

Ch. 1

Overview of COMPILER & its Structure

- 1) What is Compiler? What is front end and back end of compiler? [W-22, Q-1(a)]

Ans Compiler is a program which takes one language (Source program) as input and translates it into an equivalent another language (Target Program)

```

graph LR
    Input[Input] --> Compiler[Compiler]
    Compiler --> Output[Output]
  
```

⇒ Front end Compiler
 o Deals with Analyzing source code and it includes
 → Lexical Analysis
 → Syntax " "
 → Semantic "

⇒ Back end Compiler
 Deals with Code generation & Optimization
 o Includes
 → Intermediate Code Generation
 → Code Optimization
 → Target Code Generation

Q-2 Explain input, output and action performed by each phases of compiler with example [u-22 Q-1(c)]

Ans

- 1) Lexical Analysis
- 2) Syntax Analysis
- 3) Semantic Analysis
- 4) Intermediate Code Generation
- 5) Code Optimization
- 6) Code Generation

1) Lexical Analysis

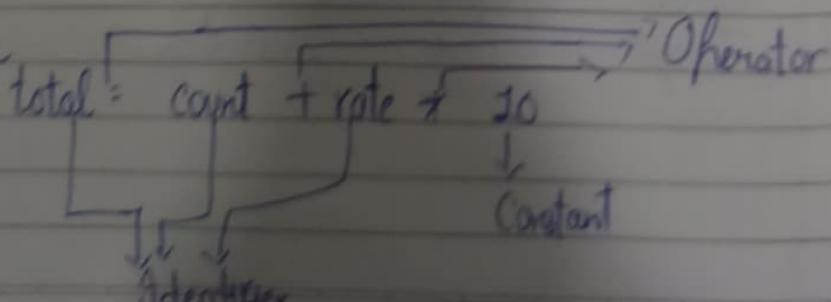
→ Also called Scanning

→ It is phase where the complete source code is scanned and your source program is broken up into group of strings called token

Tokens

- 1) identifier x, y
- 2) assignment = ? Operator
- 3) plus +
- 4) minus -
- 5) Constants
- 6) Separator /, {, }
- 7) Keyword int, Else, while

Example

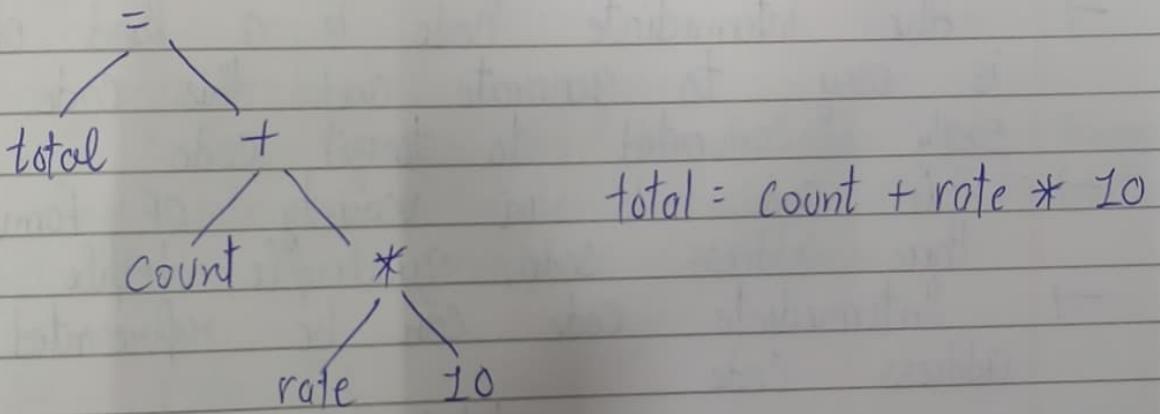


$$id1 = id2 + id3 * 10$$

After Lexical Analysis \uparrow

2) Syntax Analysis

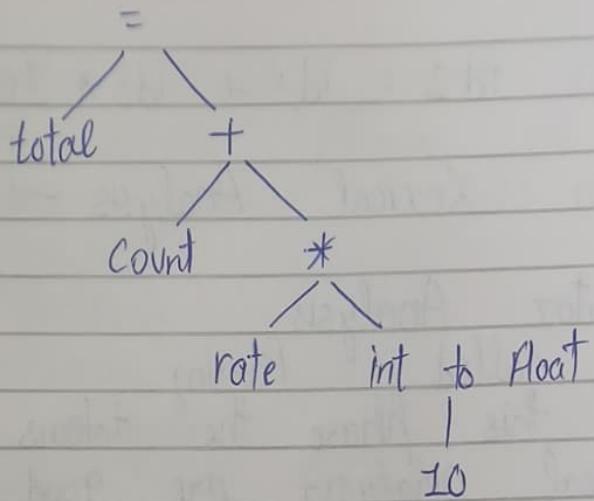
- \rightarrow Also called Parsing
- \rightarrow In this phase the tokens generated by the lexical analyser are good grafted together to form a hierarchical structure



3) Semantic Analysis

- \rightarrow This phase determines the meaning of the source string
- \rightarrow It performs following operations
 - 1) Matching or parenthesis in expression
 - 2) Matching of if-else statement
 - 3) Performing arithmetic operation that are type compatible
 - 4) Checking the scope of operation
- \Rightarrow Example

$$\text{total} : \text{count} + \text{rate} * 10$$



4) Intermediate Code Generation

- The intermediate code is a kind of code which is easy to generate and this code can be easily converted to target code
- This code is in variety of forms such as three address code, quadruple, triple, RISC
- Intermediate code can be represented in three address code

$$\text{total} = \text{count} + \text{rate} * 10$$

$$t_1 = \text{int_to_float}(10)$$

$$t_2 = \text{rate} \times t_1$$

$$t_3 = \text{count} + t_2$$

$$\text{total} = t_3$$

5) Code Optimization

- The code optimization phase attempts to improve the intermediate code
- This is necessary to have a faster executing code or less consumption of memory
- Thus overall running time of target program can be improved

Example

$$\text{total} = \text{Count} + \text{rate} * 10$$

Intermediate code

$$\left\{ \begin{array}{l} t_1 = \text{int_to_float}(10) \\ t_2 = \text{rate} + t_1 \\ t_3 = \text{count} + t_2 \\ t_3 = \text{total} \times [\text{total} = t_3] \end{array} \right.$$

Code optimization

$$\left\{ \begin{array}{l} t_2 = \text{rate} * 10 \\ \text{total} = \text{count} + t_1 \end{array} \right.$$

Q) Code Generation

- In this phase the target code gets generated
- The intermediate code instructions are translated into sequence of machine instructions

```

MOV    rate, R1
MUL    #10 , R1
MOV    Count, R2
ADD    R2, R1
MOV    R1, total

```

Q-3 Explain role of linker, loader and preprocessor in the process of compilation [W-23, Q-1(a)]

Ans

1) Linker

- The linker combines multiple object files and library files into a single executable file
- It resolves function calls between different modules

2) Loader

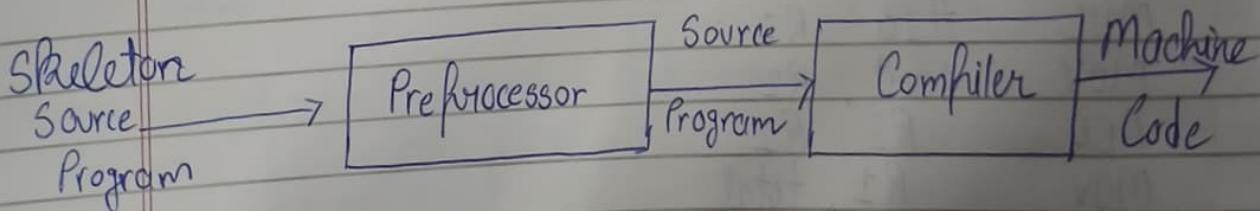
→ The process of loading consists of

- 1) Taking relocatable machine code
- 2) Altering the relocatable address
- 3) Placing the altered instructions and data memory at proper location

3) Preprocessor

→ Some tasks performed by Preprocessor

- 1) Macro processing : Allows users to define macros
- 2) File inclusion : A Preprocessor may include the header file into the program
- 3) Rational processor : It provides built in macro for construct like while or if statement
- 4) Language extensions : Add capabilities to the language using built-in macros



Q-4

Differentiate following terms

1) interpreter and compiler

2) parse tree and Syntax tree [W-24, Q-1(a)]

Ans

1) Interpreter & Compiler

i) Execution Method

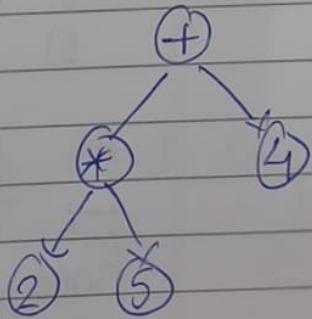
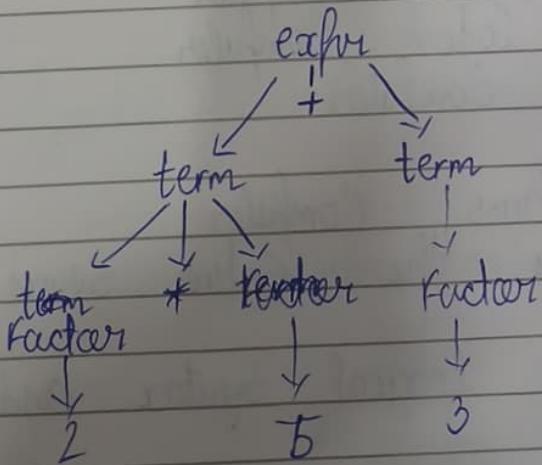
Interpreter
Translates entire program into machine code at once

Compiler
Translates and executes the program line by line

1) Output	Generates an executable file	Does not
2) Speed	Faster	Slower
3) Error Detection	Shows all errors after compilation	Stops immediately when an error is found
4) Examples	C, C++, JAVA	Python, JS, BASIC

2) Parse tree & Syntax tree

Feature	Parse Tree	Syntax Tree
1) Represents	Complete derivation using grammar	Simplified logical structure
2) Contains	All grammar symbols	Only essential nodes
3) Size	Larger	Smaller
4) Use	Syntax Analysis	Semantic Analysis, Code Generation
5) Example	$2 * 5 + 4$	



Q-5

State the applications of language processors
[S-24, Q-1(a)]

Ans

- 1) Program Translation
- 2) Program Execution
- 3) Code Optimization
- 4) Error Detection
- 5) Debugging Code
- 6) Software Development Tools

Q-6

Enlist types of compiler. Explain any two in brief
[S-24, Q-2(a)]

Ans

Types of Compiler

- 1) One pass Compiler
- 2) Two pass Compiler
- 3) Incremental Compiler
- 4) Native Code Compiler
- 5) Cross Compiler

(1) One pass Compiler

→ Translates the entire source code in one pass

→ Performs lexical, Syntax and Code Generation together

→ Fast

→ Used for simple & small programs

2) Cross Compiler

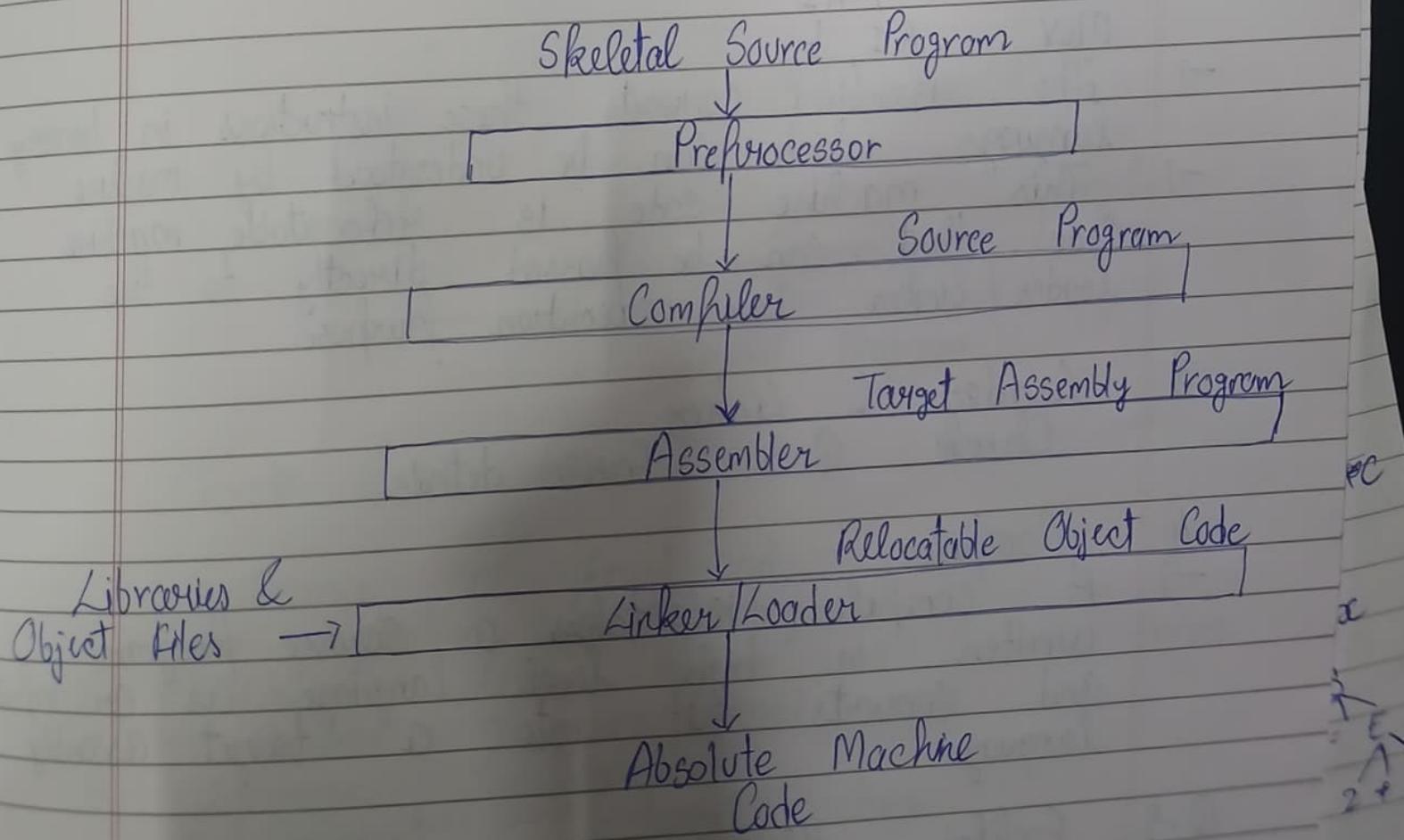
→ Used to compile a source code for different platforms

→ It runs on one machine (host) but produces executable code for another machine (target) with different hardware or operating system

Q-7 Explain Cousins of compiler in detail [S-24, Q-1(c)]

Ans

- 1) Preprocessor
- 2) Compiler
- 3) Assembler
- 4) Linker / Loader



I) Preprocessor
Check Q-3

2) Assemblers

- Some compilers produce the assembly code as output which is given to assemblers as an input
- Assembler is a kind of translator which takes the assembly program as input and produces machine code as output

MOV 0, R1
 MUL #5, R1
 ADD #7, R1
 MOV R1, b

- The assembler converts these instructions in binary language which can be understood by machine
- This machine code is relocatable machine code that can be passed directly to the loader/linker for execution purpose

3) Loader & Linker

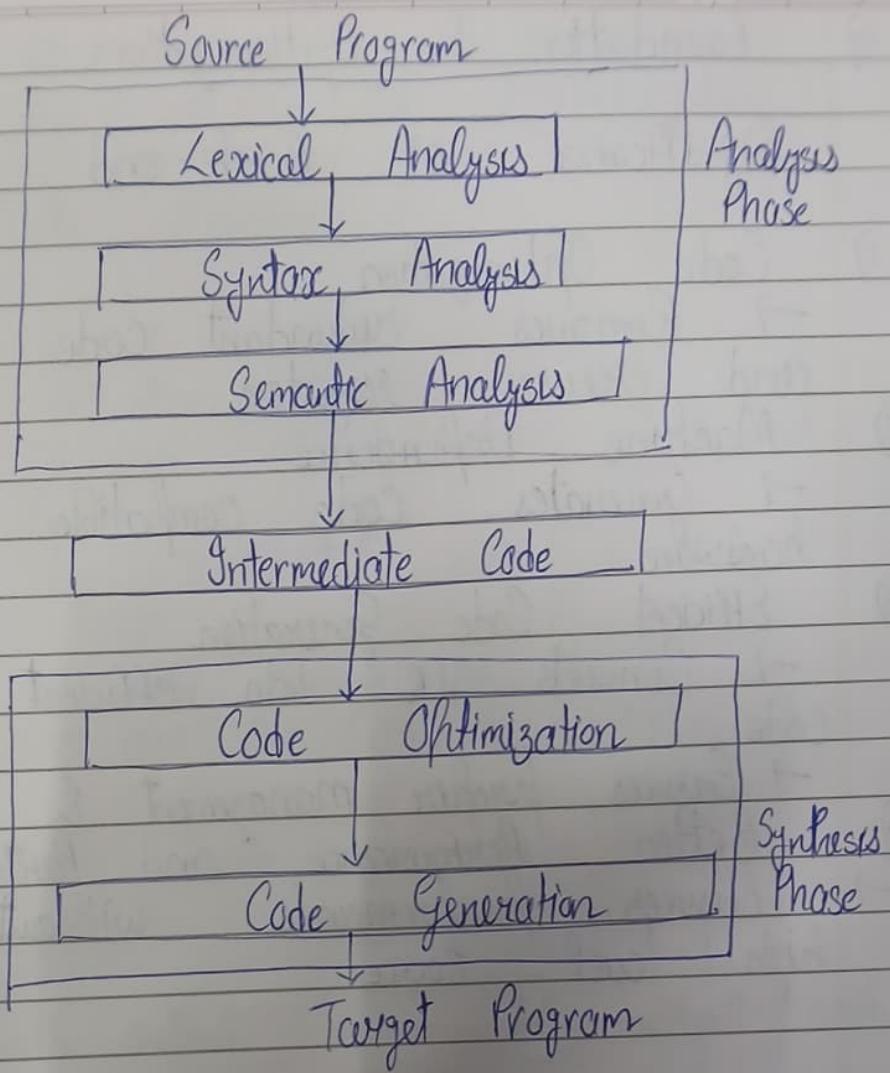
Check Q-3 for details

4) Compiler

- A compiler is takes a source program written in high level language as an input and converts it into a target assembly language

Q-8 Explain phases of compiler. Give significance of both [S-25, Q-3(c)]

Ans



Check Q-2 for more

- 1) Significance of front-end
Error Detection & Reporting
 - Detects lexical, syntax and semantic errors
 - Ensures grammar and logic
- 2) Language Independence
 - Independent of target machine
- 3) Intermediate Code Generation
 - Produces IR (Intermediate Representation)
 - which acts as bridge between Front-end and back-end

9) Foundation & Optimization

Significance of Back-end

- 1) Code Optimization
 - Removes redundant code, optimizes loops, and reuses registers
- 2) Machine Dependence
 - Generates code compatible with target hardware
- 3) Efficient Code Generation
 - Converts IR into efficient, executable machine code
 - Ensures proper management & register allocation
- 4) Better Performance and Portability
 - Ensures performance without changing the high level source

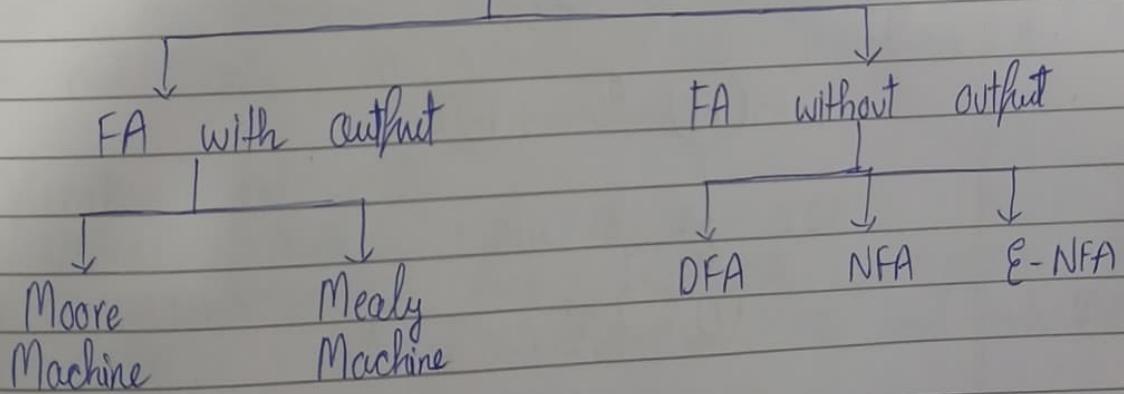
Ch-2 Lexical Analysis

o Finite State Machine

- Symbol : a, b, c, 0, 1, 2, 3
- Alphabet : Collection of symbols Eg: {a, b}
- String : Sequence of symbols Eg: a, b, 0, 1,
- Language : Set of String
Eg: $\Sigma = \{0, 1\}$

L_1 = Set of all strings of length 3
 $= \{000, 001, 010, 011, 100, 101, 110, 111\}$

Finite Automata



o DFA

- Simple
- Limited Memory

$(Q, \Sigma, q_0, F, \delta)$

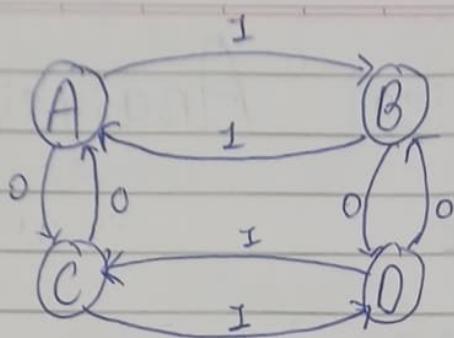
Q = Set of all states

Σ = inputs

q_0 = Start State

F = Set of Final States

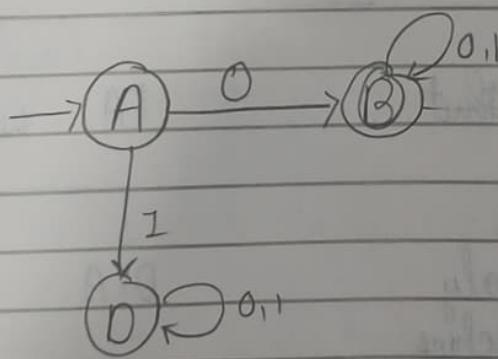
δ = transition Function From $Q \times \Sigma \rightarrow Q$



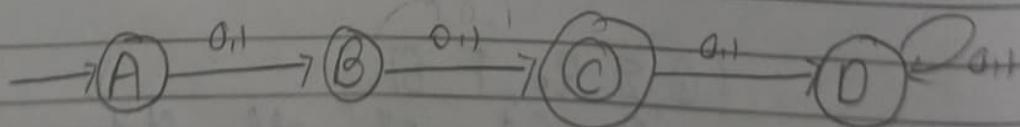
$$\begin{aligned}
 Q &= \{A, B, C, D\} \\
 \Sigma &= \{0, 1\} \\
 q_0 &= A \\
 F &= \{D\}
 \end{aligned}$$

	0	1
A	C	B
B	A	D
C	A	D
D	B	C

- 1) $L_1 = \text{Set of strings start with '0'}$
 $= \{0, 00, 01, 000, 010\}$



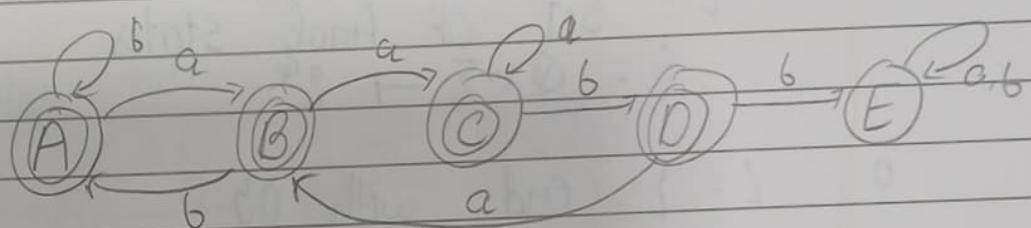
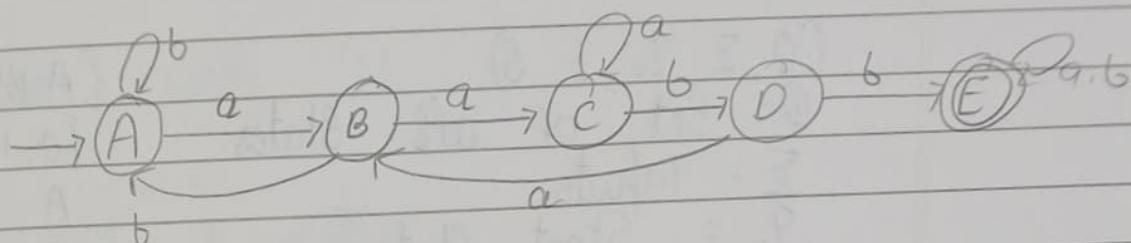
- 2) $L_2 = \{\text{0,1}\}$ of length 2
 $= \{00, 01, 10, 11\}$



③ $\{a,b\}^*$ does not contain aabb

$$\Sigma = \{a, b\}$$

aaa~~b~~aaa



o Regular Language [RL]

\Rightarrow A Language is said to be a Regular Language if and only if some FSM recognizes it

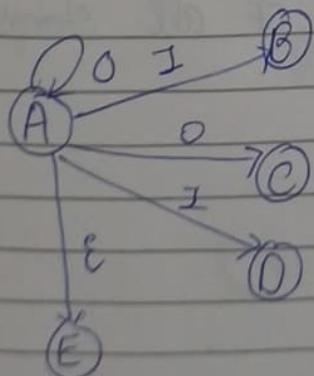
\Rightarrow Operations on RL

1) UNION : $A \cup B = \{\alpha | \alpha \in A \text{ or } \alpha \in B\}$

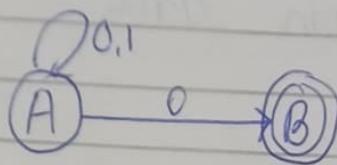
2) CONCATENATION : $A \circ B = \{\alpha y | \alpha \in A \text{ and } y \in B\}$

3) STAR : $A^* = \{\alpha_1 \alpha_2 \alpha_3 \dots \alpha_k | k \geq 0 \text{ and each } \alpha_i \in A\}$

o NFA - Non Deterministic FA



- o $L = \{ \text{Set of all strings that end with } 0\}$



$(Q, \Sigma, q_0, F, \delta)$

$Q = \text{Set of all states}$

$\Sigma = \text{inputs}$

$q_0 = \text{Start state}$

$F = \text{Set of final states}$

$\delta = Q \times \Sigma \rightarrow 2^Q$

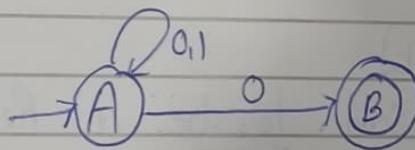
{A, B}

{0, 1}

A

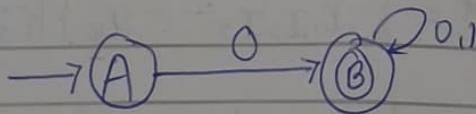
B

- o $L = \{ \text{end with } 0\}$

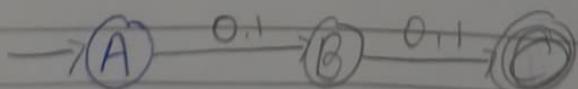


E

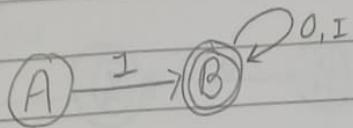
- o $L = \{ \text{start with } 0\}$



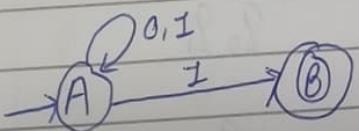
- o NFA that accepts sets of all strings over {0,1} of length 2
 $= \{00, 01, 10, 11\}$



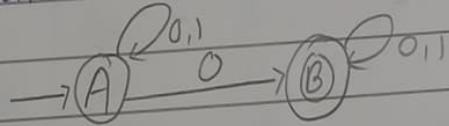
Eg: starts with 'I'



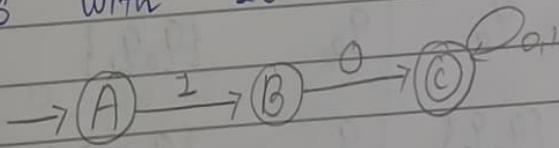
Eg: ends with 'I'



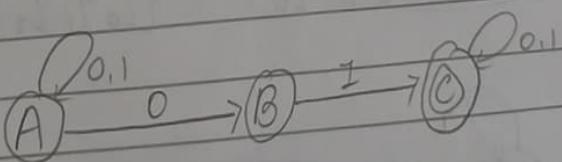
Eg: contain '0'



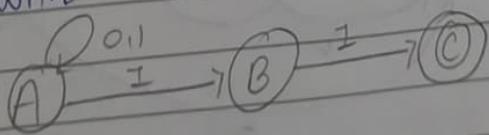
Eg: starts with '10'



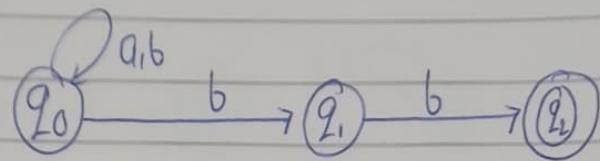
Eg: contain '01'



