CS61B Lecture #4: Simple Pointer Manipulation

Recreation   Prove that for every acute angle $\alpha > 0$,

$$\tan \alpha + \cot \alpha \geq 2$$

Announcements

- **Today:** More pointer hacking.
- **Handing in labs and homework:** We'll be lenient about accepting late homework and labs for lab1, lab2, and hw0. Just get it done: part of the point is getting to understand the tools involved. We will *not* accept submissions by email.
- We will feel free to interpret the absence of a central repository for you or a lack of a lab1 submission from you as indicating that you intend to drop the course.
- HW1 to be released tonight (roughly).
- Project 0 to be released Friday.

Small Test of Understanding

- In Java, the keyword **final** in a variable declaration means that the variable's value may not be changed after the variable is initialized.
- Is the following class valid?

```
public class Issue {

    private final IntList aList = new IntList(0, null);

    public void modify(int k) {
        this.aList.head = k;
    }
}
```

Why or why not?

Small Test of Understanding

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- Is the following class valid?

```
public class Issue {

    private final IntList aList = new IntList(0, null);

    public void modify(int k) {
        this.aList.head = k;
    }
}
```

Why or why not?

Answer: This is *valid*. Although modify changes the head variable of the object pointed to by aList, it does *not* modify the contents of aList itself (which is a pointer).

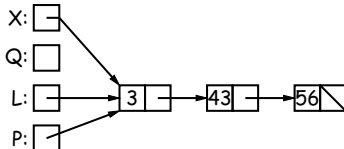
Destructive Incrementing

Destructive solutions may modify objects in the original list to save time or space:

```
/** Destructively add N to P's items. */
static IntList dincrList(IntList P, int n) {
  if (P == null)
    return null;
  else {
    P.head += n;
    P.tail = dincrList(P.tail, n);
    return P;
  }
}
/** Destructively add N to L's items. */
static IntList dincrList(IntList L, int n)
{
  // 'for' can do more than count!
  for (IntList p = L; p != null; p = p.tail)
    p.head += n;
  return L;
}
```

```
X = IntList.list(3, 43, 56);
/* IntList.list from HW #1 */
Q = dincrList(X, 2);
```
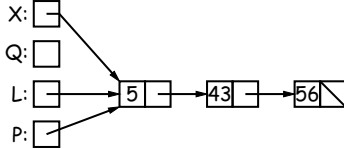

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}
/** Destructively add N to L's items. */
static IntList dincrList(IntList L, int n)
{
  // 'for' can do more than count!
  for (IntList p = L; p != null; p = p.tail)
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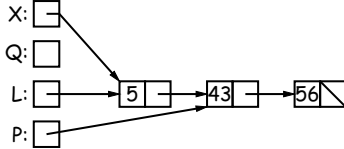
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}
/** Destructively add N to L's items. */
static IntList dincrList(IntList L, int n)
{
  // 'for' can do more than count!
  for (IntList p = L; p != null; p = p.tail)
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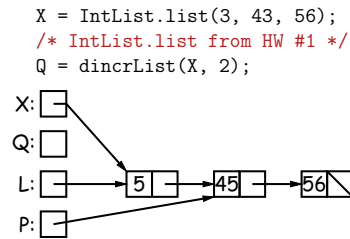
Slide 7

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    P.tail = dincrList(P.tail, n);
    return P;
  }
}
/** Destructively add N to L's items. */
static IntList dincrList(IntList L, int n)
{
  // 'for' can do more than count!
  for (IntList p = L; p != null; p = p.tail)
    p.head += n;
  return L;
}
```

```
X = IntList.list(3, 43, 56);
/* IntList.list from HW #1 */
Q = dincrList(X, 2);
```

X: →
Q:
L: → 5 → 45 → 56
P: →

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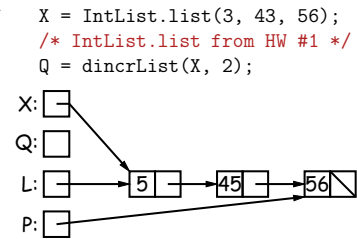### Destructive Incrementing

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}
/** Destructively add N to L's items. */
static IntList dincrList(IntList L, int n)
{
  // 'for' can do more than count!
  for (IntList p = L; p != null; p = p.tail)
    p.head += n;
  return L;
}
```

```
X = IntList.list(3, 43, 56);
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```

X: →
Q:
L: → 5 → 45 → 56
P: →

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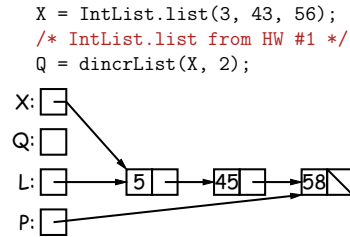### Destructive Incrementing

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}
/** Destructively add N to L's items. */
static IntList dincrList(IntList L, int n)
{
  // 'for' can do more than count!
  for (IntList p = L; p != null; p = p.tail)
    p.head += n;
  return L;
}
```

```
X = IntList.list(3, 43, 56);
/* IntList.list from HW #1 */
Q = dincrList(X, 2);
```

