

Naïve Bayes





Probability

- Probability of an event happening = Number of ways it can happen/Total number of outcomes
- Independent Events - Events are not affected by previous events.
- Dependent Events - where what happens depends on what happened before, such as taking cards from a deck makes less cards each time.

Rishi Bansal

Example: Marbles in a Bag

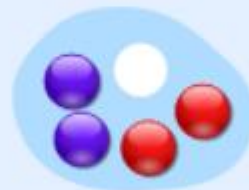
2 blue and 3 red marbles are in a bag.

What are the chances of getting a blue marble?

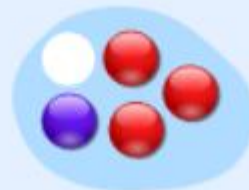
The chance is **2 in 5**

But after taking one out the chances change!

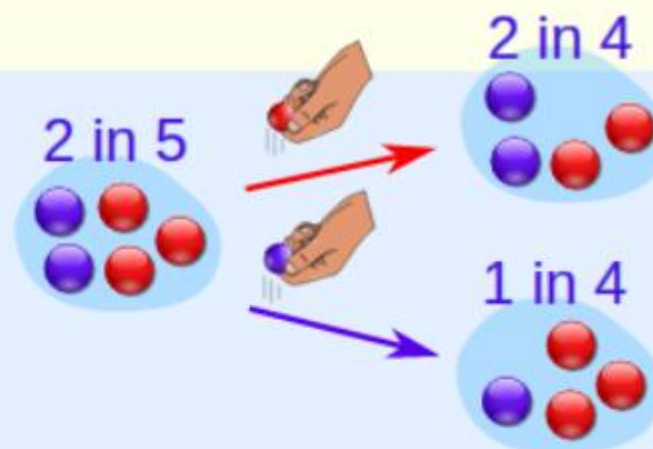
So the next time:



if we got a **red** marble before, then the chance of a blue marble next is **2 in 4**

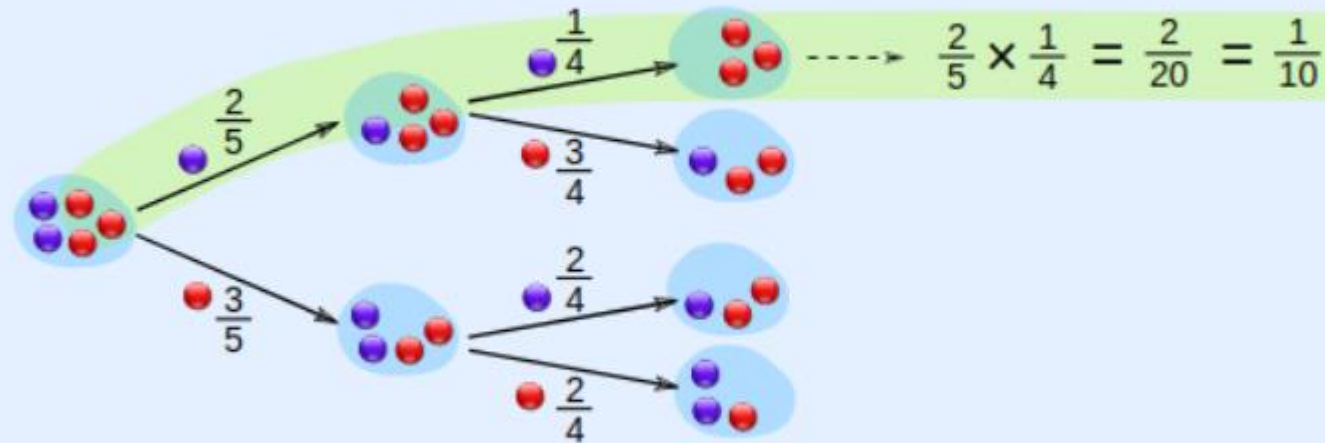


if we got a **blue** marble before, then the chance of a blue marble next is **1 in 4**



Now we can answer questions like "What are the chances of drawing 2 blue marbles?"

Answer: it is a **2/5 chance** followed by a **1/4 chance**:



Did you see how we multiplied the chances? And got 1/10 as a result.

