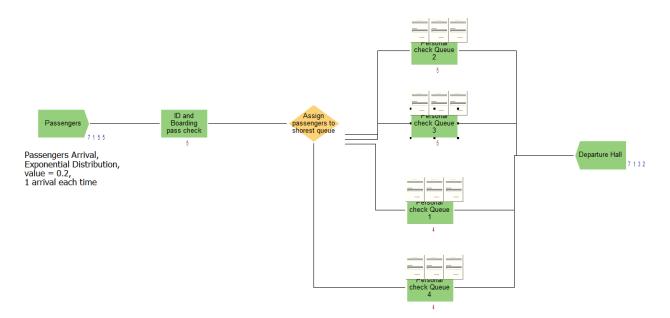
HW week 6

2022-06-25

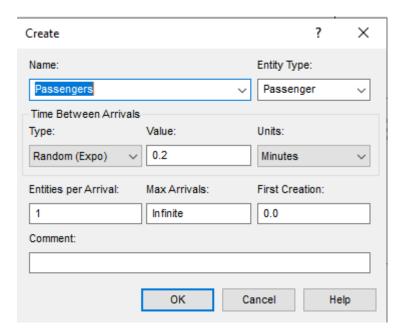
Question 13.2 Answers:

The following screenshot shows the flowchart we set up in Arena. The settings of some key blocks are also displayed in separate screenshots:

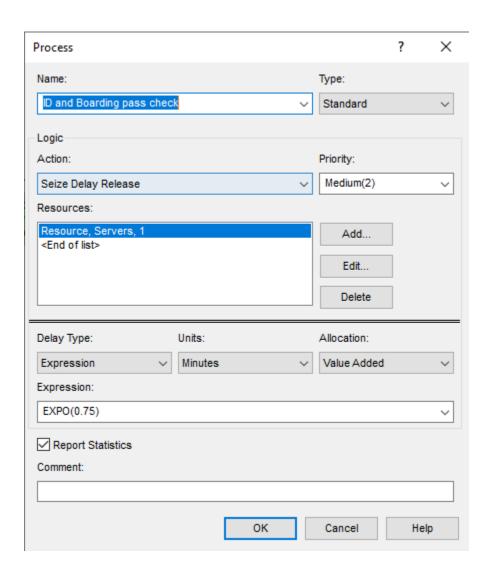
The flow chart:



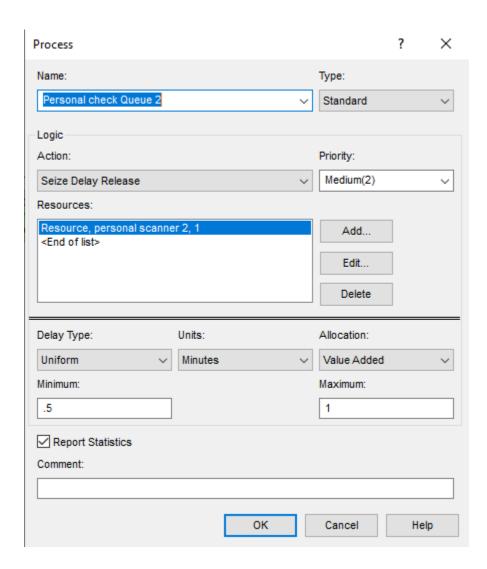
Settings of "passenger" block:



Settings of "ID and Boarding Pass Check" block:



Settings of "Personal Check Queue" block (using one out of four as example):



To change the number of personal check queues. We need to add more branches to the flowchart and change the conditions in the n-way decision activity (Assign passengers to shorest queue), so that we make sure the passengers always go to the shortest queue.