X: →
Q:
L: → 5 → 45 → 58
P: →

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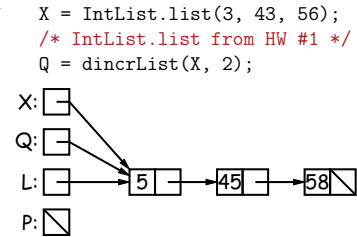### Destructive Incrementing

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static IntList dincrList(IntList L, int n)
{
  // 'for' can do more than count!
  for (IntList p = L; p != null; p = p.tail)
    p.head += n;
  return L;
}
```

```
X = IntList.list(3, 43, 56);
/* IntList.list from HW #1 */
Q = dincrList(X, 2);
```

X: →
Q: →
L: → 5 → 45 → 58
P: (null)

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Another Example: Non-destructive List Deletion

If L is the list [2, 1, 2, 9, 2], we want removeAll(L,2) to be the new list [1, 9].

```java
/** The list resulting from removing all instances of X from L
 *  non-destructively. */
static IntList removeAll(IntList L, int x) {
  if (L == null)
    return /*( null with all x's removed )*/;
  else if (L.head == x)
    return /*( L with all x's removed (L!=null, L.head==x) )*/;
  else
    return /*( L with all x's removed (L!=null, L.head!=x) )*/;
}
```

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Another Example: Non-destructive List Deletion

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static IntList removeAll(IntList L, int x) {
  if (L == null)
    return null;
  else if (L.head == x)
    return removeAll(L.tail, x);
  else
    return /*( L with all x's removed (L!=null, L.head!=x) )*/;
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Another Example: Non-destructive List Deletion

If L is the list [2, 1, 2, 9, 2], we want `removeAll(L,2)` to be the new list [1, 9].

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 *  non-destructively. */
static IntList removeAll(IntList L, int x) {
  if (L == null)
    return null;
  else if (L.head == x)
    return removeAll(L.tail, x);
  else
    return new IntList(L.head, removeAll(L.tail, x));
}
```

Iterative Non-destructive List Deletion

Same as before, but use front-to-back iteration rather than recursion.

```
/** The list resulting from removing all instances
 *  of X from L non-destructively. */
static IntList removeAll(IntList L, int x) {
  IntList result, last;
  result = last = null;
  for ( ; L != null; L = L.tail) {
    if (x == L.head)
      continue;
    else if (last == null)
      result = last = new IntList(L.head, null);
    else
      last = last.tail = new IntList(L.head, null);
  }
  return result;
}
```
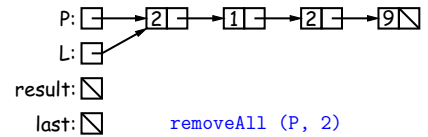

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removeAll (P, 2)

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}
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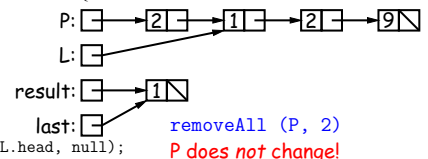

removeAll (P, 2)

P does *not* change!

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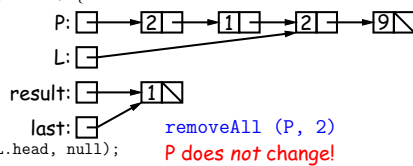

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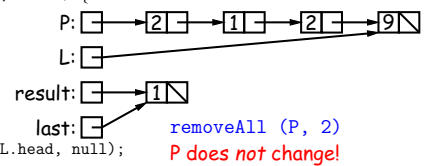
P: → 2 → 1 → 2 → 9

L:

result: → 1

last:

removeAll (P, 2)

P does not change!

