

SE

Application  
System level  
Service (SaaS)

Software

program (installation, dependencies)

Config

Documentation (user, system)

Support

Eigenschaften

Size

no physical borders

Exposure

Distribution (cheap, updates, <sup>not intended</sup>)

Changing Environment

long Lifetime

hard to measure

=> many Projects fail

Software Engineering

through

Requirement Analysis → Domain driven Design

systematic  
disciplined  
quantifiable

⇒ development  
Operation  
Maintenance

Design Principles, Patterns  
Architecture

Tools + productivity  
- getting used to

## IDE - Integrated Development Environments

- File Explorer
- Syntax Highlighting
- Code Completion
- Problem Indicators
- Code Navigation
- Refactoring
- Testing
- Debugger
- Version Control
- Terminal

## Command Shell z.B. Bash

interactive programming language  
commands = executable programs

command-Name [Flags] Arguments  
-r --recursive=arg

man Command-Name

(1) | (2) redirects std out from (1) in (2)

(1) > FILE redirects out

\* error both

exit code 0 success  
-2 if error code

(1) || (2) executes (2) if (1) fails

(1) && (2) succeeds

- touch
- ls , tree
- mv
- cp
- rm -r for directories
- chown, chmod
- cat concatenate files
- wc word count
- sort
- grep search through file
- find files
- psql
- mkdflr
- cd
- rmdir

FOO = 1

BAR = \$(( \$FOO \* 2 ))

if [ \$FOO -lt 123 ];

then echo "hi";

else -- ;

fi

for file in \$FILES; do process \$FILE; done  
while [ \$N -lt 100 ]; do N=\$((N+1)); --; done

function name()

local N=91 # first Parameter

echo --;

3

n = \$1(command argument) executes function

Build Systems - automate repetitive tasks on code  
compile, run, clean, interpreter, generate docs, style, deploy  
config build scripts    incremental: only update changed files

