10% reduction in precision. However, when the cutoff was lowered to 50% the precision rates



improved by 11.8% as shown in Figure 6, simply because 5 more variables were  
 540 added to the final features set.

Figures 8 and 9 show precision and recall rates derived by NB for the different features sets selected by the considered filtering methods when applied against the 27 classification datasets. The precision and recall rates generated against  $L^2$ 's feature sets (both versions), and for the vast majority of the considered datasets, were highly competitive when compared to the rates generated  
 545 against the CHI and IG feature sets. There are a few exceptions, however, such as the cases of the Autos and Lymphography datasets for precision results on  $L^2$ 's features set when 75% cutoff value was used as a cutoff value. For the Lymphography dataset, the reduction of the precision rates was since this dataset  
 550 contains a fewer number of instances with four class labels, two of which are imbalanced. To be clear, there are two class labels (normal, fibrosis) with just 2 and 4 instances respectively.  $L^2$ , with the threshold set to 75%, derived only 5 variables and the IG and CHI methods selected 18 and 16 variables respectively. When the scores of these variables were investigated, only one significant variable shared by the results of all feature selection methods and a high quantity  
 555 of discrepancies in the variables ranks and scores were observed.

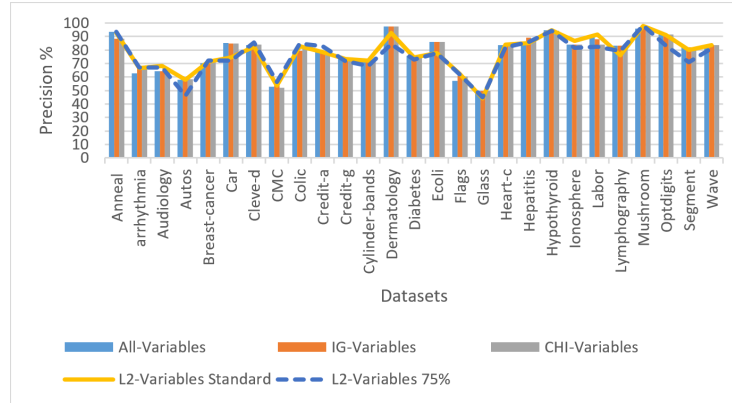


Figure 8: Precision figures in % of L2, CHI, IG, and no feature selection

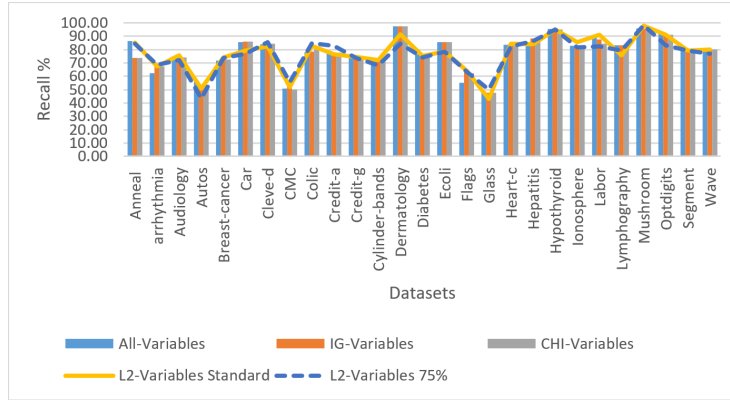


Figure 9: Recall figures in % of L2, CHI, IG, and no feature selection

## 5. Conclusions

Many classification domains are associated with datasets involving a large number of variables, which makes the data processing phase computationally expensive. Therefore, feature selection becomes a vital method for reducing the search space and enhancing the robustness of the learning algorithms during the process of building classification systems. This paper proposed a new, simplified, feature selection method called  $L^2$  that computes scores per variable based on the quantification of the distance between observed and expected variables and the class label before ranking the variables in a descending manner. The proposed method employs a cut-off value based on the variable scores, and retains the variables with scores larger than or equal to 50%. The 50% cut-off value was determined through extensive sensitivity analysis using various datasets with different sizes and characteristics. We have also considered two other cut-off values, i.e. (25%, 75%). Using these cut-off values especially the 50%, reduce the training dataset dimensionality by retaining a lower number of variables without drastically decreasing the performance of the classification system when contrasted to common filtering methods such as IG and CHI. The proposed method has been implemented in the WEKA Java environment. Experimental results on 27 varying and unique datasets using feature sets selected