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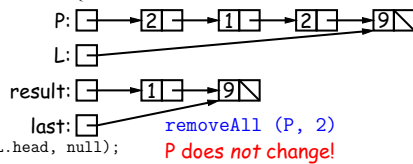
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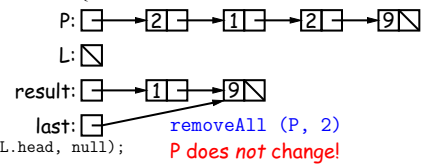
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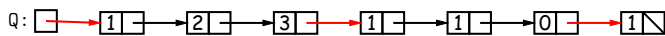
P: → 2 → 1 → 2 → 9

L:

result: → 1 → 9

last:

removeAll (P, 2)

P does not change!

Destructive Deletion

──→ : Original   ⋯⋯⋯ : after Q = dremoveAll (Q,1)

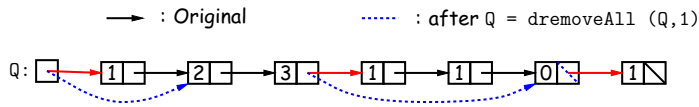Q: → 1 → 2 → 3 → 1 → 1 → 0 → 1

```
/** The list resulting from removing all instances of X from L.
 *  The original list may be destroyed. */
static IntList dremoveAll(IntList L, int x) {
  if (L == null)
    return /*( null with all x's removed )*/;
  else if (L.head == x)
    return /*( L with all x's removed (L != null) )*/;
  else {
    /*{ Remove all x's from L's tail. }*/;
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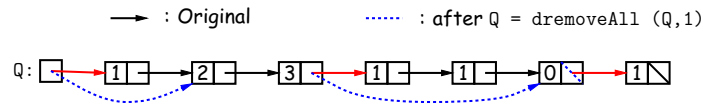
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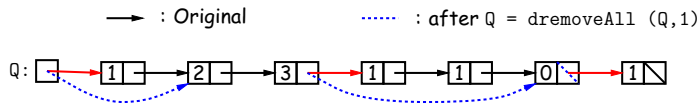Q: [·|·]→[1|·]→[2|·]→[3|·]→[1|·]→[1|·]→[0|·]→[1|\]

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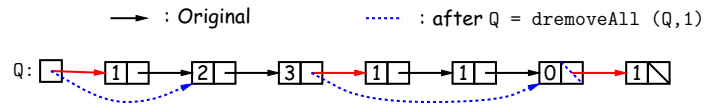Q: [·|·]→[1|·]→[2|·]→[3|·]→[1|·]→[1|·]→[0|·]→[1|\]

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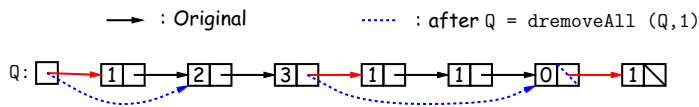Q: [·|·]→[1|·]→[2|·]→[3|·]→[1|·]→[1|·]→[0|·]→[1|\]

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Destructive Deletion

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    return dremoveAll(L.tail, x);
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}
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Destructive Deletion

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  if (L == null)
    return
  else if (L.head == x)
    return dremoveAll(L.tail, x);
  else {
    L.tail = dremoveAll(L.tail, x);
    return L;
  }
}
```

Iterative Destructive Deletion

```
/** The list resulting from removing all X's from L
 *  destructively. */
static IntList dremoveAll(IntList L, int x) {
  IntList result, last;
  result = last = null;
  while (L != null) {
    IntList next = L.tail;
    if (x != L.head) {
      if (last == null)
        result = last = L;
      else
        last = last.tail = L;
      L.tail = null;
    }
    L = next;
  }
  return result;
}
```
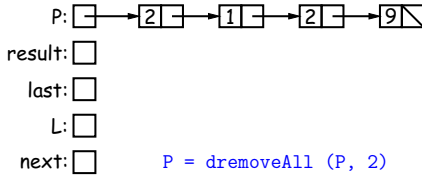
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Iterative Destructive Deletion