Eg: ends with 11

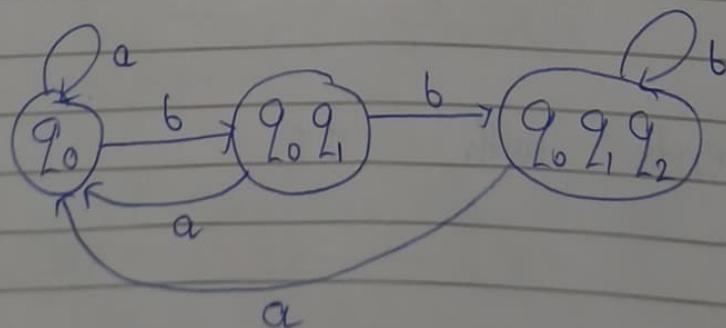


Conversion of NFA to DFA

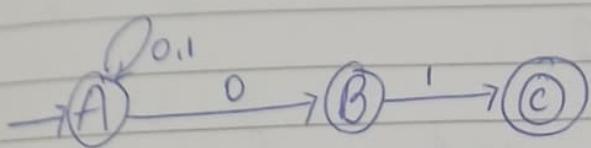


$\rightarrow q_0$	a q_0	b q_0, q_1
q_1	-	q_2
q_2	-	-

q_0	a q_0	b $\{q_0, q_1\}$
$\{q_0, q_1\}$	q_0	$\{q_0, q_1, q_2\}$
$\{q_0, q_1, q_2\}$	q_0	$\{q_0, q_1, q_2\}$

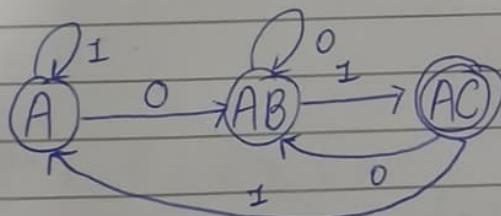


Eg:

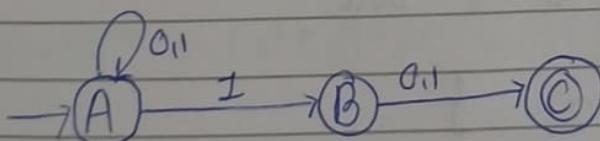


	0	1
$\rightarrow A$	A, B	A
B	\emptyset	C
C	\emptyset	\emptyset

	0	1
$\rightarrow A$	AB	A
AB	AB	AC
AC	AB	A

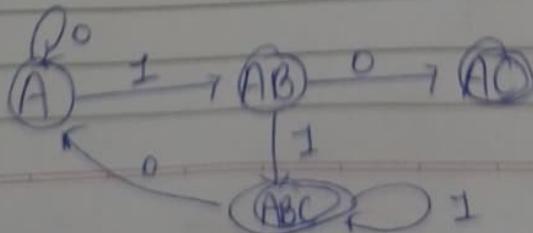


Eg: L = { second last symbol is always '1' }



	0	1
$\rightarrow A$	A	AB
B	C	-
C	-	-

	0	1
$\rightarrow A$	A	AC
AB	AC	ABC
ABC	AC	ABC
AC	A	AB
AB	AC	ABC



0 Regular Expressions

1) $a, b, c \dots \lambda, \emptyset$

2) Union OR two regular expressions
 $R_1, R_2 \quad (R_1 + R_2)$

3) Concatenation
 $R_1, R_2 \quad (R_1 R_2)$

4) $R \rightarrow R^*$

Eg: $\{0, 1, 2\}$
 $R = 0 + 1 + 2$

Eg $\{\lambda, ab\}$
 $R = \lambda ab$

Eg $\{abb, a, b, bba\}$

$R = abb + a + b + bba$

Eg $\{\lambda, 0, 00, 000, \dots\}$

$R = 0^*$

Eg $\{\lambda, 1, 11, 111, \dots\}$

$R = 1^*$

Identities OF Regular Expression

- 0) $\emptyset + R = R$
- 1) $\emptyset R + R \emptyset = \emptyset$
- 2) $\epsilon R \neq R \epsilon = R$
- 3) $\epsilon^* = \epsilon \quad \& \quad \emptyset^* = \epsilon$
- 4) $R + R = R$
- 5) $R^* R^* = R^*$
- 6) $RR^* = R^*R$
- 7) $(R^*)^* = R^*$
- 8) $\epsilon + RR^* = \epsilon + R^*R = R^*$
- 9) $(P\emptyset)^*P = P(\emptyset P)^*$
- 10) $(P+Q)^* = (P^* Q^*)^* = (P^* + Q^*)^*$
- 11) $(P+Q)R = PR + QR \quad \text{and} \quad R(P+Q) = RP + RQ$

Q. Explain construction of DFA from RE without
making NFA with suitable example [S-24, Q-2(c)]

→ RE to DFA

$(a|b)^* ab$

- 1) Create Syntax Tree
- 2) Number the leaf nodes
- 3) Find Nullable of each node
- 4) Find First Fos of each node
- 5) Find last Fos of each node
- 6) Find Follow Fos of each node

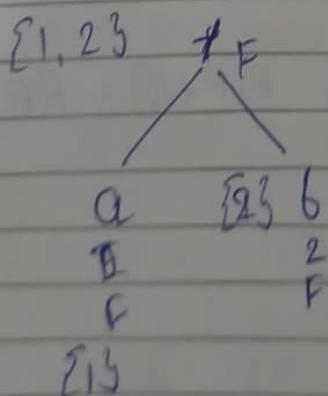
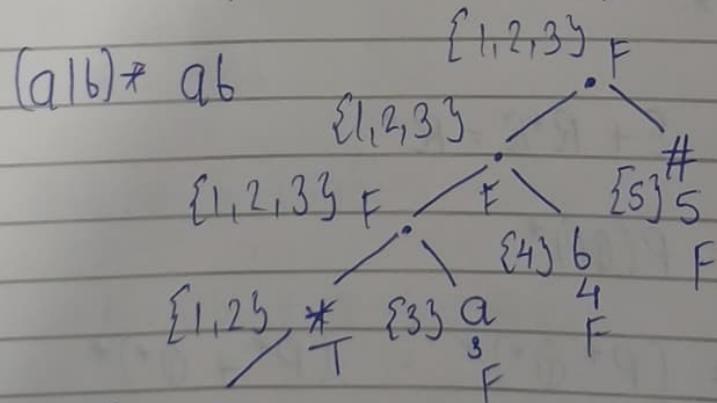
(i) $n \rightarrow \bullet$ then

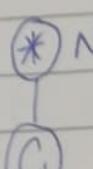
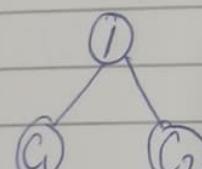
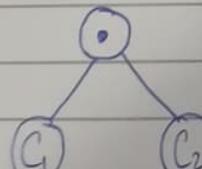
FirstFos (C_2) \rightarrow lastFos (C_1)

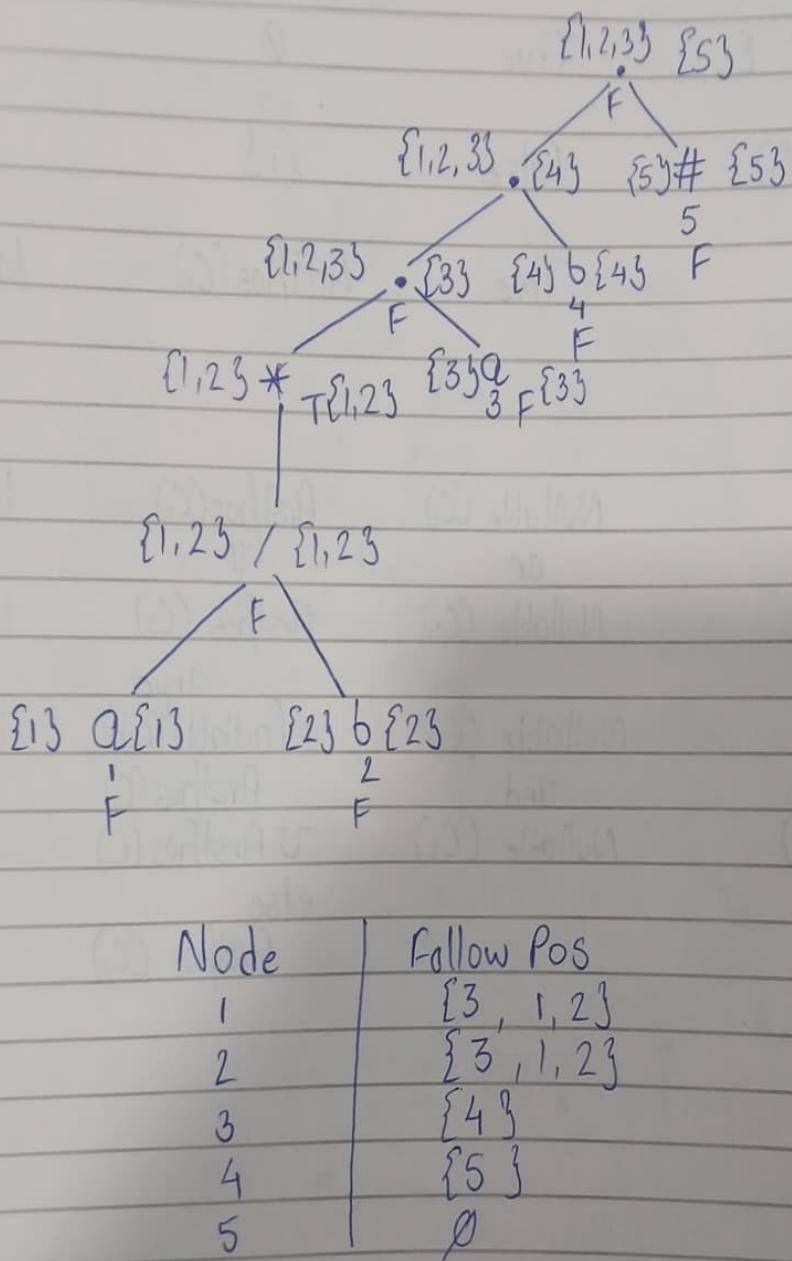
(ii) $n \rightarrow *$ then

FirstFos (n) \rightarrow lastFos (n)

Eg. $(a|b)^* ab$



Node	Nullable	firsthos(n)	lasthos(n)
1) $N \rightarrow \text{Leaf } E$	True	\emptyset	\emptyset
2) $N \rightarrow \text{leaf } (i)$	False	$\{i\}$	$\{i\}$
3)  N C1	True	firsthos(C1)	lasthos(C1)
4)  I C1 C2	Nullable(C1) or Nullable(C2)	firsthos(C1) \cup firsthos(C2)	lasthos(C1) \cup lasthos(C2)
5)  I C1 C2	Nullable(C1) and Nullable(C2)	if nullable(C1) true firsthos(C1) \cup firsthos(C2) else firsthos(C1)	if nullable(C2) true lasthos(C1) \cup lasthos(C2) else lasthos(C2)



$$\text{firstPos}(\text{Root Node}) = \{1, 2, 3\} \rightarrow A$$

$$\begin{aligned} 1) \quad (A, a) &= \{1, 3\} \\ &= FOP(1) \cup FOP(3) \\ &= \{1, 2, 3, 4\} \rightarrow (B) \end{aligned}$$

$$\text{P} \quad (A, b) := \{2\} \\ = \text{fop}(2) = \{1, 2, 3\} \rightarrow A$$

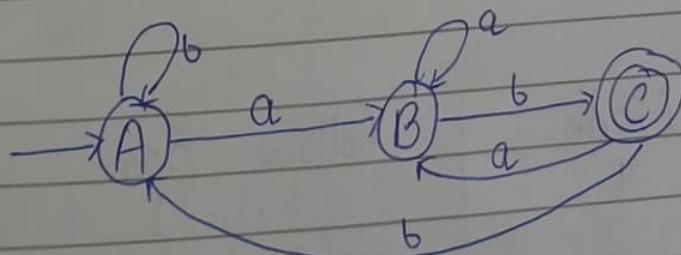
$$② (B, a) = \{1, 3\} \\ = \{1, 2, 3, 4\} \rightarrow \textcircled{B}$$

$$(B, b) = \{2, 4\} \\ = \text{For}(2) \cup \text{For}(4) \\ = \{1, 2, 3, 5\} \rightarrow \textcircled{C}$$

$$③ (C, a) = \{1, 3\} \\ = \{1, 2, 3, 4\} \rightarrow \textcircled{B}$$

$$(C, b) = \{2\} \\ = \{1, 2, 3\} \rightarrow \textcircled{A}$$

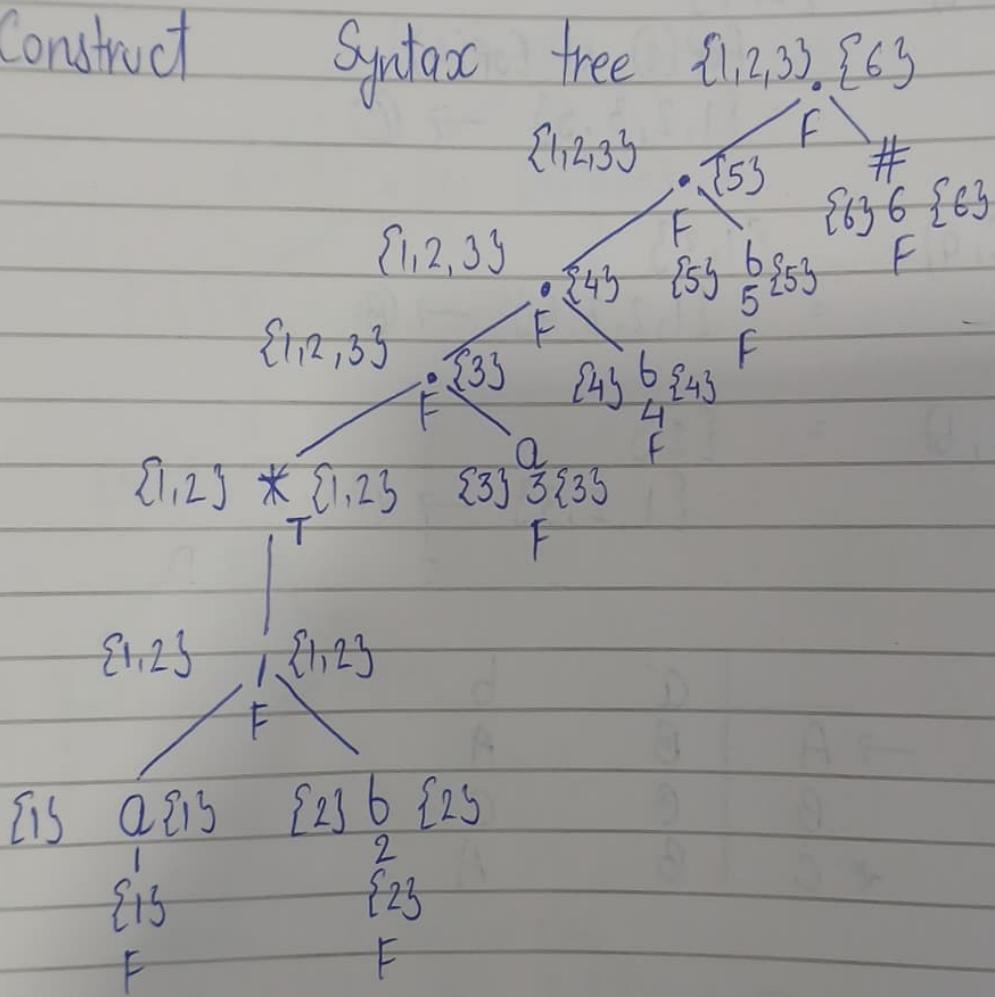
	a	b
$\rightarrow A$	B	A
B	B	C
* C	B	A



(a1b)* abb#

Construct

Syntax tree



Node	Follow Has
1	{3, 1, 2}
2	{3, 1, 2}
3	{4}
4	{5}
5	{5, 6}
6	Ø

First Pos (Root Node) = $\{1, 2, 3\} \rightarrow A$

$$1) (A, a) : \{1, 2, 3\} \quad \{1, 3\}$$

$$= Fop(1) \cup Fop(3)$$

$$= \{1, 2, 3, 4\} \rightarrow B$$

$$(A, b) = \{2\}$$

$$= \{1, 2, 3\} \rightarrow A$$

$$2) (B, a) = \{1, 2, 3, 4\} \quad \{1, 3\}$$

$$= Fop(2) \cup Fop(4)$$

$$= \{1, 2, 3, 5\} \rightarrow C$$

$$\{1, 2, 3, 4\} \rightarrow B$$

$$(B, b) = \{2, 4\}$$

$$= \{1, 2, 3, 5\} \rightarrow C$$

$$3) (C, a) = \{1, 3\}$$

$$= \{1, 2, 3, 6\} \rightarrow A$$

$$(C, b) = \{2, 5\}$$

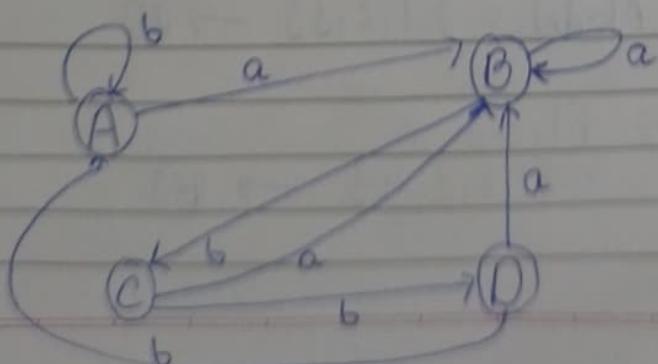
$$= \{1, 2, 3, 6\} \rightarrow O \quad D$$

$$4) (D, a) = \{1, 3\}$$

$$= \{1, 2, 3\} \rightarrow A \quad \{1, 2, 3, 4\} \rightarrow B$$

$$(D, b) = \{2\}$$

$$= \{1, 2, 3\} \rightarrow A$$



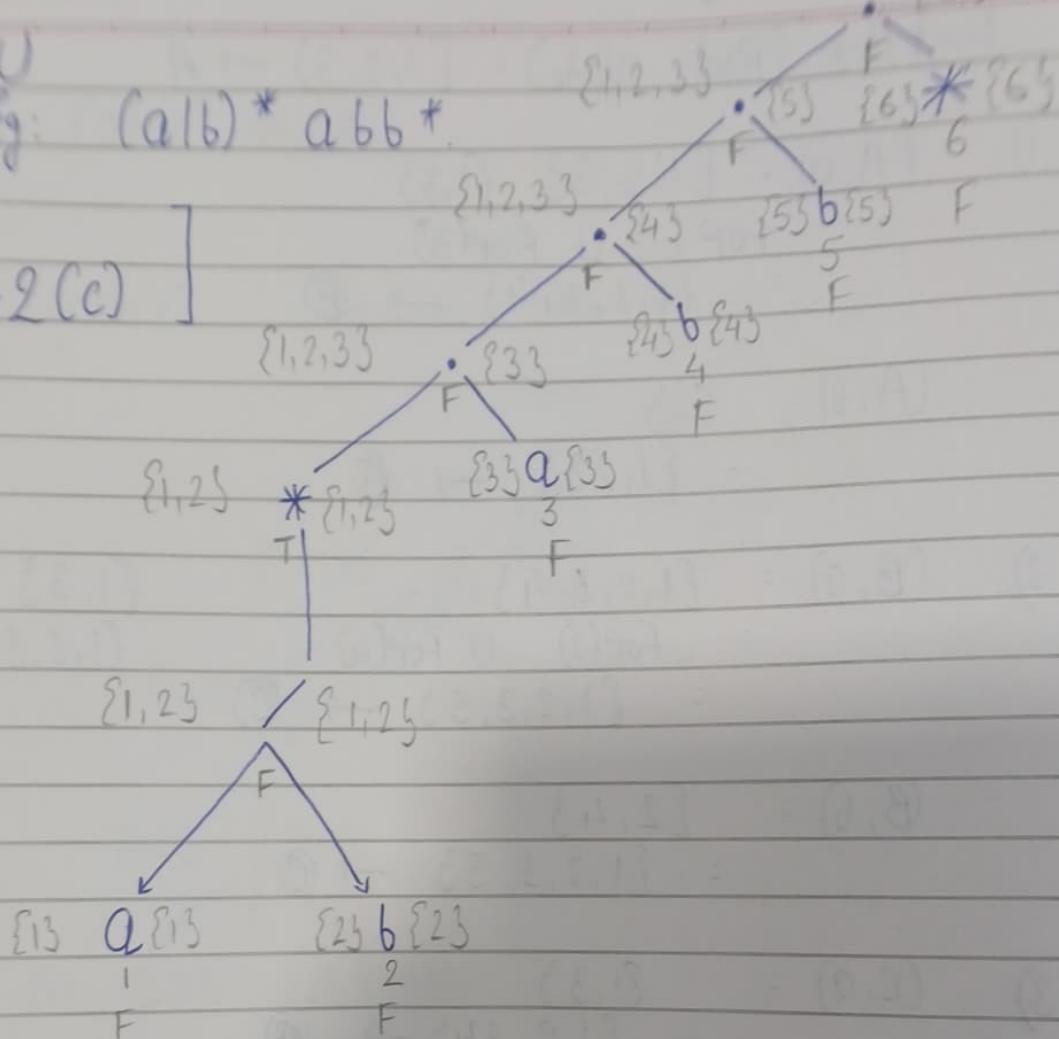
(1,2,3)

163

G-TU

Eg: $(ab)^* abb^*$

[W-22
OR Q-2(c)]



Node	Follow Pos	Pos
1	{3, 1, 23}	
2	{3, 1, 23}	
3	{43}	
4	{53}	
5	{63}	
6	\emptyset	

firstPos(Root Node) = {1,2,33} \rightarrow A

i) $(A, a) = \{1,33\}$
 $= \{1,2,3,43\} \rightarrow$ B

$$1) (A, a) = \{2\} \\ = \{1, 2, 3\} \rightarrow \textcircled{A}$$

$$2) (B, a) = \{2, 3\} \\ = \{1, 2, 3, 4\} \rightarrow \textcircled{B}$$

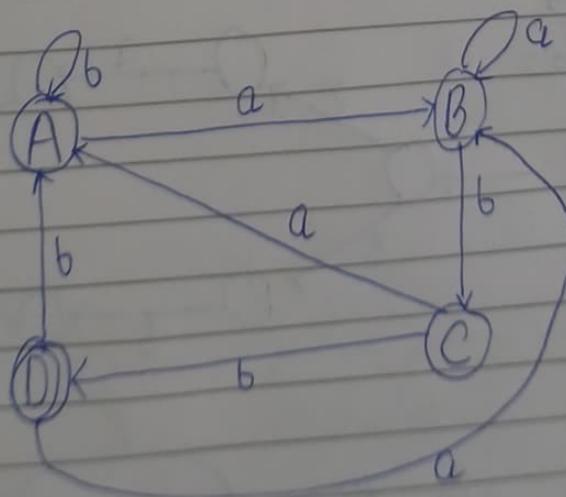
$$(B, b) = \{2, 4\} \\ = \{1, 2, 3, 5\} \rightarrow \textcircled{C}$$

$$3) (C, a) = \{1, 2\} \\ = \{1, 2, 3\} \rightarrow \textcircled{A}$$

$$(C, b) = \{2, 5\} \\ = \{1, 2, 3, 6\} \rightarrow \textcircled{D}$$

$$4) (D, a) = \{1, 3\} \\ = \{1, 2, 3, 4\} \rightarrow \textcircled{B}$$

$$(D, b) = \{2\} \\ = \{1, 2, 3\} \rightarrow \textcircled{A}$$

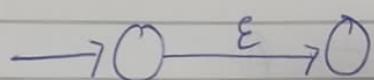


0 Regular expression to NFA conversion Using thompson's rule

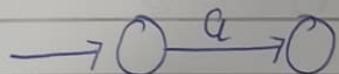
1) $(a|b)^*$

0 Thompson's Rules

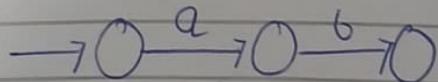
1) For ϵ ,



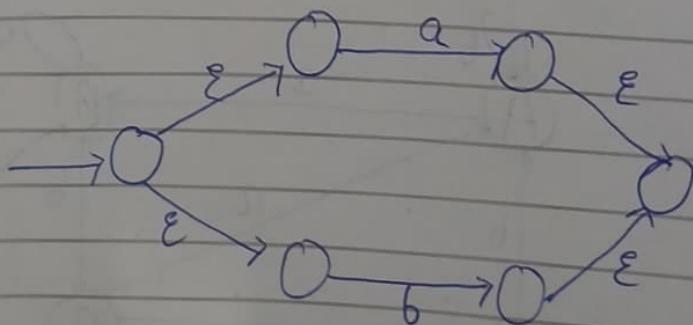
2) For a ,



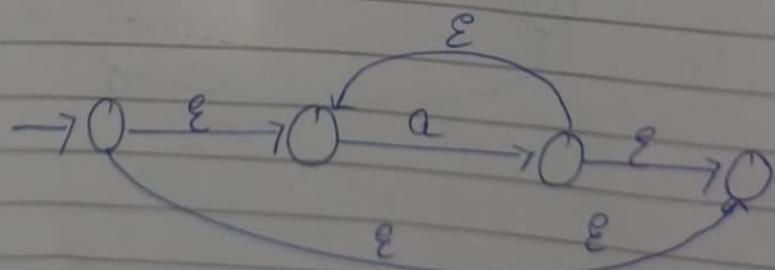
3) For $a.b$,



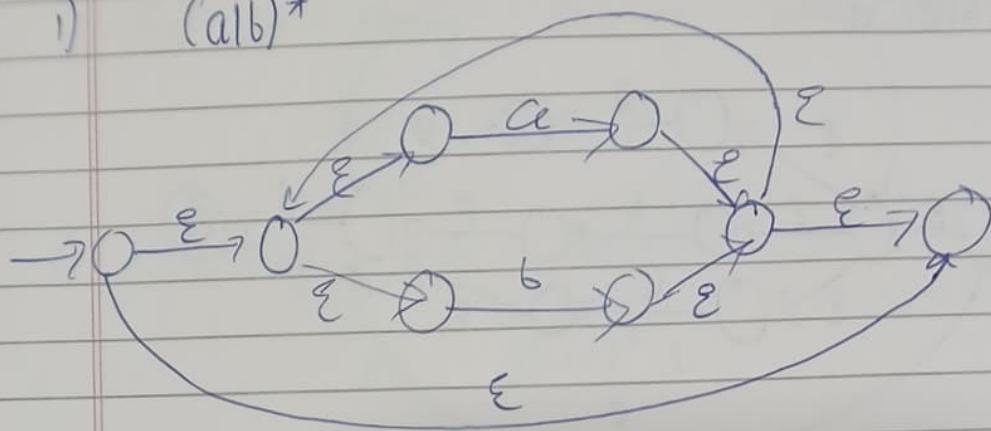
4) For $\frac{a|b}{a+b}$



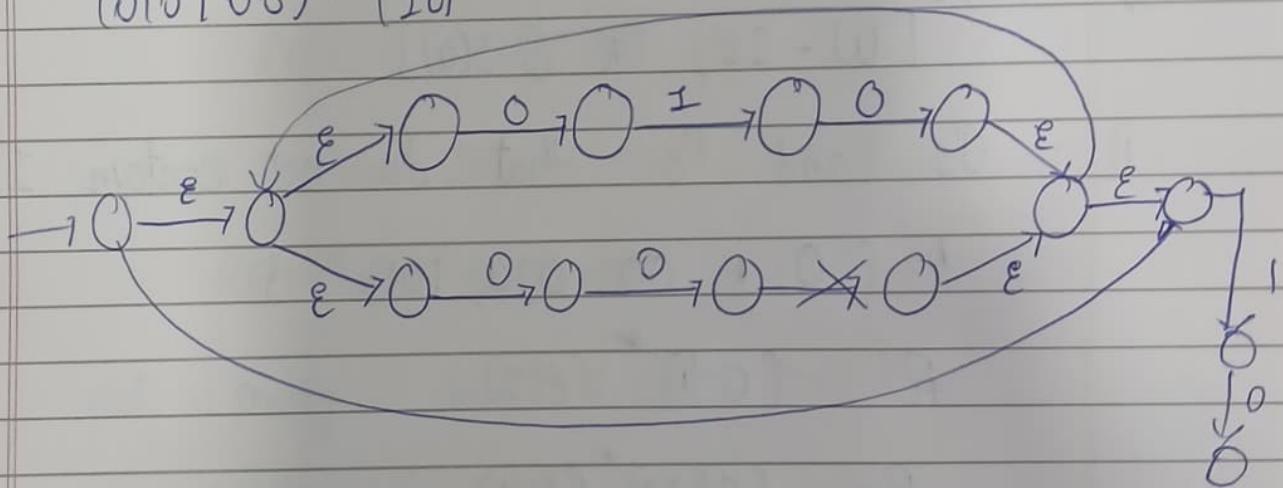
5) For a^* ,



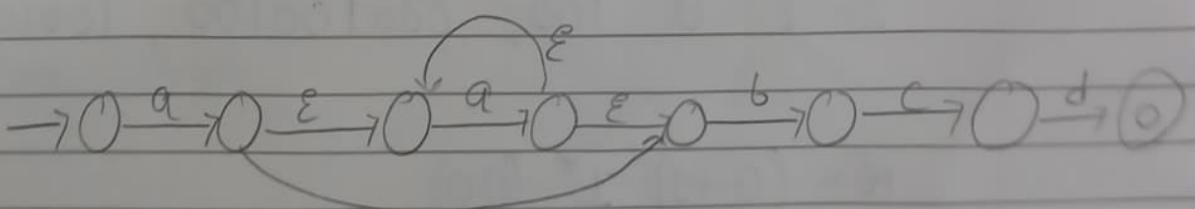
1) $(a|b)^*$



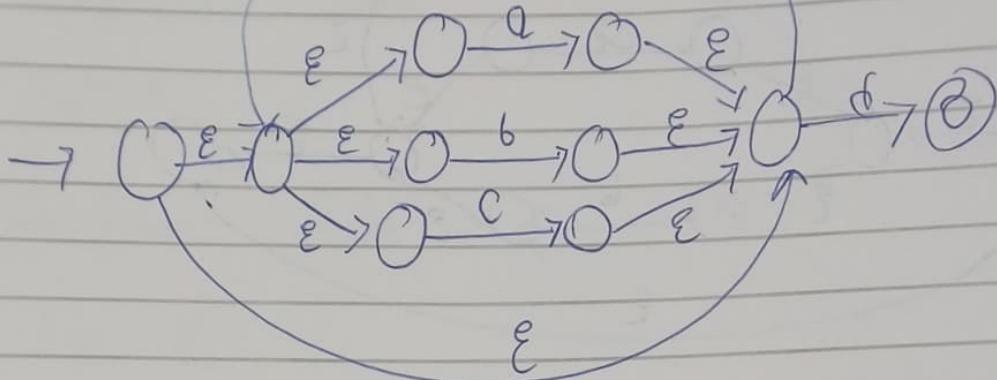
2) $(0|0|00)^* (10)$



3) a^+bcd
 $a.a^*bcd$



4)