## Version Control Systems

history  
multiple developers

VCSs  
widely used

Centralized - all changes in a single repository

Subversion  
Git, Mercurial

Distributed - multiple independent repositories

Commit - atomic change

organizer  
hash  
author, date  
message  
Line-wise additions  
deletions

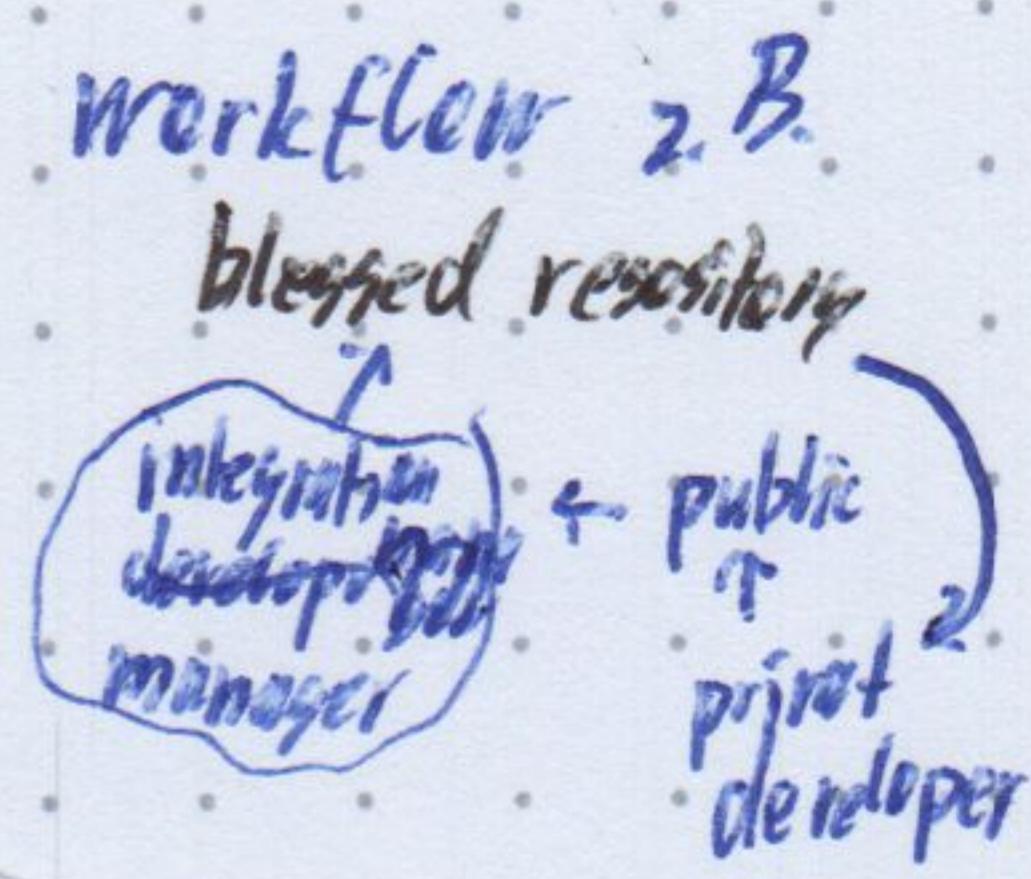
organizer

Branches - organize commits

different line of work  
commits partially ordered  
merge conflicts

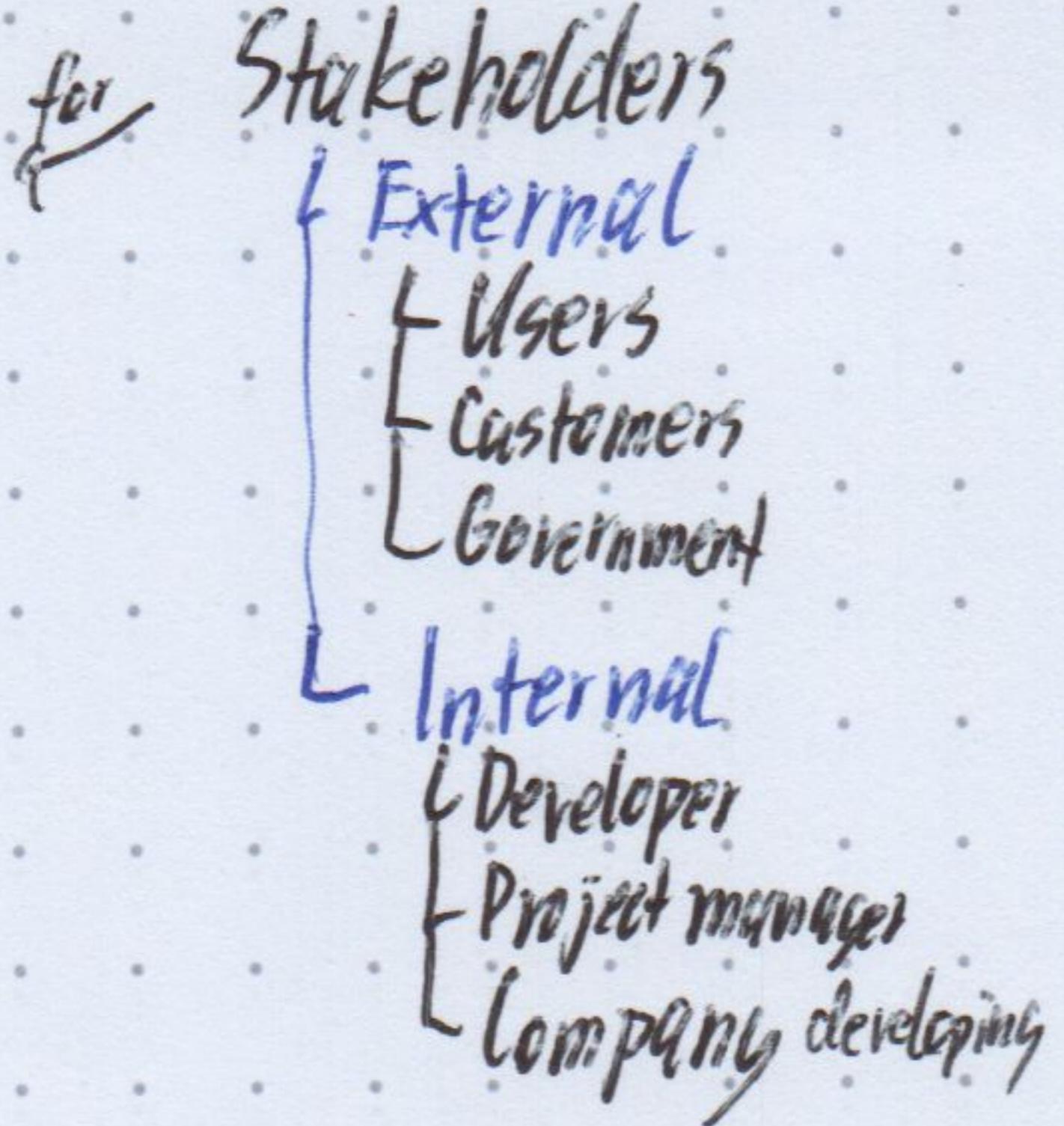
Repository

push, pull



# Software Engineering Process

responsibilities and interactions  
of development teams



Quality assurance  
Consistency, Repeatability  
Collaboration, coordination  
Risk Management anticipate problems  
Scalability, efficiency  
Continuous Improvement

## Requirement Analysis

Design

Development

Validation

(Maintenance)

Operation

Customer Feedback

Agile (many different)

iteration / sprint - result executable

fixed time, immutable

↳ backlog → next iteration

↳ changes only at end

Requirements

continuous discovery

User Stories

Description

Story points - z.B. Planning Poker

↳ simultaneous rating

until consensus

↳ break up in 4-7th tasks

↳ developers sign-up for

Planning

Stakeholder

Scope - How much until

Priority - High value

Composition of team

Date

Developers

technical consequences

detailed scheduling

maxed by capacity =  $\Sigma$  to implement Story Points

$\Sigma$  completed

~ Velocity prior iterations

~ available developers

Retrospective

often between iterations

⇒ find actions to improve process

Kanban board - team intern → Daily Standups

columns = steps

colors = type of task

who's working on what

report progress, synchronize

redistribute if problems

assign new tasks

Individuals & Interactions > Process & Tools

Working software

> Comprehensive Documentation

Customer Collaboration > Contract Negotiation

Respond to change

Requirements Analysis

- identifying documentation
- validating properties
- managing software supported to do

often informal  
⚠ implicit assumptions

Who? Stakeholder → System Requirements  
z.B. - It needs database

What?

functional  
User stories  
Use cases

non-functional

Product  
Portability  
Reliability  
Efficiency  
Usability

Organizational  
Delivery  
Implementation  
Standards

External

Interoperability

Ethical

Legislative

Safety

HIPAA - Health Insurance Portability and Accountability Act  
GDPR: General Data Protection Regulation

Performance  
Space

Space

## Elicitation

Stakeholder identification → viewpoints → Interviews, Survey

operator	Interactor	Closed → Open
uses	Indirect	cooperation?
benefits	Domain	implicit assumptions?
purchasing	L2.B. legal	
regulating		
opposed		

Gap analysis  
Prototyping  
Feasibility study  
Technical  
Operational  
Economical  
Legal  
schedule

even  
→ start?

