#### Recreation

What is the sum of the coefficients of

```
(1-3x+3x^2)^{743}(1+3x-3x^2)^{744}
```

after expanding and collecting terms?

## CS61B Lecture #5: Arrays

- An array is a structured container whose components are
  - length, a fixed integer.
  - a sequence of **length** simple containers of the same type, numbered from 0.
  - (.length field usually implicit in diagrams.)
- Arrays are anonymous, like other structured containers.
- Always referred to with pointers.
- For array pointed to by A,
  - Length is A.length
  - Numbered component i is A[i] (i is the index)
  - Important feature: index can be any integer expression.

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# A Few Samples

#### Java Results int[] x, y, z; 0 3 0 String[] a; у: x = new int[3];y = x;Z a = new String[3]; x[1] = 2;y[1] = 3;a[1] = "Hello"; Hello int[] q; q = new int[] { 1, 2, 3 }; 2 3 // Short form for declarations: $int[] r = { 7, 8, 9 };$ 8 9

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## Example: Accumulate Values

Problem: Sum up the elements of array A.

```
static int sum(int[] A) {
  int N;
  N = 0:
                                                       // New (1.5) syntax
  for (int i = 0; i < A.length; i += 1)
                                                       for (int x : A)
    N += A[i];
                                                          \mathbb{N} += x;
  return N;
// For the hard-core: could have written
int N, i;
for (i=0, N=0; i<A.length; N += A[i], i += 1)</pre>
  { } // or just ;
// But please don't: it's obscure.
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```

## Example: Insert into an Array

**Problem:** Want a call like insert(A, 2, "gnu") to convert (destructively)

```
A: bear sazelle hartebeest into skunk A: bear gazelle gnu hartebeest
```

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## (Aside) Java Shortcut

• Useful tip: Can write just 'arraycopy' by including at the top of the source file:

```
import static java.lang.System.arraycopy;
```

- This means "define the simple name arraycopy to be the equivalent of java.lang.System.arraycopy in the current source file."
- Can do the same for out so that you can write

```
out.println(...);
in place of
System.out.println(...);
```

• Finally, a declaration like

```
import static java.lang.Math.*;
```

means "take all the (public) static definitions in java.lang.Math and make them available in this source file by their simple names (the name after the last dot)."

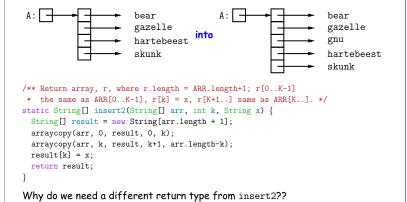
• Useful for functions like sin, sqrt, etc.

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### Growing an Array

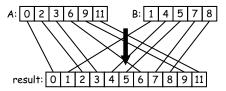
**Problem:** Suppose that we want to change the description above, so that  $A = insert2 \ (A, 2, "gnu")$  does not shove "skunk" off the end, but instead "grows" the array.



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## Example: Merging

**Problem:** Given two sorted arrays of ints, A and B, produce their *merge*: a sorted array containing all items from A and B.



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## Example: Merging Program

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**Problem:** Given two sorted arrays of ints, A and B, produce their *merge:* a sorted array containing all from A and B.

**Remark:** In order to solve this recursively, it is useful to *generalize* the original function to allow merging *portions* of the arrays.

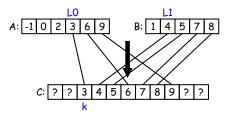
```
/** Assuming A and B are sorted, returns their merge. */
public static int[] merge(int[] A, int[] B) {
  return mergeTo(A, 0, B, 0);
/** The merge of A[LO..] and B[L1..] assuming A and B sorted. */
static int[] mergeTo(int[] A, int L0, int[] B, int L1) {
  int N = A.length - L0 + B.length - L1; int[] C = new int[N];
  if (LO >= A.length) arraycopy(B, L1, C, O, N);
                                                            What is wrong with
  else if (L1 >= B.length) arraycopy(A, L0, C, 0, N);
                                                            this implementation?
  else if (A[L0] <= B[L1]) {
     C[0] = A[L0]; arraycopy(mergeTo(A, L0+1, B, L1), 0, C, 1, N-1);
     C[0] = B[L1]; arraycopy(mergeTo(A, L0, B, L1+1), 0, C, 1, N-1);
  return C;
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```

## A Tail-Recursive Strategy

```
public static int[] merge(int[] A, int[] B) {
    return mergeTo(A, 0, B, 0, new int[A.length+B.length], 0);
}

/** Merge A[L0..] and B[L1..] into C[K..], assuming A and B sorted. */
static int[] mergeTo(int[] A, int L0, int[] B, int L1, int[] C, int k){
    ...
}
```

This last method merges part of A with part of B into part of C. For example, consider a possible call mergeTo(A, 3, B, 1, C, 2)