 $(a|b|c)^*d$ 

Q,

G.T.U

[W - 22, OR Q-3(a)]

1) 0's and 1's that do not contain 11

$$L = \{ 0, 1, 00, 010, 101, \dots \}$$

$$R = (0|1)^* (\varepsilon|1)$$

$$R = (0|10)^* (\varepsilon|1)$$

2) All strings of 0's and 1's that every 1 is followed by 00

$$L = \{ 0, 100, 0001000100, 100100 \dots \}$$

$$R = (0+1)^* 1^* . (00)$$

$$R = (0|100)^*$$

1) Set of string starting with 0

$$RE = 0(0+1)^*$$

2) ending in 1

$$RE = (0+1)^* 1$$

3) containing exactly two 0's

$$RE = 1^* 0 1^* 0 1^*$$

4) at least two 0's

$$RE = 1^* 0 1^* 0 (1+0)^*$$

5) not ending in 01

$$RE = (1+0)^* (00 + 11 + 10)$$

6) starting with 11

$$11 (1+0)^*$$

7) even length

$$RE = (00)^*$$

$$L = \Sigma \epsilon, 0$$

atleast one 0 and atleast one 1

$$RE = (0+1)^* 0 \ (0+1)^* 1 (0+1)^*$$

atleast two occurrences of 1's between any two occurrences of 0's

$$(0111^* 0)^*$$

$$RE = (1 + (0111^* 0))^*$$

G.T.U

[W-23, Q-2(a)]

i) containing exactly three 1's

$$\checkmark RE = 0^* 1 \ 0^* 1 \ 0^* 1 \ 0^*$$

ii) begins or ends with 00

$$x RE = 00 + (0+1)^* + 00$$

$$x RE = 00 + (0+1)^* + 00$$

$$\checkmark RE = 00(0+1)^* + (0+1)^* 00$$

iii) contains atleast three 1's

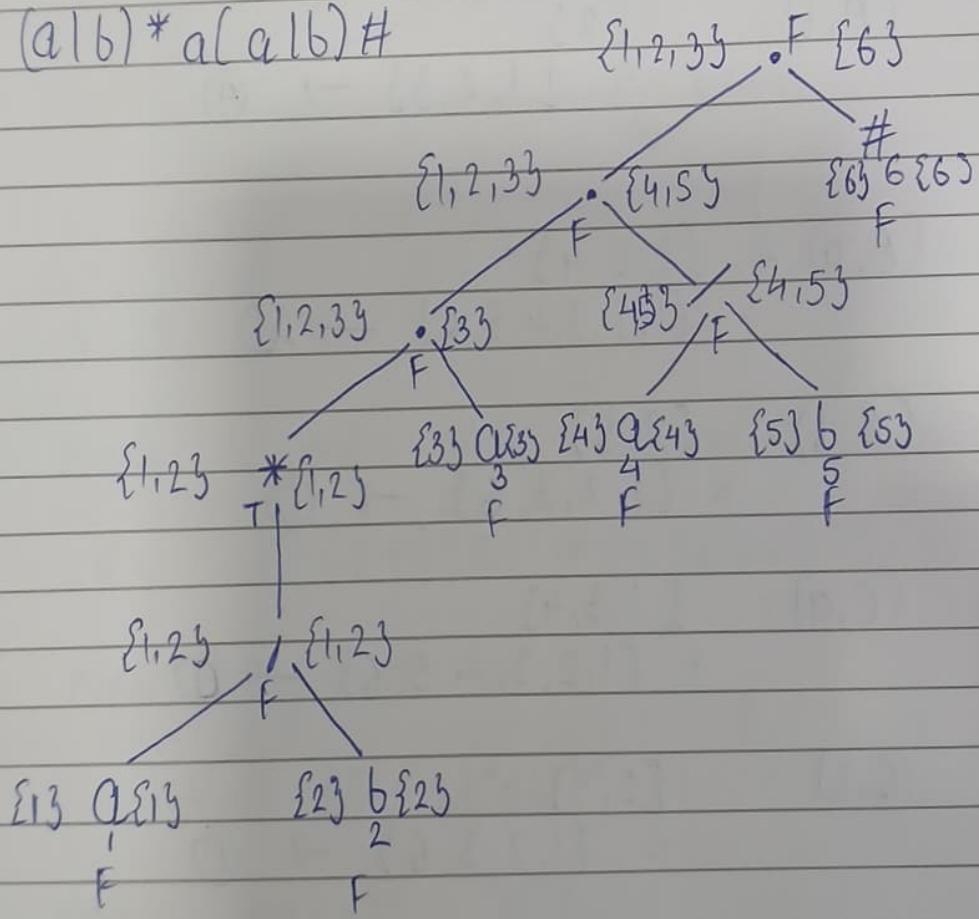
$$x RE = (0+1)$$

$$x RE = 0^* 1 \ 0^* 1 \ 0^* 1 (0+1)^*$$

$$RE = (0+1)^* \sqcup (0+1)^* \sqcup (0+1)^* \sqcup (0+1)^*$$

Q, W-23, Q-2(c)

$$(a|b)^* a(a|b) \#$$



Node	Follow has
1	{3, 1, 2}
2	{3, 1, 2}
3	{4, 5}
4	{6}
5	{6}
6	{}

Root node = $\{1, 2, 3\} \rightarrow A$

$$1) (A, a) = \{2, 3\} \\ = \{1, 2, 3, 4, 5\} \rightarrow B$$

$$(A, b) = \{2\} \\ \approx \{1, 2, 3\} \rightarrow A$$

$$2) (B, a) = \{1, 3, 4\} \\ = \{1, 2, 3, 4, 5, 6\} \rightarrow C$$

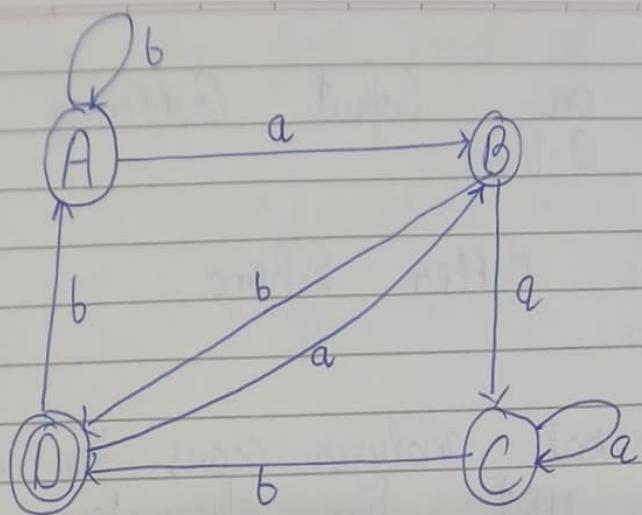
$$(B, b) = \{2, 5\} \\ = \{1, 2, 3, 6\} \rightarrow D$$

$$3) (C, a) = \{1, 3, 4\} \\ = \{1, 2, 3, 4, 5, 6\} \rightarrow E$$

$$(C, b) = \{2, 5\} \\ = \{1, 2, 3, 6\} \rightarrow D$$

$$4) (D, a) = \{1, 3\} \\ = \{1, 2, 3, 4, 5\} \rightarrow B$$

$$(D, b) = \{2\} \\ = \{1, 2, 3\} \rightarrow A$$



Q,

GTU

S-25, Q-2(b)

- i) starts & end with different symbols

$$R = 0(0+1)^*1 + 1(0+1)^*0$$

- ii) even no. of "a"

$$R = b^* (ab^*ab^*)^*$$

- iii) odd no. of "b"

$$R = a^* (ba^*ba^*)^* ba^*$$

- iv) Atleast two times a

$$R = (a+b)^* a (a+b)^* a (a+b)^*$$

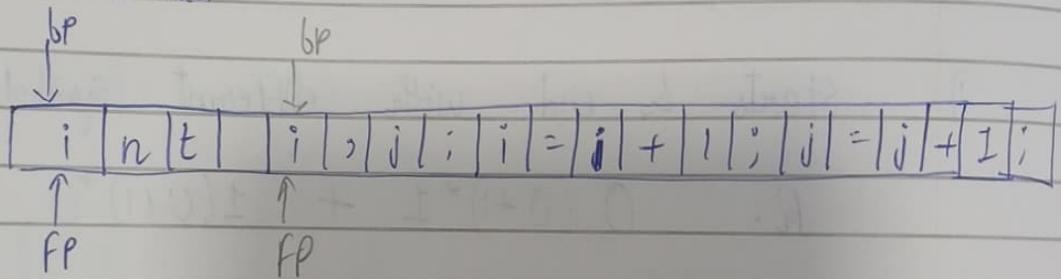
Q.

Note [W-22, Q-1(6)] on Input Buffering techniques

Ans

- 1) Single Buffer Scheme
- 2) Two " " "

- The lexical analyzer scans the input string from left to right one character at a time
- It uses two pointers begin-htr (bh) and forward-htr (fp) to keep track of portion of input scanned



The input character is thus read from Secondary storage. But reading in this way is costly

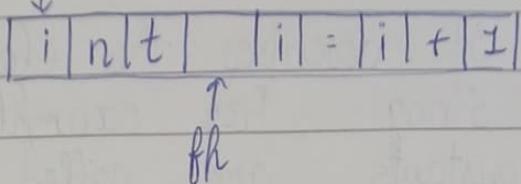
- So comes Input Buffering
- A block of data is first read into a buffer, and then scanned by lexical analyzer
- Two methods

- 1) One buffer Scheme

- In this scheme, only one buffer is used to store the input string
- But the problem with this scheme is that if lexeme is very long then it crosses the buffer boundary, to scan rest of lexeme the buffer has to be refilled, that makes

overwriting the first part of lexeme

bp



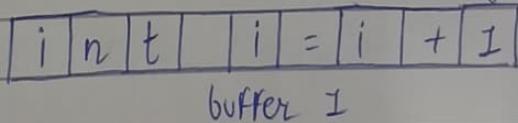
2) Two buffer Scheme

→ To overcome problem of (i) this came
 → The First and Second buffer are scanned alternatively

→ When end of current buffer is reached the other buffer is filled

→ Only problem is that if length of lexeme is longer than length of the buffer then Scanning input cannot be completely scanned

bp



;

↑
FP

buffer 2

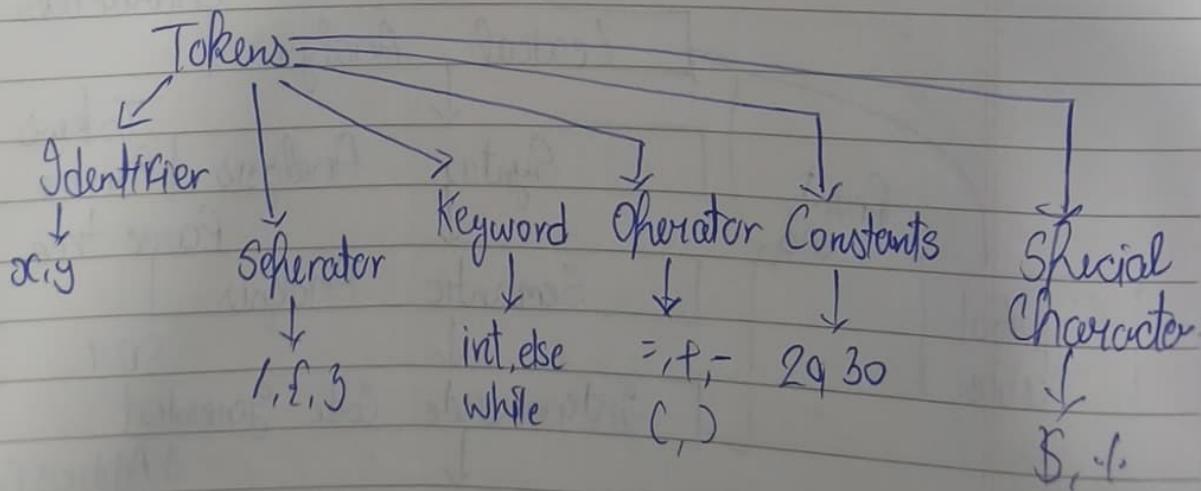
The eof character introduced at end is called Sentinel which is used to identify the end of buffer

0 Lexical Analysis

1) Tokenization

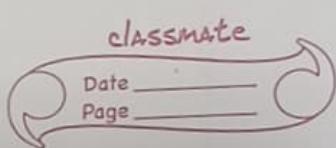
2) Give Error messages

3) Eliminate Comments , White Space



Q Define token, lexeme and pattern

Ans Tokens: It describes the class of or category of input String. For example Identifiers, Keywords, constants are called tokens

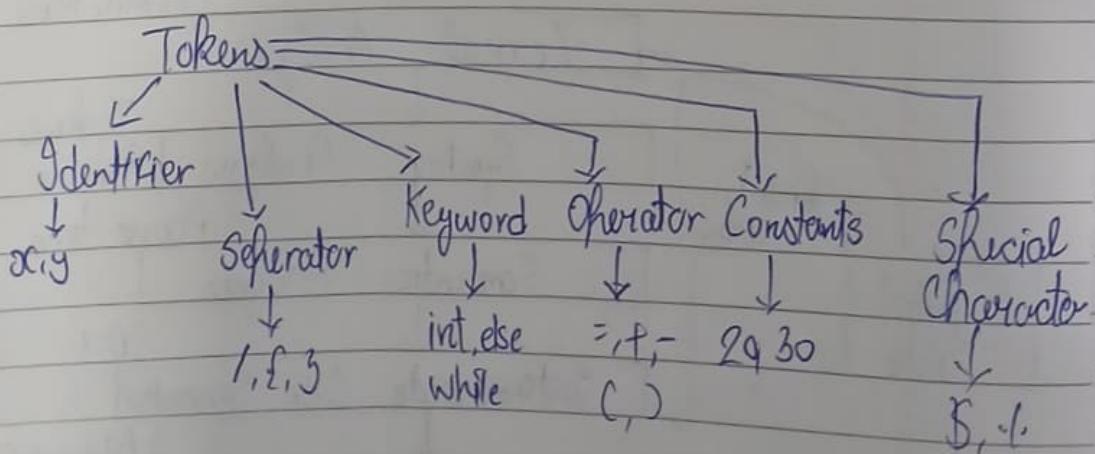


O Lexical Analysis

1) Tokenization

2) Give Error messages

3) Eliminate Comments, White Space



Patterns: set of rules that describe the token

Lexemes: Sequence of characters in the source program that are matched with the pattern of the token. For Example, int i, num, ans, char

Eg:

int x = 5;

Lexeme	tokens
int	Keyword
x	identifier
=	operator
5	constant
;	operator

Eg:

void swap (int a, int b)

{

int k;
k = a;
a = b;
b = k;

}

Lexeme	tokens
a	id
a	id
=	op
b	id
b	id
=	op
k	id
3	id
=	op
k	id
3	id

①

Lexeme
void
swap
(
int
a
,
int

Tokens
Keyword
Identifier
operator
Key
id
op
Key

②

Lexeme
b
)
int
k
k
=

Tokens
id
op
id
key
id
id
op

Q. GTU

W-22, Q - 2(c)

const h = 10;
if { a < h }

0 ++;
if (a < p) if (a == 5)
 Continue;
}

Lexeme	tokens
const	Keyword
h	identifier
=	operator
10	constant
;	operator
if	keyword
(operator
a	identifier
h	identifier
)	operator
{	operator
a	keyword
*	operator
[operator
++	operator
+	operator
;	operator
if	keyword
(operator
a	identifier
=	operator
;	operator

5

)

Continue

Q. G.T.U
W-23, Q-1(6)

```
void change (int c, int d)
{
    int m;
    m = c;
    c = d;
    d = m;
}
```

Ans

Lexeme	token	Lexeme	token
void	Keyword	c	id
change	Identifier	=	op
(op	d	id
int	key	;	op
c	id	d	id
)	op	=	op
int	key	m	id
d	id	;	op
)	op	;	op
{	op	;	op
int	key	int	id
m	id	m	id
;	op	;	op
m	id	z	op
z	op	c	id
c	op	;	op

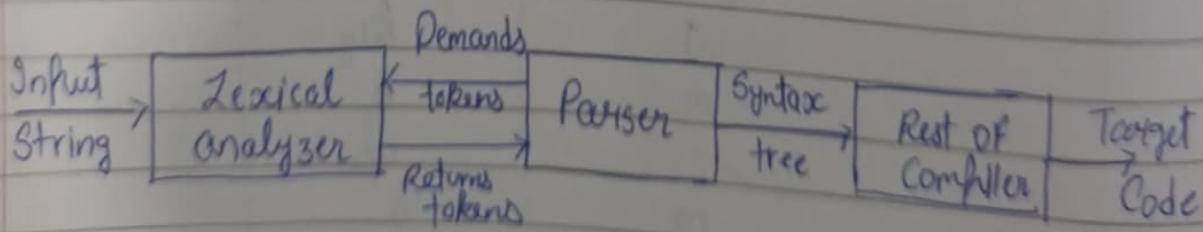
Q. What is Lexical analysis? Which are the tasks performed by lexical analyzer?

Ans Check Ch-1

Tasks performed by lexical analyzer

- 1) It produces stream of tokens
- 2) It eliminates blank and comments
- 3) It generates symbol table which stores the information about identifiers, constants encountered in the input
- 4) It keeps track of line numbers
- 5) It reports the error encountered while generating the tokens

- Lexical analyzer is the first phase of compiler
- The lexical analyzer reads the input source program from left to right one character at a time and generates the sequence of tokens
- Each token is a single logical unit such as identifier, keywords, operators and punctuation marks
- The role of lexical analyzer in the process of compilation as shown below



Q Define

- 1) Lexeme
- 2) Handle Pruning
- 3) Viable Prefixes

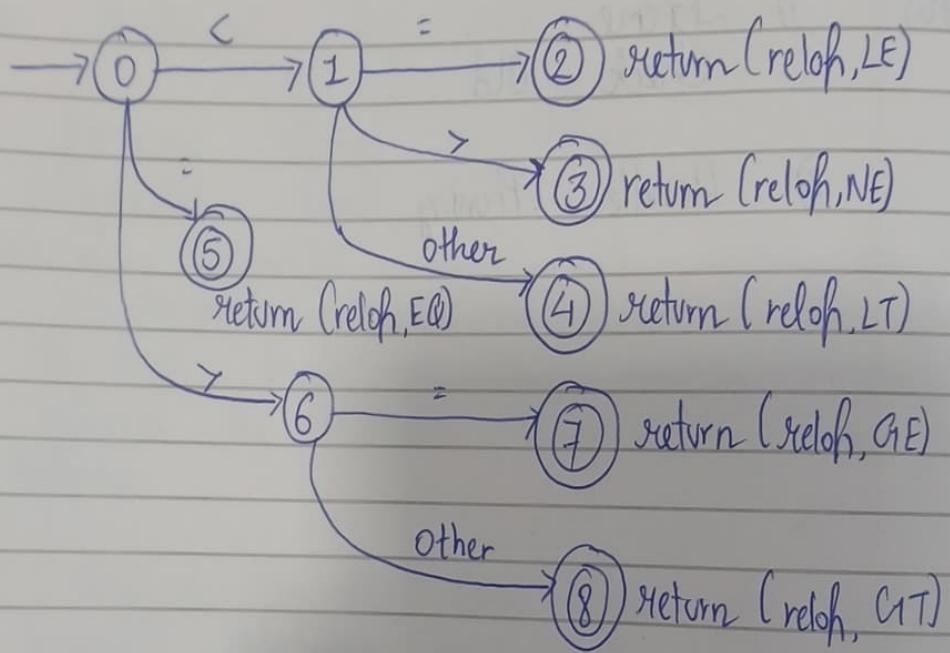
Ans

1) Lexeme
Check old

2) Handle Pruning

Q. Construct transition diagram for relational operators. Explain roles of assembler, loader, linker and preprocessor. [W-24, Q-2(c)]

Ans

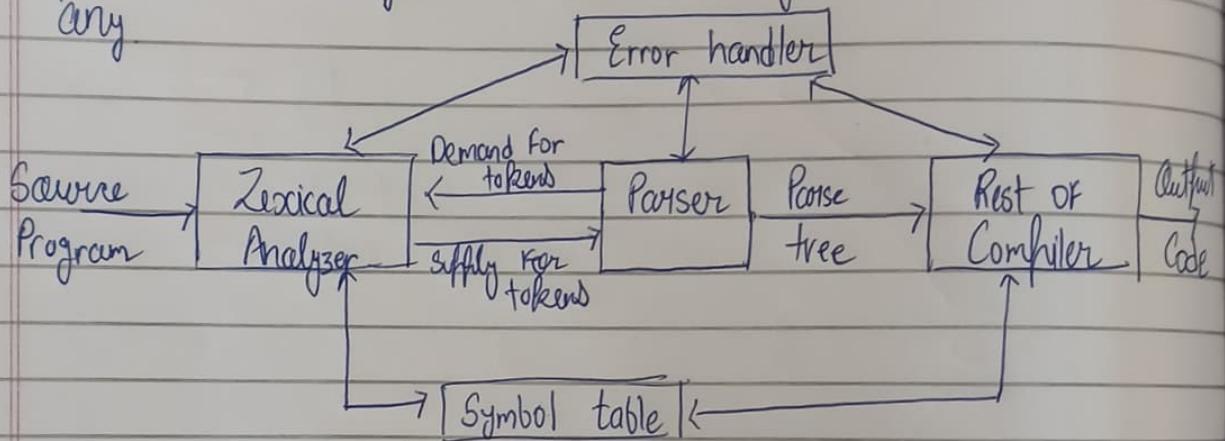


Q,

Ch-3 Syntax Analysis

o Role of Parser

The Parser collects sufficient number of tokens and builds a parse tree. Thus by building it, parser smartly finds the syntactical errors if any.



- Lexical Analyzer scans the input program and collects the tokens from it.
- On other hand Parser builds a parse tree using these tokens

o Context Free Grammar

$$G_1 = (V, T, P, S)$$

V = Set of non-terminals

T = " " Terminals

P = Set of Production Rules

S = Start Symbol

Non-terminal \rightarrow Non-terminals
or Non-terminal \rightarrow terminals

Derivation

- 1) Left Most Derivation
- 2) Right Most Derivation

Parse / Derivation tree

Root Node \Rightarrow Start Symbol

Internal / Parent Node \Rightarrow Non terminals

leaf nodes \Rightarrow terminals

Eg: $E \rightarrow E+E | E * E | (E) | id$

obtain Left most & right most derivation for string
id + id * id

Left Most Derivation

$$\begin{aligned}
 E &\rightarrow E+E & (\because E \rightarrow E+E) \\
 &\rightarrow id+E & (\because E \rightarrow id) \\
 &\rightarrow id+E * E & (\because E \rightarrow E * E) \\
 &\rightarrow id+id * E & (\because E \rightarrow id) \\
 &\rightarrow id+id * id & (\because E \rightarrow id)
 \end{aligned}$$

Right Most Derivation

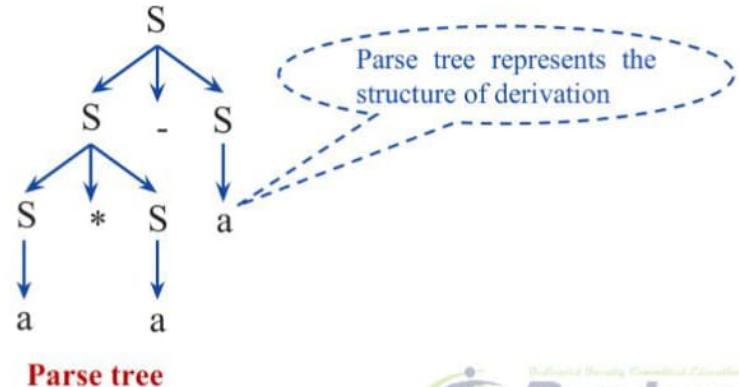
$$\begin{aligned}
 E &\rightarrow E+E \\
 &\rightarrow E+E * E & (\because E \rightarrow E+E) \\
 &\rightarrow E+E * id \\
 &\rightarrow E+id * id \\
 &\rightarrow id+id * id
 \end{aligned}$$

Leftmost derivation

- A derivation of a string W in a grammar G is a left most derivation if at every step the **left most non terminal** is replaced.
- Grammar: $S \rightarrow S+S \mid S-S \mid S^*S \mid S/S \mid a$ Output string: a^*a-a

S
 $\rightarrow \underline{S-S}$
 $\rightarrow \underline{S^*S-S}$
 $\rightarrow a^*\underline{S-S}$
 $\rightarrow a^*a\underline{-S}$
 $\rightarrow a^*a-a$

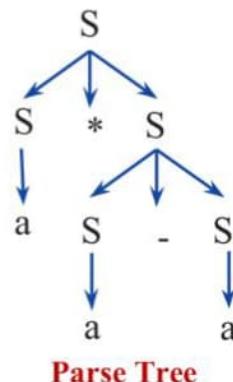
Leftmost Derivation



Rightmost derivation

- A derivation of a string W in a grammar G is a right most derivation if at every step the right most non terminal is replaced.
- It is also called canonical derivation.
- Grammar: $S \rightarrow S+S \mid S-S \mid S^*S \mid S/S \mid a$ Output string: a^*a-a

S
 $\rightarrow S^*\underline{S}$
 $\rightarrow S^*\underline{S-S}$
 $\rightarrow S^*\underline{S-a}$
 $\rightarrow S^*\underline{a-a}$
 $\rightarrow a^*\underline{a-a}$
Rightmost Derivation

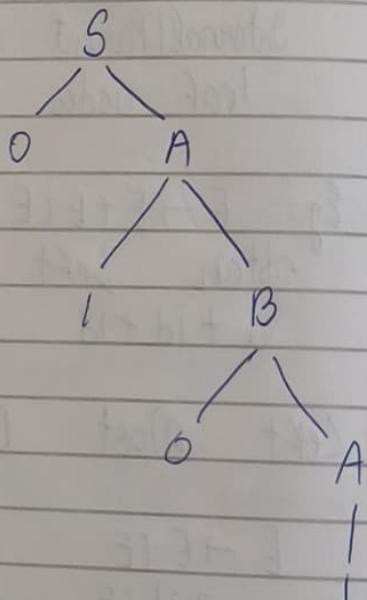


Eg: $S \rightarrow 0A|0B|0|1$
 $A \rightarrow 0S|1B|1$
 $B \rightarrow 0A|1S$

Construct LMD & Parse tree

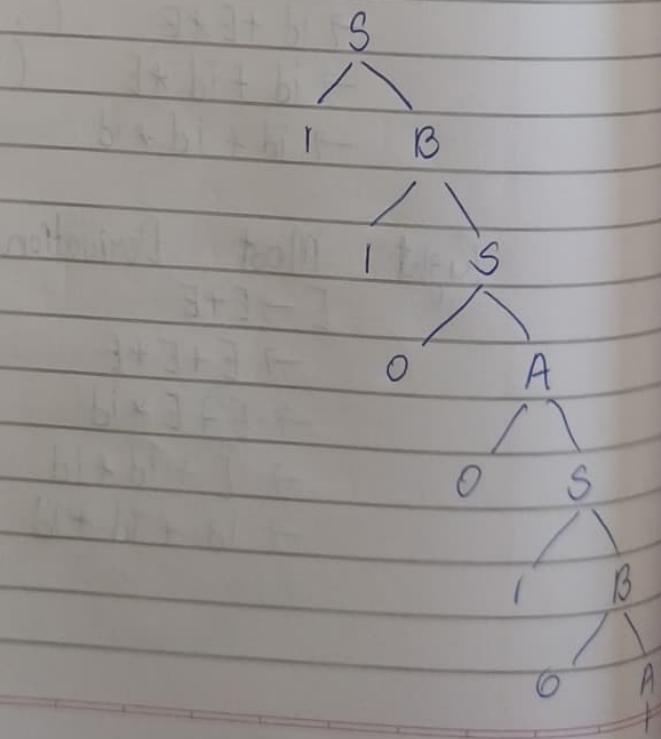
(i) 0|0|1

$S \rightarrow 0A$
 $S \rightarrow 0B$
 $S \rightarrow 0|0A$
 $S \rightarrow 0|0|1$



(ii) 1|0|0|0|1

$S \rightarrow 1B$
 $S \rightarrow 1|1S$
 $S \rightarrow 1|0A$
 $S \rightarrow 1|0|S$
 $S \rightarrow 1|0|0|B$
 $S \rightarrow 1|0|0|0A$
 $S \rightarrow 1|0|0|0|1$



Ambiguous Grammar

A grammar is said to be ambiguous if it generates more than one parse tree for corresponding input string.

