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import numpy as np
import matplotlib.pyplot as plt
class TwoLayerNet(object):
  A two-layer fully-connected neural network. The net has an input dimension of
  D, a hidden layer dimension of H, and performs classification over C classes.
  We train the network with a softmax loss function and L2 regularization on the
  weight matrices. The network uses a ReLU nonlinearity after the first fully
  connected layer.
  In other words, the network has the following architecture:
  input - fully connected layer - ReLU - fully connected layer - softmax
  The outputs of the second fully-connected layer are the scores for each class.
  def __init__(self, input_size, hidden_size, output_size, std=1e-4):
    Initialize the model. Weights are initialized to small random values and
    biases are initialized to zero. Weights and biases are stored in the
    variable self.params, which is a dictionary with the following keys:
    W1: First layer weights; has shape (H, D)
    b1: First layer biases; has shape (H,)
    W2: Second layer weights; has shape (C, H)
    b2: Second layer biases; has shape (C,)
   Inputs:
    - input_size: The dimension D of the input data.
    - hidden_size: The number of neurons H in the hidden layer.
    - output_size: The number of classes C.
    self.params = {}
    self.params['W1'] = std * np.random.randn(hidden_size, input_size)
    self.params['b1'] = np.zeros(hidden_size)
    self.params['W2'] = std * np.random.randn(output_size, hidden_size)
    self.params['b2'] = np.zeros(output_size)
  def loss(self, X, y=None, reg=0.0):
    Compute the loss and gradients for a two layer fully connected neural
    network.
    - X: Input data of shape (N, D). Each X[i] is a training sample.
    - y: Vector of training labels. y[i] is the label for X[i], and each y[i] is
     an integer in the range 0 \leftarrow y[i] \leftarrow C. This parameter is optional; if it
      is not passed then we only return scores, and if it is passed then we
     instead return the loss and gradients.
    - reg: Regularization strength.
   Returns:
    If y is None, return a matrix scores of shape (N, C) where scores[i, c] is
    the score for class c on input X[i].
    If y is not None, instead return a tuple of:
    - loss: Loss (data loss and regularization loss) for this batch of training
    - grads: Dictionary mapping parameter names to gradients of those parameters
     with respect to the loss function; has the same keys as self.params.
    # Unpack variables from the params dictionary
    W1, b1 = self.params['W1'], self.params['b1']
    W2, b2 = self.params['W2'], self.params['b2']
   N, D = X.shape
    # Compute the forward pass
    scores = None
    # YOUR CODE HERE:
      Calculate the output scores of the neural network. The result
       should be (N, C). As stated in the description for this class,
       there should not be a ReLU layer after the second FC layer.
      The output of the second FC layer is the output scores. Do not
       use a for loop in your implementation.
    Hin = X@W1.T + b1
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Hout = Hin.copy()
 Hout[Hout < 0] = 0
 Z = Hout@W2.T + b2
 scores = Z
 # END YOUR CODE HERE
 # If the targets are not given then jump out, we're done
 if y is None:
  return scores
 # Compute the loss
 loss = None
            ------ #
 # YOUR CODE HERE:
 # Calculate the loss of the neural network. This includes the
    softmax loss and the L2 regularization for W1 and W2. Store the
    total loss in teh variable loss. Multiply the regularization
 # loss by 0.5 (in addition to the factor reg).
 exp_x = np.exp(scores - np.max(scores, axis=1).reshape(-1, 1))
 sum_x = np.sum(exp_x, axis=1).reshape(-1, 1)
 prob = exp_x / sum_x
 loss = 0.5 * reg * (np.power(np.linalg.norm(W1, "fro"), 2) + np.power(np.linalg.norm(W2, "fro"), 2)) # L2 regularization