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  while (L != null) {
    IntList next = L.tail;
    if (x != L.head) {
      if (last == null)
        result = last = L;
      else
        last = last.tail = L;
      L.tail = null;
    }
    L = next;
  }
  return result;
}
```
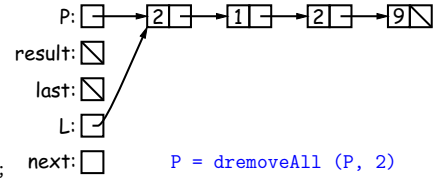
P: → 2 → 1 → 2 → 9
result:
last:
L:
next:

P = dremoveAll (P, 2)

Slide 32

Iterative Destructive Deletion

```
/** The list resulting from removing all X's from L
 *  destructively. */
static IntList dremoveAll(IntList L, int x) {
  IntList result, last;
  result = last = null;
  while (L != null) {
    IntList next = L.tail;
    if (x != L.head) {
      if (last == null)
        result = last = L;
      else
        last = last.tail = L;
      L.tail = null;
    }
    L = next;
  }
  return result;
}
```
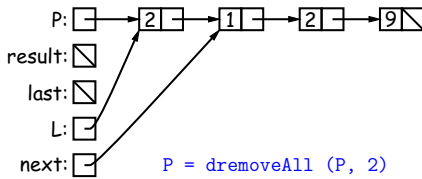
P: → 2 → 1 → 2 → 9
result:
last:
L:
next:

P = dremoveAll (P, 2)

Slide 33

Iterative Destructive Deletion

```
/** The list resulting from removing all X's from L
 *  destructively. */
static IntList dremoveAll(IntList L, int x) {
  IntList result, last;
  result = last = null;
  while (L != null) {
    IntList next = L.tail;
    if (x != L.head) {
      if (last == null)
        result = last = L;
      else
        last = last.tail = L;
      L.tail = null;
    }
    L = next;
  }
  return result;
}
```
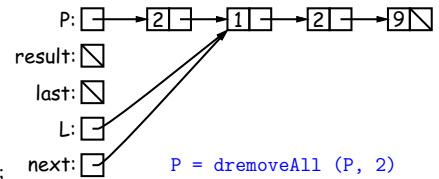
P: → 2 → 1 → 2 → 9
result:
last:
L:
next:

P = dremoveAll (P, 2)

Slide 34

Iterative Destructive Deletion

```
/** The list resulting from removing all X's from L
 *  destructively. */
static IntList dremoveAll(IntList L, int x) {
  IntList result, last;
  result = last = null;
  while (L != null) {
    IntList next = L.tail;
    if (x != L.head) {
      if (last == null)
        result = last = L;
      else
        last = last.tail = L;
      L.tail = null;
    }
    L = next;
  }
  return result;
}
```
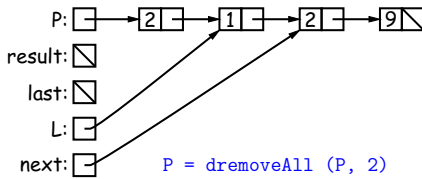
P: → 2 → 1 → 2 → 9
result:
last:
L:
next:

P = dremoveAll (P, 2)

Slide 35

Iterative Destructive Deletion

```
/** The list resulting from removing all X's from L
 *  destructively. */
static IntList dremoveAll(IntList L, int x) {
  IntList result, last;
  result = last = null;
  while (L != null) {
    IntList next = L.tail;
    if (x != L.head) {
      if (last == null)
        result = last = L;
      else
        last = last.tail = L;
      L.tail = null;
    }
    L = next;
  }
  return result;
}
```
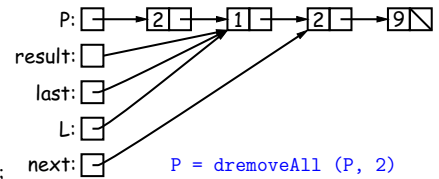
P: → 2 → 1 → 2 → 9
result:
last:
L:
next:

P = dremoveAll (P, 2)

Slide 36

Iterative Destructive Deletion

```
/** The list resulting from removing all X's from L
 *  destructively. */
static IntList dremoveAll(IntList L, int x) {
  IntList result, last;
  result = last = null;
  while (L != null) {
    IntList next = L.tail;
    if (x != L.head) {
      if (last == null)
        result = last = L;
      else
        last = last.tail = L;
      L.tail = null;
    }
    L = next;
  }
  return result;
}
```

P: → 2 → 1 → 2 → 9
result:
last:
L:
next:

P = dremoveAll (P, 2)

Slide 37

Iterative Destructive Deletion