by  $L^2$ , IG, and CHI, have been derived on WEKA. NB probabilistic algorithm was then used to derive the classification systems using the results of the feature selection methods. The results, in terms of recall, precision, and error rate demonstrated that  $L^2$  is a highly competitive feature selection method that not only substantially minimizes the dimensionality of the datasets but also maintains acceptable rates of recall, precision, and error rate. More importantly,  $L^2$  was able to cut down the search space for the majority of the datasets considered when contrasted with results of the CHI and IG feature sets. Next steps involve the utilization of more advanced search algorithms to enhance the way variables are selected. This enables new ways for defining the cut-off in an automated manner to be identified and will be presented soon.

## References

- [1] N. Abdelhamid, F. Thabtah, H. Abdel-Jaber, Phishing detection: A recent intelligent machine learning comparison based on models content and features, in: 2017 IEEE International Conference on Intelligence and Security Informatics: Security and Big Data, ISI 2017, Institute of Electrical and Electronics Engineers Inc., 2017, pp. 72–77. doi:10.1109/ISI.2017.8004877.
- [2] G. Chandrashekar, F. Sahin, A survey on feature selection methods, Computers and Electrical Engineering 40 (1) (2014) 16–28. doi:10.1016/j.compeleceng.2013.11.024.
- [3] R. P. Bunker, F. Thabtah, A machine learning framework for sport result prediction, Applied Computing and Informatics 15 (1) (2019) 27–33. doi:10.1016/j.aci.2017.09.005.  
URL <https://linkinghub.elsevier.com/retrieve/pii/S2210832717301485>
- [4] L. McCluskey, F. Thabtah, R. M. Mohammad, Intelligent rule-based phishing websites classification, IET Information Security 8 (3) (2014)

- 153–160. doi:10.1049/iet-ifs.2013.0202.
- 605 URL <https://digital-library.theiet.org/content/journals/10.1049/iet-ifs.2013.0202>
- [5] F. Kamalov, F. Thabtah, A Feature Selection Method Based on Ranked Vector Scores of Features for Classification, *Annals of Data Science* 4 (4) (2017) 483–502. doi:10.1007/s40745-017-0116-1.
- 610 [6] M. A. Hall, Correlation-based Feature Selection for Machine Learning (April).  
URL <http://citeseerx.ist.psu.edu/viewdoc/summary?doi=10.1.1.37.4643>
- [7] Hanchuan Peng, Fuhui Long, C. Ding, Feature selection based on mutual information criteria of max-dependency, max-relevance, and min-redundancy, *IEEE Transactions on Pattern Analysis and Machine Intelligence* 27 (8) (2005) 1226–1238. doi:10.1109/TPAMI.2005.159.  
615 URL <http://ieeexplore.ieee.org/document/1453511/>
- [8] J. Li, K. Cheng, S. Wang, F. Morstatter, R. P. Trevino, J. Tang, H. Liu, Feature Selection, *ACM Computing Surveys* 50 (6) (2017) 1–45. doi:10.1145/3136625.  
620 URL <http://dl.acm.org/citation.cfm?doid=3161158.3136625>
- [9] N. Hoque, D. Bhattacharyya, J. Kalita, MIFS-ND: A mutual information-based feature selection method, *Expert Systems with Applications* 41 (14) (2014) 6371–6385. doi:10.1016/j.eswa.2014.04.019.  
625 URL <https://linkinghub.elsevier.com/retrieve/pii/S0957417414002164>
- [10] H. Zhou, J. Guo, Y. Wang, M. Zhao, A Feature Selection Approach Based on Interclass and Intraclass Relative Contributions of Terms, *Computational Intelligence and Neuroscience* 2016 (2016) 1–8. doi:10.1155/2016/1715780.  
630 URL <http://www.hindawi.com/journals/cin/2016/1715780/>