Eg: $E \rightarrow E+E \mid E * E \mid (E) \mid id$

LMD

RMP

$$E \rightarrow E+E$$

$$\Rightarrow id+E * E$$

$$\Rightarrow id+id * E$$

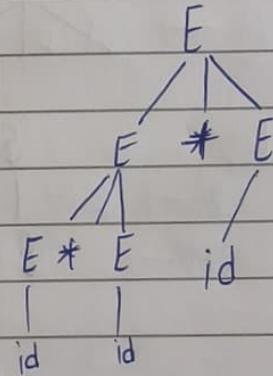
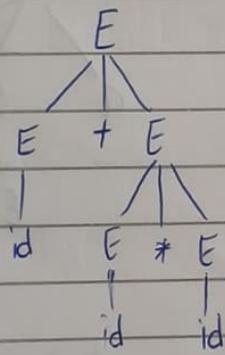
$$\Rightarrow id+id * id$$

$$E \rightarrow E+E$$

$$\rightarrow E + id * E$$

$$\rightarrow E + id * id$$

$$\rightarrow id + id * id$$



Eg: Show that following grammar is ambiguous

$$S \rightarrow aSbS$$

$$S \rightarrow bSas$$

$$S \rightarrow \epsilon$$

String:

$$S \rightarrow aSbS$$

$$S \rightarrow aSbS$$

$$S \rightarrow a b S a S b S$$

$$S \rightarrow a S b S$$

$$S \rightarrow a b \epsilon a \epsilon b S$$

$$\rightarrow a b a \epsilon b S$$

$$S \rightarrow a b a b \epsilon$$

$$\rightarrow a b a b \epsilon$$

$$S \rightarrow a b a b$$

$$\rightarrow a b a b$$

Ambiguity

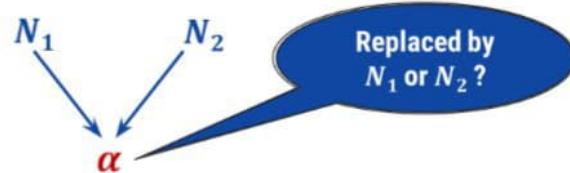
- In formal language grammar, ambiguity would arise if identical string can occur on the RHS of two or more productions.

- ▶ Grammar:

$$N_1 \rightarrow \alpha$$

$$N_2 \rightarrow \alpha$$

- ▶ α can be derived from either N_1 or N_2

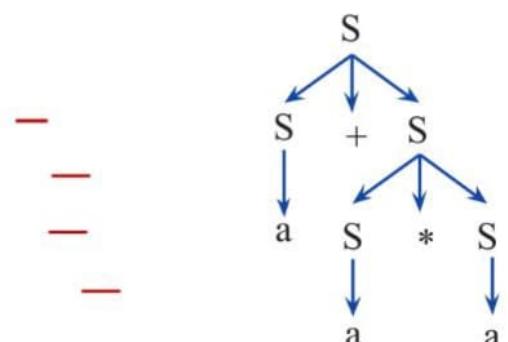
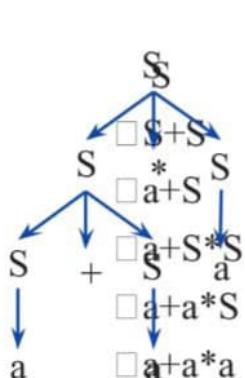
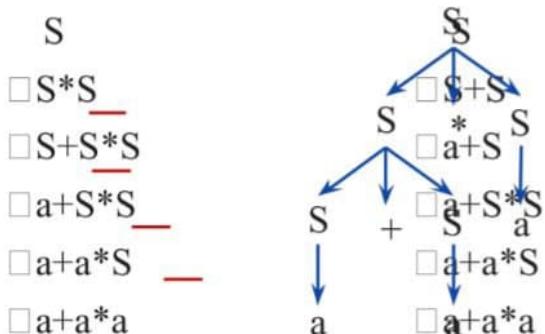


Ambiguous grammar

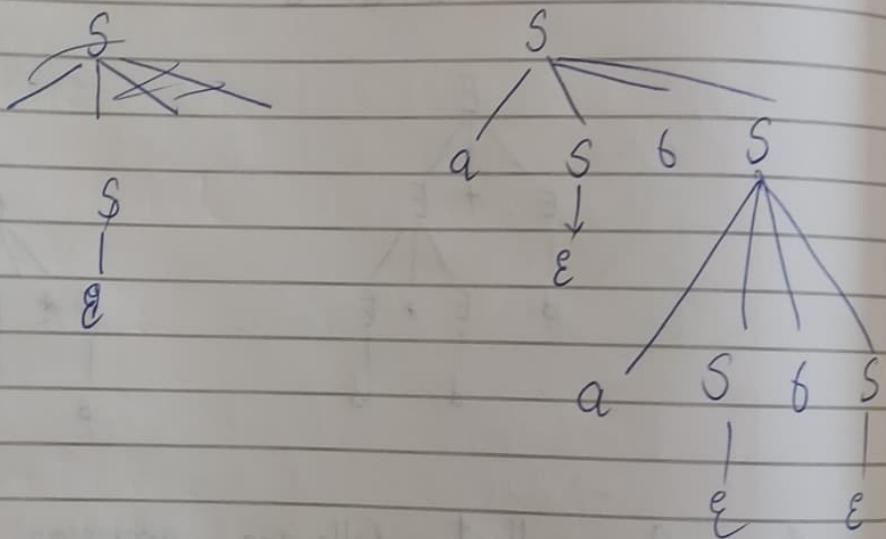
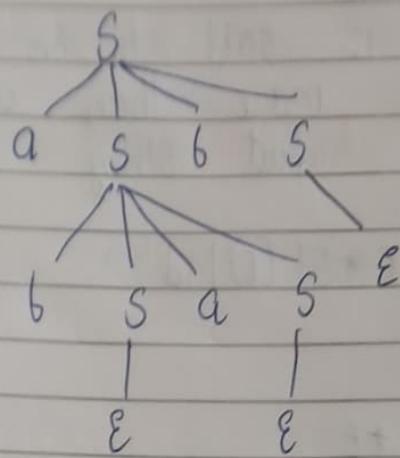
- Ambiguous grammar is one that produces more than one leftmost or more than one rightmost derivation for the same sentence.

Grammar: $S \rightarrow S+S | S^*S | (S) | a$

Output string: $a+a^*a$



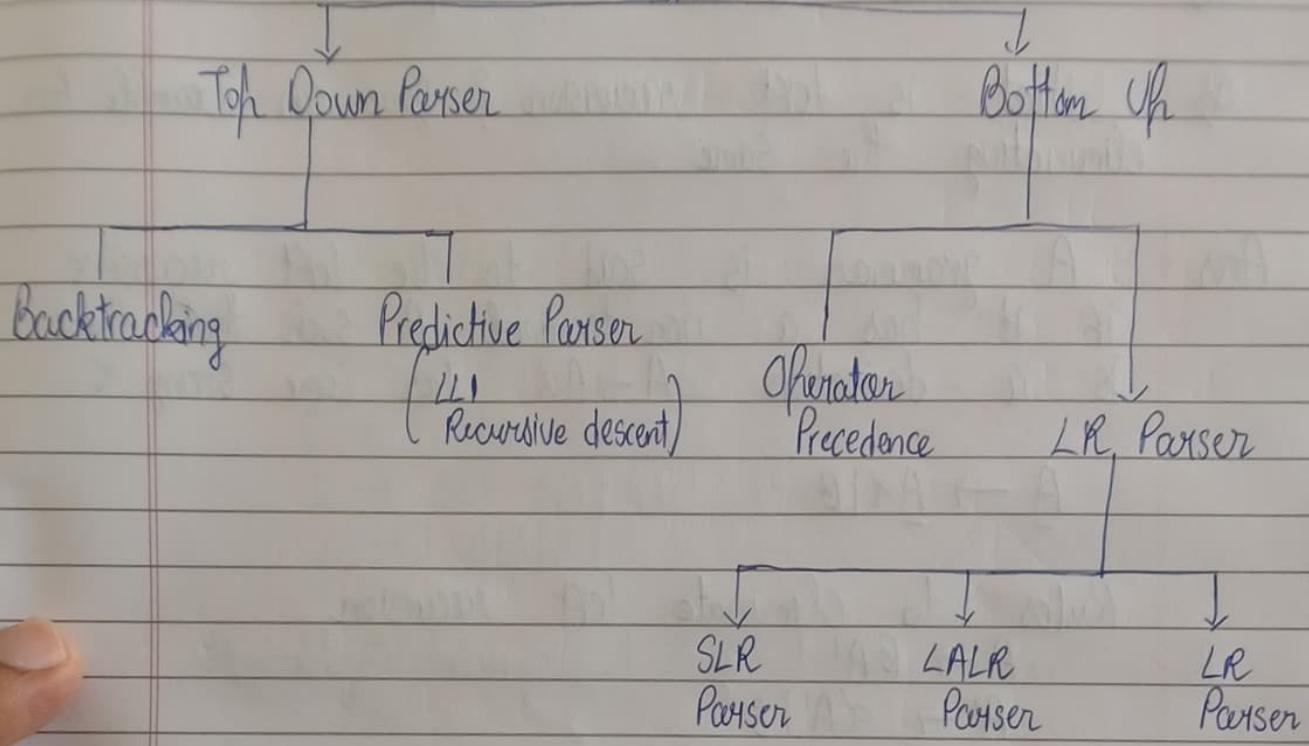
- Here, Two leftmost derivation for string $a+a^*a$ is possible hence, above grammar is ambiguous.



o Parsing

It is a technique that takes input string and produces output either a parse tree if string is valid sentence of grammar, or an error message, indicating that string is not a valid

TYPES OF PARSERS



Q, Differentiate Top-Down & Bottom Up Parsing

Top Down

- 1) Parse tree can be built from root to leaves
- 2) Simple to implement
- 3) Less efficient
- 4) Applicable to small class of languages
- 5) Eg: 1) Recursive descent
2) Predictive Parser

Bottom - Up

- 1) Parse tree is built from leaves to root
- 2) Complex
- 3) More Efficient
- 4) to broad class of languages
- 5) Eg: 1) Shift reduce
2) Operator Precedence
3) LR parser

Differentiate Parse tree & Syntax tree

Ans Check Q-4 of Chapter-1

Q What is left recursion? Give an example for eliminating the same

Ans A grammar is said to be left recursive if it has a non terminal A such that there is a derivation $A \rightarrow A\alpha$ for some string α

$$A \rightarrow A\alpha | \beta$$

Rules to eliminate left recursion

$$A \rightarrow BA'$$

$$A' \rightarrow \alpha A' | \epsilon$$

Eg:

$$E \rightarrow E + T | T$$

$$T \rightarrow T * F | F$$

$$F \rightarrow (E) | id$$

$$E \rightarrow E + T | T$$

$\cancel{\alpha}$ β

$$E \rightarrow TE'$$

$$E' \rightarrow +TE'| \epsilon$$

$$T \rightarrow T + F | F$$

α β

$$T \rightarrow FT'$$

$$T' \rightarrow *FT'| \epsilon$$

$$F \rightarrow (E) | id$$

$$E \rightarrow TE'$$

$$E' \rightarrow +TE'| \epsilon$$

$$T \rightarrow FT'$$

$$T' \rightarrow *FT'| \epsilon$$

Ex:

$$S \rightarrow \frac{S_0}{A} \frac{S_1 S_2}{\alpha} \frac{| \alpha}{B}$$

$$S \rightarrow 0 | S'$$

$$S' \rightarrow 0 S_1 S_2 | \epsilon$$

Eg:

$$S \rightarrow (L) | \alpha$$

$$L \rightarrow \frac{L_1}{A} \frac{S_1 S_2}{\alpha} \frac{| \alpha}{B}$$

$$S \rightarrow (L) | \alpha$$

$$L \rightarrow S | L'$$

$$L' \rightarrow , S L' | \epsilon$$

$$A \Rightarrow A\alpha_1 | A\alpha_2 | \dots | B_1 | B_2$$

then

$$Eg: A \rightarrow B_1 A' | B_2 A'$$

$$A' \rightarrow \alpha_1 A' | \alpha_2 A' | \epsilon$$

$$Eg: expr \rightarrow \underbrace{expr}_A + \underbrace{expr}_A | \underbrace{expr}_A * \underbrace{expr}_A | id_B$$

$$expr \rightarrow id \ expr'$$

$$expr' \rightarrow + expr' \ expr' | * expr \ expr' | \epsilon$$

$$Eg: S \rightarrow \underbrace{Sx}_{A \alpha_1} | \underbrace{Sb}_{A \alpha_2} | \underbrace{Sx}_{B_1} | \underbrace{a}_{B_2}$$

$$S \rightarrow x \ S' | XSS' | as'$$

$$S' \rightarrow x S' | Sb S' | \epsilon$$

Eg: $S \rightarrow Aa|b$
 $A \rightarrow Acl|sd|f$

Indirect Left recursion

$S \rightarrow Aa|b$
 $A \rightarrow Acl|Aad|bd|f$
 $A \rightarrow A_1 A_2 \quad \beta_1 \quad \beta_2$

$S \rightarrow Aa|b$
 $A \rightarrow bdA'$
 $A \rightarrow AC|Aa$
 $A \rightarrow bdA'|FA'$
 $A' \rightarrow CA'|adA'|e$

Q) Left Factoring (Recursive factoring)

$A \rightarrow \alpha\beta_1 | \alpha\beta_2 | \alpha\beta_3 | \dots Y_1 | Y_2 \dots$

then we replace it with

$A \rightarrow \alpha A' | Y_1 | Y_2$
 $A' \rightarrow \beta_1 | \beta_2 | \beta_3 \dots$

Eg: I

$S \rightarrow iEts | iEt \underset{\beta_1}{s} e s \underset{\beta_2}{a}$
 $E \rightarrow b$

$\theta \rightarrow iEts' | a$
 $S' \rightarrow S \underset{\beta_1}{s} e s$

$S \rightarrow iEts' | a$
 $S' \rightarrow E | es$

Eg:2

$$A \rightarrow aAB|aA|a$$

$$B \rightarrow \underset{a}{b} \underset{\beta_1}{B} \underset{a}{b}$$

$$A \rightarrow aAB|aA|a$$

$$\underset{\alpha}{a} \underset{\beta_1}{B} \underset{\gamma}{a}$$

$$A \rightarrow / a A' | a$$

$$A' \leftarrow B | \epsilon$$

$$A \rightarrow \underset{a}{a} \underset{\beta_1}{AB} | \underset{a}{a} \underset{\beta_2}{A} | \underset{a}{a} \underset{\beta_3}{}$$

$$A \rightarrow a A'$$

$$A' \rightarrow AB | A | \epsilon$$

$$B \rightarrow b B'$$

$$B' \rightarrow B | \epsilon$$

Eg:3

$$X \rightarrow \underset{a}{X} + \underset{\beta_1}{X} | \underset{a}{X} * \underset{\beta_2}{X} | D Y$$

$$D \rightarrow 1 | 2 | 3$$

$$X \rightarrow X X' | D$$

$$X' \rightarrow + X | * X$$

$$D \rightarrow 1 | 2 | 3$$

Eg:4

$$E \rightarrow T + E | T$$

$$T \rightarrow \text{int} | \text{int} * T | (E)$$

$$E \rightarrow T E'$$

$$E' \rightarrow + E | \epsilon$$

$$T \rightarrow \text{int} T | (E)$$

$$T' \rightarrow \epsilon | * T$$

- o First & Follow
- o Rules to compute First or Non-Terminal
 - 1) If $A \rightarrow a\alpha$, $\alpha \in (V \cup T)^*$
then $\text{First}(A) = \{a\}$
 - 2) If $A \rightarrow \epsilon$ then $\text{First}(A) = \{\epsilon\}$
 - 3) if $A \rightarrow BC$ then
 $\text{First}(A) = \text{First}(B)$ if $\text{First}(B)$ doesn't contain ϵ
 if $\text{First}(B)$ contains ϵ then
 $\text{First}(A) = \text{First}(B) \cup \text{First}(C)$
- o Rules for finding follow
 - 1) If 'S' then $\text{Follow}(S) = \{\$\}$
 - 2) If $A \rightarrow \alpha B \beta$ then $\text{Follow}(B) = \text{First}(\beta)$
 if $\text{First}(\beta)$ does not contain epsilon (ϵ)
 - 3) if $A \rightarrow \alpha \beta$ then $\text{Follow}(\beta) = \text{Follow}(A)$
 - 4) If $A \rightarrow \alpha B \beta$ where $B \rightarrow \epsilon$
 then $\text{Follow}(B) = \text{Follow}(A)$

Ex:

$$E \rightarrow TE' \epsilon$$

$$E' \rightarrow +TE' | \epsilon$$

$$T \rightarrow FT'$$

$$T' \rightarrow *FT' | \epsilon$$

$$F \rightarrow (E) | id$$

$$\text{First}(E) = \{ (, id\}$$

$$\text{First}(E') = \{ +, \epsilon\}$$

$$\text{First}(T) = \{ (, id\}$$

$$\text{First}(T') = \{ *, \epsilon\}$$

$$\text{First}(F) = \{ (, id\}$$

$$\text{Follow}(E) = \{ \$,) \}$$

$$\text{Follow}(E') = \{ \$,) \}$$

$$\text{Follow}(T) = \{ +, \epsilon \} \quad \{ +, \$,) \} \quad \{ +, (, id\} \quad \{ +, \$,) \}$$

$$\text{Follow}(T') = \{ +, \epsilon \} \quad \{ +, \$,) \} \quad \{ +, \$,) \}$$

$$\text{Follow}(F) = \{ *, \epsilon \} \quad \{ *, +, \$,) \}$$

Eg: $S \rightarrow ABCDE$

$$A \rightarrow a| \epsilon$$

$$B \rightarrow b| \epsilon$$

$$C \rightarrow c$$

$$D \rightarrow d| \epsilon$$

$$E \rightarrow e| \epsilon$$

$$S \rightarrow A C O E$$

$$S \rightarrow E B C O E$$

$$S \rightarrow C O E$$

$$S \rightarrow A B$$

First

$$S = \{ a, b, c \}$$

$$A = \{ a, \epsilon \}$$

$$B = \{ b, \epsilon \}$$

$$C = \{ c \}$$

$$D = \{ d, \epsilon \}$$

$$E = \{ e, \epsilon \}$$

Follow

$$S = \{ \$ \}$$

$$A = \{ b, c \}$$

$$B = \{ c \}$$

$$C = \{ d, e, \$ \}$$

$$D = \{ e, \$ \}$$

$$E = \{ \$ \}$$

$$S \rightarrow Bb|Cd$$

$$B \rightarrow aB|E$$

$$C \rightarrow cC|E$$

First

$$S = \{a, b, c, d\}$$

$$B = \{a, E\}$$

$$C = \{c, E\}$$

Follow

$$S = \{\$\}$$

$$B = \{b\}$$

$$C = \{d\}$$

Eg:

$$S \rightarrow ACB|CBB|Ba$$

$$A \rightarrow da|BC$$

$$B \rightarrow g|E$$

$$C \rightarrow h|E$$

$$S \rightarrow ACB$$

$$S \rightarrow CBB$$

$$S \rightarrow Ba$$

$$A \rightarrow BC$$

First

$$S = \{d, a, g, h, b\}$$

$$A = \{d, g, h, E\}$$

$$B = \{g, E\}$$

$$C = \{h, E\}$$

Follow

$$S = \{\$\}$$

$$A = \{h, g, E, \$\}$$

$$B = \{\$, a, h, b\}$$

$$C = \{\$, a, h,$$

$$C = \{g, \$, b, h\}$$

$$\text{Eg: } S \rightarrow aABb$$

$$A \rightarrow c|E$$

$$B \rightarrow d|E$$

First

$$S = \{a\}$$

$$A = \{c, E\}$$

$$B = \{d, E\}$$

Follow

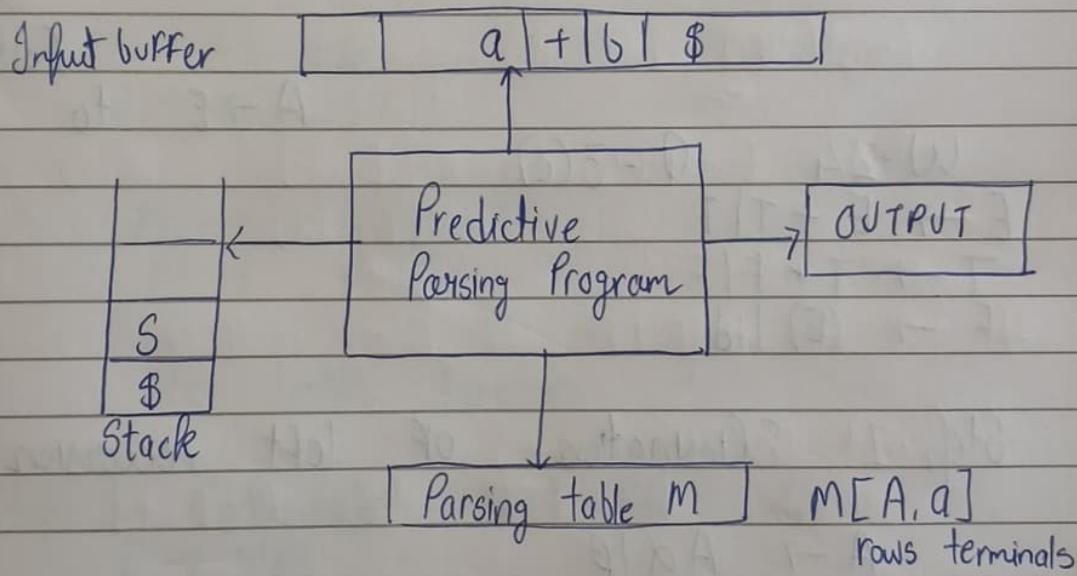
$$\text{Follow}(S) = \$$$

$$\text{Follow}(A) = \{c, b\}$$

$$\text{Follow}(B) = \{b\}$$

o LL(1) Parser or Predictive Parser or Non-recursive descent parser

- 1) First L indicates input is scanned from left to right
- 2) The second L means it uses leftmost derivation for input string
- 3) 1 means it uses only input symbol to predict the parsing process



Steps to construct LL(1) parser

- 1) Remove left recursion / Perform left factoring (if any)
 - 2) Compute First & Follow of non terminals
 - 3) Construct Predictive parsing table
 - 4) Parse the input string using parsing table
- OR
- 4) Check whether iIP string is accepted by parser or not

Construction of Parse table

$A \rightarrow \alpha$

1) $A \rightarrow \alpha$

First (α)

$\hookrightarrow a$

Add $A \rightarrow \alpha$ to $m[A, a]$

2) if First (α) contains ϵ or $A \rightarrow \epsilon$



Follow (A) = b

$A \rightarrow \epsilon$ to $m[A, b]$

Q,

W-24 Q - 3(c)
 $E \rightarrow E + T \mid T$
 $T \rightarrow T * F \mid F$
 $F \rightarrow (E) \mid id$

Step: 1 Elimination of left recursion

$A \rightarrow Ad \mid \beta$

$A \rightarrow \beta A'$
 $A' \rightarrow d A' \mid \epsilon$

$\frac{E}{A} \rightarrow \frac{E}{A} + T \mid T$
 $\frac{d}{\beta}$

$E \rightarrow TE'$
 $E' \rightarrow +TE' \mid \epsilon$

$T \rightarrow T * F \mid F$
 $\frac{T}{d} \frac{*}{\beta} \frac{F}{P}$

$$\begin{array}{l} T \rightarrow FT' \\ T' \rightarrow *FT'| \epsilon \end{array}$$

$F \rightarrow (E) | id$ No left recursion

After eliminating left recursion

$$E \rightarrow TE'$$

$$E' \rightarrow +TE'| \epsilon$$

$$T \rightarrow FT'$$

$$T \rightarrow *FT'| \epsilon$$

$$F \rightarrow (E) | id$$

Step: 2 Eliminate of left factoring

$$A \rightarrow \alpha\beta_1 | \alpha\beta_2 | Y_1 | Y_2$$

$$A \rightarrow \alpha A' | Y_1 | Y_2$$

$$A' \rightarrow \beta_1 | \beta_2$$

No left factors

Step: 3 Calculate First & Follow

$$E \rightarrow TE'$$

$$E' \rightarrow +TE'| \epsilon$$

$$T \rightarrow FT'$$

$$T' \rightarrow *FT'| \epsilon$$

$$F \rightarrow (E) | id$$

First

$$E = \{ (, id \}$$

$$E' = \{ +, \epsilon \}$$

$$T = \{ (, id \}$$

$$T' = \{ *, \epsilon \}$$

$$F = \{ (, id \}$$

Follow

$$E = \{ \$, ? \}$$

$$E' = \{ \$, ? \}$$

$$T = \{ +, ?, \$, ? \}$$

$$T' = \{ +, ?, \$, ? \}$$

$$F = \{ *, +, \$, ? \}$$

Step: 4

Construction of Parsing table

	+	*	()	id	\$
E			$E \rightarrow TE'$		$E \rightarrow TE'$	
E'	$E' \rightarrow +TE'$		$E' \rightarrow \epsilon$			$E' \rightarrow \epsilon$
T			$T \rightarrow FT'$		$T \rightarrow FT'$	
T'	$T' \rightarrow *FT'$	$T' \rightarrow FT'$		$T' \rightarrow *FT'$		$T' \rightarrow *FT'$
F			$F \rightarrow (E)$		$F \rightarrow id$	

1) $\frac{E}{A} \rightarrow \frac{T}{\alpha} E'$

$$\text{First}(TE') = \{ (, id \}$$

Add $E \rightarrow TE'$ to $M[E, (]$
 $M[E, id]$

2) $\frac{E'}{A} \rightarrow \frac{+}{\alpha} TE' \mid \epsilon$

2) $E' \rightarrow +TE' \mid \epsilon$

$$\text{First}(+TE') = \{ + \}$$

Add $E' \rightarrow +TE'$ to $M[E', +]$

$\text{First}(E')$

$$E' \rightarrow \epsilon$$

$$\text{Follow}(E') = \{ \$,) \}$$

Add $E' \rightarrow \epsilon$ to $M[E', \$]$
 $M[E',)]$

3) $T \rightarrow \frac{FT'}{\alpha}$

$$\text{First}(FT') = \{ (, id \}$$

Add $T \rightarrow FT'$ to $M[T, C]$
 $M[E, id]$

4) $T' \rightarrow *FT'| \epsilon$

$T' \rightarrow *FT'$
First ($*FT'$) = { $*$ }

Add $T' \rightarrow *FT'$ to $M[T', *]$

$T' \rightarrow \epsilon$
Follow (T') = {+, \$,)} \cup

Add to $M[F, f]$, $M[T', \$]$, $M[T',)]$

5) $F \rightarrow (E) | id$

First ((E)) = { $($ }

Add $F \rightarrow (E)$ to $M[F, C]$

$F \rightarrow id$
First (id) = {id}

Add $F \rightarrow id$ to $M[F, id]$

Step: 5

Let string be id + id \$

Stack
\$E

Input String
id + id \$
↑

Action
E → TE'

\$E'T

id + id \$

T → FT'

\$E'T'F

id + id \$

F → id

\$E'T'id
↑

id + id \$

hoh

Same then perform pop

\$E'T'

+ id \$

T' → E

\$E'

+ id \$

E' → TE'

\$E'T +

+ id \$

hoh

\$E'T

id \$

T → FT'

\$E'T'F

id \$

F → id

\$E'T'

\$

hoh

\$E'

\$

T' → E

\$E'

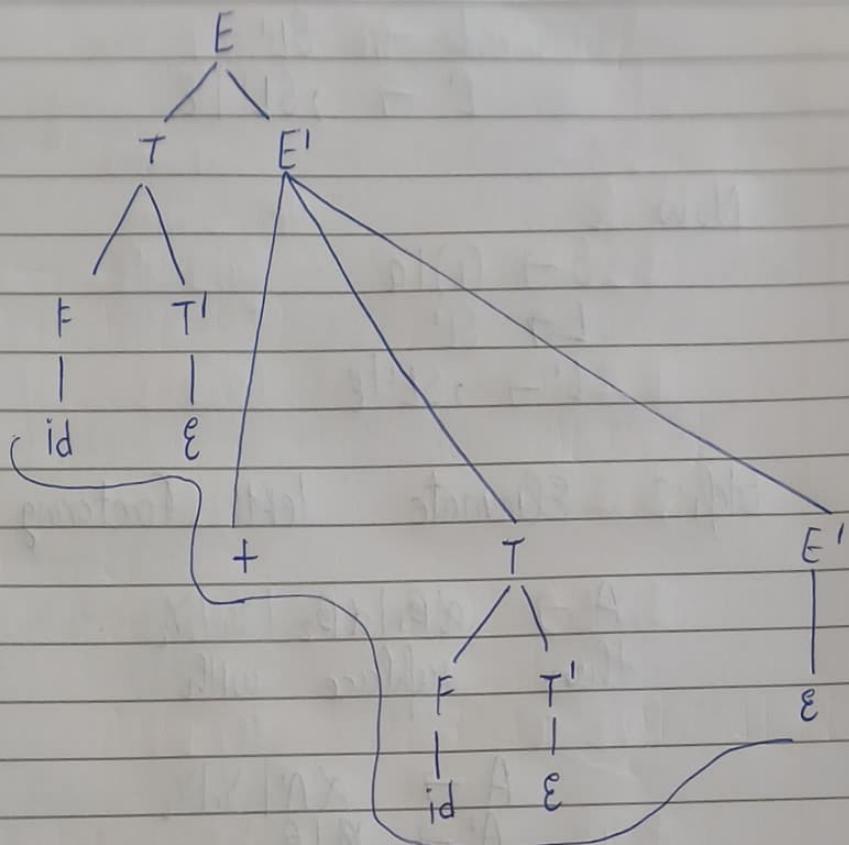
\$

E' → E

\$

\$

Accepted



$\text{id } \epsilon + \text{id} \epsilon \epsilon$
 $\Rightarrow \text{id} + \text{id}$

Eg: 2

$$S \rightarrow (L) \mid a$$

$$L \rightarrow L, S \mid S$$

Step: I

Elimination of left recursion

$$A \rightarrow \alpha A \beta \mid \beta$$

then

$$A \rightarrow \beta A'$$

$$A' \rightarrow \alpha A' \mid \epsilon$$

$$S \rightarrow (L) \mid a$$

$$L \rightarrow \frac{1}{\alpha} \frac{S}{\alpha} \mid S \beta$$

$$\begin{aligned} L &\rightarrow SL' \\ L' &\rightarrow , SL' | \epsilon \end{aligned}$$

Now

$$\begin{aligned} S &\rightarrow (L) | a \\ L &\Rightarrow SL' \\ L' &\rightarrow , SL' | \epsilon \end{aligned}$$

Step: 2 Eliminate left factoring

$$\begin{aligned} A &\rightarrow \alpha \beta_1 | \alpha \beta_2 | Y_1 | Y_2 \\ \text{then} &\quad \text{replace with} \end{aligned}$$

$$\begin{aligned} A &\rightarrow \alpha A' | Y_1 | Y_2 \\ A' &\rightarrow \beta_1 | \beta_2 \end{aligned}$$