## Documentation

### Standard Dokument

#### Introduction

Purpose of Document  
Scope of Product  
Definitions, acronyms  
References  
Overview

#### General description

Product Perspective  
functions  
User characteristics  
Limitations  
Assumptions, dependencies

#### Specific requirements

Appendices, Index, etc.

### Requirements

non-functional: free form

#### functional

User Stories ← Informal → Use cases  
Who, What, Why

As a ... I want ... so that ...

Acceptance Criteria

Informal

Brief

→

Understandable

Valueable

Sized

Approprietary

Estimatable Effort

Independent

Testable

Mnemonic: INVEST

negotiable

### Structured Sections

Title

Primary Actor

Goal

Scope

stakeholders for this

Precondition

Main success scenario

Acceptance Criteria

### Validation

written before/concurrently to impl.  
to fail again

Acceptance tests if user story/case done → never allowed

Metrics for non-functional requirements → continuously monitored

Code review (by 3rd Party) z.B. before investments by governments

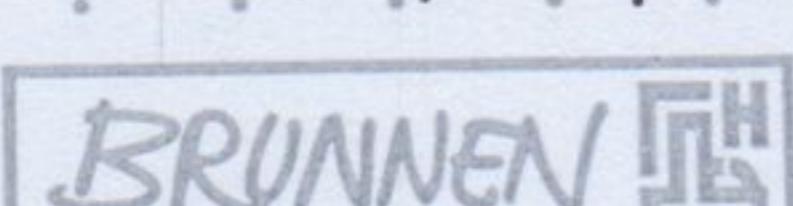
## Illustrations

### Flow chart

Notes:  
round → initial or terminal states  
rectangle → intermediate states  
rhombus → decisions  
Arrows → transitions

↓ extends

BPMN - Business Process Model and Notation  
rows for departments



→ concurrent processes

# Domain-Driven Design DDD - goal reduce incidental complexity language of domain

domain - subject area of software

" models - abstract concepts

in language of domain

visualized with UML-Diagrams

not static view consider abstraction of code

need to be kept up to date (when code changes)

solution space - implementation

close to model & craft

multiple years working experience

## Modelling Vocabulary of Domain

1. Identify concepts

talk to domain experts (structured Interviews)

-synonyms

noun phrases candidates for concepts, + specific meaning

-generic

category list list categories first z.B. Physical objects, Specifications

-impl.-details

2. generalizations between concept B specific case of A

list categories first z.B. Physical objects, Specifications

-impl.-details

3. properties B can be used in context expecting A

B-Dat

-Places, Events, Transactions [etc.]

attributes Separate sections

-Organisations, Roles, Containers

associations for primitive type) include when

need to be preserved

-just a name

4. derived properties

A part of B

-verb/phrase

can be computed from other properties

line item of transaction B

-optional association Name

associations for compound type)

related transaction

-verb/phrase

association = depending on access direction and mult

[list of] accessor in one concept type

-verb/phrase

derived properties = accessor functions?

product of transaction B

-verb/phrase

## Implementation

Concepts  $\Rightarrow$  traits or classes

generalizations  $\Rightarrow$  traits, extended by classes

attributess  $\Rightarrow$  " with accessors

association  $\Rightarrow$  depending on access direction and mult

[list of] accessor in one concept type

derived properties  $\Rightarrow$  accessor functions?

## UML types

### Behavior Domain Models

#### UML State Machine Diagram

finite state machine diagram

equi  
time  
change

trigger

bed expr.

z.B. method call

initialstate

state 1

entry

action

action

entry / action on entry

do / action while in state

exit

z.B. method calls

state 2

final state

terminal state

## Implementation

States  $\Rightarrow$  enum

transitions as func-

class

var current state : States = Initial

def transition : Unit =

current state match

case initial =

val guard = ...

if (guard){}

output initial();

current state = ...

