

⇒ ACTIVATION FUNCTIONS IN NN :

⇒ What are Activatⁿ functⁿ?

⇒ In ANN, each neuron forms a weighted sum of its i/p & passes the resulting scalar value through a function referred as ^{an} activatⁿ functⁿ (or) transfer functⁿ.

⇒ If a neuron has n i/p's the o/p (or) activatⁿ of a neuron is

$$a = g(w_1 x_1 + w_2 x_2 + w_3 x_3 + \dots + w_n x_n).$$

\downarrow
activatⁿ functⁿ.

⇒ It decides whether a neuron should be activated (or) not, and how strongly it should be activated.

⇒ Why do we need activatⁿ functⁿ?

⇒ If we don't apply A.F, the network will become a linear regression model, because o/p of the NN without AF, is simply linear combinatⁿ of i/p's.

⇒ \therefore To capture the non-linear nature of the data, we use A.F.

⇒ Ideal Activatⁿ Function : (characteristics):

- 1) Non-linear → To capture non-linearity.
- 2) Differentiable → to apply Gradient descent. → (then to apply backpropagatⁿ)
- 3) Computationally Inexpensive → calculatⁿ derivative, should be simple & fast.
- 4) Zero-centered : → the o/p from activatⁿ functⁿ should be normalized / zero-centered (mean = 0).
→ Ex: tanh

5) Non-saturating :- Saturatⁿ occurs in A.F when the o/p of the functⁿ approaches its max or min value. → (causes vanishing gradient problem)

⇒ like sigmoid squeeze o/p's to $[0, 1]$ & tanh to $[-1, 1]$

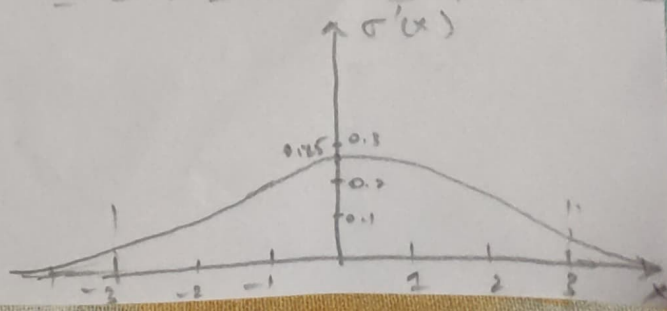
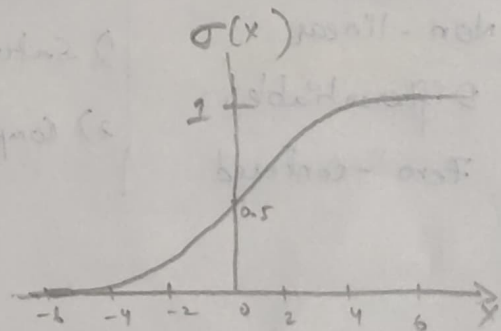
⇒ ReLU is a non-saturating, which operates in big range.

$$f(x) = \max(0, x)$$

⇒ SIGMOID ACTIVATION FUNCT^N :

$$\sigma(x) = f(x) = \frac{1}{1 + e^{-x}}$$

$$\max(\sigma'(x)) = 0.25$$



Advantages:

- 1) $\sigma(x) \in [0, 1] \rightarrow$ can be treated as probability
 \rightarrow can be used as "o/p layer" (for Binary classification)
- 2) Non-linear
- 3) It is Differentiable \rightarrow Grad. Descent can be applied

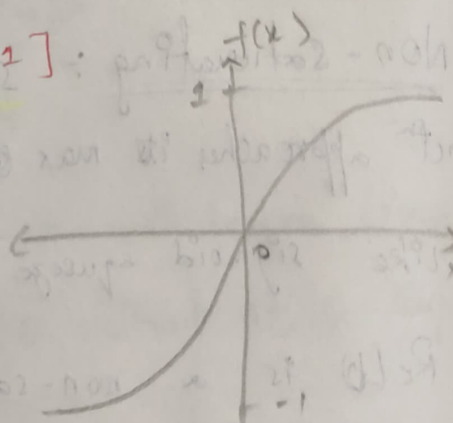
Disadvantages:

- \Rightarrow 1) Saturating function \rightarrow can cause vanishing gradient.
- \Rightarrow 2) Non-zero centered.

\Rightarrow Tanh Activation Function: $\in [-1, 1]$

$$f(x) = \frac{e^x - e^{-x}}{e^x + e^{-x}}$$

$$f'(x) = (1 - \tanh^2(x))$$

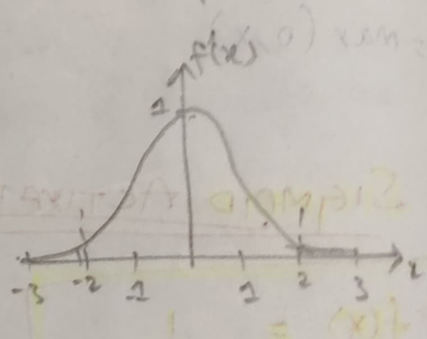


Advantages:

- 1) Non-linear
- 2) Differentiable
- 3) Zero-centered

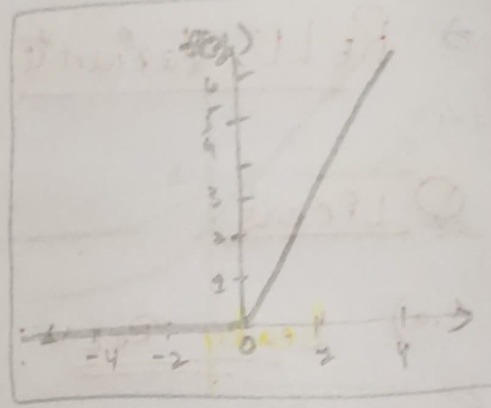
Disadv

- 1) Saturating function
- 2) Computationally expensive



⇒ ReLU Activation function :

$$f(x) = \max(0, x)$$



⇒ Adv.

1) Non-linear

2) Non-saturated in +ve region.

3) Computationally inexpensive

4) Convergence → faster

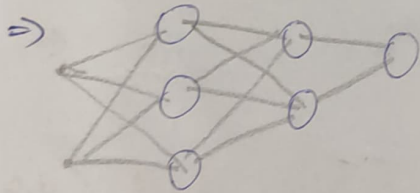
Dis Adv.

1) Not completely differentiable (Not differentiable at '0')

2) Non-zero centered.

3) Dying ReLU problem.

⇒ Dying ReLU Problem :



⇒ For some neurons, the value of O/p becomes 0 for any given I/P. (dead neuron)

⇒ These dead neuron, is forever dead.

⇒ If this happens to more than 50% neurons, the learning/capturing data will be less than 50%.

⇒

⇒ Solutions :

↳ ① set low learning rate

↳ ② bias → +ve value → 0.01

↳ ③ Don't use ReLU → instead use its variants.