- [11] F. Thabtah, N. Abdelhamid, Deriving Correlated Sets of Website Features for Phishing Detection: A Computational Intelligence Approach, *Journal of Information & Knowledge Management* 15 (04) (2016) 1650042. doi:10.1142/S0219649216500428.  
URL <https://www.worldscientific.com/doi/abs/10.1142/S0219649216500428>
- [12] A. Al-Thubaity, N. Abanumay, S. Al-Jerayyed, A. Alrukban, Z. Man-naa, The effect of combining different feature selection methods on arabic text classification, in: *SNPD 2013 - 14th ACIS International Conference on Software Engineering, Artificial Intelligence, Networking and Parallel/Distributed Computing*, 2013, pp. 211–216. doi:10.1109/SNPD.2013.89.
- [13] B. Azhagusundari, A. S. Thanamani, Feature Selection based on Information Gain, *International Journal of Innovative Technology and Exploring Engineering (IJITEE)* 2 (2) (2013) 18–21. doi:2278–3075.  
URL <http://citeseerx.ist.psu.edu/viewdoc/summary?doi=10.1.1.674.9620>
- [14] I. H. Witten, E. Frank, M. A. Hall, *Data Mining: Practical Machine Learning Tools and Techniques*, Third Edition (The Morgan Kaufmann Series in Data Management Systems), 2011.  
URL <http://www.amazon.com/Data-Mining-Practical-Techniques-Management/dp/0123748569?%3FSubscriptionId=%3D1V7VTJ4HA4MFT9XBJ1R2-%3Dtag%3Dmekentosjcom-20%3D>
- [15] S. R. Shahamiri, S. S. B. Salim, A Multi-Views Multi-Learners Approach Towards Dysarthric Speech Recognition Using Multi-Nets Artificial Neural Networks, *IEEE Transactions on Neural Systems and Rehabilitation Engineering* 22 (5) (2014) 1053–1063. doi:10.1109/TNSRE.2014.2309336.  
URL <http://ieeexplore.ieee.org/document/6762967/>
- [16] F. Kamalov, Sensitivity Analysis for Feature Selection, in: *Proceedings - 17th IEEE International Conference on Machine Learning and Applica-*

tions, ICMLA 2018, Institute of Electrical and Electronics Engineers Inc., 2019, pp. 1466–1470. doi:10.1109/ICMLA.2018.00238.

- [17] H. Uuz, A two-stage feature selection method for text categorization by using information gain, principal component analysis and genetic algorithm, Knowledge-Based Systems 24 (7) (2011) 1024–1032. doi:10.1016/j.knosys.2011.04.014.

URL <https://linkinghub.elsevier.com/retrieve/pii/S0950705111000803>

- [18] S. L. Salzberg, C4.5: Programs for Machine Learning by J. Ross Quinlan. Morgan Kaufmann Publishers, Inc., 1993, Machine Learning 16 (3) (1994) 235–240. doi:10.1007/bf00993309.

- [19] O. Abedinia, N. Amjady, H. Zareipour, A New Feature Selection Technique for Load and Price Forecast of Electrical Power Systems, IEEE Transactions on Power Systems 32 (1) (2017) 62–74. doi:10.1109/TPWRS.2016.2556620.

URL <http://ieeexplore.ieee.org/document/7458187/>

- [20] S. R. Shahamiri, W. M. Wan-Kadir, S. Ibrahim, S. Z. M. Hashim, Artificial Neural Networks as multi-networks automated test oracle, Automated Software Engineering 19 (3) (2012) 303–334. doi:10.1007/s10515-011-0094-z.

- [21] K. D. Rajab, New Hybrid Features Selection Method: A Case Study on Websites Phishing, Security and Communication Networks 2017 (2017) 1–10. doi:10.1155/2017/9838169.

URL <https://www.hindawi.com/journals/scn/2017/9838169/>

- [22] M. Yousef, M. D. Saçar Demirci, W. Khalifa, J. Allmer, Feature Selection Has a Large Impact on One-Class Classification Accuracy for MicroRNAs in Plants, Advances in Bioinformatics 2016 (2016) 1–6. doi:10.1155/2016/5670851.