}

else { ... }

# Software Quality

Factors:		intern dev.	extern stakeholder
Validity	Efficiency	state dev.	measure how positive it is perceived
Responsiveness	Reusability		
Ease of use			
Functionality	Extensibility		
Compatibility	Maintainability		
Portability	Understandability		
	Enjoyability		

## Assure Quality

external	internal quality
continuous feedback stack	Design principles and code metrics
Domain Modeling	Design patterns
Testing	Architecture
Static Analysis	

low quality  $\Rightarrow$  fail

## + assure quality

Testing - confirm find detect

- requirements, vulnerabilities, regressions

- can only proof existence of bugs

- costly 15-25% dev time

- hard maintainance

Who

automated  
manual

Techniques

{ Example-Based example inputs, expected (+easy)  
Property-Based mathematical properties, random inputs (-often not exhaustive)

{ Fuzz Testing test if crash (+exhaustive)  
discover vulnerabilities (-difficult)

What Purpose

Acceptance (Requirements)

- smoke  
- usability  
- accessibility  
- security  
- performance

fuzzer can use be based on  
input structure (Grammar e.g. SQL, JSON)

File formats  
protocols

dynamic analysis information

e.g. { coverage of code  
Concise Execution (conditions in rule)

happy path - how it was meant to be used, no trigger errors  
corner, exceptional cases - e.g. null, negative, empty param  
non-trivial behaviour - test them, not getters/setters

AAA pattern - Arrange, Act, Assert

DRY - don't repeat yourself  $\Rightarrow$  helper func.

KISS - Keep it simple, stupid! so tests don't need testing

Title  $\rightarrow$  problem should be clear

Isolation  $\rightarrow$  where bug?  $\Rightarrow$  reduce dependencies if possible

Test Fakes, Mock through Dependency Injection

avoid

check if called

imitate functionality

val m = mock[Class]

m.expects("func with args  
(...)")

Side Effects  $\rightarrow$  before, after function to exec. Effects for test case

I can cause beforeAll, beforeEach, afterAll, afterEach

Floaky Tests - sometimes fail, sometimes pass

## Test Coverage

### Structural

Statement coverage = % All statmt

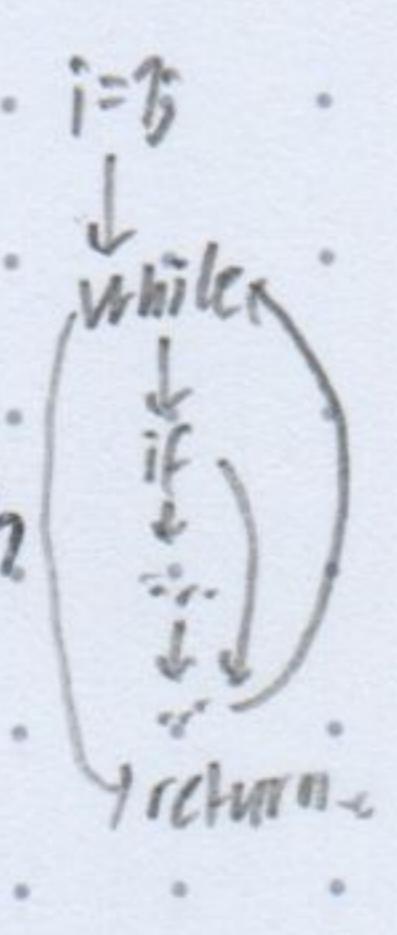
Edge coverage percentage of edges

in control-flow graph

Path coverage % paths from start to end

- unachievable in Praxis

can be infinite or unfeasible paths



### Logical

Condition  $\Delta$  - short circuit evaluation

% conditions at least one evaluated true and false

Decisions = boolean Expressions without &, ||, !, ?, :, ;

Decisions = "Decisions" alternative Def. branch point but tmp vars wouldn't change

Decisions = all boolean Expressions (and parts)  $\subseteq$  Conditions Decisions

MCDC - Modified Condition/Decision Coverage

% entry and exit points must be invoked

% decisions outcomes min one?

% conditions in a decision shown to independently affect decisions outcome

+ for critical software

# Static Analysis

Tests can't prove absence of bugs

Formal Verification  
+ can prove absence 100%  
- time, specific, which property?

Dynamic Analysis  
analyse trace data of exec.  
- Limited inputs, which?

Static Analysis - extract info without executing  
+ automated  
+ strong guarantees  
- undecidable  
+ possible exec. paths

## Usage

IDE | Recommendations  
Refactorings

Compilers | check  
optimize

Formal Verification  
gather info  
ensure valid spec

Security analysis  
find vulnerabilities  
malware  
data leaks

Intra- ↔ Interprocedural  
method at whole program  
a time

Flow-sensitive ↔ insensitive  
compute result @ statements  
globally valid

Context-sensitive ↔ insensitive  
use multiple contexts  
consider each piece  
only once  
e.g. calling method

Completeness - no results runtime impossible  
Precision =  $\frac{\# \text{true positives}}{\# \text{results}}$

Soundness - produce results possible @ runtime  
Recall =  $\frac{\# \text{true positives}}{\# \text{expected results}}$

often not achievable  $\Rightarrow$  Soundness  
Deliberate, document  
unsound choices

Scalability  $\Rightarrow$   
large software, limited time  
memory

## Control Flow Analysis

- order & dependencies of stmts

## Data Flow Analysis

where value used  
defined

Abstract Interpretation + for soundness  
over-approximate semantics z.B. abstract values  
T, P, PC

Symbolic Execution - Path explosion

interpret with symbolic values z.B.

Fork branch Fork on branches  
 $i = \lambda$   
 $i = \lambda + 2, \lambda > 0$   
? else  
? ...