To change the number of servers at "ID and boarding pass check", we simply need to change the capacity of "Servers" in the resources table:

	Name	Туре	Capacity	Busy / Hour	ldle / Hour	Per Use	StateSet Name	Failures	Report Statistics	Comment
1 🕨	Servers	Fixed Capacity	4 🗸	0.0	0.0	0.0		0 rows	\checkmark	
2	personal scanner 1	Fixed Capacity	1	0.0	0.0	0.0		0 rows		
3	personal scanner 2	Fixed Capacity	1	0.0	0.0	0.0		0 rows	\checkmark	
4	personal scanner 3	Fixed Capacity	1	0.0	0.0	0.0		0 rows		
5	personal scanner 4	Fixed Capacity	1	0.0	0.0	0.0		0 rows	\checkmark	

After trying different numbers of servers and personal check queues, we finally decide to keep 4 servers and 4 personal check queues in the flowchart, because this setting:

- 1. Avoids the error of exceeding 150 maximum passengers waiting in queues
- 2. Keeps the average waiting time below 15 minutes

Note: In this simulation, we let the software to run 10 replications. Each replication will last 24 hours to make sure the results are not biased. Here's one of the 10 replication that has the longest average waiting time:

ARENA Simulation Results suiwenyu@hotmail.com - License: STUDENT

Summary for Replication 5 of 10

Project: Unnamed Project
Analyst: suiwenyu@hotmail.com
Run execution date: 6/27/2022
Model revision date: 6/27/2022

Replication ended at time : 1440.0 Minutes

Base Time Units: Minutes

TALLY VARIABLES

Identifier	Average	Half Width	Minimum	Maximum	Observations
Passenger.VATime	1.4965	.02274	.51274	7.1201	7227
Passenger.NVATime	.00000	.00000	.00000	.00000	7227
Passenger.WaitTime	4.9610	(Corr)	.00000	18.675	7227
Passenger.TranTime	.00000	.00000	.00000	.00000	7227
Passenger.OtherTime	.00000	.00000	.00000	.00000	7227
Passenger.TotalTime	6.4575	(Corr)	.69317	22.129	7227
Personal check Queue 2.Queue.WaitingTime	2.4410	(Corr)	.00000	9.8191	1913
Personal check Queue 1.Queue.WaitingTime	2.2077	(Corr)	.00000	10.288	1806
Personal check Queue 3.Queue.WaitingTime	2.2850	(Corr)	.00000	9.7478	1894
Personal check Queue 4.Queue.WaitingTime	2.2536	(Corr)	.00000	9.4243	1618
ID and Boarding pass check.Queue.WaitingTi	2.6553	(Corr)	.00000	14.969	7246

Question 14.1.1 Question 14.1.1 Answer:

In this part, we will use mean/mode to impute missing values. First read the data. From the summary info we can see that only column V7 has 16 missing values. (about 2.29% of total number of rows)

```
##
          ۷1
                               ٧2
                                                 VЗ
                                                                   ۷4
##
                                : 1.000
                61634
                                                  : 1.000
                                                                    : 1.000
    Min.
                        Min.
                                          Min.
                                                             Min.
    1st Qu.: 870688
                        1st Qu.: 2.000
                                           1st Qu.: 1.000
                                                             1st Qu.: 1.000
                                          Median : 1.000
    Median : 1171710
                        Median : 4.000
                                                             Median : 1.000
##
##
    Mean
            : 1071704
                        Mean
                                : 4.418
                                          Mean
                                                  : 3.134
                                                             Mean
                                                                     : 3.207
##
    3rd Qu.: 1238298
                        3rd Qu.: 6.000
                                           3rd Qu.: 5.000
                                                             3rd Qu.: 5.000
##
           :13454352
                                :10.000
                                                  :10.000
                                                                     :10.000
    {\tt Max.}
                        Max.
                                          Max.
                                                             Max.
##
```

```
##
           ۷5
                             ۷6
                                                ۷7
                                                                  V8
            : 1.000
                              : 1.000
                                                 : 1.000
                                                                   : 1.000
##
    Min.
                                         Min.
                      Min.
                                                            Min.
                       1st Qu.: 2.000
##
    1st Qu.: 1.000
                                         1st Qu.: 1.000
                                                            1st Qu.: 2.000
##
    Median : 1.000
                      Median : 2.000
                                         Median : 1.000
                                                            Median : 3.000
##
    Mean
            : 2.807
                      Mean
                              : 3.216
                                         Mean
                                                 : 3.545
                                                            Mean
                                                                   : 3.438
    3rd Qu.: 4.000
                       3rd Qu.: 4.000
##
                                         3rd Qu.: 6.000
                                                            3rd Qu.: 5.000
            :10.000
                              :10.000
##
    Max.
                      Max.
                                         Max.
                                                 :10.000
                                                            Max.
                                                                   :10.000
                                         NA's
##
                                                 :16
##
          ۷9
                            V10
                                              V11
            : 1.000
##
    Min.
                       Min.
                              : 1.000
                                         Min.
                                                 :2.00
    1st Qu.: 1.000
                       1st Qu.: 1.000
                                         1st Qu.:2.00
    Median : 1.000
                       Median : 1.000
                                         Median:2.00
##
##
    Mean
           : 2.867
                              : 1.589
                                         Mean
                                                 :2.69
                      Mean
##
    3rd Qu.: 4.000
                       3rd Qu.: 1.000
                                         3rd Qu.:4.00
##
            :10.000
                              :10.000
                                                 :4.00
    Max.
                      Max.
                                         Max.
##
    #Display all rows with missing values
    missing_rows <- is.na(data$V7)</pre>
    data[missing_rows,]
```

```
##
             V1 V2 V3 V4 V5 V6 V7 V8 V9
                                            V10
                                                V11
## 24
       1057013
                     4
                         5
                            1
                               2 NA
                                      7
                                          3
                                              1
                                                   2
        1096800
                  6
                     6
                         6
                            9
                               6 NA
                                      7
                                              1
                                                   2
## 140 1183246
                     1
                         1
                            1
                               1 NA
                                      2
                                          1
                                              1
                  1
## 146 1184840
                     1
                         3
                            1
                               2 NA
                                                   2
                  1
## 159 1193683
                  1
                     1
                         2
                            1
                               3 NA
                                      1
                                          1
                                              1
                                                   2
  165 1197510
                  5
                     1
                         1
                            1
                               2 NA
                                      3
                                                   2
## 236 1241232
                  3
                         4
                            1
                               2 NA
                                      3
                                                   2
                     1
                                          1
                                              1
## 250
         169356
                  3
                     1
                            1
                               2 NA
                                      3
                                                   2
                         1
                               2 NA
                                      2
                                                   2
## 276
        432809
                  3
                     1
                         3
                            1
                                          1
                                              1
## 293
        563649
                     8
                        8
                            1
                               2 NA
                                                   4
                  8
                                      6 10
                                              1
## 295
         606140
                  1
                     1
                        1
                            1
                               2 NA
                                      2
                                          1
                                              1
                                                   2
## 298
          61634
                  5
                     4
                        3
                            1
                               2 NA
                                      2
                                         3
                                              1
                                                   2
                                                   2
                        5
                               7 NA
                                          9
## 316
        704168
                  4
                     6
                            6
                                      4
                                              1
## 322
        733639
                  3
                     1
                         1
                            1
                               2 NA
                                      3
                                              1
                                                   2
                                      2
                                                   2
## 412 1238464
                  1
                     1
                         1
                            1
                               1 NA
                                              1
## 618 1057067
                 1
                     1
                        1
                            1
                               1 NA
                                      1
                                                   2
```