No left factoring

Step: 3 Find First & Follow

NT	First	Follow
S	{(, a)}	{\$,), }}
L	{(, a)}	{)}
L'	{, ε}	{)}

$$\begin{aligned} S &\rightarrow (L) | a \\ L &\Rightarrow SL' \\ L' &\rightarrow , SL' | \epsilon \end{aligned}$$

Step: 4 Construction of Parse table

	()	,	a	\$
S	$S \rightarrow (L)$			$S \rightarrow @$	
L	$L \rightarrow SL'$			$L \rightarrow SL'$	
L'		$L' \rightarrow , SL'E$	$L' \rightarrow , SL'$		

1) $S \rightarrow (L) | a$

$$S \rightarrow (L)$$

$$\text{First}(S) = \{\emptyset\}$$

Add $S \rightarrow (L)$ to $M[S, \emptyset]$

$$\text{Follow}(a) = \{q_5\}$$

2) $L \rightarrow SL'$

$$\text{First}(SL') = \{(, q_3\}$$

3) $L' \rightarrow , SL'E$

$$\text{First}(, SL') = \{\}\}$$

$$L' \rightarrow E$$

$$\text{Follow}(L') = \{\}\}$$

2) String be (a) \$

Stack	IP String	Action
\$ S	(a) \$	$S \rightarrow (L)$
\$) L ((a) \$	push
\$) L	a) \$	$L \rightarrow SL'$
\$) L' S	a) \$	$S \rightarrow (L)$
\$) L' a	a) \$	push
\$) L') \$	$L' \rightarrow \epsilon$
\$)) \$	push
\$	\$	accepted

Example : 3

input string = "aabbb"

$S \rightarrow AAB \mid BAE$
 $A \rightarrow AAB \mid E$
 $B \rightarrow BB \mid E$

Step 1 & Step 2

No need bro

	First	Follow
S	{a, b, ε}	{\$}
A	{a, ε}	{b, \$}
B	{b, ε}	{B}

	a	b	\$
S	$S \rightarrow aAB$	$S \rightarrow bA$	$S \rightarrow \epsilon$
A	$A \rightarrow aAb$	$A \rightarrow \epsilon$	$A \rightarrow \epsilon$
B		$B \rightarrow bB$	$B \rightarrow \epsilon$

1) $S \rightarrow aAB \mid bA \mid \epsilon$

$S \rightarrow aAB$

First(aAB) = {a}

$S \rightarrow bA$

First(bA) = {b}

$S \rightarrow \epsilon$

Follow(S) = {\$}

2) $A \rightarrow aAb \mid \epsilon$

$A \rightarrow aAb$

First(aAb) = {a}

$A \rightarrow \epsilon$

Follow(A) = {b, \$}

3) $B \rightarrow bB \mid \epsilon$

$B \rightarrow bB$

First(bB) = {b}

$B \rightarrow \epsilon$
Follow(B) = { \$ }

Stack
\$ \$

input string
aabb\$

action
 $S \rightarrow aAb$

\$ \$ BAa

aabb\$

pop

\$ \$ BA

aabb\$

$A \rightarrow aAb$

\$ B b Aa

aabb\$

pop

\$ B b A

bbs

$A \rightarrow \epsilon$

\$ B b

bbs

pop

\$ B

b \$

$B \rightarrow bB$

\$ Bb

b \$

pop

\$ B

\$

$B \rightarrow \epsilon$

\$

\$

accepted

Example: 4

$S \rightarrow tEtS \quad tEtSeSa$
 $E \rightarrow b$

Step 1: No Left Recursion

Step 2

$$S \rightarrow iEtS \quad | \quad EtSe \quad | \quad a$$

$\alpha \quad \beta \quad \alpha \quad \beta \quad \gamma$

$$S \rightarrow iEtSS' \quad | \quad a$$

$$S' \rightarrow e \quad | \quad es$$

$$E \rightarrow b$$

	First	Follow
S	{i, a}	{e, \$}
S'	{e, es}	{e, \$}
E	{b}	{t}

Step: 4

	i	a	e	b	\$	t
S	$S \rightarrow iEtSS'$	$S \rightarrow a$				
S'			$S' \rightarrow e$			$S \rightarrow e$
E						

i) $S \rightarrow iEtSS' \quad | \quad a$

At is Not
LL(1) Grammar

a) $S \rightarrow iEtSS'$

First ($iEtSS'$) = i

ii) $S \rightarrow a$

ii) $S' \rightarrow e \quad | \quad es$

follow (S') = {e, \$}

First (es) = {e}

Q 6-25 CTU Q-2 (c)

$$S \rightarrow aABb$$

$$A \rightarrow c\epsilon$$

$$B \rightarrow d\epsilon$$

Step: 1 Eliminate Left recursion

Not there

Step: 2 Eliminate Left Factoring

Not there

Step: 3 Find First & Follow

	First	Follow
S	{a}	{\\$}
A	{c, ε}	{d, b}
B	{d, ε}	{e}

Step: 4 Parsing table

	a	b	c	d	\$
S	$S \rightarrow aABb$				
A		$A \rightarrow \epsilon$	$A \rightarrow c$	$A \rightarrow \epsilon$	
B				$B \rightarrow d$	$B \rightarrow \epsilon$

Step: 1

$$S \rightarrow aABb$$

$$1) \text{First}(aABb) = a$$

2) $A \rightarrow C|E$

a) $\text{First}(C) = C$

b) $\text{Follow}(A) = \{d, e\}$

3) $B \rightarrow d|e$

a) $\text{First}(d) = d$

b) $\text{Follow}(B) = \{e\}$

Q1, find out First & Follow set for all Non
Terminals

W-23, OR Q-3(b) ATU

$S \rightarrow I A B | E$

$A \rightarrow I A C | O C$

$B \rightarrow O S$

$C \rightarrow I$

NT	First	Follow
S	$\{I, \$\}$	$\{\$\}$
A	$\{I, O\}$	$\{I, O\}$
B	$\{O\}$	$\{\$\}$
C	$\{I\}$	$\{I, O\}$

Recursive Descent Parser

1) Non-Terminal
 \hookrightarrow Call

2) if input is terminal then compare terminal with corresponding input symbol
 if they are same input ++

3) If NT produces more than one production then all production rules should be written in corresponding function

4) No need to declare any main function or variable

Eg: $E \rightarrow iE'$

$$E' \rightarrow +iE'|E$$

i) Define procedure for E

$E()$
 {

if (input == 'i')
 input++;
 EPRIME();

}
 EPRIME()

{
 if (input == '+')
 input++;

```

if (input == 'i')
{
    input +=;
    EPRIME();
}
else
    return;
}

```

2) $E \rightarrow TE'$
 $E' \rightarrow +TE' | \epsilon$
 $T \rightarrow FT'$
 $T' \rightarrow +FT' | \epsilon$
 $F \rightarrow (E) | id$

$E()$
 $\{$
 $T();$
 $EPRIME();$
 $\}$

$EPRIME()$
 $\{$

if (input == '+')
 $\{$

input +=;
 $T();$

EPRIME();

$\}$

else

return;

$\}$

$I()$
 $\{$
 $F();$
 $TPRIME();$
 $\}$

$TPRIME()$
 $\{$

if (input == '*')
 $\{$

input +=;
 $F();$
 $TPRIME();$

$\}$

else

return;

H()

{

if (input == '(')

{

input ++;

E();

if (input == ')')

input ++;

}

else if (input == 'id')

input ++;

}

Q) Implement the following grammar using Descent Parser

S → Aa | bAc | bBa

A → d

B → d

Procedure S()

{

S → bAc | bBa

if (lookahead == 'b')

{

B();

if (lookahead == 'c')

match('c')

else if (lookahead == 'a')

match('a')

else if (lookahead == '\$')

{

declare SUCCESS;

else

{ // S → Aa

A();

if (lookahead = 'a')

match ('a');

}

}

Procedure (A)

A → d

{

if (lookahead = 'd')

match ('d')

else

error();

}

Procedure (B)

{

if (lookahead = 'd')

match ('d')

else

error();

}

Q) Explain Recursive descent parsing technique
with suitable example

2)	In ambiguous grammar there are less number of non-terminals.	In unambiguous grammar there are more number of non-terminals.
3)	The length of generated parse tree is less.	The length of generated parse tree is large.
4)	For example - $E \rightarrow E + E \mid E * E \mid id$.	For example - $E \rightarrow E + T$ $E \rightarrow T$ $T \rightarrow T * F$ $T \rightarrow F$ $F \rightarrow id$

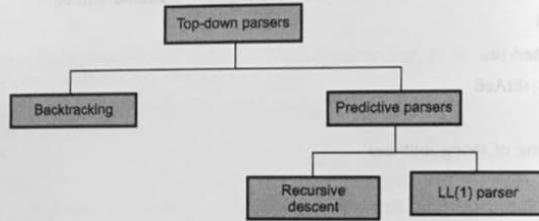


Fig. 3.3.6 Types top - down parsers

There are two types by which the top-down parsing can be performed.

1. Backtracking
2. Predictive parsing

A backtracking parser will try different production rules to find the match for the input string by backtracking each time. The backtracking is powerful than predictive parsing. But this technique is slower and it requires exponential time in general. Hence backtracking is not preferred for practical compilers.

As the name suggests the predictive parser tries to predict the next construction using one or more lookahead symbols from input string. There are two types of predictive parsers :

1. Recursive descent
2. LL(1) parser.

Let us discuss these types along with some examples.

3.3.2 Recursive Descent Parser

A parser that uses collection of recursive procedures for parsing the given input string is called **Recursive Descent (RD) Parser**. In this type of parser the CFG is used to

build the recursive routines. The R.H.S. of the production rule is directly converted to a program. For each non-terminal a separate procedure is written and body of the procedure (code) is R.H.S. of the corresponding non-terminal.

Basic steps for construction of RD parser

1. The R.H.S. of the rule is directly converted into program code symbol by symbol.
2. If the input symbol is non-terminal then a call to the procedure corresponding to the non-terminal is made.
3. If the input symbol is terminal then it is matched with the lookahead from input. The lookahead pointer has to be advanced on matching of the input symbol.
4. If the production rule has many alternates then all these alternates has to be combined into a single body of procedure.
4. The parser should be activated by a procedure corresponding to the start symbol.

Let us take one example to understand the construction of RD parser. Consider the grammar having start symbol E.

$$E \rightarrow num T$$

$$T \rightarrow * num T \mid \epsilon$$

```

procedure E
{
    if lookahead = num then
    {
        match(num);
        T; /* call to procedure T */
    }
    else
        error;
    if lookahead = $
    {
        declare success; /* Return on success */
    }
    else
        error;
}/*end of procedure E*/
procedure T
{
    if lookahead = '*'
    {
        match('*');
        if lookahead ='num'
        {
            match(num);
        }
    }
}
  
```

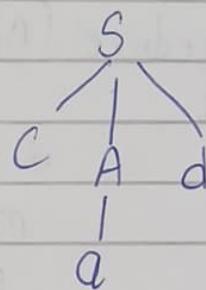
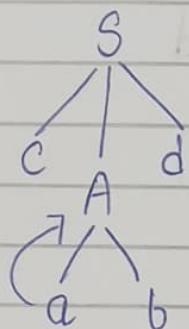
o Backtracking

Eg 1:

$$S \rightarrow cAd$$

$$A \rightarrow abla$$

"cad"



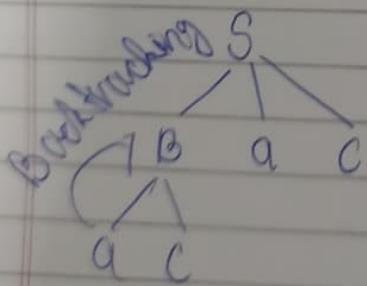
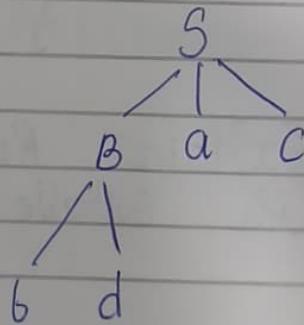
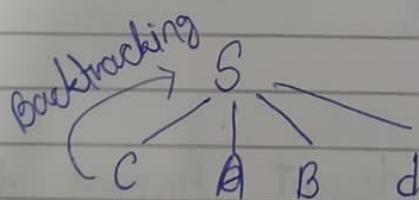
Eg: 2

$$S \rightarrow cABd \mid Bac$$

$$A \rightarrow Bcd \mid abc$$

$$B \rightarrow ac \mid da \mid bd$$

"bdac"



Start-Symbol (Root) Node

Bottom-Up Parsing



Bottom (leaves) → Input String (Leaves) Node

Eg

$$\begin{aligned} S &\rightarrow aABe \\ A &\rightarrow Abc|b \\ B &\rightarrow d \end{aligned}$$

input string "abbcde"

a bbcd e (A → b) Handle

a Abcd e (Abc → A) Handle

a Ade (d → B) Handle

a ABe (S → aABe)

S

Process of reducing input string to the starting symbol of the grammar is called Bottom-Up Parsing

S

$$\begin{aligned} S &\rightarrow aABe \\ &\rightarrow aAbe \\ &\rightarrow aAbcde \\ &\rightarrow abbcde \end{aligned}$$

Eg:

$$\begin{array}{l} E \rightarrow E + T \mid T \\ T \rightarrow T * F \mid F \\ F \rightarrow (E) \mid id \end{array}$$

$id * id$

$$\begin{array}{ll} id * id & (F \rightarrow id) \\ F * id & (T \rightarrow F) \\ F + id & (F \rightarrow id) \\ T * F & (T \rightarrow T + F) \\ T & (E \rightarrow T) \\ E & \end{array}$$

O Handle & Handle Pruning [G7v]

1) Handle

→ A "handle" of a string is a substring of the string that matches the right side of a production and whose reduction of the non-terminal of production is one step along the reverse of Rightmost Derivation

2) Handle Pruning

The process of discovering a handle and reducing it to appropriate left hand side non-terminal is called handle pruning

$$\begin{array}{l} S \rightarrow aABe \\ A \rightarrow Abelb \\ B \rightarrow d \end{array}$$

Handles during parsing of abbcde

Right	Selected From	Handle	Reducing Production
abbcde		b	A \rightarrow b
aAbcde		Abc	A \rightarrow Abc
aAde		d	B \rightarrow d
aABe		aABe	S \rightarrow aABe
S			

0 Shift Reduce Parser (SRP)
 \rightarrow Stack , input buffer
 Actions of SRP

- 1) Shift
- 2) Reduce
- 3) Accept
- 4) Error

Eg:

$$\begin{array}{l} E \rightarrow E + T \mid T \\ T \rightarrow T * F \mid F \\ F \rightarrow (E) \mid \text{lid} \end{array}$$

Stack

E → E(t)
T → T(t)
E → (t) | t

Page No.
Date

id * b

Stock	Input Buffer	Action
\$	id * \$	Shift
\$ id	* id \$	Reduce by S → id
\$ F	* id \$	Reduce T → F
\$ T	* id \$	Shift
\$ E * id		
\$ T *	id \$	Shift
\$ T * id	\$	reduce S → id
\$ T * F	\$	reduce T → F or
\$ T	\$	Reduce T → E
\$ E	\$	Accepted

- i) Shift - reduce conflict
- ii) Sh. reduce - reduce conflict

Ex 2 S → (L) | a
L → L, SIS

(a, (a,a))

Stock	Input Buffer	Action
\$	(a, (a,a)) \$	Shift
\$ L	a, (a,a) \$	Shift
\$ (a	, (a,a) \$	
\$ (S	, (a,a) \$	Reduce S → a
\$ (L	(a,a) \$	Reduce L → S
\$ (L,	(a,a) \$	Shift
		Shift

\$ (L, C	a, a)) \$	shift
\$ (L, (a	, a)) \$	Reduce S->a
\$ (L, (S	, a)) \$	Reduce L->S
\$ (L, (L	, a)) \$	shift
\$ (L, (L,	a)) \$	shift
\$ (L, (L, a)) \$	Reduce S->a
\$ (L, (L, S)) \$	L->L,S
\$ (L, (L)) \$	shift
\$ (L, (L)) \$	E->(L)
\$ (L, S) \$	L->L,S
\$ (L) \$	shift
\$ (L)	\$	reduce S->(L)
\$	\$	

Operator Precedence Parser

(OPG) Operator Grammar: To define mathematical operations
 To perform some restrictions

- 1) 2 variables can't be adjacent on right side
- 2) No Epsilon (ϵ) on right side of production

Eg: $E \rightarrow E+E \mid E * E \mid id$

Eg: $E \rightarrow EA \mid id \quad \text{Non} \quad A \rightarrow + \mid *$ $\quad \text{Op}$

$E \rightarrow E+E \mid E * E \mid id \quad \text{gts}$
 $A \rightarrow + \mid *$ $\quad \text{op}$

Parse the input string id + id * id

Step 1: Check operator grammar or not

Step 2: Operator Precedence Relation table

Step 3: Parse the input string

Step 4 Generate Parse tree

$$E \rightarrow E + E \mid E * E \mid id$$

id + id * id

	+	*	id	\$
+	>	<	<	>
*	>	>	<	>
id	>	>	-	>
\$	<	<	<	Accept

id, a, b → high

\$ → lower

+ > +

+ < *

* > *

Operator	Precedence	Associative
↑	1	right
*, /	2	left
+, -	3	left

Stack

Input String

Output

qf

Stack	Relation	Input String	Operation
\$	<	id + id * id \$	Shift Id
\$id	>	+ id * id \$	reduce E → id
\$E	<	+ id * id \$	Shift +
\$E+	<	id * id \$	Shift id
\$E+id	>	* id \$	reduce E → id
\$E+E	<	* id \$	Shift *
\$E+E*	<	id \$	Shift id
\$E+E*id	>	\$	reduce E → id
\$E+E+E	>	\$	reduce E → E+E
\$E+E	>	\$	reduce E → E+E
\$E		\$	Accept

Eq: 2

$$a+b*c*d$$

$$E \rightarrow E + T/T$$

$T \rightarrow T * F | F$

$F \rightarrow a|b|c|d$

Stack	Relation	Input String	Operation
\$	<	a+b*c*d\$	Shift a
\$a	>	+b*c+d\$	Reduce F->a
\$F	<	+b*c*d\$	Shift +
\$F+b	<	b*c*d\$	Shift b
\$F+F	>	*c*d\$	Reduce F->F
\$F+fF*	<	*c*d\$	Shift *
\$F+fF*c	>	c*d\$	Shift c
\$F+fF*f	>	*d\$	Reduce F->c
\$F+fF*T	>	*d\$	Reduce F->f
\$F+T	<	*d\$	Reduce T->T*f
\$F+fT*	<	d\$	Shift *
\$F+T*d	>	\$	Shift d
\$F+T*f	>	\$	Reduce F->d
\$F+fT	>	\$	Reduce T->T*f
		\$	Not accepted

Explain Operator Grammar . Generate audience
table

$$E \rightarrow EAElid$$

$$A \rightarrow +\mid *$$

$$E \rightarrow E+E \mid E * E \mid id$$

$$A \rightarrow + \mid *$$

	+	*	id	\$
+	>	<	<	>
*	>	>	<	>
id	>	>	-	>
\$	<	<	-	>

Accept

$id + id * id$

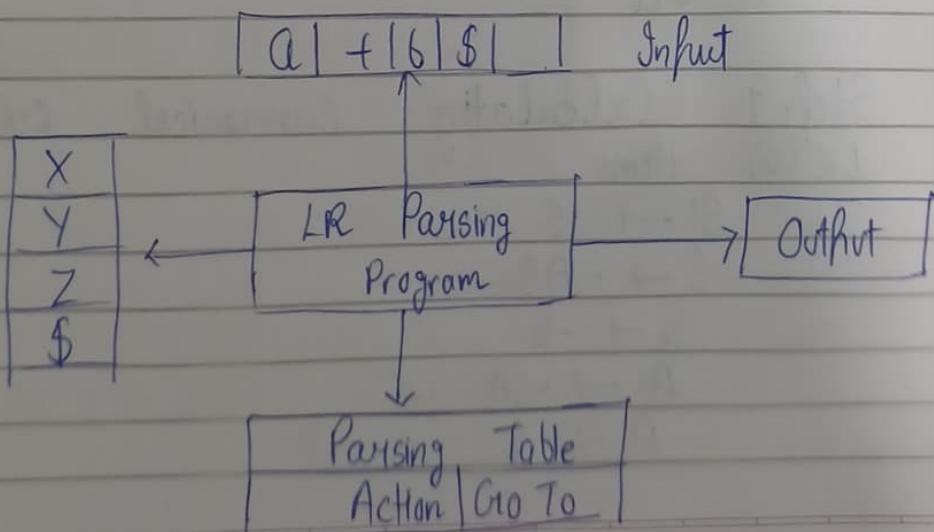
Stack	Relation	Input String	Operation
\$	id = id . C	$id + id * id $$	Shift id
\$ id	>	$+ id * id $$	reduce E → id
\$ E	<	$+ id * id $$	Shift +
\$ E +	<	$id * id $$	Shift id
\$ E + id	>	$* id $$	reduce idE → id
\$ E + F	<	$* id $$	Shift *
\$ E + E *	<	$id $$	Shift id
\$ E + E * id	>	$$$	Shift E → id
\$ E + E * E	>	$$$	reduce E → E+F
\$ E + E	>	$$$	reduce E → E+F
\$ E		$$$	Accept.

Q) Explain LR(1) Parser with suitable example
 LR(1) means SLR for eg.

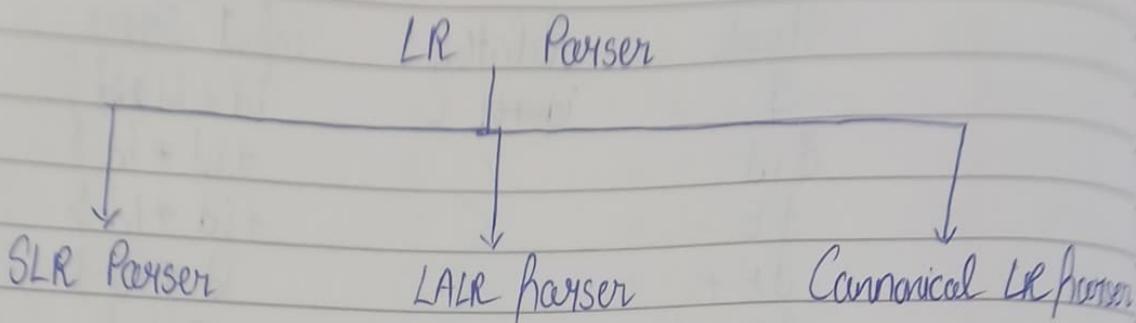
Ans

Bottom-up Parser

- OL stands for left to right scanning
- OR stands for rightmost derivation in reverse
- R is number of input symbols. When R is omitted R is assumed to be 1



Types of LR Parser



SLR Parser

$$S \rightarrow AS1b$$

$$A \rightarrow SA1a$$

Construct SLR parse table for grammar.
Show actions for string "abab".

Augmented Grammar

$$S' \rightarrow S$$

$$S \rightarrow AS$$

$$S \rightarrow b$$

$$A \rightarrow SA$$

$$A \rightarrow a$$

Step 1: Calculating canonical collection of
LR(0) items

$$I_0 : S' \rightarrow \cdot S \quad \checkmark$$

$$S \rightarrow \cdot AS$$

$$S \rightarrow \cdot b$$

$$A \rightarrow \cdot SA \quad \checkmark$$

$$A \rightarrow \cdot a$$

goto (I_0, S): $S \rightarrow S.$
 $I_1 : A \rightarrow S.A$
 $A \rightarrow S$
 $A \rightarrow .a$
 $S \rightarrow .AS$
 $S \rightarrow .b$

goto (I_0, A): $S \rightarrow A.S$
 $I_2 : S \rightarrow .AS$
 $S \rightarrow .b$
 $A \rightarrow .SA$
 $A \rightarrow .a$

goto (I_0, b): $I_3 : S \rightarrow b.$

goto (I_0, a): $I_4 : A \rightarrow a.$

goto (I_1, A): $A \rightarrow SA.$
 $I_5 : S \rightarrow A.S$
 $S \rightarrow b.$
 $S \rightarrow .AS$
 $A \rightarrow .SA$
 $A \rightarrow .a$

goto (I_1, S): $A \rightarrow S.$
 $I_6 : A \rightarrow .SA$
 $A \rightarrow .a$
 $S \rightarrow .AS$
 $S \rightarrow .b$

goto (I_1, a): $A \rightarrow a. I_4$

goto (I_1, b):
 I_3

goto (I_2, θ):

$S \rightarrow AS.$
 $A \rightarrow S.A$
 $I_7 \quad A \rightarrow .SA$
 $A \rightarrow .a$
 $S \rightarrow AS$
 $S \rightarrow .b$

goto (I_2, θ):

$S \rightarrow A.S$
 $S \rightarrow .AS$
 $S \rightarrow .b$
 $A \rightarrow .SA$
 $A \rightarrow .a$

goto (I_2, a):

I_9

goto (I_2, b): I_3

goto (I_5, S):

$S \rightarrow AS.$
 $A \rightarrow S.A$
 $A \rightarrow .a$
 $A \rightarrow .SA$
 $S \rightarrow ^SAS$
 $S \rightarrow .b$

goto (I_5, A):-

$$\left. \begin{array}{l} S \rightarrow AS \\ S \rightarrow A \cdot AS \\ S \rightarrow \cdot b \\ A \rightarrow a \\ A \rightarrow \cdot SA \end{array} \right\} I_5$$

I_2 state che

goto (I_5, a): $A \rightarrow a \cdot \quad \} I_4$

goto (I_5, b): $B \rightarrow b \cdot \quad \} I_3$

goto ($I_6, \$$): $\left. \begin{array}{l} A \rightarrow SA \\ S \rightarrow AS \end{array} \right\} I_5$

goto (I_6, S): $\left. \begin{array}{l} A \rightarrow S.A \\ A \rightarrow \cdot a \\ A \rightarrow S.A \\ S \rightarrow \cdot AS \\ S \rightarrow \cdot b \end{array} \right\} I_6$

goto (I_6, a): I_4

goto (I_6, b): I_3

goto (I_7, A): $\left. \begin{array}{l} A \rightarrow SA \\ \emptyset \rightarrow AS \\ S \rightarrow \cdot b \\ A \rightarrow a \\ A \rightarrow \cdot SA \\ S \rightarrow \cdot AS \end{array} \right\} I_5$

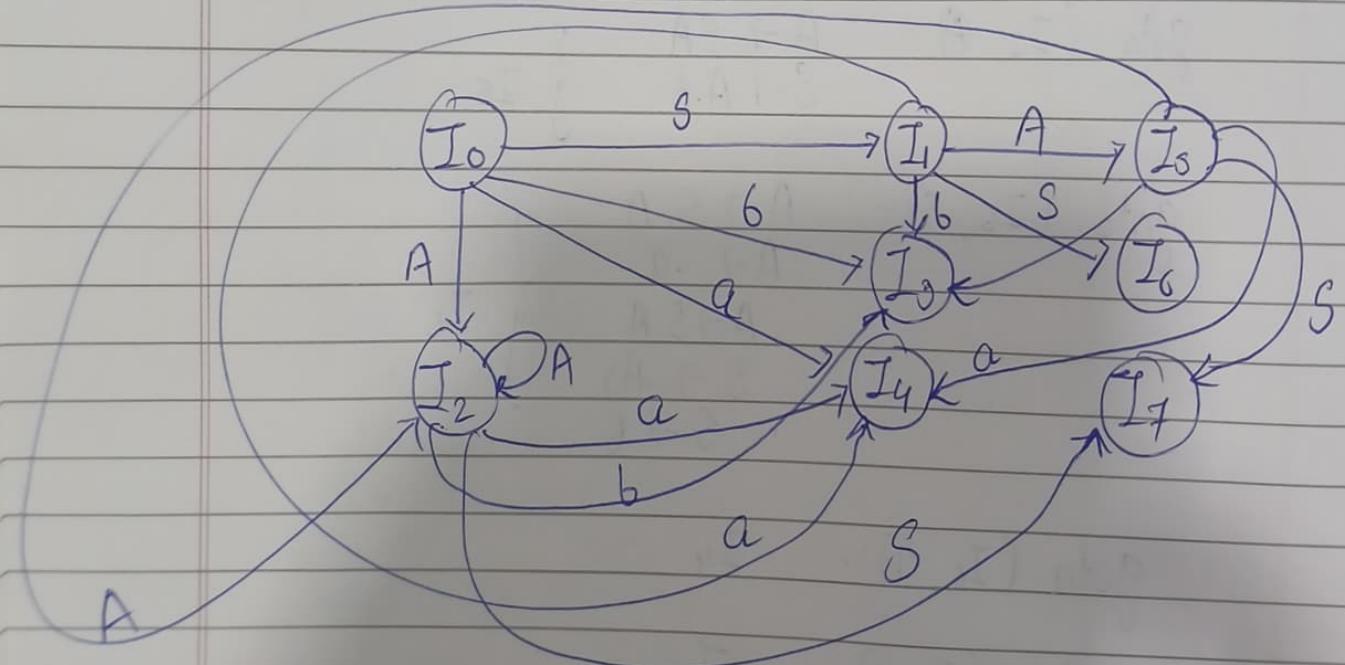
goto (I_7, S):
 A \rightarrow S.A
 I_6

goto (I_7, a):
 A \rightarrow a. I_4

goto (I_7, b):
 B \rightarrow b. I_3

Step 2:

Define FA



Step 3

Construction of SLR Parse Statement

$$S \rightarrow AS \mid b$$

$$A \rightarrow SA \mid a$$

$$\text{First}(S) = \{b, a\}$$

$$\text{First}(A) = \{a, b\}$$

$$\text{Follow}(S) = \{\$, a, b\}$$

$$\text{Follow}(A) = \{a, b\}$$

Parse Table

		Action			goto	
	a	b	\$		S	A
0	\$4	\$3			1	2
1	\$4	\$3	Accepted		6	5
2	\$4	\$3			7	2
3	\$1 ₂	\$2	\$2			
4	\$4	\$4				
5	\$4/\$5	\$3/\$5			7	2
6	\$4	\$3			6	5
7	\$4/\$1 ₁	\$3/\$1 ₁	\$1 ₁		6	5

$$I_1: S^* \rightarrow S.$$

$$I_3: S \rightarrow b.$$

Final Item

I ₀ : 0	$S^* \rightarrow S$	0
1	$S \rightarrow AS$	1
2	$S \rightarrow b$	2
3	$A \rightarrow SA$	3
4	$A \rightarrow a$	4

I_S: S → b.