Constraint Based Analysis - may be hard  
to solve  
extract constraints on solution  
solve for most precise solution

Type and Effect Systems  
Type System assign types to Expr. z.B. already  
compile time  
Effect System assign effect seltener  
(follows from subexpressions)

## Common Analysis

### CFG - Control Flow Graph

Dominator tree - Which stmt exec before another  
Post-dominator tree - after v

### Escape & Alias Analysis

dynamic scope of objects  
e.g. it's limits often may 2 vars same object  
for optimizing flow (alias) sensitivity

### Monotone Data Flow

Liveness - value reusable after certain point  
Reaching definitions - where can values come from  
Available expressions - value already computed

### Immutability

Purity - deterministic,  
no side effects

+ safe, maintainable

### Graph-Based Interprocedural Data-Flow

fun into graph reachability problems  
efficient for suitable problems (important: distributivity)  
e.g. for taint analysis (track sensitive/dangerous data)

### Slicing - slicing criterion

Forward - Stmt affected by

Backward - Stmt affecting

+ debugging  
clone detection  
parallelization

### Call Graph

prerequisite interprocedural analysis  
diff algorithms precision scalability

### Points-To Analysis e.g. for Call Graphs

Which objects can var refer to

Type Abstraction  
precise Allocation-site Abstraction  
Shape Abstraction

# Design Principles

KISS - Keep it simple, stupid!

complexity → harder to understand, test, maintain  
 /  
 accidental      essential  
 ↳ from implementation      ↳ from domain  
 ↳ refactoring      unavoidable

- Lack of documentation
  - ↳ understand → reuse
- Bad architectural decision
- Premature performance optimizations
  - ↳ only if problem affecting stakeholder
- Uncontrolled side-effects
  - ↳ non-deterministic
- Developer inexperience
  - ↳ don't use patterns → pair with experienced
- Software evolution
  - ↳ pressure from stakeholders

## - metrics

fan in - # functions calling measured func. ) static analyses  
 fan out - called by overapproximates practice

length of Function - # lines

cyclomatic complexity - # independent paths through control

$$= |E_{\text{edges}}(G)| - |N_{\text{nodes}}(G)| + 2 \cdot |C_{\text{components}}(G)|$$

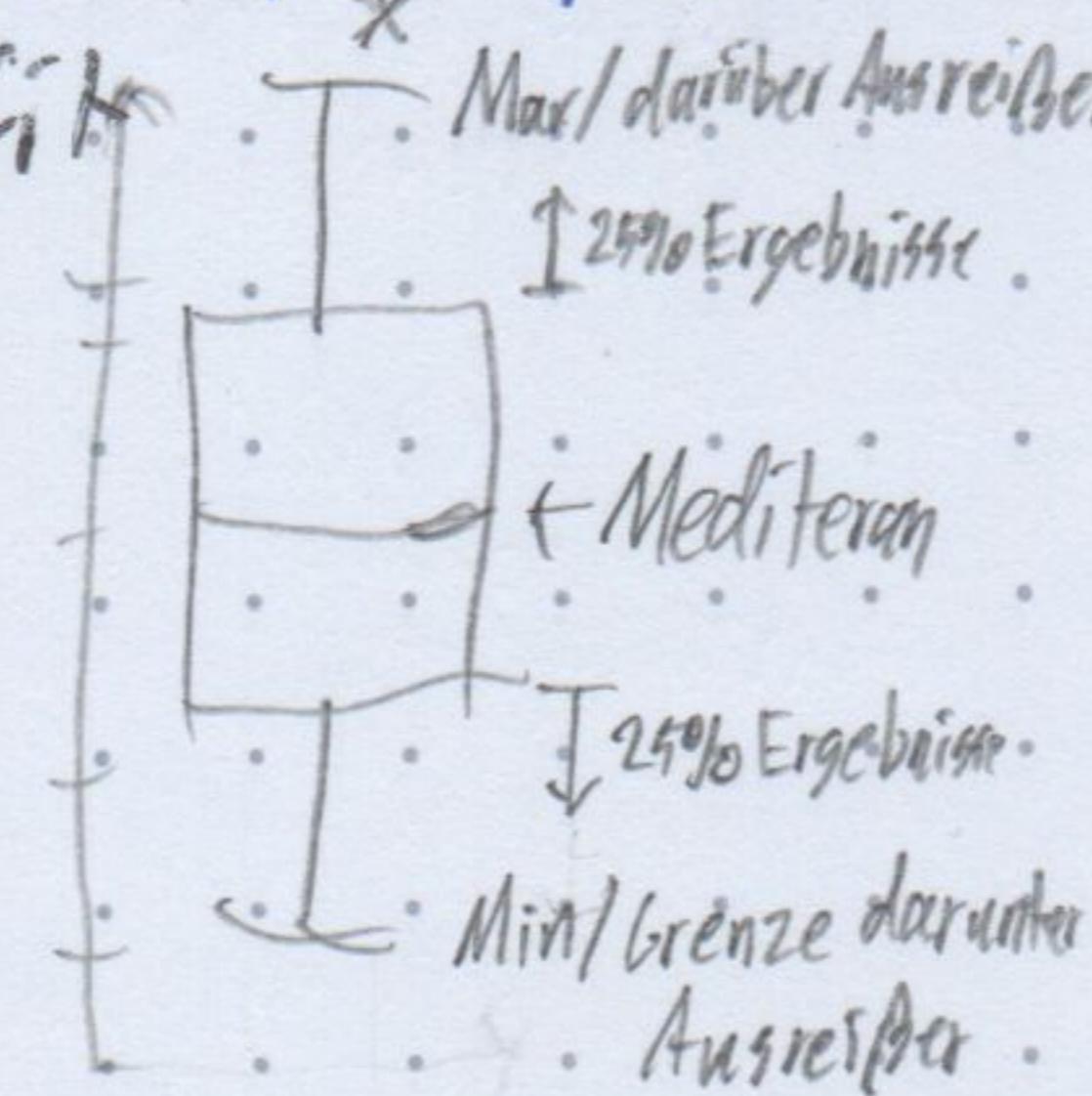
↳ diff set of edges ↳ for single method  
 ↳ connected subgraph not part of larger  
 ↳ 1 pair undirected path