```
/** The list resulting from removing all X's from L
 *  destructively. */
static IntList dremoveAll(IntList L, int x) {
  IntList result, last;
  result = last = null;
  while (L != null) {
    IntList next = L.tail;
    if (x != L.head) {
      if (last == null)
        result = last = L;
      else
        last = last.tail = L;
      L.tail = null;
    }
    L = next;
  }
  return result;
}
```
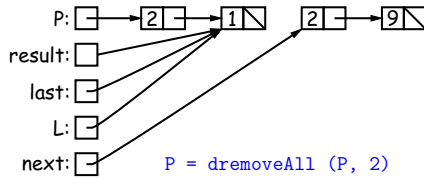
P: 2 → 1 ∅   2 → 9 ∅
result:
last:
L:
next:

P = dremoveAll (P, 2)

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Iterative Destructive Deletion

```
/** The list resulting from removing all X's from L
 *  destructively. */
static IntList dremoveAll(IntList L, int x) {
  IntList result, last;
  result = last = null;
  while (L != null) {
    IntList next = L.tail;
    if (x != L.head) {
      if (last == null)
        result = last = L;
      else
        last = last.tail = L;
      L.tail = null;
    }
    L = next;
  }
  return result;
}
```
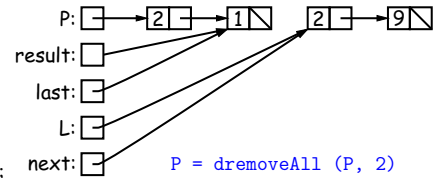
P: 2 → 1 ∅   2 → 9 ∅
result:
last:
L:
next:

P = dremoveAll (P, 2)

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Iterative Destructive Deletion

```
/** The list resulting from removing all X's from L
 *  destructively. */
static IntList dremoveAll(IntList L, int x) {
  IntList result, last;
  result = last = null;
  while (L != null) {
    IntList next = L.tail;
    if (x != L.head) {
      if (last == null)
        result = last = L;
      else
        last = last.tail = L;
      L.tail = null;
    }
    L = next;
  }
  return result;
}
```
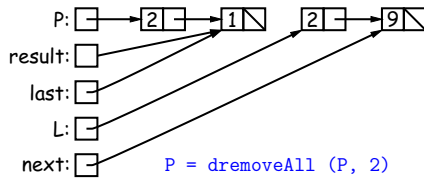
P: 2 → 1 ∅   2 → 9 ∅
result:
last:
L:
next:

P = dremoveAll (P, 2)

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Iterative Destructive Deletion

```
/** The list resulting from removing all X's from L
 *  destructively. */
static IntList dremoveAll(IntList L, int x) {
  IntList result, last;
  result = last = null;
  while (L != null) {
    IntList next = L.tail;
    if (x != L.head) {
      if (last == null)
        result = last = L;
      else
        last = last.tail = L;
      L.tail = null;
    }
    L = next;
  }
  return result;
}
```
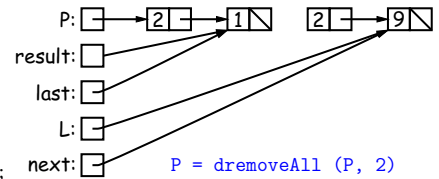
P: 2 → 1 ∅   2 → 9 ∅
result:
last:
L:
next:

P = dremoveAll (P, 2)

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Iterative Destructive Deletion

```
/** The list resulting from removing all X's from L
 *  destructively. */
static IntList dremoveAll(IntList L, int x) {
  IntList result, last;
  result = last = null;
  while (L != null) {
    IntList next = L.tail;
    if (x != L.head) {
      if (last == null)
        result = last = L;
      else
        last = last.tail = L;
      L.tail = null;
    }
    L = next;
  }
  return result;
}
```
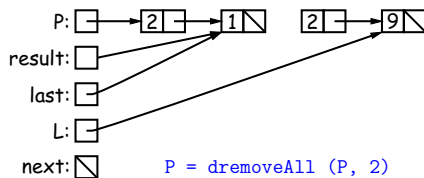
P: 2 → 1 ∅   2 → 9 ∅
result:
last:
L:
next: ∅

P = dremoveAll (P, 2)

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Iterative Destructive Deletion