M₂

Follow(S) = {S, a, b}

I_A: A → a

M₄

Follow(A) = {a, b}

I_S: A → SA.

M₃

Follow(A) = {a, b}

I_T: A $\not\rightarrow$ SA. A → AS.
M_S M₁

a, b

Stack	Input Buffer	Action
\$0	a b a \$	shift 4
\$0a4	b a b \$	reduce A → a
\$0A2	b a b \$	shift 3
\$0A2b3	a b \$	reduce S → AS b
<u>\$0A2S7</u>	a b \$	reduce S → AS
\$0S1	a b \$	shift 4
\$0S1a4	b \$	reduce A → a
\$0S1AS	b \$	reduce A → AS

\$0A2
\$0A2b3

68
\$

Shift 3
Reduce S→b

\$0A2Sf

\$

Rede S→AS

\$ 0S1

\$

Accepted

S → L=R|R

L → *R|id

R → L

Augmented grammar

S' → S 0

S → L=R 1

S → R 2

L → *R 3

L → Id 4

R → L 5

Canonical LR(0) Items

0 I₀: S' → .S

1 S → .L=R

2 S → .R

3 L → .*R

4 L → .Id

5 R → .L

goto (I₀, S): S' → S.

I₁: S → L=R

goto (I₀, L): - S → L = R
I₂ R → L.

goto (I_0, R) :-

I_3 :- $S \rightarrow R.$

goto ($I_0, *$) :- $L \rightarrow * . R$

I_4 $R \rightarrow . L$

$L \rightarrow . * R$

~~goto ($I_0, =$)~~ :- $L \rightarrow . id$

goto (I_0, id) :- $L \rightarrow id.$

I_5

goto ($I_2, =$) :- $S \rightarrow L = . R$

$R \rightarrow . L$

I_6 $L \rightarrow . * R$

$L \rightarrow . id$

goto (I_4, R) :- $L \rightarrow * R.$

I_7

goto (I_4, L) :- $R \rightarrow L.$

I_8

goto ($I_4, *$) :- $L \rightarrow * . R$

$R \rightarrow . L$

I_4

$L \rightarrow . * R$

$L \rightarrow . id$

goto (I_4, id) :- $L \rightarrow id.$

I_5

goto (I_6, R) :

$I_9 \quad S \rightarrow L:R.$

goto (I_6, L) :

$I_8 \quad R \rightarrow L.$

goto ($I_6, *$) :

$L \rightarrow * . R$

$I_4 \quad R \rightarrow . L$

$L \rightarrow . + R$

$L \rightarrow . + id$

goto (I_6, id) :

$I_5 \quad L \rightarrow id.$

SLR	Parse tree	Action	\$	=	\$	goto	L	R
0	S_4	i_5				I	2	3
1				Accept				
2				M_3	$S_6 r_5$	Accept		
3				M_2				
4	S_4	S_5					8	7
5				M_4	M_4			
6	S_4	S_5					8	9
7				M_3	M_3			
8				M_5	M_5			
9				M_1				

$I_1: S^* \rightarrow S.$

Final term

$I_2: R \rightarrow L.$

Final item

$S \rightarrow L = R$

$S \rightarrow R$

$L \rightarrow *R$

$L \rightarrow id$

$R \rightarrow L$

$\text{Follow}(S) = \{\$\}$

$\text{Follow}(L) = \{=, \$\}$

$\text{Follow}(R) = \{=\, \$\}$

$I_2: R \rightarrow L$

M_5

$\text{Follow}(R) = \{=\, \$\}$

$I_3: S \rightarrow R$

M_2

$\text{Follow}(S) = \{\$\}$

$I_4: L \rightarrow id$

M_4

$\text{Follow}(L) = \{=\, \$\}$

$I_5: L \rightarrow *R$

M_3

$=, \$$

$I_6: R \rightarrow L$

$\text{Follow}(R) = \{=\, \$\}$

M_5

$I_7: S \rightarrow L = R$

M_1

$\text{Follow}(S) = \{\$\}$

Stack

$\$ 0$

$\$ \Theta * 4$

$\$ 0 * 4 id 5$

$\$ 0 * 4 L 8$

$\$ 0 * 4 R 7$

$\$ 0 L 2$

$\$ 0 L 2 = 6$

$\$ 0 L 2 = 6 id 5$

$\$ 0 L 2 = 6 L 8$

$\$ 0 L 2 = 6 R 9$

IP buffer

*id=id \$

id=id \$

=id \$

=id \$

=id \$

=id \$

=id \$

id \$

\$

\$

\$

Action

Shift 4

Shift 5

reduce L \rightarrow id

Reduce R \rightarrow L

Reduce L \rightarrow *R

Shift 6 Reduce R \rightarrow L

Shift 5

R \rightarrow L \rightarrow id

R \rightarrow L

S \rightarrow L \cdot R

$\$ 0 S I$

\$

Accept

Q

W - 22 OR Q - 3(c)

$S \rightarrow (L) | a$

$L \rightarrow L, S | S$

Augmented grammar

0 $S' \rightarrow S$

1 $S \rightarrow (L)$

2 $a \rightarrow a$

3 $L \rightarrow L, S$

4 $L \rightarrow S$

Follow(S) = { \$,), , }

Follow(L) = {), , }

Canonical LR(0) items

I₀:

$S' \rightarrow .S$

$S \rightarrow .(L)$

$S \rightarrow .a$

$L \rightarrow .L, S$

$L \rightarrow .S$

goto (I_0, S) : $S' \rightarrow S.$ Then
 I_1 $L \rightarrow S.$ If

goto (I_0, L) : $L \rightarrow L., S$
 I_2 .

goto (I_0, a) :
 I_3 $S \rightarrow a.$ If

goto ($I_0, ()$)
 I_4 $S \rightarrow (.L)$
 $L \rightarrow .L, S$
 $L \rightarrow .S$
 $S \rightarrow .(L)$

goto (I_2, a)
 I_5 $L \rightarrow L., S$
 $S \rightarrow .a$
 $S \rightarrow .(L)$

goto (I_4, S) : ~~$S \neq$~~ $L \rightarrow S.$
 I_6 If

goto (I_4, L) : $S \rightarrow (L.)$
 I_7 $L \rightarrow L., S$

goto ($I_4, ()$) : $S \rightarrow (.L)$
 I_8

goto (I_1, L): $S \rightarrow$

goto (I_8, S): $L \rightarrow L, S.$ fi

goto (I_5, a): $S \rightarrow a.$

goto (I_8, C): $S \rightarrow (.)L)$
 I_8

Parse Table

	Action						goto	
	()	,	\$	a	S	L	
I_0	S_4				S_3	I_0	I_2	
I_1		H_4	H_4	Accept				
I_2		S_5		H_4		I_0		-
I_3		H_2	H_2		H_2			
I_4		S_8				I_6	I_7	
I_5	S_8				S_3	I_8		
I_6		H_4	H_4					
I_7								
I_8								
I_9		H_3	H_3					

$I_1: S^* \rightarrow S.$
 $L \rightarrow S.$ H_4
follow (L): $\{ \}, \}$

$I_3: S \rightarrow a.$
 H_2 $\{ \$, \}, \}$

I₆: $L \rightarrow S$
Follow(L): { , }
 $\{ \}_{1_4} \}$

I₉: $L \rightarrow L, S$
 $\{ \}_{1_3} \}$

Follow(L) = { , }
{ , }

Q

GTU

S-25

Q-3(c)

$S \rightarrow AaAb \mid BbBa$

$A \rightarrow \epsilon$

$B \rightarrow \epsilon$

Follow(S) = { \$ }
{ \$ }

Follow(A) = { a, b }
{ a, b }

Follow(B) = { a, b }
{ a, b }

I₀:

0 $S' \rightarrow S$

1 $S \rightarrow AaAb$

2 $S \rightarrow BbBa$

3 $A \rightarrow \epsilon$

4 $B \rightarrow \epsilon$

I₀:

$S' \rightarrow S$

$S \rightarrow AaAb$

$S \rightarrow BbBa$

$A \rightarrow \epsilon$

$B \rightarrow \epsilon$

goto (I_0, S) : $S' \rightarrow S$. f_i
 I_1

goto (I_0, A) : $S \rightarrow A.aA6$
 I_2

goto (I_0, B) : $S \rightarrow B.bB_a$
 I_3

goto (I_2, a) : $S \rightarrow Aa.A6$
 I_4 $A \rightarrow .\cancel{Aa}6$ A

goto (I_3, b) : $S \rightarrow Bb.B_a$
 I_5 $B \rightarrow .$ A

goto (I_4, A) : $S \rightarrow AaA.b$
 I_6

goto (I_5, B) : $S \rightarrow BbB.a$
 I_7

goto (I_6, b) : $S \rightarrow AaAb.$ f_i
 I_8

goto (I_7, a) : $S \rightarrow BbBa.$ f_i
 I_9

I_1 : $S' \rightarrow S.$

I_8 : $S \rightarrow AaAb.$

follow(S) = {

State	Action	goto
0	a H ₃ /H ₄	b H ₅ /H ₄
1		s 1
2	S ₄	
3		S ₅
4	H ₃	H ₃
5	H ₄	H ₄
6		S ₈ /H ₄
7	S ₉	
8		
9		

I₄: A → .

I₅: B → .

Ok got it

0 Go

o Construct CLR Parser for following grammar

In SLR LR(0)

In CLR $LR(1) = LR(0) + \text{lookahead}$

$S \rightarrow CC$

$C \rightarrow CClD$

Eg: $S \rightarrow CC$
 $C \rightarrow CClD$

Ans

$S \rightarrow CC$

$C \rightarrow CC$

$C \rightarrow d$

Step: I Augmented grammar

0 $S \rightarrow S$

1 $S \rightarrow CC$

2 $C \rightarrow CC$

3 $C \rightarrow d$

Step: 2 Calculating LR(1) items

$I_0 : US' \rightarrow \cdot S, \$$

1 $S \rightarrow \cdot CC, \$$

2 $C \rightarrow \cdot CC, ClD$

3 $C \rightarrow \cdot d, ClD$

goto (I_0, S): $S' \rightarrow S \cdot, \$$
 I_1

goto (I_0, C): $S \rightarrow C \cdot C, \$$
 I_2 $C \rightarrow \cdot CC, \$$
 $C \rightarrow \cdot d, \$$

0 Lookahead Calculation

$S' \rightarrow S, \$$

$S^* \rightarrow S \cdot E$ \$
 $S \rightarrow$ First ($E \cdot \$$)
 (\$)

$$S \rightarrow .CC(S)$$

First (C.C. §)

$$\text{First } (C) = \{c, d\}$$

~~✓~~

~~goto l-~~

$S \rightarrow C.C(\$)$

First (\$) = \$

goto (I_0, c) : $C \rightarrow C.C, cld$
 $C \rightarrow .CC, cld$
 $I_3 \quad C \rightarrow .d, cld$

goto (I_0, d): $C \rightarrow d.$, Cd R
 I_4

goto (I_2, C): $S \rightarrow CC, \$$ fi
 I_3

goto (J₂, c) : C → C.C, \$
J₆ C → .CC, \$
C → .d, \$

goto (I_2, d):

$I_7 \quad C \rightarrow d., \$$

goto (I_3, c):

$I_8 \quad C \rightarrow CC., cld \quad Fi$
 $C \rightarrow \cdot CC, cld$

goto (I_3, c):

$I_3 \quad C \rightarrow c.C, cld$
 $C \rightarrow \cdot CC, cld$
 $C \rightarrow \cdot d, cld$

goto (I_3, d):

$C \rightarrow d., cld$
 I_4

goto (I_6, C):

$C \rightarrow CC., \$ \quad Fi$
 I_6

goto (I_6, c):

$C \rightarrow c.C, \$$
 $C \rightarrow \cdot CC, \$$
 $I_6 \quad C \rightarrow \cdot d, \$$

goto (I_6, d):

$C \rightarrow d., \$ \quad I_7 \quad Fi$

Construction of CIR finite table

State

		Action		goto
0	C S_3	d S_4	$\$$	S 1
1				C 2
2	S_6	S_7	Accepted	
3	S_3	S_4		5
4	H_3	H_3		8
5			H_1	
6	S_6	S_7		9
7			H_2	
8	H_2	H_2		
9			H_2	

I₁: $S' \rightarrow S, \$ \quad F$

I₂: $C \rightarrow$

I₄: $C \rightarrow d, cld \quad F$

I₅: $S \rightarrow CC, \$ \quad F$

I₆: $C \rightarrow d, \$ \quad F$

I₈: $C \rightarrow CC, cld \quad F$

I₉: $C \rightarrow CC, \$ \quad F$

Stack	Input	String	Actions
\$0	d	\$	Shift 4
\$0d4	d	\$	reduce C→d
\$0C2	d	\$	Shift 7
\$0C2d7	\$		reduce C→d
\$0C2C5		\$	S→cc
\$0SI		\$	Accepted

Construct LALR Parser

$$\begin{array}{l} S \rightarrow L = R \mid R \\ L \rightarrow *R \text{ id} \\ R \rightarrow L \\ \text{B} \neq \text{id} \end{array}$$

LALR is compressed version of CLR above eg
 $L \rightarrow *R, =\$$ & $L \rightarrow *R, \$$
 $S \rightarrow +R., =\$$ & $S \rightarrow +R., \$$

Augmented Grammar

$$\begin{array}{l} S' \rightarrow S \\ S \rightarrow L = R \\ S \rightarrow R \\ L \rightarrow *R \\ L \rightarrow \text{id} \\ R \rightarrow L \end{array}$$

different lookahead symbol
so they can be merged
that's the concept of
LALR

LR(1) Items

$$\begin{array}{ll} S' \rightarrow \cdot S, \$ & \text{First}(z, \$) \\ S \rightarrow \cdot L = R, \$ & \\ S \rightarrow \cdot R, \$ & \\ L \rightarrow \cdot *R, \$ & \\ L \rightarrow \cdot \text{id}, \$ & \\ R \rightarrow \cdot L, \$ & \end{array}$$

goto (I_0, S):

$I_1 := S \rightarrow S., \$$ $\text{if } I_1$

goto (I_0, L)

$I_2 := S \rightarrow L. = R, \$$
 $R \rightarrow L., \$$ $\text{if } I_2$

goto (I_0, R)

$I_3 := S \rightarrow R., \$$ $\text{if } I_3$

goto (I_0, \neq):

$I_4:$
 $L \rightarrow *R, = \$$
 $R \rightarrow .L, = \$$
 $L \rightarrow .*R, = \$$
 $L \rightarrow .id, = \$$

goto (I_0, id):

I_5 $L \rightarrow id., = \$$ $\text{if } I_5$

goto ($I_2, =$):

$I_6:$
 $S \rightarrow L = .R, \$$
 ~~$R \rightarrow .*R,$~~
 $R \rightarrow .L, \$$
 $L \rightarrow .*R, \$$
 $L \rightarrow .id, \$$

goto (I_4 ,

goto (I_0, R):

I_7 $L \rightarrow *R., = \$$ $\text{if } I_7$

Date _____

31: goto (I_4, L):
 $R \rightarrow L.$, =IS A I_1

goto ($I_4, *$):
 $L \rightarrow * . R$, =IS
 $I_4:$ $R \rightarrow . L$, =IS
 $L \rightarrow . * R$, =IS
 $L \rightarrow . id$, =IS

goto (I_4, id):
 I_5 $L \rightarrow id.$, =IS A I_5

goto (I_6, R):
 I_9 $S \rightarrow L = R.$, \$

goto (I_6, L):
 I_{10} $R \rightarrow L.$, \$

goto ($I_6, *$)
 $L \rightarrow * . R$, \$
 $R \rightarrow . L$, \$
 I_{11} $L \rightarrow . * R$, \$
 $L \rightarrow . id$, \$

goto (I_6, id)
 I_{12} $L \rightarrow id.$, \$ A

goto (I_6, R):
 I_{13} $L \rightarrow * R.$, \$ F

goto (I_{11}, L):
 I_{10} $R \rightarrow L.$, \$ A

goto (I_4, L):
 $I_1: R \rightarrow R., =\$ \quad F \quad I_1$

goto ($I_4, *$):
 $L \rightarrow * . R, =\$$
 $I_4: R \rightarrow . L, =\$$
 $L \rightarrow . * R, =\$$
 $L \rightarrow . id, =\$$

goto (I_4, id):
 $I_5 \quad L \rightarrow id., =\$ \quad F \quad I_5$

goto (I_6, R):
 $I_9 \quad S \rightarrow L=R., \$$

goto (I_6, L):
 $I_{10} \quad R \rightarrow L., \$$

goto ($I_6, *$)
 $L \rightarrow * . R, \$$
 $R \rightarrow . L, \$$
 $I_{11} \quad L \rightarrow . * R, \$$
 $L \rightarrow . id, \$$

goto (I_6, id)
 $I_{12} \quad L \rightarrow id., \$ \quad F$

goto (I_{10}, R):
 $I_{13} \quad L \rightarrow * R., \$ \quad F$

goto (I_{11}, L):
 $I_{10} \quad R \rightarrow L., \$ \quad F$

goto (I_0, C)

I_0

$C \rightarrow c.C, \text{cl}_d$
 $C \rightarrow .CC, \text{cl}_d$
 $C \rightarrow .d, \text{cl}_d$

I_{36}

goto (I_0, D)

I_4

$C \rightarrow d., \text{cl}_d$

A

goto (I_2, C)

I_5

$S \rightarrow CC., \$$

A

goto (I_2, C)

I_6

$C \rightarrow c.C, \$$

$C \rightarrow .d, \$$

$C \rightarrow .CC, \$$

I_5

goto (I_2, D)

I_7

$C \rightarrow d., \$$

H

goto (I_6, C)

I_8

$C \rightarrow CC., \$$

goto (I_3, C)

I_8

$C \rightarrow CC., \text{cl}_d$

A

goto (I_3, C)

$C \rightarrow$

$c.C, \text{cl}_d$

$C \rightarrow$

$.CC, \text{cl}_d$

$C \rightarrow$

$.d, \text{cl}_d$

goto $C \rightarrow$

goto (I_1 , ϵ):

$L \rightarrow * \cdot R, \$ \} I_1$

goto (I_1 , id):

$L \rightarrow id \cdot , \$ \quad I_{12}$

Combine $I_4 \& I_{11} \rightarrow I_{411}$

Combine $I_5 \& I_{12} \rightarrow I_{512}$

Combine $I_7 \& I_{13} \rightarrow I_{713}$

Combine $I_8 \& I_{10} \rightarrow I_{810}$

Construction of LALR Parse tree.

	Action				goto		
	id	$=$	$*$	$\$$	S	L	R
0	$S 512$		$S 411$		1		
1					Accepted		
2		$S 6$			M_5		
3					M_2		
411	$S 512$		$S 411$			810	713
512		M_4			M_4		
6	$S 512$		$S 411$			810	9
713		M_3			M_3		
810		M_5			M_5		
9					M_1		

Stack

\$0

\$0 id512

\$0 L2

\$0 L2 = 6

\$0 L2 = 6 id 512

\$0 L2 = 6 L 810

\$0 L2 = 6 R 9

\$0 I

IP String

id: id \$

= id \$

Action

S 512

reduce L → id

86

S 512

reduce L → id

reduce R → L

S → L = R

Accept

Q,

Design LALR Parsing table

[GATE, W-24 OR Q-3(c)]

Ans

S → CC

C → CCId

Augmented Grammar

I₀: S' → S, \$

S → CC, \$

C → .CC, \$ CId

C → .d, \$ CId

goto (I₀, S)

I₁: S' → S., \$ fi

goto (I₀, C)

I₂: S → C.C, \$

C → .CC, \$

C → .d, \$

goto (I_0, C)

I_0 $C \rightarrow C.C, \text{cl}_d$ I_{36}
 $C \rightarrow .CC, \text{cl}_d$
 $C \rightarrow .d, \text{cl}_d$

goto (I_0, d)

I_4 $C \rightarrow d., \text{cl}_d$ fi I_{74}

goto (I_2, C)

I_5 $S \rightarrow CC., \$$ fi

goto (I_2, c)

I_6 $C \rightarrow C.C, \$$ $I_5 I_6$
 $C \rightarrow .d, \$$
 $C \rightarrow .CC, \$$

goto (I_2, d)

I_7 $C \rightarrow d., \$$ fi $I_7 I_4$

goto (I_6, C)

I_8 $C \rightarrow CC., \$$

goto (I_3, C)

I_8 $C \rightarrow CC., \text{cl}_d$ fi I_{89}

goto (I_3, c)

$C \rightarrow C.C, \text{cl}_d$
 $C \rightarrow .CC, \text{cl}_d$
 $C \rightarrow .d, \text{cl}_d$ } I_3

goto (I_3, d)

I_9 $C \rightarrow d., \text{cl}_d$ fi

goto (I_6, C):
 $I_9 \quad C \rightarrow CC, \$ \quad I_{69}$

goto (I_6, c)
 $I_6 \quad C \rightarrow c.C, \$$
 $C \rightarrow .CC, \$$
 $C \rightarrow .d, \$$

goto (I_6, d):
 $I_7 \quad C \rightarrow d., \$ \quad A$

Construction of CLR

		Action		goto	
.	c	d	\$	S	C
0	S2	S47		I	2
1					
2	S36	S47			5
3	S36	S47			89
4					
5					
6	S36	S47			89
7					
8					
9					

Combine $I_3 \& I_6$ into I_{36}
" " $I_7 \& I_8$ into I_{74}
Combine $I_1 \& I_9$ into I_{59}

Stack	IIP String	Action
\$0	id:id \$	S 512
\$0 id512	= id \$	reduce L \Rightarrow id
\$0 L2	= id \$	86
\$0 L2 = 6	id \$	S 512
\$0 L2 = 6 id 512	\$	reduce L \Rightarrow id
\$0 L2 = 6 L 8 0	\$	reduce R \Rightarrow L
\$0 L2 = 6 R 9	\$	S \Rightarrow L = R
\$0	\$	Accept

Q Design LALR Parsing table [ATU, W-24 OR Q-3(C)]

Ans $S \rightarrow CC$
 $C \rightarrow CCId$

Augmented Grammar
 $I_0: S' \rightarrow S, \$$
 $S \rightarrow CC, \$$
 $C \rightarrow .CC, \$$ $cl d$
 $C \rightarrow .d, \$$ $cl d$

goto (I_0, S)
 $I_1: S' \rightarrow S., \$$ F_i

goto (I_0, C)
 $I_2: S \rightarrow C.C, \$$
 $C \rightarrow .CC, \$$
 $C \rightarrow .d, \$$

goto (I_0, c)

I_5

$C \rightarrow c.C, \text{cld}$

I_{36}

$C \rightarrow .CC, \text{cld}$

$C \rightarrow .d, \text{cld}$

goto (I_0, d)

I_4

$C \rightarrow d., \text{cld}$

$f_i I_{74}$

goto (I_2, C)

I_5

$S \rightarrow CC., \$$

f_i

$I_5 I_6$

goto (I_2, c)

I_6

$C \rightarrow C.C, \$$

$C \rightarrow .d, \$$

$C \rightarrow .CC, \$$

goto (I_2, d)

I_7

$C \rightarrow d., \$$

f_i

$I_7 I_4$

goto (I_6, C)

I_8

$C \rightarrow CC., \$$

goto (I_3, C)

I_8

$C \rightarrow CC., \text{cld}$

f_i

I_{89}

goto (I_3, c)

$C \rightarrow c.C, \text{cld}$

$C \rightarrow .CC, \text{cld}$

$C \rightarrow .d, \text{cld}$

$\} I_3$

goto (I_3, d)

I_9

$C \rightarrow d., \text{cld}$

f_i

goto (I_6, C):- $I_9 \rightarrow CC, \$$ I_{69} goto (I_6, c) $C \rightarrow c.C, \$$ $I_6 \rightarrow C \rightarrow .CC, \$$ $C \rightarrow .d, \$$ goto (I_6, d):- $I_7 \rightarrow C \rightarrow d., \$$ A

Construction of CLR

		Action		goto	
	c	d	\$	s	c
0	S2	S47		1	2
1					
2	S36	S47			5
3	S36	S47			89
4					
5					
6	S36	S47			89
7					
8					
9					

Combine I_3 & I_6 into I_{36} " " I_7 & I_8 into I_{74} Combine I_1 & I_9 into I_{69}

Shift reduce parser

The shift reduce parser performs following basic operations:

1. **Shift:** Moving of the symbols from **input buffer onto the stack**, this action is called shift.
2. **Reduce:** If handle appears on the top of the stack then **reduction of it by appropriate rule** is done. This action is called reduce action.
3. **Accept:** If **stack contains start symbol only and input buffer is empty** at the same time then that action is called accept.
4. **Error:** A situation in which parser **cannot either shift or reduce** the symbols, it cannot even perform accept action then it is called error action.

Example: Shift reduce parser

Grammar:

$E \rightarrow E + T \mid T$

$T \rightarrow T * F \mid F$

$F \rightarrow id$

String:

$id + id * id$

Stack	Input Buffer	Action

Operator precedence parsing

- **Operator Grammar:** A Grammar in which there is no ϵ in RHS of any production or no adjacent non terminals is called operator grammar.
- Example: $E \rightarrow EAE \mid (E) \mid id$
 $A \rightarrow + \mid * \mid -$
- Above grammar is not operator grammar because right side **EAE** has consecutive non terminals.
- In operator precedence parsing we define following disjoint relations:

Relation	Meaning
$a < b$	a “yields precedence to” b
$a = b$	a “has the same precedence as” b
$a > b$	a “takes precedence over” b



Precedence & associativity of operators

Operator	Precedence	Associative
\uparrow	1	right
$\ast, /$	2	left
$+, -$	3	left

Steps of operator precedence parsing

1. Find Leading and trailing of non terminal
2. Establish relation
3. Creation of table
4. Parse the string

Leading & Trailing

Leading:- Leading of a non terminal is the **first terminal or operator** in production of that non terminal.

Trailing:- Trailing of a non terminal is the **last terminal or operator** in production of that non terminal.

Example: $E \rightarrow E+T \mid T$

$T \rightarrow T^*F \mid F$

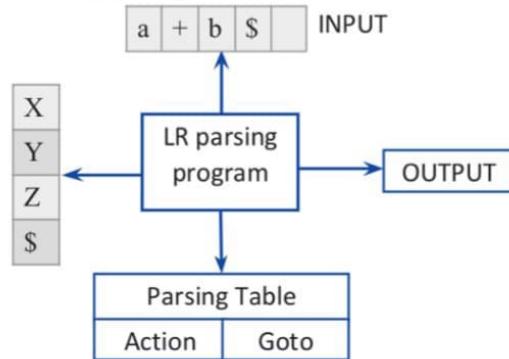
$F \rightarrow id$

Non terminal	Leading	Trailing
E		
T		
F		

Introduction to LR Parser

LR parser

- LR parsing is most efficient method of bottom up parsing which can be used to parse large class of context free grammar.
- The technique is called LR(k) parsing:
 1. The “L” is for **left to right** scanning of input symbol,
 2. The “R” for constructing **right most derivation in reverse**,
 3. The “k” for the **number of input symbols** of look ahead that are used in making parsing decision.



Solution : For LL(1) grammar refer example 3.3.16. To show that this grammar is not SLR(1) we will construct a canonical collection of set of item -

$$I_0 : S \rightarrow * A a A b$$

$$S \rightarrow * B b B a$$

$$A \rightarrow *$$

$$B \rightarrow *$$

$$I_1 : \text{goto } (I_0, A)$$

$$S \rightarrow A * a A b$$

$$I_2 : \text{goto } (I_0, B)$$

$$S \rightarrow B * b B a$$

$$I_3 : \text{goto } (I_1, a)$$

$$S \rightarrow A a * A b$$

$$A \rightarrow *$$

$$I_4 : \text{goto } (I_2, b)$$

$$S \rightarrow B b * B a$$

$$B \rightarrow *$$

$$I_5 : \text{goto } (I_3, A)$$

$$S \rightarrow A a A * b$$

$$I_6 : \text{goto } (I_4, B)$$

$$S \rightarrow B b B * a$$

$$I_7 : \text{goto } (I_5, b)$$

$$S \rightarrow A a A b *$$

$$I_8 : \text{goto } (I_6, a)$$

Parsing table

State	Action		goto			
	c	d	\$	S	T	C
0	S3	S4			1	2
1			ACCEPT			
2	S3	S4				5
3	S3	S4				6
4	r4	r4	r4			
5			r2			
6	r3	r3	r3			

Parsing of string cdcd will be

Stack	Input	Action
\$ 0	cdcd \$	shift 3
\$ 0c3	dcd \$	shift 4
\$ 0c3d4	cd \$	reduce by C → d
\$ 0c3c6	cd \$	reduce by C → cC
\$ 0c2	cd \$	Shift 3
\$ 0c2c3	d \$	Shift 4
\$ 0c2c3d4	\$	reduce by C → d

$$S \rightarrow B b B a$$

The parsing table can be constructed as follows -

State	Action		goto			
	a	b	\$	S	A	B
0	r3/r4	r3/r4			1	2
1	S3					
2		S4				
3	r3	r3				5
4	r4	r4				6
5		S7				
6	S8					
7						
8						

As conflicting entries appear in above table. This grammar is not SLR(1).

Example 3.7.12 Construct SLR parsing table for the following grammar.