Depth of conditional nesting (if, loops)

Coupling - interdependence of classes

→ detect complex components in package/project / longitudinal analysis

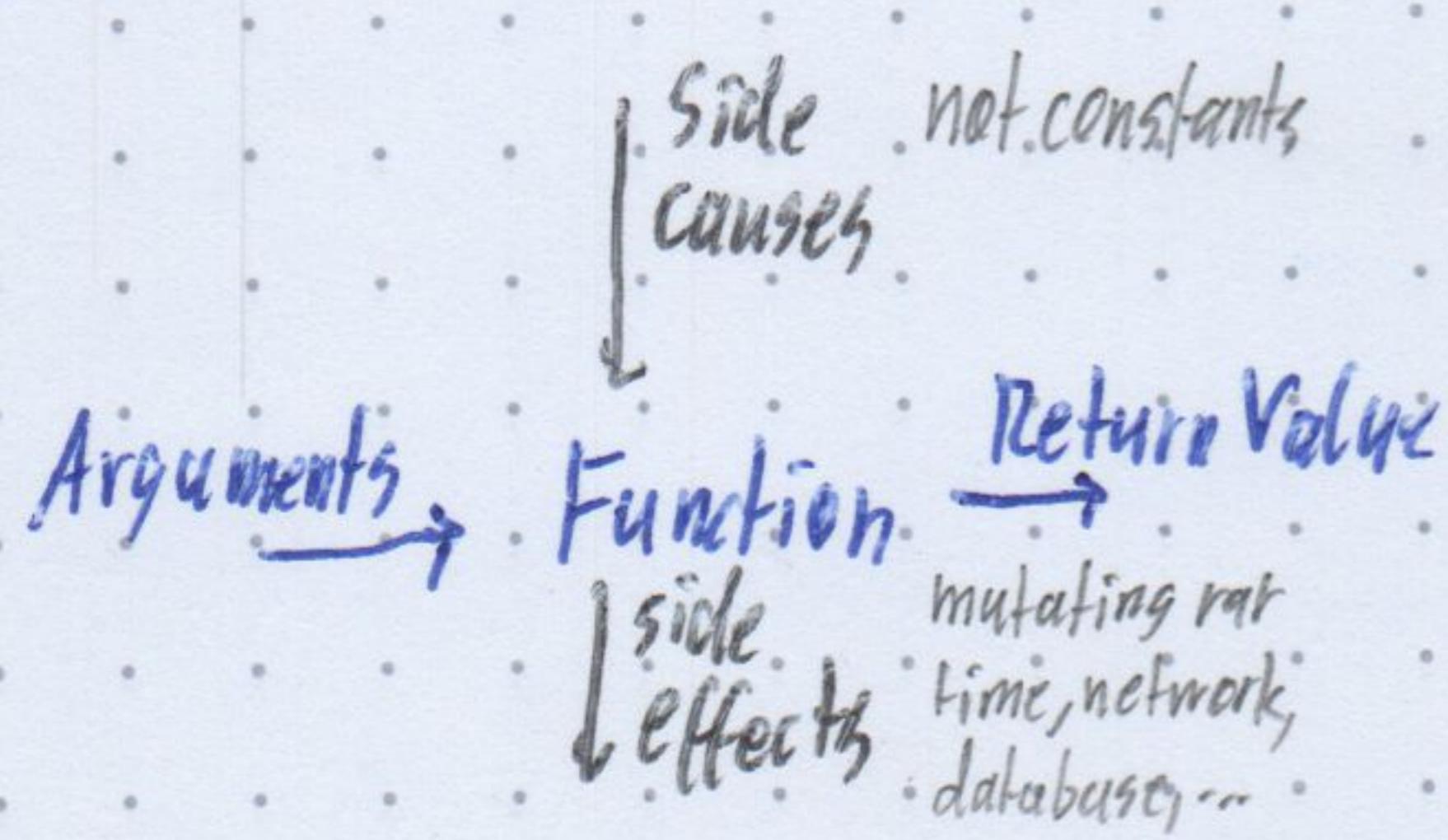
Grafik



↳ trends over time

## Separating Side-Effects from Domain Logic

↳ non-deterministic, implicit → harder to understand  
 pure - code without side-effects



functional stuff imperative

extract Pure Core

immutable Parameter immutable allows destructive updates  
 ↳ return new copy instead