Then we are going to impute the missing values with mean and mode. We are going to use mfv() function in "modeest" package to find the mode. Here's the approach:

```
library(modeest)
```

```
# Copy the data
data_impute_mean <- data
#impute missing values with mean
data_impute_mean$V7[missing_rows] <- mean(data$V7, na.rm = TRUE)

#Display all rows with missing values in original data
#(filled with mean value)
data_impute_mean[missing_rows,]</pre>
```

```
##
             V1 V2 V3 V4 V5 V6
                                         V7 V8 V9 V10 V11
## 24
       1057013
                  8
                     4
                        5
                                2 3.544656
                                             7
                                                 3
                                                          4
                            1
                                                     1
                                                          2
        1096800
                     6
                         6
                            9
                                6 3.544656
                                                          2
  140 1183246
                         1
                                1 3.544656
                  1
                     1
                            1
                                                 1
                                                     1
   146 1184840
                  1
                     1
                         3
                            1
                                2 3.544656
                                             2
                                                 1
                                                          2
                         2
                                3 3.544656
                                                          2
##
  159 1193683
                  1
                     1
                            1
                                             1
                                                 1
                                                     1
                                2 3.544656
                                                          2
  165 1197510
                  5
                     1
                         1
                            1
                                             3
                                                 1
                                2 3.544656
                                                          2
## 236 1241232
                  3
                     1
                         4
                            1
                                             3
                                                 1
                                                     1
##
  250
         169356
                  3
                     1
                         1
                            1
                                2 3.544656
                                             3
                                                 1
                                                     1
                                                          2
                                                          2
## 276
         432809
                  3
                     1
                         3
                            1
                                2 3.544656
                                             2
                                                 1
                                                     1
  293
         563649
                  8
                     8
                         8
                            1
                                2 3.544656
                                             6 10
                                                     1
                                                          4
                                                          2
  295
         606140
                                2 3.544656
                                             2
##
                  1
                     1
                         1
                            1
                                                 1
                                                     1
                         3
                                                          2
##
   298
          61634
                  5
                     4
                            1
                                2 3.544656
                                             2
                                                 3
                                                     1
                                                          2
         704168
                         5
                            6
                                                 9
##
  316
                  4
                     6
                                7 3.544656
                                             4
                                                     1
## 322
         733639
                  3
                            1
                                2 3.544656
                                             3
                                                 1
                                                          2
                     1
                         1
                                                     1
                                                          2
## 412 1238464
                  1
                     1
                         1
                            1
                                1 3.544656
                                             2
                                                 1
                                                     1
## 618 1057067
                                1 3.544656
                                                          2
                  1
                     1
                         1
                            1
```

```
# Copy the data
data_impute_mode <- data
#impute missing values with mode
mode <- mfv(data$V7)
data_impute_mode$V7[missing_rows] <- mode

#Display all rows with missing values in original data
#(filled with mode value)
data_impute_mode[missing_rows,]</pre>
```

```
##
              V1 V2 V3 V4 V5 V6 V7 V8 V9 V10
                                                   V11
## 24
        1057013
                      4
                          5
                                                      2
                          6
                             9
                                 6
                                        7
                                            8
## 41
        1096800
                   6
                      6
                                     1
                                                 1
## 140 1183246
                                        2
                                                      2
                   1
                      1
                          1
                             1
                                 1
                                     1
                                                 1
## 146 1184840
                   1
                      1
                          3
                             1
                                 2
                                     1
                                                 1
                                                      2
## 159 1193683
                      1
                          2
                             1
                                 3
                                     1
                                        1
                                            1
                                                 1
                                                      2
                   1
                                                      2
                                 2
                                        3
## 165 1197510
                   5
                      1
                          1
                              1
                                     1
                                            1
                                                 1
## 236 1241232
                   3
                      1
                          4
                             1
                                 2
                                     1
                                        3
                                            1
                                                 1
                                                      2
## 250
                                 2
                                        3
                                                      2
         169356
                   3
                      1
                          1
                              1
                                     1
                                            1
                                                 1
## 276
         432809
                   3
                      1
                          3
                             1
                                 2
                                     1
                                        2
                                            1
                                                 1
                                                      2
## 293
         563649
                   8
                      8
                          8
                             1
                                 2
                                     1
                                        6
                                           10
                                                 1
                                                      4
##
   295
         606140
                      1
                             1
                                 2
                                        2
                                            1
                                                      2
                   1
                          1
                                     1
                                                 1
                                                      2
##
   298
          61634
                   5
                      4
                          3
                             1
                                 2
                          5
                             6
                                 7
                                                      2
##
   316
         704168
                      6
                                     1
                                        4
                                                 1
                   4
   322
         733639
                   3
                      1
                          1
                             1
                                 2
                                        3
                                                      2
## 412 1238464
                   1
                      1
                          1
                             1
                                 1
                                     1
                                        2
                                            1
                                                 1
                                                      2
## 618 1057067
                      1
                                                      2
```

Question 14.1.2 Answer:

In this part, we are going to impute the missing values with regressions.