## A Tail-Recursive Solution

```
public static int[] merge(int[] A, int[] B) {
    return mergeTo(A, 0, B, 0, new int[A.length+B.length], 0);
}

/** Merge A[LO..] and B[L1..] into C[K..], assuming A and B sorted. */
    static int[] mergeTo(int[] A, int L0, int[] B, int L1, int[] C, int k){
        if (??) {
            return C;
        } else if (??) {
            C[k] = A[L0];
            return mergeTo(A, ??, B, ??, C, ??)
        } else {
            C[k] = B[L1];
            return mergeTo(A, ??, B, ??, C, ??)
        }
}
```

## A Tail-Recursive Solution

```
public static int[] merge(int[] A, int[] B) {
    return mergeTo(A, 0, B, 0, new int[A.length+B.length], 0);
}

/** Merge A[LO..] and B[L1..] into C[K..], assuming A and B sorted. */
static int[] mergeTo(int[] A, int L0, int[] B, int L1, int[] C, int k){
    if (LO >= A.length && L1 >= B.length) {
        return C;
    } else if (??) {
        C[k] = A[LO];
        return mergeTo(A, ??, B, ??, C, ??)
} else {
        C[k] = B[L1];
        return mergeTo(A, ??, B, ??, C, ??)
}
```

#### A Tail-Recursive Solution

```
public static int[] merge(int[] A, int[] B) {
    return mergeTo(A, 0, B, 0, new int[A.length+B.length], 0);
}

/** Merge A[L0..] and B[L1..] into C[K..], assuming A and B sorted. */
    static int[] mergeTo(int[] A, int L0, int[] B, int L1, int[] C, int k){
        if (L0 >= A.length && L1 >= B.length) {
            return C;
        } else if (L1 >= B.length || (L0 < A.length && A[L0] <= B[L1])) {
            C[k] = A[L0];
            return mergeTo(A, ??, B, ??, C, ??)
        } else {
            C[k] = B[L1];
            return mergeTo(A, ??, B, ??, C, ??)
        }
    }
}</pre>
```

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#### A Tail-Recursive Solution

```
public static int[] merge(int[] A, int[] B) {
    return mergeTo(A, 0, B, 0, new int[A.length+B.length], 0);
}

/** Merge A[LO..] and B[L1..] into C[K..], assuming A and B sorted. */
static int[] mergeTo(int[] A, int L0, int[] B, int L1, int[] C, int k){
    if (L0 >= A.length && L1 >= B.length) {
        return C;
    } else if (L1 >= B.length || (L0 < A.length && A[L0] <= B[L1])) {
        C[k] = A[L0];
        return mergeTo(A, L0 + 1, B, L1, C, k + 1);
    } else {
        C[k] = B[L1];
        return mergeTo(A, ??, B, ??, C, ??)
    }
}</pre>
```

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## A Tail-Recursive Solution

```
public static int[] merge(int[] A, int[] B) {
    return mergeTo(A, 0, B, 0, new int[A.length+B.length], 0);
}

/** Merge A[L0..] and B[L1..] into C[K..], assuming A and B sorted. */
    static int[] mergeTo(int[] A, int L0, int[] B, int L1, int[] C, int k){
        if (L0 >= A.length && L1 >= B.length) {
            return C;
        } else if (L1 >= B.length || (L0 < A.length && A[L0] <= B[L1])) {
            C[k] = A[L0];
            return mergeTo(A, L0 + 1, B, L1, C, k + 1);
        } else {
            C[k] = B[L1];
            return mergeTo(A, L0, B, L1 + 1, C, k + 1);
        }
}</pre>
```

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#### **Iterative Solution**

In general, we don't use either of the previous approaches in languages like C and Java. Array manipulation is most often iterative:

```
public static int[] merge(int[] A, int[] B) {
   int[] C = new int[A.length + B.length];
   // mergeTo(A, 0, B, 0, C, 0)
   int L0, L1, k;
   L0 = L1 = k = 0;

while (???) {
    if (L1 >= B.length || (L0 < A.length && A[L0] <= B[L1])) {
        C[k] = A[L0];
        ??
    } else {
        C[k] = B[L1];
        ??
    }
}
return C;
</pre>
```

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## **Iterative Solution**

In general, we don't use either of the previous approaches in languages like  ${\it C}$  and Java. Array manipulation is most often iterative:

```
public static int[] merge(int[] A, int[] B) {
    int[] C = new int[A.length + B.length];
    // mergeTo(A, O, B, O, C, O)
    int LO, L1, k;
    LO = L1 = k = 0;

while (LO < A.length || L1 < B.length) {
        if (L1 >= B.length || (L0 < A.length && A[LO] <= B[L1])) {
            C[k] = A[LO];
            ??
        } else {
            C[k] = B[L1];
            ??
        }
    }
    return C;
}</pre>
```