## Avoid Using Ambiguous Data Types

↳ no info about meaning  
 static type system prevents errors

enum  
klassen

## LSP - Liskov Substitution Principle / strong behavioral subtyping

subtypes may replace types without breaking program

formal:  $\varphi(x) \Rightarrow \forall y : S \subset T. \varphi(y)$

$$\forall x : T. \varphi(x) \Rightarrow \forall y : S \subset T. \varphi(y)$$

↳ subtypes

parameters contravariant in subtype

↳ präziser

return types covariant

+ no new exceptions

Preconditions strengthened/weakened

Post- strengthened

Invariants

limit extend of changes, Wiederverwendbarkeit

DRY - Don't Repeat Yourself  
may forget repetition when changing

variables for common values  
expressions  $\Delta$  Seiteneffekte

Code Similarity Metrics  
↳ Token-based

new function for repetition inside functions  
↳ auch höherer Ordnung

↳ tree-based

new or super class for repetition inside classes

↳ Semantik-based  
↳ dependence graph  
↳ control  
data

SRP - Single Responsibility Principle  
↳ Doing - Calculate, Create, Controlling  
↳ Knowing - Provide access, keep references

refactor into multiple classes

High Cohesion, Low Coupling

↳ class interface A coupled to B  $\Leftarrow$  A requires B  
indirekt  
↳ has attribute

↳ hard to understand  
in isolation

metric CBO-coupling between objects  
for class  
 $CBO(C) = \frac{1}{|E|} \sum_{D \in E} |C \text{ coupled to } D|$   
↳ contains (sub-)expression  
calls methods of  
↳ has method that references  
(as param, local var, return type)  
↳ is subtype

relation between methods of a class  
low  $\Rightarrow$  little in common  $\Rightarrow$  hard to understand  
metric LCOM - Lack of Cohesion of Methods  
 $\Rightarrow$  accidental coupling

$LCOM(C) = H$  connected components of  $G(M, E)$   
 $E[0, |M|]$

$\Leftarrow \{ F_{m,n} \mid F \in M \times M \} \cap F \in F : m, n \text{ access } F, m \neq n \}$

M = methods of C  
F = instance fields of C

ISP - Interface Segregation Principle  
implement users only need what they want  $\Rightarrow$  avoids coupling  
 $\Rightarrow$  shorter impl.

Violation in Java standard library

Iterator<E>:  
boolean hasNext();  
E next();  
void remove();  $\leftarrow$  nicht für alle  
 $\Rightarrow$  UnsupportedOperationException  
 $\Rightarrow$  Iterator<E>  $\leftarrow$  RemovingIterator<E>

## Design Patterns - proven solutions

- + not reinvent wheel
- + hide complexity
- boilerplate (<sup>code</sup> not immediately for domain)
- Unjustified <sup>use don't</sup> smaller design
- Dogmatic - apart pattern

languages still often used  
indication for

missing language features

- Monad Pattern => Built-in effects
- Singleton " => Scala's objects
- Prototype " => Scala's object classes
- Visitor " => Pattern matching
- Strategy " => anonymous functions

easily misused features

- decorator pattern delegation over inheritance
- RAII pattern manage memory management

## Object-Oriented Design Patterns by a book 1994

Creational - How objects are created, Structural - class composition, Behavioral - class interaction responsibility distribution

### Abstract Factory + portability through different factories

Participants

Abstract Factory - Interface

Concrete Factories

Abstract Product

Concrete Product

Client - calls concrete factories through interface

+ abstract concrete products

as product families

consistent family changing easy through diff. factory

- hard to add unforeseen products

change all factories

- non-standard Learning required

### Structural - class decomposition

#### Decorator - extend fun

structure

Component - interface

Decorators - extend referenced component

Basic Components - core functionality

+ extend class functionality without inheritance z.B. avoids multiple inheritance

? + dynamic ↔ static at runtime

- hard to make order independent (decorator stack)

- boilerplate for not extended methods

#### Iterator

trait Iterator[A]:

def next: Option[A]

+ hides complexity of data structure

? less error prone, efficient

multiple revisions tree

? depth first breadth first

- imperative → hard to parallelize

? Folds are functional version of it

~~Observer~~

Structure

Subject

attach

detach

notifyObservers()

→ Observer - interface

update(...)

? z.B. Subject, Delta

+ abstracts coupling

+ allows broadcasts

- update cascades

- no differentiating update types

Concrete Subject (→) Concrete Observer

only place holders (getstate(): T, modifyState(T))

update(...)

# many instances

## Functional Design Patterns inspired from abstract algebra, category theory

### Monoids ( $A, \text{combine}, \text{empty}$ )

$\text{combine}: A \times A \rightarrow A$  - assoziativ

$\text{empty}: A$  - left & right identity

implemented as scala type class

+ abstract accumulation

scala stuff

type class - instance inferred  
given object by compiler

type constructor - func: Type  $\rightarrow$  Type  
 $F[-]$

### Foldable

- types defining Foldl function

- accumulate elements of data structure with Monoid

$\text{fold}: \text{structure of } As \times \text{Monoid of } A \rightarrow A$

$\text{foldMap}: \text{structure of } As \times \text{Monoid of } A \times \text{Monoid of } Bs \times f: A \rightarrow B$