One simple way is to use mice() function in "mice" packages, which contains built-in imputation functionalities. Hereare the documentations of this function and some tutorials that i have referred to:

```
https://www.rdocumentation.org/packages/mice/versions/3.14.0/topics/mice \\ https://www.analyticsvidhya.com/blog/2016/03/tutorial-powerful-packages-imputing-missing-values/https://rpubs.com/McCloud77/300268
```

To run an imputation with linear regression, we simply need to set the "method" parameter in mice() function to be "norm.predict". Here's the approach:

```
library(mice)
##
## Attaching package: 'mice'
## The following object is masked from 'package:stats':
##
##
       filter
## The following objects are masked from 'package:base':
##
##
       cbind, rbind
    impute_reg <- mice(data, method = "norm.predict")</pre>
##
##
    iter imp variable
            ۷7
         1
##
     1
         2
            ۷7
##
     1
         3
            ۷7
##
     1
            ٧7
##
     1
         4
         5
            ۷7
##
     1
##
     2
         1
            ۷7
         2
##
     2
            ۷7
##
     2
         3
            ۷7
##
     2
         4
            ۷7
##
     2
         5 V7
##
     3
         1 V7
##
     3
         2
            ۷7
##
     3
         3
            ۷7
         4
            ۷7
##
     3
##
     3
         5
            ۷7
         1
            ۷7
##
     4
##
     4
         2
            ۷7
##
     4
         3
            ۷7
         4
            ۷7
##
     4
         5
##
     4
            ۷7
##
     5
         1
            ۷7
     5
         2 V7
##
##
     5
         3 V7
##
     5
         4
            ۷7
##
     5
         5 V7
```

```
data_impute_reg <- complete(impute_reg)

#Display all rows with missing values in original data
#(filled with predictions from linear regression)
data_impute_reg[missing_rows,]</pre>
```

```
##
           V1 V2 V3 V4 V5 V6
                                 V7 V8 V9 V10 V11
## 24
      1057013 8 4 5
                      1
                         2 7.191237
                                     7
                                        3
                                           1
                                               4
## 41 1096800
                 6
                    6
                       9
                          6 3.419208
                                               2
              6
                                     7
                                           1
                                               2
## 140 1183246 1
                         1 1.188951
                 1
                    1
                       1
                                           1
                                       1
## 146 1184840 1
                    3
                       1
                         2 1.579936
                                               2
                 1
## 159 1193683 1
                    2
                         3 1.260453
                                               2
                 1
                      1
                                    1
                                       1
                                           1
## 165 1197510 5 1
                    1
                       1
                         2 1.428797
                                     3 1
                                           1
                                               2
## 236 1241232 3
                    4
                       1
                         2 1.943842
                                     3 1
                                               2
                 1
                                           1
                    1
                                               2
## 250
      169356 3 1
                       1 2 1.562574
                                     3 1
                                           1
                                               2
## 276
      432809 3 1
                    3 1 2 1.740990
                                    2 1
                                           1
                                    6 10
## 293
       563649 8 8 8 1 2 6.432884
                                               4
                                           1
## 295
       606140 1
                 1
                    1
                       1
                         2 1.303253
                                               2
## 298
       61634 5
                 4
                    3
                      1
                         2 1.186205
                                    2 3
                                           1
                                               2
                    5
                       6
                         7 2.083334
                                               2
## 316
       704168 4
                 6
                                    4 9
                                           1
## 322 733639 3
                       1 2 1.469119
                                    3 1
                                               2
                 1
                    1
                                           1
                                               2
## 412 1238464 1
                 1
                    1
                       1
                         1 1.179806
                                     2
                                       1
                                           1
## 618 1057067 1 1 1 1 1 1.059370 1 1
                                               2
```