```
/** The list resulting from removing all X's from L
 *  destructively. */
static IntList dremoveAll(IntList L, int x) {
  IntList result, last;
  result = last = null;
  while (L != null) {
    IntList next = L.tail;
    if (x != L.head) {
      if (last == null)
        result = last = L;
      else
        last = last.tail = L;
      L.tail = null;
    }
    L = next;
  }
  return result;
}
```
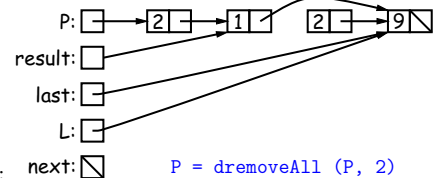
P: 2 → 1   2 → 9 ∅
result:
last:
L:
next: ∅

P = dremoveAll (P, 2)

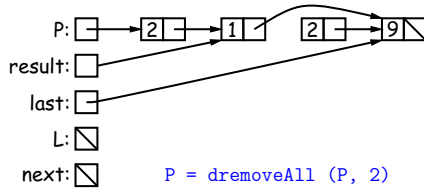*Last modified: Mon Feb 3 16:54:41 2020*   CS61B: Lecture #4   42

Iterative Destructive Deletion

```java
/** The list resulting from removing all X's from L
 *  destructively. */
static IntList dremoveAll(IntList L, int x) {
  IntList result, last;
  result = last = null;
  while (L != null) {
    IntList next = L.tail;
    if (x != L.head) {
      if (last == null)
        result = last = L;
      else
        last = last.tail = L;
      L.tail = null;
    }
    L = next;
  }
  return result;
}
```

P = dremoveAll (P, 2)

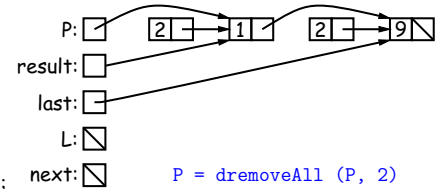## Iterative Destructive Deletion

```java
/** The list resulting from removing all X's from L
 *  destructively. */
static IntList dremoveAll(IntList L, int x) {
  IntList result, last;
  result = last = null;
  while (L != null) {
    IntList next = L.tail;
    if (x != L.head) {
      if (last == null)
        result = last = L;
      else
        last = last.tail = L;
      L.tail = null;
    }
    L = next;
  }
  return result;
}
```

P = dremoveAll (P, 2)

Aside: How to Write a Loop (in Theory)

- Try to give a description of how things look on *any arbitrary iteration* of the loop.

- This description is known as a *loop invariant,* because it is always true at the start of each iteration.

- The loop body then must
  - Start from any situation consistent with the invariant and condition;
  - Make progress in such a way as to make the invariant true again.

    ```
    // Invariant must be true here
    while (condition) { // condition must not have side-effects.
      // (Invariant and condition are necessarily true here.)
      loop body
      // Invariant must again be true here
    }
    // Invariant true and condition false.
    ```

- So if our loop gets the desired answer whenever *Invariant* is true and *condition* false, our job is done!

Relationship to Recursion

- Another way to see this is to consider an equivalent recursive procedure:

  ```
  /** Assuming Invariant, produce a situation where Inveriant
   *  is true and condition is false. */
  void loop() {
    // Invariant assumed true here.
    if (condition) {
      // Invariant and condition true here.
      loop body
      // Invariant must be true here.
      loop()
      // Invariant true here and condition false.
    } else { /* condition false here. */ }
  }
  ```

- Here, the invariant is the precondition of the function **loop**.

- The loop maintains the invariant while making the condition false.

- Idea is to arrange that our actual goal is implied by this post-condition.

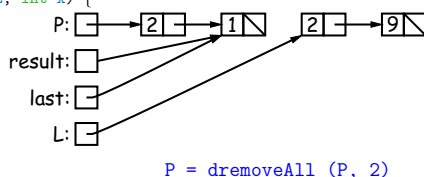## Example: Loop Invariant for dremoveAll

```java
/** The list resulting from removing all X's from L
 *  destructively. */
static IntList dremoveAll(IntList L, int x) {
  IntList result, last;
  result = last = null;
  while ** (L != null) {
    IntList next = L.tail;
    if (x != L.head) {
      if (last == null)
        result = last = L;
      else
        last = last.tail = L;
      L.tail = null;
    }
    L = next;
  }
  return result;
}
```

P = dremoveAll (P, 2)

** Invariant:

- `result` points to the list of items in the final result except for those from L onward.

- `L` points to an unchanged tail of the original list of items in `L`.

- `last` points to the last item in `result` or is null if `result` is null.