 loss += -np.sum(np.log(prob[np.arange(N), y])) / N # softmax loss
 # END YOUR CODE HERE
 grads = {}
 # YOUR CODE HERE:
 # Implement the backward pass. Compute the derivatives of the
    weights and the biases. Store the results in the grads
    dictionary. e.g., grads['W1'] should store the gradient for
 # W1, and be of the same size as W1.
 C, H = W2.shape
 indicator = np.zeros((N,C))
 indicator[np.arange(N), y] = 1
 softmax = (prob.T - indicator.T) / N
 grads['W2'] = softmax@Hout + reg * W2
 grads['b2'] = np.sum(softmax, axis=1)
 relu_indicator = Hout/Hin
 H_grad = np.multiply(relu_indicator, (W2.T@softmax).T).T
 grads['W1'] = H_grad@X + reg * W1
 grads['b1'] = np.sum(H_grad, axis=1)
 # END YOUR CODE HERE
 return loss, grads
def train(self, X, y, X_val, y_val,
        learning_rate=1e-3, learning_rate_decay=0.95,
        reg=1e-5, num_iters=100,
        batch size=200, verbose=False):
 Train this neural network using stochastic gradient descent.
 Inputs:
 - X: A numpy array of shape (N, D) giving training data.
 - y: A numpy array f shape (N,) giving training labels; y[i] = c means that
   X[i] has label c, where 0 <= c < C.
 - X_val: A numpy array of shape (N_val, D) giving validation data.
 - y_val: A numpy array of shape (N_val,) giving validation labels.
   learning_rate: Scalar giving learning rate for optimization.
 - learning_rate_decay: Scalar giving factor used to decay the learning rate
  after each epoch.
 - reg: Scalar giving regularization strength.
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- num_iters: Number of steps to take when optimizing.
 - batch_size: Number of training examples to use per step.
 - verbose: boolean; if true print progress during optimization.
 num train = X.shape[0]
 iterations_per_epoch = max(num_train / batch_size, 1)
 # Use SGD to optimize the parameters in self.model
 loss history = []
 train_acc_history = []
 val_acc_history = []
 for it in np.arange(num iters):
   X_batch = None
   y batch = None
   # YOUR CODE HERE:
   # Create a minibatch by sampling batch_size samples randomly.
   batch_indices = np.random.choice(num_train, batch_size, replace=True)
   X batch = X[batch indices]
   y_batch = y[batch_indices]
   # END YOUR CODE HERE
   # ----- #
    # Compute loss and gradients using the current minibatch
   loss, grads = self.loss(X_batch, y=y_batch, reg=reg)
   loss_history.append(loss)
   # YOUR CODE HERE:
      Perform a gradient descent step using the minibatch to update
   # all parameters (i.e., W1, W2, b1, and b2).
   self.params['W1'] -= learning_rate * grads['W1']
   self.params['b1'] -= learning_rate * grads['b1']
   self.params['W2'] -= learning_rate * grads['W2']
   self.params['b2'] -= learning_rate * grads['b2']
   # END YOUR CODE HERE
   if verbose and it % 100 == 0:
    print('iteration {} / {}: loss {}'.format(it, num_iters, loss))
   # Every epoch, check train and val accuracy and decay learning rate.
   if it % iterations_per_epoch == 0:
     # Check accuracy
     train_acc = (self.predict(X_batch) == y_batch).mean()
     val_acc = (self.predict(X_val) == y_val).mean()
     train_acc_history.append(train_acc)
     val_acc_history.append(val_acc)
     # Decay learning rate
     learning_rate *= learning_rate_decay
   'loss_history': loss_history,
   'train_acc_history': train_acc_history,
   'val_acc_history': val_acc_history,
def predict(self, X):
 Use the trained weights of this two-layer network to predict labels for
 data points. For each data point we predict scores for each of the C
 classes, and assign each data point to the class with the highest score.
 Inputs:
 - X: A numpy array of shape (N, D) giving N D-dimensional data points to
  classify.
 Returns:
 - y_pred: A numpy array of shape (N,) giving predicted labels for each of
   the elements of X. For all i, y_pred[i] = c means that X[i] is predicted
   to have class c, where 0 \le c \le C.
 y_pred = None
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