Question 14.1.3

Answer:

To run an imputation using linear regression with perturbations, we simply need to set the "method" parameter in mice() function to be "norm.nob". Here's the approach:

```
set.seed(100)
impute_reg_per <- mice(data, method = "norm.nob")</pre>
```

```
##
##
    iter imp variable
##
         1
            ۷7
         2 V7
##
     1
##
     1
         3 V7
##
     1
         4 V7
##
         5
            ۷7
     1
##
     2
         1 V7
##
     2
         2 V7
     2
         3 V7
##
##
     2
         4
            ۷7
##
     2
         5 V7
         1 V7
##
     3
         2 V7
##
     3
##
     3
         3 V7
     3
##
         4 V7
```

```
##
      3
          5
              ۷7
##
      4
          1
              V7
##
          2
              ۷7
              ۷7
##
      4
          3
##
          4
              ۷7
      4
          5
              ۷7
##
      5
          1
              ۷7
##
      5
          2
              ۷7
##
##
      5
          3
              ۷7
##
      5
          4
             ۷7
##
      5
              ۷7
```

```
data_impute_reg_per <- complete(impute_reg_per)

#Display all rows with missing values in original data
#(filled with predictions from linear regression with perturbations)
data_impute_reg_per[missing_rows,]</pre>
```

```
##
            V1 V2 V3 V4 V5 V6
                                        V7 V8 V9 V10 V11
                       5
                                 6.2341409
## 24
       1057013
               8
                    4
                          1
                              2
                                             7
                       6
                          9
                              6
                                 2.0999387
                                                         2
## 41
       1096800
                    6
                                                    1
## 140 1183246
                    1
                       1
                          1
                              1
                                 2.5470044
                                             2
                                                    1
                                                        2
                1
                              2
                                                        2
## 146 1184840
                       3
                                             2
                1
                    1
                          1
                                 1.3691798
                                                    1
                       2
                              3
                                                         2
## 159 1193683
               1
                    1
                          1
                                 0.3528212
                                             1
                                                    1
## 165 1197510
                                                         2
                    1
                       1
                              2
                                                    1
                5
                          1
                                 4.1122555
                                             3
                                                        2
## 236 1241232
                3
                    1
                       4
                          1
                              2
                                 3.9161831
                                             3
                                                    1
##
  250
        169356
                3
                    1
                       1
                          1
                              2 -0.8288733
                                             3
                                                        2
## 276
        432809
                3
                       3
                          1
                              2
                                 0.5910234
                                             2
                                                         2
                    1
                                                    1
                              2
## 293
        563649
                    8
                       8
                          1
                                 8.3972921
                                                         4
## 295
                             2 -2.0122315
                                             2
                                                        2
        606140
                          1
                1
                    1
                       1
                                                    1
## 298
         61634
                5
                    4
                       3
                          1
                              2 -1.0535735
                                                    1
                                                        2
                             7 -0.2588221
## 316
        704168
                4
                    6
                       5
                          6
                                                    1
                                                        2
  322
        733639
                    1
                       1
                          1
                              2 -0.8094779
                                                        2
## 412 1238464
                                                        2
                              1 -1.3904081
                                             2
                    1
                       1
                          1
                                                    1
                1
## 618 1057067
                       1
                          1
                             1
                                0.7757454
```

Question 15.1 Answer:

A plant that produces multiple types of products can use optimization to determine the quantity of each type of products to be produced each year. The best production plan should maximize the gross margin ratio of the plant. Here are some data that may be needed:

- 1. Sales price and production cost for each type of product
- 2. The quantity of raw materials and labor that each type of product will consume in production (may be needed for setting constraints)
- 3. Maximum quantity of each product that the plant is able to produce each year