1) $E \rightarrow E - T \mid T$ 2) $T \rightarrow F \uparrow T \mid F$ 3) $F \rightarrow (E) \mid id$

GTU : Summer-15, Marks 7

Solution : We will construct a canonical set of items for given production rules.

$$I_3 : \text{goto } (I_0, F)$$

$$T \rightarrow F \uparrow T$$

$$T \rightarrow F *$$

$$I_4 : \text{goto } (I_1, ()$$

$$F \rightarrow (* E)$$

$$E \rightarrow * E - T$$

$$E \rightarrow * T$$

$$T \rightarrow * F \uparrow T$$

$$T \rightarrow * F$$

$$F \rightarrow * (E)$$

$$F \rightarrow * id$$

$$I_5 : \text{goto } (I_0, id)$$

$$F \rightarrow id *$$

$$I_6 : \text{goto } (I_1, -)$$

Ch-4 Error Recovery

Q. Explain Error Recovery Strategies
[4m & 7m sometimes]

Ans

- 1) Panic mode
- 2) Phase Level Recovery
- 3) Error Production
- 4) Global Generation

1) Panic Mode

→ On discovering an error, the parser discards input symbols one at a time until one of a designated a set of synchronizing tokens is found.

→ The synchronizing tokens are usually delimiters, such as Semicolon or ;

→ These tokens indicate an end of the statement

→ If there is less number of errors in the same statement then this strategy is best choice.

Eg:

int a, b;
 ↑
 sum, \$2;
 ↑
 Panic mode stuff

- 2) Phase level Recovery
- In this method, on discovering an error parser performs local correction on remaining input
 - the local correction can be
 - 1) Replacing comma by semicolon
 - 2) Deletion of semicolons
 - 3) Inserting missing semicolon
 - This type of local correction is decided by Compiler designer
 - This method is used in many error-reducing compilers

3) Error Production

- If we have good knowledge of common errors that might be encountered, then we can augment the grammar for corresponding language with error production that generates the erroneous constructs
 - Then we use the grammar augmented by these error production to construct a parser
 - If error production is used then, during parser we can generate appropriate error message and parsing can be continued
- Eg: abcd

$$S \rightarrow A$$

$$A \rightarrow aA \mid bA \mid a \mid b$$

$$B \rightarrow cd$$

x

$$E \rightarrow SB$$

$$S \rightarrow A$$

$$A \rightarrow aA \mid bA \mid a \mid b$$

$$B \rightarrow cd$$

✓

- 4) Global Correction
→ We often want such a compiler that makes very few changes in processing an incorrect input string.
- Given an incorrect input string x and grammar G , the algorithm will find a parse tree for a related string y , such that number of insertions, deletions and changes of token require to transform x into y is as small as possible.
- Such methods increase time and space requirements at parsing time.
- Global correction is thus simply a theoretical concept.

Ch 5 Run Time Environments

Ch-5 Intermediate Code Generation

- 0 Construction of Syntax trees
- 1) mkenode (oh, left, right)
- 2) mkleaf (id, entry to Symbol Table)
- 3) mkleaf (num, value)

Eg: 1 $x * y - s + z$

Steps to construct Syntax tree for
 $x * y - s + z$

Symbol	Generation
x	$P_1 = \text{mkleaf}(\text{id}, \text{entry}-x)$
y	$P_2 = \text{mkleaf}(\text{id}, \text{entry}-y)$
*	$P_3 = \text{mkenode}(*, P_1, P_2)$
5	$P_4 = \text{mkleaf}(\text{num}, 5)$
-	$P_5 = \text{mkenode}(-, P_3, P_4)$
z	$P_6 = \text{mkleaf}(\text{id}, \text{entry}-z)$
+	$P_7 = \text{mkenode}(+, P_5, P_6)$

SOD for $x+y - S + Z$

(production)

$E \rightarrow E_1 + T$

$E \rightarrow E_1 - T$

$E \rightarrow E_1 * T$

$E \rightarrow T$

$T \rightarrow id$

$T \rightarrow num$

Enode = mknode (+, E1.node, T.node)

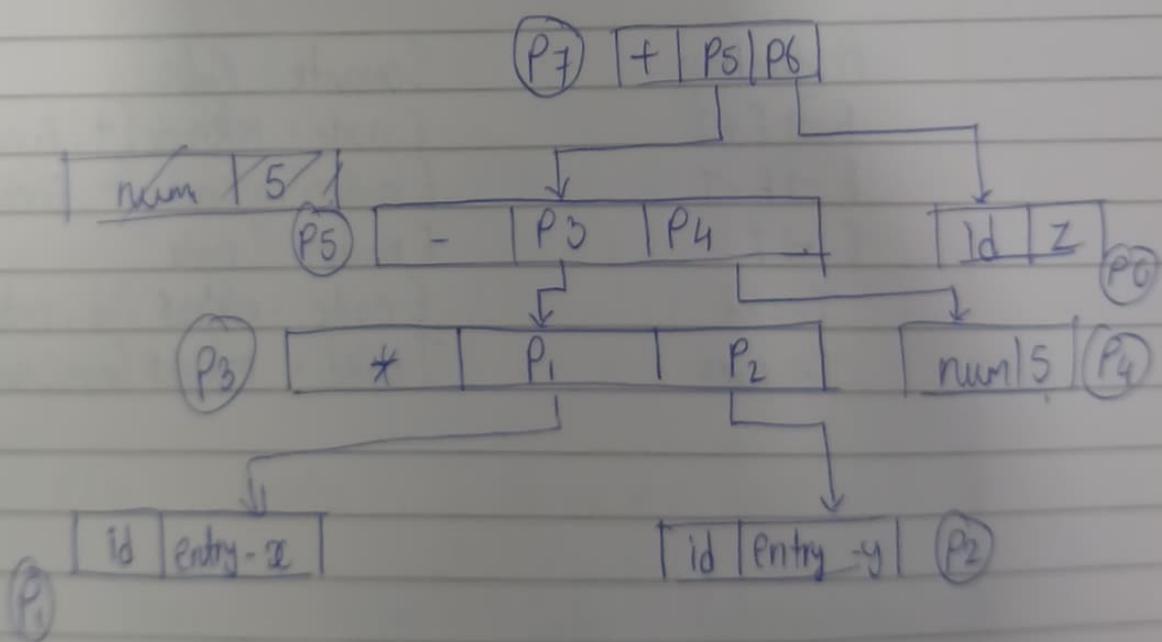
Enode = mknode (-, E1.node, T.node)

Enode = mknode (*, E1.node, T.node)

Enode = T.node

T.node = mkleaf (id, id.entry)

T.node = mkleaf (num, num.value)



Q: $a - 4 + c$

Steps

P₁ = mkleaf (id, entry -a)

P₂ = mkleaf (num, 4)

P₃ = mknоде (-, P₁, P₂) (-, P₁, P₂)

P₄ = mkleaf (id, entry -c)

P₅ = mknоде (+, P₃, P₄)

SOD

Productions

E → E + T

E → E - T

E → T

T → id

T → num

Semantic Rules

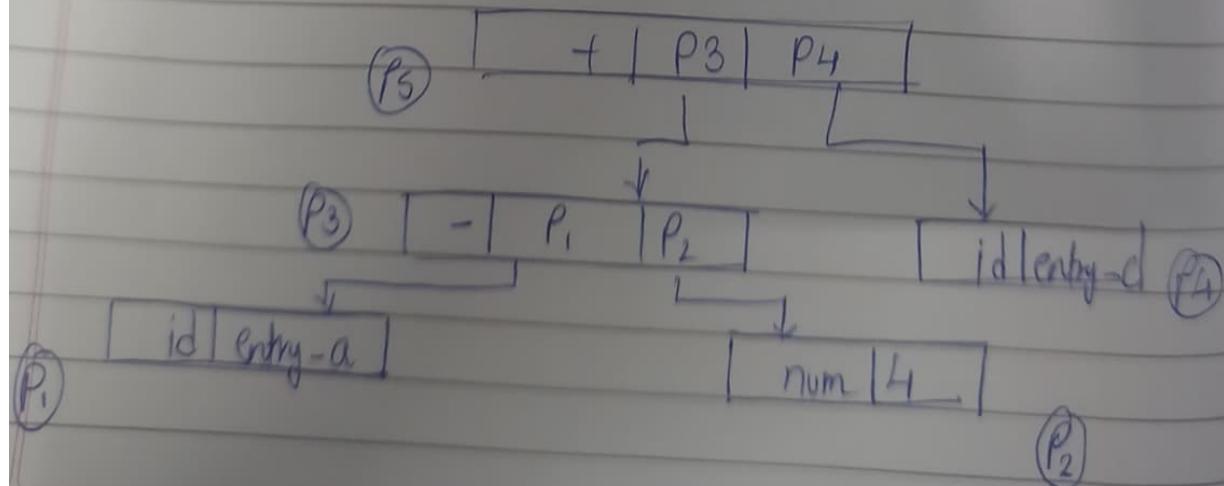
E.node = mknоде (+, E.node, T.node)

E.node = mknоде (-, E.node, T.node)

E.node = T.node

E.node = mkleaf (id, entry to S1)

T.node = mkleaf (num, num.value)



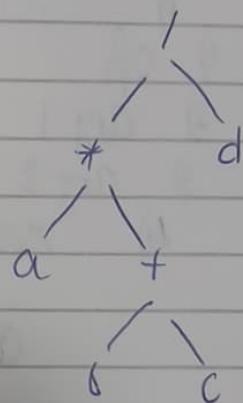
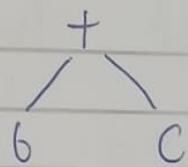
o Forms of Intermediate Code:-

1) Using Syntax trees or AST

2) Postfix notation

3) Three - Address code representation

Eg: $a * (b + c) / d$



(1) Syntax Trees

Eg: $(a + b) * c$ Infix

Prefix Postfix ab + c *

Eg: (3) Three Address Code Representation

(1) Each Instruction should contain at most 3 addresses

(2) Atmost 1 operator on RHS

Represented by:-

- 1) Quadruple
- 2) Triple
- 3) Indirect Triple

Eg: $x + y * z$

$$t_1 = y * z$$

$$t_2 = x + t_1$$

Eg: $a = b * -c + b * -c$

Quadruple Contains Four Fields

- 1) y
- 2) oh
- 3) $\text{arg } 1$
- 4) $\text{arg } 2$
- 5) result

$$a = b * -c + b * -c$$

$$\hookrightarrow t_1 = -c$$

$$t_2 = b * t_1$$

$$\begin{aligned} t_3 &= -c \\ t_4 &= b * t_3 \\ t_5 &= t_2 + t_3 \end{aligned} \quad \left. \begin{array}{l} t_3 = b * t_1 \\ t_4 = t_2 + t_3 \end{array} \right\}$$

	oh	$\text{arg } 1$	$\text{arg } 2$	Result
(0)	-	c		t_1
(1)	*	b	t_1	t_2
(2)	* -	b c	t_3	$t_2 + t_3$
(3)	*	b	t_3	t_4
(4)	+	t_2	t_4	t_5

2) Trifile
3 fields

	OP	arg 1	arg 2
(0)	-	C	
(1)	*	b	(0)
(2)	-	C	
(3)	*	b	(2)
(4)	+	(1)	(3)

3) Indirect trifile

$$a = b * -c + b * -c$$

(100)	(0)
101	(1)
102	(2)
103	(3)
104	(4)

Q, Explain Quadruplet, Trifile and indirect Trifile with example [G.T.U]

Ans Quadruplet

→ It is a structure with at the most four fields such as op, arg1, arg2, and result

→ The op field is used to represent the internal code for operator

→ The arg1 and arg2 represent the two operands

→ And result field is used to store the result of an expression

$$x = -a * b + -a * b$$

$$t_1 = -a$$

$$t_2 = t_1 * b$$

$$t_3 = -a$$

$$t_4 = t_3 * b$$

$$t_5 = t_2 + t_4$$

$$\therefore x = t_5$$

	Op	arg1	arg2	Result
(0)	-	a		t_1
(1)	*	t_1	b	t_2
(2)	-	a		t_3
(3)	*	t_3	b	t_4
(4)	+	t_2	t_4	t_5
(5)	=	t_5		x

2) Trifle

→ To avoid entering temporary names into symbol table, we might refer a temporary value by the position of statement that computes it.
 → It has three fields: op, arg1 & arg2

	Op	Arg 1	Arg 2
(0)	-	a	
(1)	*	b	(0)
(2)	-	a	(1)
(3)	*	b	(2)
(4)	+	(1)	(3)
(5)	=	x	(4)

3) Indirect Triple

- In the Indirect triple representation, the listing of triples has been done. And pointers are used instead of using statement.
- This implementation is called indirect triples.

100	(0)
101	(1)
102	(2)
103	(3)
104	(4)
105	(5)

Eg: $-(a+b)*(c+d)*(a+b*c)$

$$t_1 = (a+b)$$

$$x \quad t_1 = a+b$$

$$t_2 = c+d$$

$$t_3 = t_1 * t_2$$

$$t_4 = a+b$$

$$t_5 = t_4 * c$$

$$t_6 = t_5 * t_3$$

$$t_1 = a+b$$

$$t_2 = c+d$$

$$t_3 = b*c$$

$$t_4 = a+t_3$$

$$t_5 = t_1 * t_2$$

$$t_6 = t_5 * t_4$$

$$t_7 = -t_6$$

Quadruple

	Op	arg 1	arg 2	Result
(0)	+	a	b	t ₁
(1)	+	c	d	t ₂
(2)	*	t ₁	t ₂	t ₃
(3)	+	a	b	t ₄
(4)	*	t ₄	c	t ₅

$$-(a+b) + (c+d) - (a+b+c+d)$$

$$t_1 = a+b$$

$$t_2 = -t_1$$

$$t_3 = c+d$$

$$t_4 = t_2 + t_3$$

$$t_5 = a+b$$

$$t_6 = t_5 + t_3$$

$$t_7 = t_4 - t_6$$

Quadruple

	Op	Arg 1	Arg 2	Result
(0)	+	a	b	t ₁
(1)	minus	t ₁		t ₂
(2)	+	c	d	t ₃
(3)	+	t ₂	t ₃	t ₄
(4)	+	a	b	t ₅
(5)	+	t ₅	t ₃	t ₆
(6)	-	t ₄	t ₆	t ₇

Triple

	Op	arg1	arg2
(0)	*	a	b
(1)	minus	(0)	
(2)	+	c	d
(3)	+	(1)	(2)
(4)	+	a	b
(5)	+	(4)	(2)
(6)	-	(3)	(5)

Indirect Triple

100	(0)
101	(1)
102	(2)
103	(3)
104	(4)
105	(5)
106	(6)

o Directed Acyclic graph

$$X = ((a+a) + (a+a)) + ((a+a) + (a+a))$$

t_1 t_2 t_3 t_4 t_5 t_6 t_7

$$t_1 = a+a$$

$$t_2 = a+a$$

$$t_3 = t_1 + t_2$$

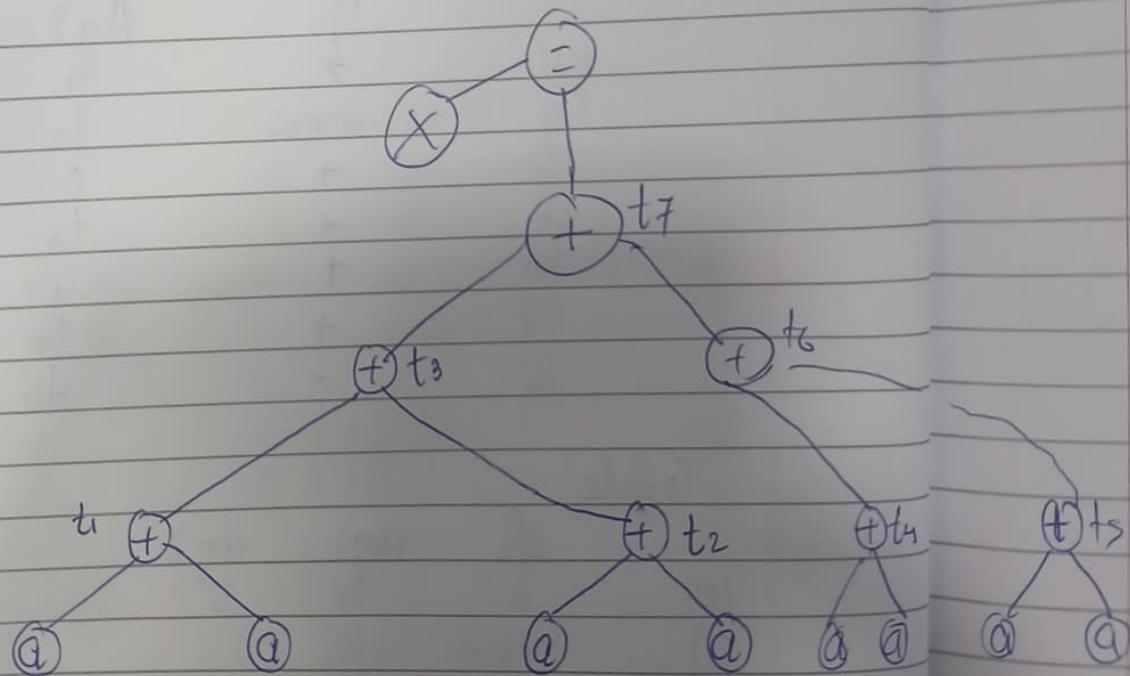
$$t_4 = a+a$$

$$t_5 = a+a$$

$$t_6 = t_4 + t_5$$

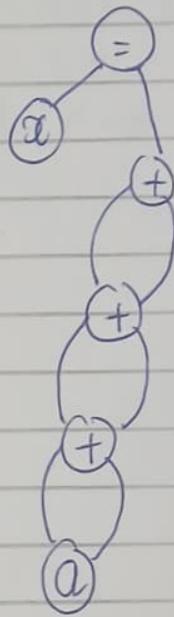
$$t_7 = t_3 + t_6$$

$$X = t_7$$

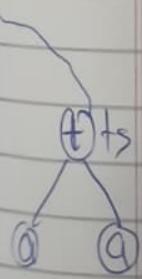


$a + a$ Syntax tree

o DAG

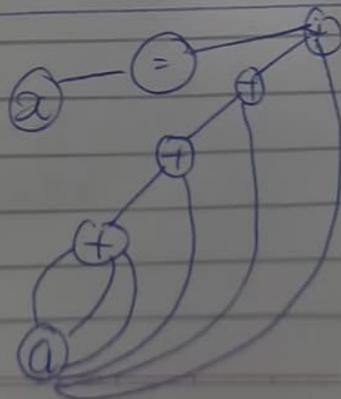


$$X = a + a + a + a + a + a$$



Syntax

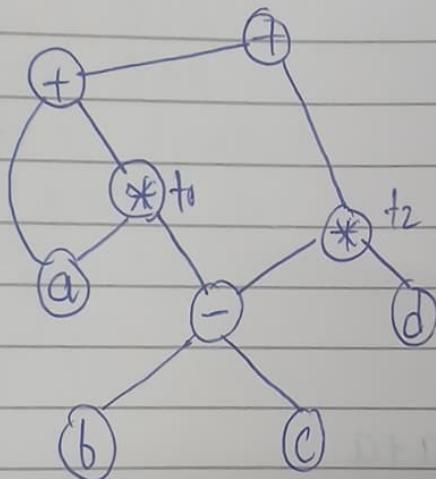
DAG



Eg: 2

$$\frac{a}{t_1} + \frac{a * (b - c)}{t_2} + \frac{(b - c) * d}{t_2}$$

$$a + t_1 + t_2$$



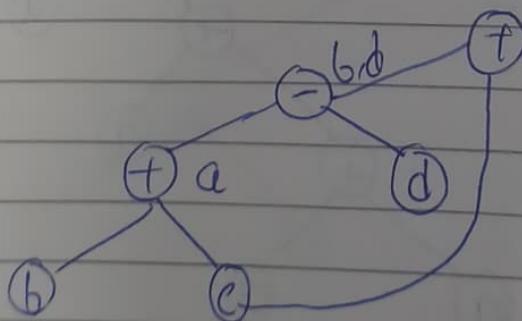
Eg: 3

$$a = b + c$$

$$b = a - d$$

$$c = b + c$$

$$d = a - d$$



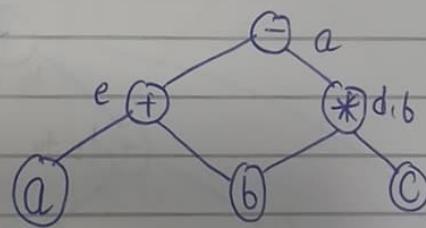
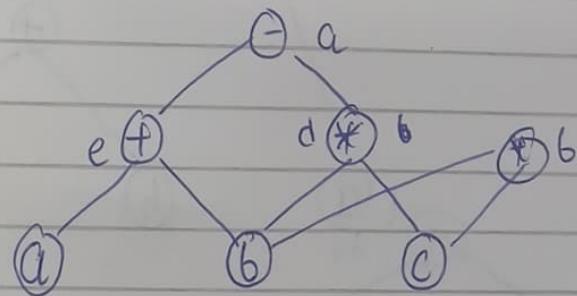
Eg. 4

$$d = b * c$$

$$b = a + b$$

$$b = b * c$$

$$a = e - d$$



Q,

Construct Syntax Tree & OAG

$$x = \underbrace{a * \underbrace{(b + c)}_{t_2}}_{t_1} - \underbrace{(b + c) * d}_{t_3}$$

$$t_1 = a$$

$$t_2 = b + c$$

$$t_3 = t_1 * t_2$$

$$t_4 = b + c$$

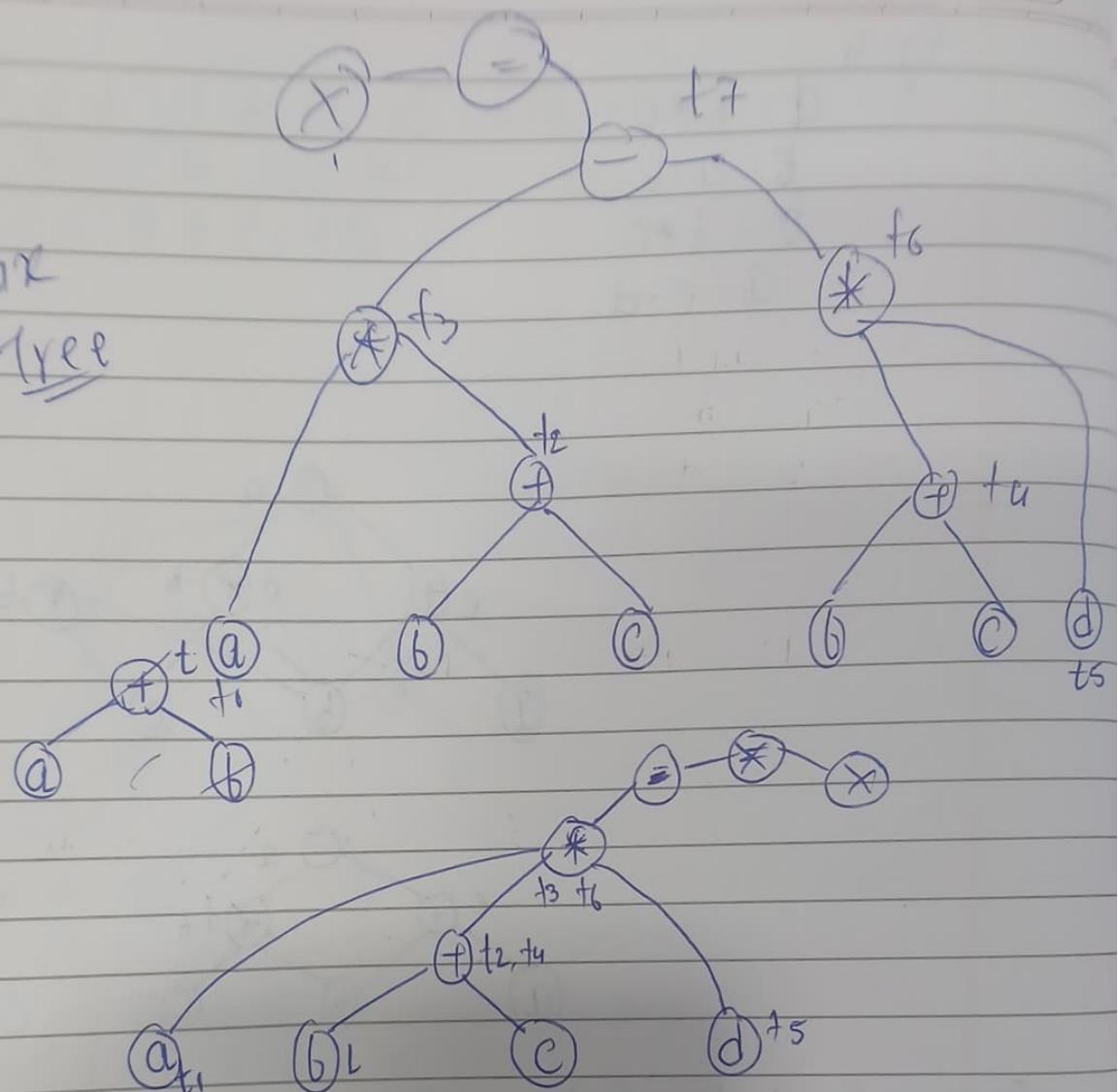
$$t_5 = d$$

$$t_6 = t_4 * t_5$$

$$t_7 = t_3 - t_6$$

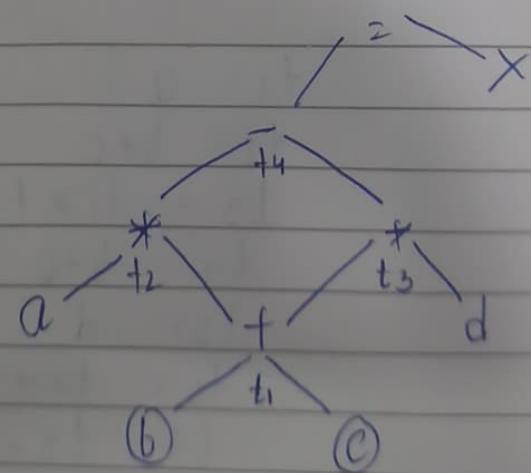
$$x = t_7$$

Syntax Tree



DAG

$$\begin{aligned}
 t_1 &= b + c \\
 t_2 &= a * t_1 \\
 t_3 &= t_1 * d \\
 t_4 &= t_2 - t_3 \\
 x &= t_4
 \end{aligned}$$



Q) $a + a * \frac{(b - c)}{t_3} + \frac{(b - c)}{t_6} * d$

$$t_1 = a$$

$$t_2 = b - c$$

$$t_3 = t_1 * t_2$$

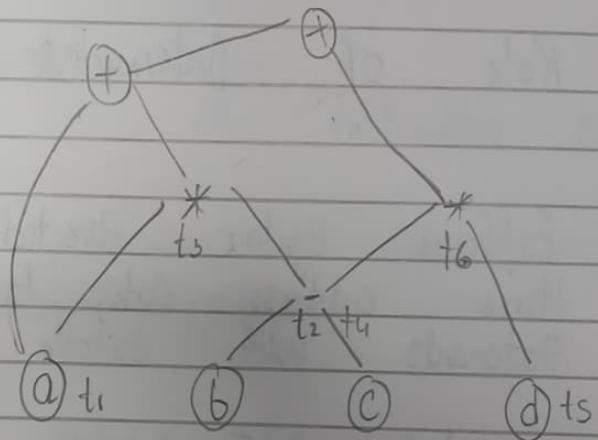
$$t_4 = b - c$$

$$t_5 = d$$

$$t_6 = t_4 * t_5$$

$$t_7 = t_3 + t_6$$

$$t_8 = a + t_7$$



Q) Write three address code can be asked

$$a = b^* - c + b^* - c$$

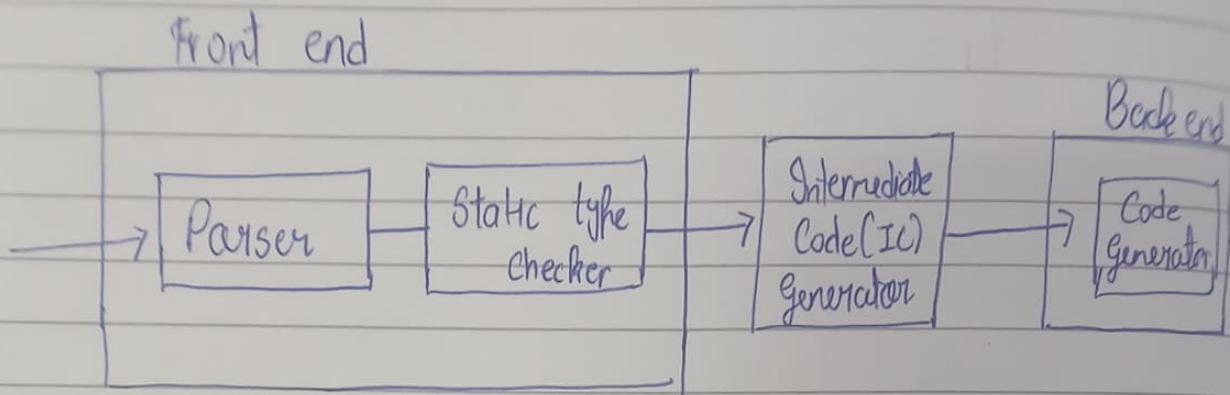
$$t_1 = -c$$

$$t_2 = b^* t_1$$

$$t_3 = t_2 + t_2$$

$$a = t_3$$

O Intermediate Code Generation



Role of Intermediate Code Generation

Q/ Explain Syntax directed derivation to produce three address codes for flow of control statements with suitable example

Ans Watch YT Video Sudhakar Achala

Ch - 6 Run-Time Environment

Q. Write a short note on Activation Tree

Ans An activation tree is like a tree showing which functions call which other functions while a program runs

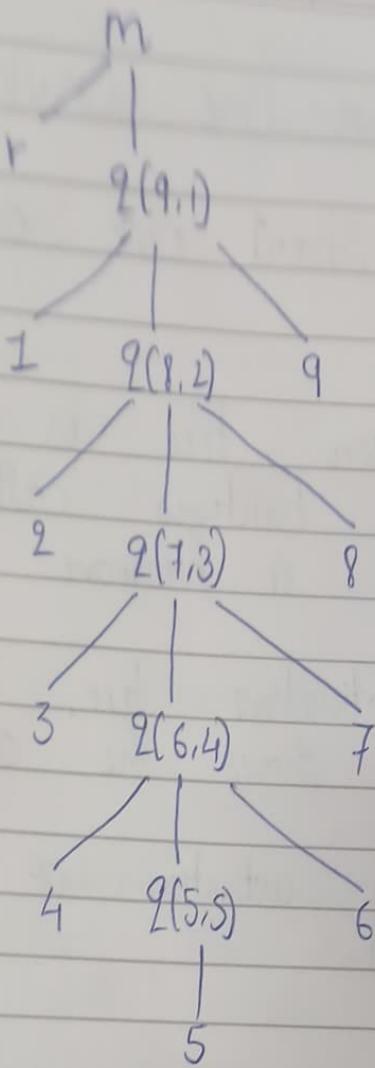
In an activation tree,

- 1) Each node shows the activation of procedures
- 2) For showing activation of main program root is used
- 3) If

Properties of Activation tree are

- 1) Each node represents an activation of procedure
- 2) The root shows activation of main function
- 3) The node for procedure 'x' is the parent node for procedure 'y' if and only if the control flows from procedure x to procedure y

Eg. Activation tree for QuickSort



Write a short note on Activation Record

The Activation Record is a block of memory used for managing information needed by a single execution of a procedure

Return Value
Actual Parameters
Control Link (Dynamic)
Access Link (Static)
Saved Machine Status
Local Variables
Temporaries

Fields of Activation Record

0) Temporary values:-

The temporary values are needed during the evaluation of expressions. Such variables are stored in temporary field of activation record.

