

Problem Understanding

You're given an array A.

In **one step**, you can:

- Select the **largest element** in the array
- Replace it with the **second largest** element.

Goal:

Make **all elements equal** with the **minimum number of steps**.

Key Insight (Observation):

All elements will eventually become equal to the **smallest element** of the array.

Why?

Because you can **only reduce** values to a lower value (no increasing), and the only way elements get updated is to copy smaller values.

Optimized Approach using map ($O(N \log N)$)

Idea:

- Use a `map<int, int>` as it is sorted no unordered to store **frequency of each number**.
- Since `map` is sorted in C++, we can always access the **largest and second largest** easily.
- In one operation:
 - Replace all elements with the **largest key** by the **second largest key**.
 - Decrease count of largest, add to second largest.
 - Repeat until only one key (value) remains in the map.

C++ code:

```
#include <iostream>
```

```
#include <map>
```

```
#include <vector>
```

```
using namespace std;
```

```
int minStepsToMakeAllEqual(vector<int>& A) {
```

```
    map<int, int> freq;
```

```

for (int val : A) {
    freq[val]++;
}

int steps = 0;

while (freq.size() > 1) {
    auto it_largest = prev(freq.end());    // Largest element
    auto it_second = prev(freq.end(), 2);  // Second largest

    int largest = it_largest->first;
    int count = it_largest->second;
    int second = it_second->first; // second largest

    freq[second] += count; // Convert all 'largest' to 'second'
    freq.erase(largest);   // Remove largest
    steps += count;        // Each conversion is a step
}

return steps;
}

int main(){
    vector<int> a={5,5,4,4,2};
    cout<<minStepsToMakeAllEqual(a);
}

```

☒ Summary:

Function	Use
prev(it)	Go one step back from it
prev(it, n)	Go n steps back from it
In map/set	Often used to get largest / second largest

Syntax	Meaning	When to Use
.	Access member of an object	When you have the object
->	Access member through pointer or iterator	When you have a pointer/iterator

In C++, `std::prev` is a utility function from the `<iterator>` header. It is used to get an iterator pointing to the previous element from a given iterator.

Max Distance Between Two Occurrences

C++CODE:

```
int maxDistance(vector<int> &arr) {
    int ans = 0; // To store the final answer (maximum distance found)
    unordered_map<int, int> mp; // To store the first occurrence index of each element

    for (int i = 0; i < arr.size(); i++) {
        if (mp.find(arr[i]) == mp.end()) {
            // If the element is seen for the first time, store its index
            mp[arr[i]] = i;
        } else {
            // If the element was seen before, calculate the distance
            // and update the maximum distance if it's larger
            ans = max(ans, i - mp[arr[i]]);
        }
    }

    return ans; // Return the maximum distance between two equal elements
}
```

 **Summary Notes:**

- The map stores the first index where each element appears.
- On every repeated occurrence, we compute the distance to the first, and keep the maximum.
- This is a classic hash map-based linear solution for finding max distance between equal elements.

Time Complexity: $O(N)$

Space Complexity: $O(N)$

✅ Java Code with Comments:

```
public int maxDistance(int[] arr) {

    int ans = 0; // Variable to store the maximum distance found so far


    // HashMap to store the first occurrence index of each element
    HashMap<Integer, Integer> mp = new HashMap<>();


    // Iterate through the array
    for (int i = 0; i < arr.length; i++) {

        // If the element is seen for the first time, store its index
        if (!mp.containsKey(arr[i])) {

            mp.put(arr[i], i);

        } else {

            // If the element is already seen, calculate the distance between
            // current index and the first occurrence, and update the max distance
            ans = Math.max(ans, i - mp.get(arr[i]));

        }

    }


    // Return the maximum distance found

    return ans;

}
```

First Unique Character in a String

C++ Code with Comments:

```
int firstUniqChar(string s) {  
    int n = s.length(); // Get the length of the string  
    unordered_map<char, int> mp; // Hash map to store character frequencies  
  
    // Step 1: Count frequency of each character in the string  
    for (int i = 0; i < n; i++) {  
        mp[s[i]]++; // Increment frequency count for character s[i]  
    }  
  
    // Step 2: Find the first character with frequency == 1  
    for (int i = 0; i < n; i++) {  
        if (mp[s[i]] == 1) { // If character occurs only once  
            return i;      // Return its index  
        }  
    }  
  
    // If no unique character is found, return -1  
    return -1;  
}
```

Why this works efficiently:

- The first loop counts character frequencies → $O(N)$
 - The second loop finds the first unique character → $O(N)$
 - `unordered_map<char, int>` gives $O(1)$ average access time for both insert and lookup.
-

Time and Space Complexity:

Operation	Complexity
-----------	------------

Time	$O(N)$
------	--------

Space (unordered_map) $O(1)^*$

*Because there are only 26 lowercase letters (as per typical constraints), space is constant.