+ abstracts accumulation

hiding structure implementation

- can't profitate

z.B. search in sorted structure

### Categorys ( $C, \text{Obj}, \text{id}, \circ$ )

$\circ: ((Y, Z) \times ((X, Y) \rightarrow ((X, Z)))$  assoziativ

$\text{id}: ((X, X))$  left & right identity

Menge Objekte  $X, Y, Z \in \text{Obj}$

typischerweise Typen  $\in \text{Obj}$   $\Rightarrow C(X, Y) = \text{funktion}(X \rightarrow Y)$  Category of types and functions

+ generalizes Monoid

gibt nicht zwischen allen Elementen Pfeile

### set of Arrows ( $C(X, Y)$ )

$\Rightarrow$  nicht zwischen allen Paaren existiert Pfeil

### Functors $F: C \rightarrow D$

categorys

$F_{\text{obj}}: \text{Obj}_C \rightarrow \text{Obj}_D$  preserves identity

$F_{\text{fun}}: ((X, Y) \rightarrow D(F_{\text{obj}}(X), F_{\text{obj}}(Y)))$  preserves composition

### Monads ( $F, \text{pure}, \text{join}$ )

combined arrow to normal arrows

$\circ: ((F(F(A)), F(A))$

$((A, F(A))$

Functor  $F: C \rightarrow C$

+ abstracts side effects

Associativity:  $\text{join} \circ F(\text{join}) = \text{join} \circ \text{join}$

Left identity:  $\text{join} \circ F(\text{pure}) = \text{id}$

Right identity:  $\text{join} \circ \text{pure} = \text{id}$

2 1 0 2 2 2

### Traversables

+ generalizes Folds  
collecting in Monad

Software Architecture - high level design, organization

## Dimensions

## Architecture Characteristics

Operational about execution.

Availability incl. failure recovery

Performance

latency; throughput; resources

Scalability

threads; servers; database

Structural about code

Extensible

new functionality

Maintainability

adapting, enhancing

Reuseability

requires low coupling

Configurability

for user

Cross-cutting - affect all parts

Localization

diff languages, units

requires good abstraction

Accessibility

users with disability?

Privacy

Security

## Architecture Styles - components

organisation, dependencies  
communication between

Software often uses multiple

### Layered

open ↔ closed

requests must pass layers

Layer bypassing

+ separation of concerns

+ easy

- sinkhole anti-pattern (overhead/crust for request through layers with little processing)

- vertical ⇒ hard to scale

### Service Oriented

independent services on bus

shared ↔ own database

I don't need to know each other

independence

! consistency

+ encapsulating (follows third party service)

+ scale by new instances of service

- hard to debug

- network overhead

- large scale - unclear dependencies

### Pipes and Filters

pipes connecting

Filters - transforms datatype

independent

stateless

branching pipes allowed

stream/chunks of data

+ Filters concurrent (z.B. parallel on diff machines)

+ separation of concerns

+ may small data chunks

- pipes overhead (buffer, serialization)

- some Filter need all data ⇒ not only chunks

- error handling (keep original data until success)

### Broker, Microservices

Development process:

requirement analyses

→ Choosing Architecture + structure into components → Development Team

designing class structure...

Influences:

Demands

Requirements

Architecture characteristics

Organizational factors

Development process

Hard to change,

enforce retroactively

but often delayed (feur of wrong)

⇒ experts/prototype

Hard to enforce

⇒ clear communication

### Document decision

z.B. one file in repository + sync with code

structured text, diagrams

Recent changes

open source ⇒ cheap

standards ⇒ easier snapping Komponenten

Container (lightweight virtualization)

⇒ easily added/removed ⇒ microservices architecture

Performance Engineering  
ressources      useful work  
response time

! premature optimization  $\Rightarrow$  complexity  
only critical

## Application $\leftrightarrow$ System

### Metrics

Running Time

- **variating**  $\Rightarrow$  repeat

⚠ dead code elimination

Wall time

system load  
disk usage  
thread sync

User CPU time - excl kernel  
 $\Sigma$  threads

JIT-Just In Time optimization  
Garbage collection  $\Rightarrow$  warm up Phase  
to allow deallocation

System CPU time - excl user

### Benchmark

JMH - Java Microbenchmark Harness

@Param(Array("100", "1000"))

var size: Int =

var array: Array[Long] =

@Setup

def method

@Benchmark

def method

CPU Usage

programm used cycles  
max. cycles

Profiler z.B. visualvm

Memory Usage

in Bytes over time

garbage collection  $\Rightarrow$  spikes

memory  $\Rightarrow$  costly allocation

identify big objects

KB =  $10^3$  B      KB =  $2^{10}$  B  
MB =  $10^6$  B      MB =  $2^{20}$  B  
GB =  $10^9$  B      GB =  $2^{30}$  B  
TB =  $10^{12}$  B      TB =  $2^{40}$  B  
PB =  $10^{15}$  B      PB =  $2^{50}$  B

Throughput  
operations / time

Peak - max measured

Bandwidth - theoretical max

FLOPS - # Floating-point ops  
IOPS - disk I/O ops

# Bytes send/received / s

# Requests handled / s

JIT - Just In Time Optimizations

optimize Null check elimination

if getting invalid

$\Rightarrow$  unpredictable

Tool:

jitracer  
Shows when  
method optimized

Branch reorder

Methods inlined

Loop unrolling

invariant renazierung

Theoretical - scaling for  $n$

Time Complexity

Worst Case - Big O

Average Case - Theta O

e.g. Quicksort  $O(\log n)$

$O(n^2)$