URL <http://www.hindawi.com/journals/abi/2016/5670851/>

- [23] J. Wang, L. Wu, J. Kong, Y. Li, B. Zhang, Maximum weight and minimum redundancy: A novel framework for feature subset selection, *Pattern Recognition* 46 (6) (2013) 1616–1627. doi:10.1016/j.patcog.2012.11.025.
- [24] Feng Yang, K. Z. Mao, Robust Feature Selection for Microarray Data Based on Multicriterion Fusion, *IEEE/ACM Transactions on Computational Biology and Bioinformatics* 8 (4) (2011) 1080–1092. doi:10.1109/TCBB.2010.103.  
URL <http://ieeexplore.ieee.org/document/5611484/>
- [25] K. K. H. Kunasekaran, R. Sugumaran, Exploratory Analysis of Feature Selection Techniques in Medical Image Processing, *International Conference on Information Engineering, Management and Security 2016 (Iciems)* (2016) 33–37.  
URL <https://www.semanticscholar.org/paper/Exploratory-Analysis-of-Feature-Selection-in-Image-Kunasekaran-Sugumaran/ce4c8cf20ca1ba650efecbb396347fd9b814f7f9>
- [26] F. Min, J. Xu, Semi-greedy heuristics for feature selection with test cost constraints, *Granular Computing* 1 (3) (2016) 199–211. doi:10.1007/s41066-016-0017-2.
- [27] S. Li, S. Oh, Improving feature selection performance using pairwise pre-evaluation, *BMC Bioinformatics* 17 (1) (2016) 312. doi:10.1186/s12859-016-1178-3.  
URL <http://bmcbioinformatics.biomedcentral.com/articles/10.1186/s12859-016-1178-3>
- [28] M. Yuan, Z. Yang, G. Huang, G. Ji, Feature selection by maximizing correlation information for integrated high-dimensional protein data, *Pattern Recognition Letters* 92 (2017) 17–24. doi:10.1016/j.patrec.2017.03.011.  
URL <https://linkinghub.elsevier.com/retrieve/pii/S0167865517300764>

- 720 [29] L. Lefakis, F. Fleuret, Jointly informative feature selection made tractable by Gaussian modeling, *Journal of Machine Learning Research* 17 (2016) 1–39.
- [30] J. R. Quinlan, Induction of decision trees, *Machine Learning* 1 (1) (1986) 81–106. doi:10.1007/bf00116251.
- 725 [31] H. Liu, R. Setiono, Chi2: feature selection and discretization of numeric attributes, in: *Proceedings of the International Conference on Tools with Artificial Intelligence*, IEEE, 1995, pp. 388–391. doi:10.1109/tai.1995.479783.
- [32] S. Hegde, K. K. Achary, S. Shetty, Statistical analysis of features and classification of alphasyllabary sounds in Kannada language, *International Journal of Speech Technology* 18 (1) (2014) 65–75. doi:10.1007/s10772-014-9250-8.
- 730 [33] F. Thabtah, F. Kamalov, K. Rajab, A new computational intelligence approach to detect autistic features for autism screening, *International Journal of Medical Informatics* 117 (2018) 112–124. doi:10.1016/j.ijmedinf.2018.06.009.
- 735 URL <https://linkinghub.elsevier.com/retrieve/pii/S1386505618300546>
- [34] M. Hall, E. Frank, G. Holmes, B. Pfahringer, P. Reutemann, I. H. Witten, The WEKA data mining software, *ACM SIGKDD Explorations Newsletter* 11 (1) (2009) 10. doi:10.1145/1656274.1656278.
- 740 [35] S. R. Shahamiri, S. S. Binti Salim, Artificial neural networks as speech recognisers for dysarthric speech: Identifying the best-performing set of MFCC parameters and studying a speaker-independent approach, *Advanced Engineering Informatics* 28 (1) (2014) 102–110. doi:10.1016/j.aei.2014.01.001.
- 745



- [36] A. Asuncion, D. J. Newman, UCI Machine Learning Repository: Data Sets (2007).

URL <https://archive.ics.uci.edu/ml/datasets.php>  
750 <http://www.ics.uci.edu/~mlearn/MLRepository.html>  
<https://archive.ics.uci.edu/ml/datasets.html>

- [37] D. J. Hand, K. Yu, Idiot's Bayes - Not so stupid after all?, International Statistical Review 69 (3) (2001) 385–398. doi:10.1111/j.1751-5823.2001.tb00465.x.

755 URL <http://doi.wiley.com/10.1111/j.1751-5823.2001.tb00465.x>