The chances of drawing 2 blue marbles is 1/10



Conditional Probability

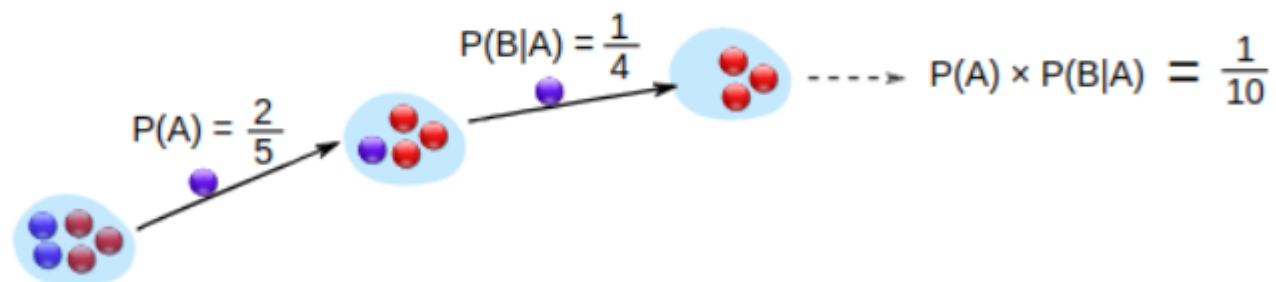
- $P(A)$ means "Probability Of Event A"
- In our marbles example Event A is "get a Blue Marble first" with a probability of $2/5$:
- $P(A) = 2/5$
- And Event B is "get a Blue Marble second" ... but for that we have 2 choices:
 - If we got a Blue Marble first the chance is now $1/4$
 - If we got a Red Marble first the chance is now $2/4$
- So we have to say which one we want, and use the symbol "|" to mean "given":
- $P(B|A)$ means "Event B given Event A"
- In other words, event A has already happened, now what is the chance of event B?

$P(B|A)$ is also called the "Conditional Probability" of B given A.

And in our case:

$$P(B|A) = 1/4$$

So the probability of getting **2 blue marbles** is:





Naïve Bayes

Its Naive(innocent) because it assumes that all the features are independent of each other. Which is almost never possible.

- Easy to understand.
- All features are independent.
- All impact results equally.
- Need small amount of data to train the model.
- Fast – up to 100X faster.
- It is highly scalable.
- It can make probabilistic predictions.
- It's simple & out-performs many sophisticated methods.
- Stable to data changes.



Bayes Theorem

- It describes the probability of an event, based on prior knowledge of conditions that might be related to the event

$$P(A|B) = \frac{P(B|A)*P(A)}{P(B)}$$

Rishi Bansal



Bayes Theorem Explained

Suppose:

- Fact_1 = 200 cars/day
- Fact_2 = 300 cars/day
- Out of all Cars produced: 2% are faulty/having issue Out of these faulty cars 50% came from each Factory.
- Question: What is the probability that a car manufactured by Fact_1 is faulty? $P(\text{Faulty} \mid \text{Fact}_1)$?



Bayes Theorem Explained

Solution:

- Car Manufactured by Factory 1: $P(\text{Fact_1}) = 200/200+300=0.4$
- Car Manufactured by Factory 2: $P(\text{Fact_2}) = 300/200+300=0.6$
- 2% of cars are Faulty = $P(\text{Faulty}) = 0.02$
- Probability of a Faulty Car coming out of Factory 1: $P(\text{Fact_1} \mid \text{Faulty}) = 0.5$
- Probability of a Faulty Car coming out of Factory 2: $P(\text{Fact_2} \mid \text{Faulty}) = 0.5$
- $P(\text{Faulty} \mid \text{Fact_1}) = P(\text{Fact_1} \mid \text{Faulty}) * P(\text{Faulty}) / P(\text{Fact_1}) = 0.5 * 0.02 / 0.4 = 2.5\%$



Bayes Theorem Explained

Example:

- Total 500 Cars
 - Fact_1 = 200
 - Fact_2 = 300
 - Faulty = 10
 - 50% came from Fact_1 = 5
 - % of Faulty Cars came from Fact_1 = $5/200 = 2.5\%$
- Rishi Bansal*



Types of Naïve Bayes

- Gaussian Naive Bayes - Feature columns are normal distribution
- Multinomial Naive bayes - Feature columns are counters
- Bernouli's Naive bayes - Feature columns are boolean

Rishi Bansal





Compare

Bernoulli Naive Bayes :

- assumes features are binary (e.g: 0 or 1)
- 0: word does not occur in the document
- 1: word occurs in the document

Multinomial Naive Bayes :

- used for discrete data (E.g: rolling dice, movie rating from 1 to 10, etc)
- In text learning we have the count of each word to predict the class or label.

Gaussian Naive Bayes :

- used for normal distribution which means all features are continuous



Bernouli vs Multinomial

In case of email classifier

Bernoulli :

- Assume spam mail has email handle in subject
- Build a feature where 0 means it's not present and 1 if it is there
- Binomial distribution

Multinomial:

- In addition to above condition, more dollar sign means spam more likely
- Same kind of word e.g: CASH or LOTTERY
- Label these words by their count
- Multinomial distribution