1) Local Variables

→ The local data is a data that is local to the execution of procedure is stored in this field of activation record.

2) Saved Machine Status:-

→ This field holds the information regarding the status of machine just before the procedure is called. This field contains the machine registers and program counter.

3) Control link

→ This field is optional. It points to the activation record of calling procedure. also called Dynamic Link

4) Access Link

→ Optional Field

→ It refers to non local data in other activation record

→ also called static link field

5) Actual Parameters

→ Holds info about actual parameters

→ These actual parameters are passed to the called procedure

6) Return Values:-

It is used to store result of function call

→ The size of each field of activation record is determined at the time when a procedure is called

Q, Compare Static Vs Dynamic Memory Allocation

Ans

Static Memory Allocation	Dynamic Memory
1) Memory is set aside before the program starts running	1) Set aside while the program is running as needed
2) Implemented using stack or data segment	2) heap
3) Fixed memory size	3) Flexible
4) Speed is faster (allocation happens at compile time)	4) Speed is slower (allocation happens during runtime)
5) Managed automatically by compiler	5) Manually managed by programmer
6) Less prone to errors	6) More
7) Less efficient in memory usage	7) More efficient

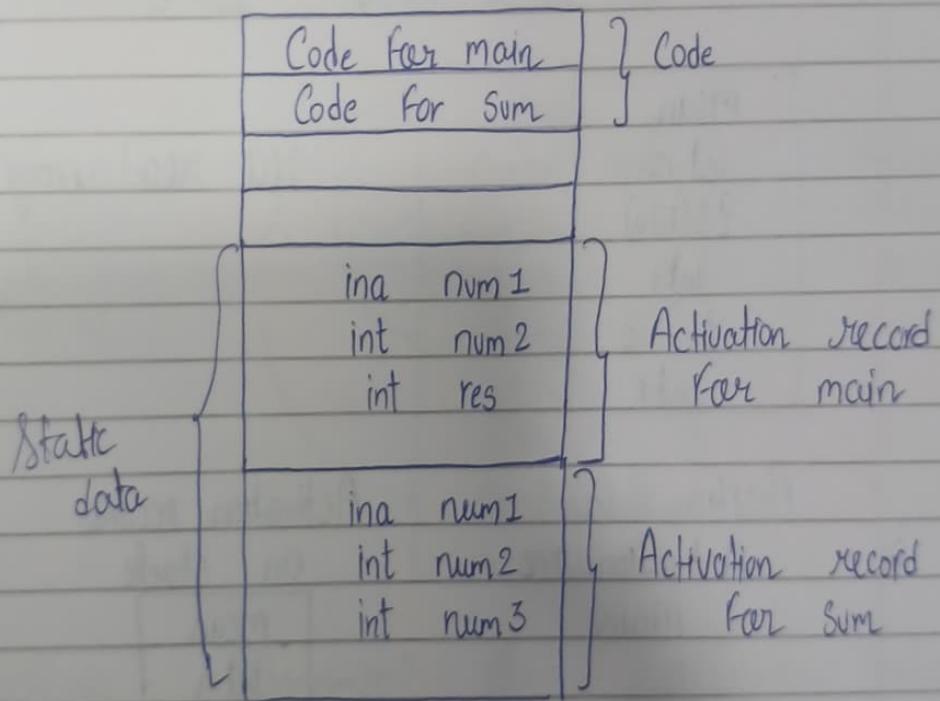
Q, Explain Storage allocation strategies

Ans

- 1) Static Allocation
- 2) Stack Allocation
- 3) Heap Allocation

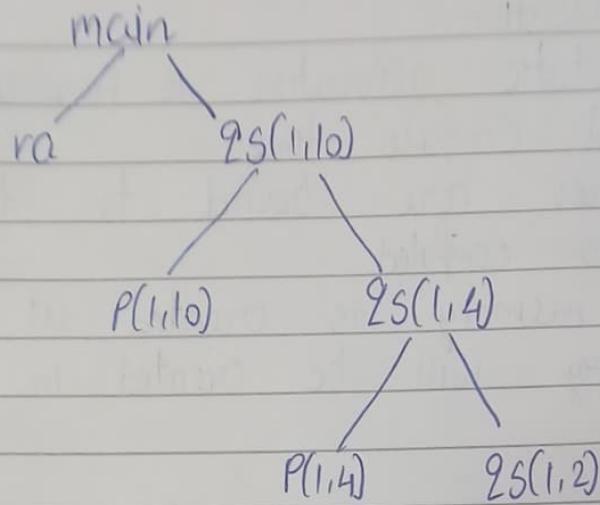
1) Static Allocation

- The static allocation is for all the data objects at compile time.
- Names are bound to storage as the program is compiled.
- If memory is created at compile time then the memory will be created in static area only once.



2) Stack Allocation

- Each time a procedure is called, space for its local variables is pushed onto a stack.
- And
- When a procedure terminates, the space is popped off the stack.
- Locals are bound to fresh storage in each activation.
- Locals are deleted when the activation ends.



main
int n
QS(1,10)
int i
QS(1,4)
int i

RA : read array()

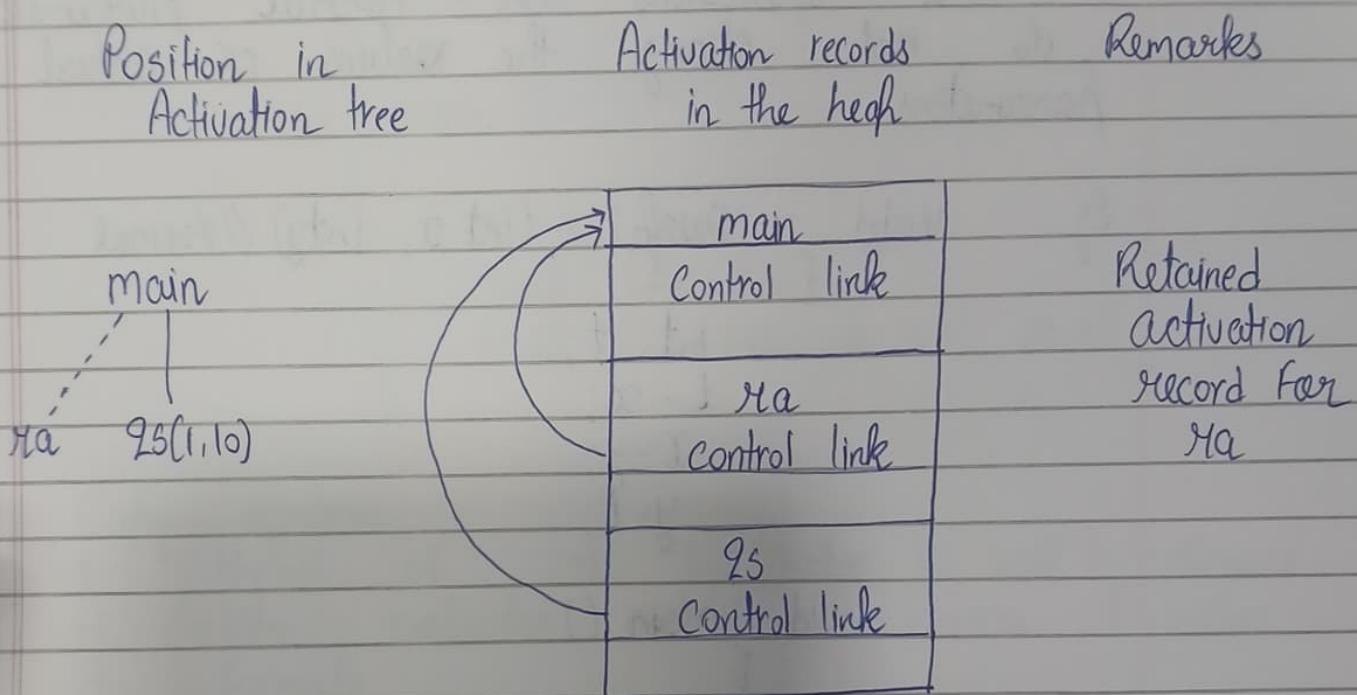
Position in Activation tree	Activation records on stack	Remarks		
i) Main	<table border="1"> <tr><td>main</td></tr> <tr><td>int n</td></tr> </table>	main	int n	Frame for main
main				
int n				

2)	<table> <tr><td>main</td></tr> <tr><td>/</td></tr> <tr><td>ra</td></tr> </table>	main	/	ra	<table border="1"> <tr><td>main</td></tr> <tr><td>intn</td></tr> <tr><td>ra</td></tr> <tr><td>inti</td></tr> </table>	main	intn	ra	inti	RA is activated
main										
/										
ra										
main										
intn										
ra										
inti										

3)	<table> <tr><td>main</td></tr> <tr><td>/</td></tr> <tr><td>ra</td></tr> <tr><td>QS(1,10)</td></tr> </table>	main	/	ra	QS(1,10)	<table border="1"> <tr><td>main</td></tr> <tr><td>intr</td></tr> <tr><td>QS(1,10)</td></tr> <tr><td>int i</td></tr> </table>	main	intr	QS(1,10)	int i	Frame ra has been popped & QS(1,10) is pushed
main											
/											
ra											
QS(1,10)											
main											
intr											
QS(1,10)											
int i											

3) Heap Allocation

- Stack Allocation is not possible when or
- 1) The values of local names must be retained when an activation ends
 - 2) A called activation outlives the caller



Q, Explain "Dynamic" Storage allocation techniques

Ans Write about Stack & Heap allocation

Q, Explain Various parameter passing methods

- Ans
- 1) call by value
 - 2) call by reference
 - 3) copy restore
 - 4) call by name

- 1) Call by value
- Simplest method
 - the actual parameters are evaluated and their r-values are passed to called procedure
 - the operations on formal parameters do not change the values of actual parameters

Eg: void swap (int x, int y) // formal

```
{  
    int t;  
    t = x;  
    x = y;  
    y = t;  
}
```

void main ()

{

// r-values

1, 2

(l)-value

a = 1 a
1
1000

int a=1, b=2;

swap (a, b); // Actual Parameters

printf ("a=%d, b=%d", a, b);

}

- 2) Call by Value Reference

→ This method is also called as call by address or call by location

→ The L-value, the address of actual parameter is passed to the called routines activation record

→ The values of actual parameters can be changed

→ Actual parameters should have an L-value

Eg:

```
void swap (int *x, int *y)
{
```

```
    int t;
    t = *x;
    *x = *y;
    *y = t;
```

```
}
```

```
void main ()
{
```

```
    int a=1, b=2;
    swap (&a, &b);
    printf ("a=%d, b=%d", a, b);
}
```

3) Copy Restore

- Hybrid of call by value & call by reference
- Caller evaluates actuals & passes r-value to formals
- During execution of called procedure, the actual parameters value is not affected
- When control returns, r-values of formals are copied back into l-values of actuals

Eg:

```
int y;
copy_restore (int x)
```

```
x=2;
```

```
y=0;
```

```
}
```

```
main () {
```

```
    y = 10;
```

```
    copy_restore (y);
```

```
    cout << y;
```

```
}
```

4) Call by Name

→ Actual parameters are literally substituted
for the formals
by macro expression or inline expansion

Eg:

```

int i=100;
Void callbyname (int x)
{
    foint(x);
    foint(x);
}
main()
{
    callbyname(i=i+1);
}
  
```

Q, Write a short note on Symbol table Management.

Ans

Symbol Table

→ Symbol tables are data structures that are used by compiler to hold information about source program constraints

→ It is used to store information about the occurrence of various entities such as objects, classes, variable names, functions etc

It is used by both analysis phase and synthesis phase

O Used for following purposes:-

→ It is used to store the name of all entities in a structured form at one place

- It is used to verify if a variable has been declared
- It is used to determine the scope of a name
- It is used to implement type checking by verifying assignments and expressions in source code are semantically correct.

Q. Difference between stack allocation and heap allocation of space

Ans	Parameter	Stack	Heap
1) Basic	Memory is allocated in a contiguous block	Memory is allocated in any random order	
2) Allocation and De-allocation	Automatic by compiler instructions	Manual by the programmer	
3) Cost	Less	More	
4) Implementation	Easy	Hard	
5) Main Issue	Shortage of memory	Memory Fragmentation	
6) Flexibility	Fixed size	Resizing is possible	

Q. What do you mean by dangling references

Ans A dangling reference is a situation in C where a pointer or reference points to a memory location that has been deallocated or released.

→ This can happen when an object is deleted or goes out of scope, but the reference to it still exists and is later accessed

Eg: `int *p = malloc(sizeof(int));`

`*p = 10;`

`free(p)`

`printf("%d", *p); // Invalid (dangling reference)`

Ch-7 Code Generation & Optimization

Q-1

Explain various issues in design of code generator [Asked 4 times] [7m]

Ans

Issues in Code Generation are

- 1) Input to code generator
- 2) Target Program
- 3) Memory Management
- 4) Instruction Selection
- 5) Register Allocation
- 6) Choice of evaluation
- 7) Approaches to good code generation

1) Input to code generator

→ Input to code generator consists of the intermediate representation of the source program.

→ Types of intermediate language are

1) Postfix Notation

2) Three Address Code

3) Syntax trees or DAGs

→ The detection of semantic error should be done before submitting the input to the code generator

→ The code generation phase requires complete error free intermediate code as an input

2) Target Program

The output maybe in form of

1) Absolute machine language : It can be placed in a memory location and immediately execute

- 2 Relocatable machine language : the subroutine can be compiled separately. A set of relocatable object modules can be linked together and loaded for execution.
- 3 Assembly language: Producing an assembly language program as output makes the process of code generation easier, then assembler is required to convert code in binary form.

3) Memory Management

- Mapping names in the source program to addresses of data objects in run time memory
- is done cooperatively by the Front-end and the code generator
- We assume that a name in a three-address statement refers to a symbol table entry for the name
- From the symbol table information, a relative address can be determined for the name in a data area

4) Instruction Selection

Example: the sequence of statements

$a = b + c$

$d = a + e$

would be translated into

MOV b,R0

ADD c,R0

MOV R0,a

MOV a,R0

ADD e,R0

MOV R0,d

MOV b,R0

ADD c,R0

ADD e,R0

MOV R0,d

→ So, we can eliminate redundant statements.

5) Register Allocation

- the use of registers is often subdivided into two sub problems
- During register allocation, we select the set of variables that will reside in registers at a point in the program
- During a subsequent register assignment phase, we pick the specific register that a variable will reside in
- Finding an optimal assignment of registers to variables is difficult, even with single register value.
- Mathematically the problem is NP-Complete

6) Choice of Evaluation

- The order in which computations are performed can affect the efficiency of the target code
- Some computation orders require fewer registers to hold intermediate results than others
- Picking a best order is another difficult, NP-Complete problem.

7) Approaches to code generation

- The most important criterion for a code generator is that it produces correct code
- the design of code generator should be in such a way so it can be implemented, tested, and maintained easily.

Ch - 7

Q-2

Describe various code optimization techniques with example

Ans

- (1) Compile time Evaluation
- (2) Common sub expressions elimination
- (3) Code Movement or Code Motion
- (4) Dead Code Elimination
- (5) Reduction in Strength

(1) Compile time Evaluation

→ Compile time evaluation means shifting of computations from run time to compilation time
Two methods

i) Folding

→ In this technique, the computation of constant is done at compile time instead of execution time
For example:

$$\text{length} = \frac{22}{7} * d$$

Here folding is implied by performing the computation of $\frac{22}{7}$ at compile time instead of execution time

ii) Constant Propagation

→ Here value of variable is replaced and computation of an expression is done at compilation time

Example : $\pi = 3.14;$

$$r = 5;$$

$$\text{Area} = \pi * r * r$$

$f_1 \rightarrow 314$
 $f \rightarrow 5$

- 2) Common Sub Expression Elimination
-1 Common sub expression is an expression occurring repeatedly in the program which is computed previously
→ If operands of this sub expression do not get changed at all then result of each sub expression is used instead of recomputing it each time.

For Example

$$\begin{aligned}t_1 &= 4 * i \\t_2 &= a[t_1] \\t_3 &= 4 * j \\t_4 &= 4 * i \\t_5 &= n \\t_6 &= b[t_4] + t_5\end{aligned}$$

After Optimization

$$\begin{aligned}t_1 &= 4 * i \\t_2 &= a[t_1] \\t_3 &= 4 * j \\t_5 &= n \\t_6 &= b[t_1] + t_5\end{aligned}$$

- 3) Code Movement or Code Motion
There are two basic goals of code movement:-
1) To reduce the size of the code ie to obtain
the complexity

To reduce the frequency of execution or code complexity
i.e. to obtain the time

Eg:

for { i=0; i<10; i++ }

$$x = y * 5;$$

$$\{ k = (y * 5) + 50;$$

After

$$\text{temp} = y * z$$

for { i=0; i<10; i++ }

$$x = z;$$

$$k = z + 50;$$

}

(4) Dead Code Elimination

- The variable is said to be dead at a point in a program if the value contained into it is never been used
- The code containing such a variable supposed to be dead code

Eg:

i = 0
if (i == 1)
{
 a = x + 5
}

} Dead Code

→

If statement is a dead code as the condition will never get satisfied hence, statement can be eliminated and optimization can be done.

5)

Strength Reduction
the strength of certain operators is higher than others

→

For instance strength of * is higher than +
In strength reduction technique the higher strength operators can be replaced by lower strength operators

For example

```
for (i=0; i<=50; i++)  
{  
    count = i * 7;  
}
```

Count values as 7, 14, 21

temp = 7

```
temp = 7  
  
for (i=0; i<=50; i++)  
{  
    count = temp;  
    temp = temp + 7;  
}  
end
```

Q-3

Explain Basic Block with example

Ans

A basic block is a sequence of consecutive statements in which flow of control enters at the beginning and leaves at the end or possibility of branching except at the end or halt.

Input: A sequence of three-address statements

Output: A list of basic blocks with each three address statement in exactly one block

Method

- 1) We first determine the set of leaders, for that we use the following rules:

- a) The first statement is leader
- b) Any statement that is the target of a conditional or unconditional goto is a leader
- c) Any statement that immediately follows a goto or conditional goto statement is a leader

- 2) For each leader, its basic block consists of the leader and all statements up to but not including the next leader or end of program

For example

$$(1) \quad \text{fmod} = 0$$

$$(2) \quad i := 1$$

$$(3) \quad t1 := 4 * i$$

$$(4) \quad t2 := a[t1]$$

$$(5) \quad t3 := 4 + i$$

$$(6) \quad t4 := b[t3]$$

$$(7) \quad ts := t2 * t4$$

$$(8) \quad t6 := \text{fmod} + ts$$

$$(9) \quad \text{fmod} := t6$$

$$(10) \quad t7 := i + 1$$

$$(11) \quad i := t7$$

$$(12) \quad \text{if } i < 20 \text{ goto(3)}$$

Explain Peephole optimization technique

Peephole optimization is a technique used to make the generated target code (like machine code or assembly code) slightly better (faster & smaller).

→ It's considered a local optimization because it only looks at a very small number of instructions at a time

Common Peephole Optimization Techniques

- 1) Redundant Store & Loads Elimination
- 2) Flow of Control Optimization
- 3) Algebraic Simplification
- 4) Reduction in Strength
- 5) Machine Idioms

1) Redundant Store & Loads Elimination

→ It is used to remove instructions that are unnecessary

Eg:

Original:

MOV R0, x

MOV x, R0

Optimization: If the value of x or R0 hasn't changed between these two instructions, the second MOV x,R0 is redundant and can be deleted

2) Flow of Control Optimization
 Explanation: Simplifying Sequences of jump

Eg. 1 (Jump over Jump)

Original

goto L1

--

L1: goto L2

Can be changed to goto L2;

If L1 is not targeted by any other jump;
 the L1: goto L2 might also become unreachable

Eg. 2 (Conditional Jump)

Original:

if a < b goto L1

--

L1: goto L2

Optimization:

Can be changed to if a < b goto L2;

3) Algebraic Simplification

→ Peephole optimization is an effective technique for algebraic simplification

→ The statements such as $x = x + 0$ or $x = x * 1$ can be eliminated by peephole optimization

4) Reduction in Strength

- Certain machine instructions are cheaper than others.
- In order to improve performance of the intermediate code we want replace these instructions by equivalent cheaper instruction.
- For example, x^2 is cheaper than $x * x$.
- Similarly, addition & subtraction are cheaper than multiplication and division. So we can add effectively equivalent add & sub for mul & div.

5) Using Machine Idioms

- The target instructions have equivalent machine instructions for performing some operations.
- Hence we can replace these target instructions by equivalent machine instructions in order to improve the efficiency.
- Some machines have auto-increment or auto-decrement addressing modes
(Eg: Inc i)
- These modes can be used in code for statement like $i = i + 1$

Q. What is global optimization? Name the 2 types of analysis performed for global optimization. **3M S22**

Global Optimization refers to code improvement techniques that look at larger parts of the program, like whole functions or loops, instead of just small sequences of instructions (basic blocks). The aim is to make the program better by understanding how different sections interact.

The two main types of analysis used for global optimization are:

1. **Control Flow Analysis:** This involves figuring out the structure of the program - how execution can jump between different sections (basic blocks). It helps identify loops and different paths the program might take.
2. **Data Flow Analysis:** This analysis tracks how data (the values stored in variables) moves through the program along the paths identified by control flow analysis. It helps determine things like where a variable gets its value, where that value is used, and whether a calculation might be redundant across different program sections.

Ch - 8 Instruction-level Parallelism

Q-1 Explain Code Scheduling Constraints

Ans Code scheduling is a form of program optimization that applies to the machine code that is produced by code generator.

Three kinds of constraints

- 1) Control dependence constraints: All the operations executed in original program must be executed in the optimized one.
- 2) Data Dependence constraints: The operations in the optimized program must produce the same result as the corresponding ones in the original program.
- 3) Resource Constraints: The schedule must not oversubscribe the resources of the machine.

- These scheduling constraints guarantee that the optimized program produces the same result as original.
- However, because code scheduling changes the order in which the operation execute, the state of the memory at any one point may not match any of the memory states in sequential execution.

Q-2 Explain Basic Block Scheduling in brief

Ans

- 1) Data-Dependence Graphs:
 - First step. We create a graph where each instruction (operation) is a node.
 - An edge from instruction A to instruction B means B depends on A's result.

- the edge is labeled with the delay needed between starting A and starting B
- this graph shows us the fundamental order we must respect

2 List Scheduling of Basic Blocks

- this is the main algorithm used for scheduling
- it keeps a list of instructions that are "ready" to run (all their dependencies are met)
- cycle by cycle, it picks one or more instructions from the ready list and schedules them making sure not to use more resources (like multipliers or memory units) than the processor has
- once scheduled, an instruction is removed, potentially making other instructions ready

3) Prioritized Topological Orders:

3. Prioritized Topological Orders:

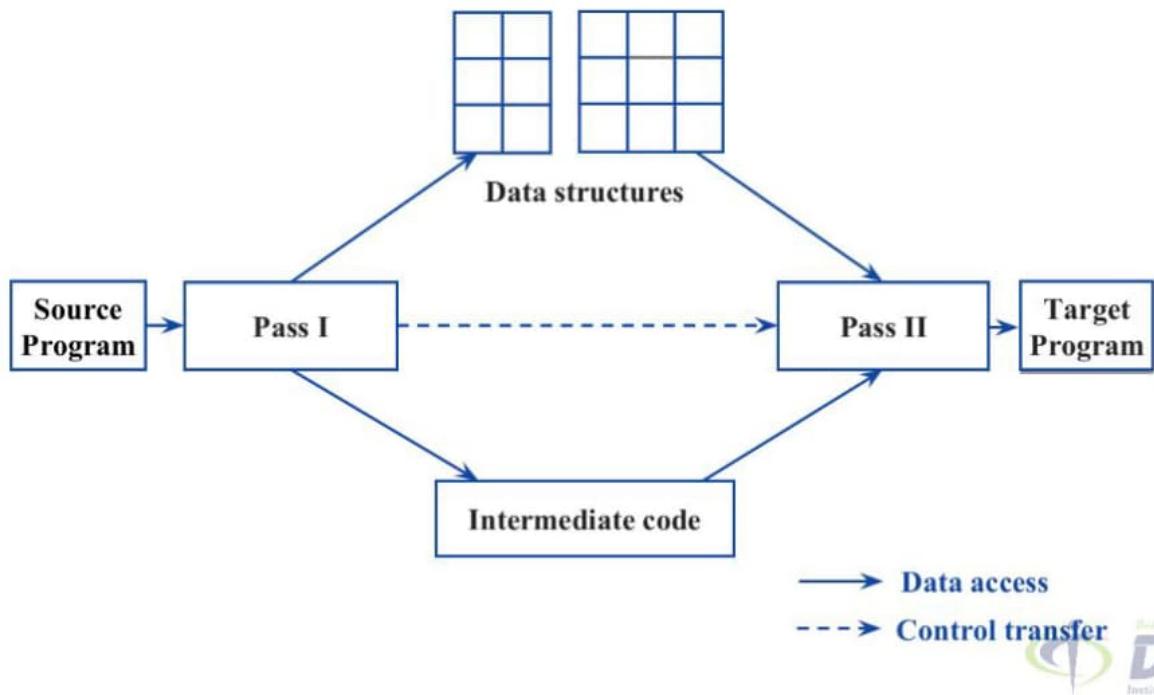
- This isn't a separate scheduling algorithm, but rather the **strategy** used within List Scheduling to decide **which instruction(s)** to pick from the ready list in each cycle. Since there might be multiple ready instructions, we need a way to prioritize.
- Common priorities (heuristics) include:
 - **Longest Path:** Pick the instruction that is part of the **longest remaining chain** of dependent instructions first. Finishing tasks on the longest chain helps the entire block finish sooner.
 - **Resource Usage:** Pick the instruction that needs a **busy or rare resource** first. This frees up that limited part sooner so other waiting instructions can use it.
 - **Source Order:** If multiple instructions seem equally important (it's a tie), just pick the one that appeared **earlier in the original code**.
- So, List Scheduling follows a topological order (respecting dependencies), but it uses these priorities to choose **which valid topological order** to create.

In short: You build the **Dependence Graph** first. Then you use the **List Scheduling algorithm**, and *within* that algorithm, you use a **Prioritized Topological Order** strategy to

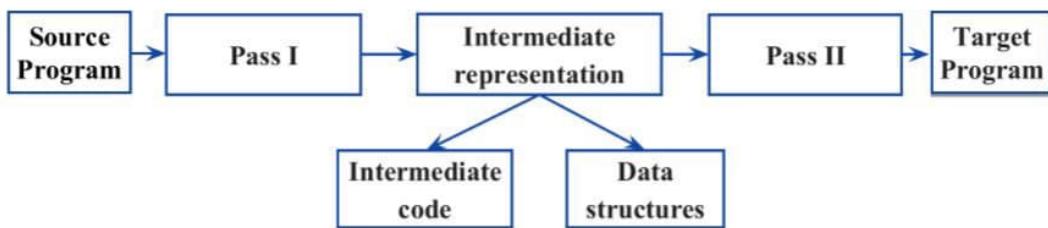
Pass structure of assembler

- A complete scan of the program is called pass.
- Types of assembler are:
 1. Two pass assembler (Two pass translation)
 2. Single pass assembler (Single pass translation)

Two pass assembler (Two pass translation)

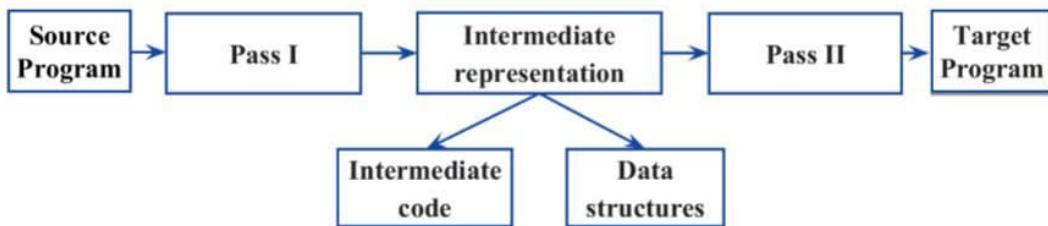


Two pass assembler (Two pass translation)



- The first pass performs **analysis of the source program**.
- The first pass performs **Location Counter processing** and records the addresses of symbols in the symbol table.
- It **constructs intermediate representation** of the source program.
- Intermediate representation consists of following two components:
 1. Intermediate code
 2. Data structures

Two pass assembler (Two pass translation)



- The second pass synthesizes the target program by using address information recorded in the symbol table.
- Two pass translation **handles a forward reference** to a symbol naturally because the address of each symbol would be known before program synthesis begins.

Use of a Symbol that
precedes its definition in a
program.

One pass assembler (One pass translation)

- A one pass assembler **requires one scan** of the source program to generate machine code.
- Location counter processing, symbol table construction and target code generation proceed in single pass.
- The issue of **forward references** can be solved using a process called **back patching**.