## Iterative Solution

In general, we don't use either of the previous approaches in languages like  ${\cal C}$  and Java. Array manipulation is most often iterative:

```
public static int[] merge(int[] A, int[] B) {
    int[] C = new int[A.length + B.length];
    // mergeTo(A, 0, B, 0, C, 0)
    int L0, L1, k;
    L0 = L1 = k = 0;

while (L0 < A.length || L1 < B.length) {
        if (L1 >= B.length || (L0 < A.length && A[L0] <= B[L1])) {
            C(k] = A[L0];
            L0 += 1; k += 1;
        } else {
            C(k] = B[L1];
            L1 += 1; k += 1;
        }
    }
    return C;
}</pre>
```

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### Iterative Solution II

```
The same, with a for loop:
```

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```
public static int[] merge(int[] A, int[] B) {
   int[] C = new int[A.length + B.length];
   int LO, L1;
   L0 = L1 = 0;
   for (int k = 0; k < C.length; k += 1) {
       if (L1 >= B.length || (L0 < A.length && A[L0] <= B[L1])) {
            C[k] = A[LO]; LO += 1;
        } else {
            C[k] = B[L1]; L1 += 1;
   return C:
Invariant (true after int k = 0):
  0 \leq L0 \leq A.length \ \land \ 0 \leq L1 \leq B.length \ \land \ C.length = A.length \ + B.length \ \land \ k = L0 + L1
  \land \ C[0:k] \ \text{is a permutation of A[0:L0] + B[0:L1]}
  \wedge C[0:k], A, B are sorted.
```

## Alternative Solution: Removing k

Using previous invariant that k=L0+L1 simplifies things:

```
public static int[] merge(int[] A, int[] B) {
   int[] C = new int[A.length + B.length];
   int L0, L1; L0 = L1 = 0;
   while (L0 + L1 < C.length) {</pre>
       if (L1 >= B.length || (L0 < A.length && A[L0] < B[L1])) {
           C[LO + L1] = A[LO]; LO += 1;
           C[LO + L1] = B[L1]; L1 += 1;
   return C;
                sorted
                                      В
                                                  sorted
                   10
                                                      1.1
                                         0
               sorted
         permutation of \alpha + \beta
```

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LO+L1

O

## Multidimensional Arrays

What about two- or higher-dimensional layouts, such as

$$A = \begin{array}{|c|c|c|c|c|c|}\hline 2 & 3 & 4 & 5 \\\hline 4 & 9 & 16 & 25 \\\hline 8 & 27 & 64 & 125 \\\hline \end{array}$$

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## Multidimensional Arrays in Java

These are not primitive in Java, but we can build them as arrays of arrays:

```
int[][] A = new int[3][];
  A[0] = new int[] {2, 3, 4, 5};
  A[1] = new int[] \{4, 9, 16, 25\};
  A[2] = new int[] \{8, 27, 64, 125\};
// or
  int[][] A;
  A = new int[][] { {2, 3, 4, 5},}
                    {4, 9, 16, 25},
                    { 8, 27, 64, 125} };
  int[][] A = { {2, 3, 4, 5},}
                                                              8 27 64 125
                {4, 9, 16, 25},
                {8, 27, 64, 125} };
// or
  int[][] A = new A[3][4];
  for (int i = 0; i < 3; i += 1)
      for (int j = 0; j < 4; j += 1)
          A[i][j] = (int) Math.pow(j + 2, i + 1);
```

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A.length+B.length

## Exotic Multidimensional Arrays

• Since every element of an array is independent, there is no single "width" in general:

```
int[][] A = new int[5][];
A[0] = new int[] {};
                                                         0 1
A[1] = new int[] \{0, 1\};
                                                         2 3 4 5
A[2] = new int[] \{2, 3, 4, 5\};
A[3] = new int[] \{6, 7, 8\};
A[4] = new int[] \{9\};
```

• What does this print?

```
int[][] ZERO = new int[3][];
ZERO[0] = ZERO[1] = ZERO[2] =
   new int[] {0, 0, 0};
ZERO[0][1] = 1;
System.out.println(ZERO[2][1]);
```

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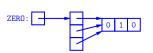
## Exotic Multidimensional Arrays

• Since every element of an array is independent, there is no single "width" in general:

```
int[][] A = new int[5][];
A[0] = new int[] {};
A[1] = new int[] \{0, 1\};
                                                             3 4 5
A[2] = new int[] \{2, 3, 4, 5\};
A[3] = new int[] \{6, 7, 8\};
A[4] = new int[] \{9\};
```

• What does this print?

```
int[][] ZERO = new int[3][];
ZERO[0] = ZERO[1] = ZERO[2] =
   new int[] {0, 0, 0};
ZERO[0][1] = 1;
System.out.println(ZERO[2][1]);
```



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