Notes:

- Use unordered_map for fast insert and lookup.
- This approach preserves the original order of the string while checking frequency.
- Returns the first unique character's index, not the character itself.

[1002. Find Common Characters](#)

Problem Statement:

Given an array of strings words, return all characters that appear in every string, including duplicates.

- The result can be in any order.
 - Characters are all lowercase English letters.
-

Key Observations:

- We need to return only characters that are common across all strings.
 - If a character appears k times in each word, it should appear k times in the result.
 - Duplicates matter! For example, "l" appears twice in "bella" and "label" → include both.
-

Optimal Approach (Using Arrays):

Since we only deal with lowercase letters 'a' to 'z', we can use fixed-size arrays (size 26) to store frequencies efficiently.

Steps:

1. Initialize a `minFreq[26]` array with `INT_MAX`.
This will store the minimum frequency of each character across all words.
2. For each word in words:
 - Create a local `freq[26]` array to count character frequencies in that word.
 - Update `minFreq[i] = min(minFreq[i], freq[i])` for all 26 characters.
3. After processing all words:
 - Loop over `minFreq`. For each character with non-zero frequency:
 - Add that character `minFreq[i]` times to the result.

Using Unordered map:

```
vector<string> commonChars(vector<string>& words) {  
    unordered_map<char, int> mp;    // Store min frequency of each char  
    vector<string> ans;  
  
    // Step 1: Count frequency of characters in the first word  
    for (char ch : words[0]) {  
        mp[ch]++;  
    }  
  
    // Step 2: Intersect with each subsequent word  
    for (int i = 1; i < words.size(); i++) {  
        unordered_map<char, int> currmp;  
        for (char ch : words[i]) {  
            currmp[ch]++;  
        }  
  
        // Update global map with minimum frequency  
        for (auto& it : mp) {  
            it.second = min(it.second, currmp[it.first]);  
        }  
    }  
}
```

```
}
```

```
// Step 3: Add each character to result according to its min frequency
```

```
for (auto it : mp) {
```

```
    for (int i = 0; i < it.second; i++) {
```

```
        ans.push_back(string(1, it.first)); // Convert char to string
```

```
    }
```

```
}
```

```
return ans;
```

```
}
```

Metric	Complexity
--------	------------

 Time (TC)	$O(N \times L)$
---	-----------------

 Space (SC)	$O(1)$
--	--------

Why $O(1)$ space?

We use only two maps with max 26 keys (lowercase letters), so space doesn't grow with input size.

Using array of 26 characters:

```
vector<string> commonChars(vector<string>& words) {
```

```
    vector<int> minFreq(26, INT_MAX);
```

```
    for (string word : words) {
```

```
        vector<int> freq(26, 0);
```

```
        for (char ch : word) {
```

```
            freq[ch - 'a']++;
```

```
        }
```

```
        for (int i = 0; i < 26; i++) {
```

```
            minFreq[i] = min(minFreq[i], freq[i]);
```

```
        }
```

```
    }
```



```

vector<string> result;

for (int i = 0; i < 26; i++) {
    while (minFreq[i] -- > 0) {
        result.push_back(string(1, i + 'a'));
    }
}

return result;
}

```

Time & Space Complexity:

Complexity Value

Time $O(N * L + 26) \rightarrow \approx O(N * L)$

Space $O(26)$

- N = number of words
- L = average word length

IMP POINTS:

1. By Reference in C++

Always use `auto&` in range-based loops to avoid copying elements when you want to modify the original container.

◆ Example:

```
for (auto& it : mp) it.second = min(it.second, curr[it.first]);
```

2. Char to String in One Line

Use `string(1, ch)` to convert a single character `ch` to a string containing one character.

◆ Example:

```
string s = string(1, 'a'); // s = "a"
```

```
string s1 = string(5, 'x'); // "xxxxx"
```