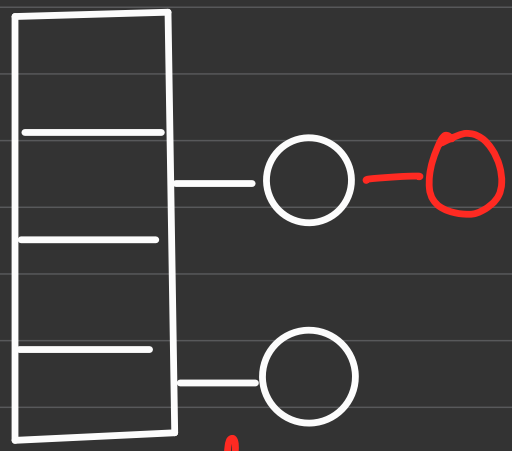


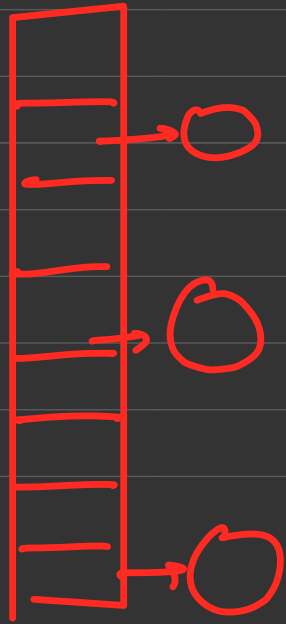
$\lambda = 0.5$



Relashij

1

$O(n)$



Completely analyse for arrays.

Internally arrays are always of fixed size.

How arrays handles dynamic insertion.

the moment the arrays is full & we need to insert more elements, we create a new

array of double the size of prev array &

then insert all the prev array elements to new array

Arrays

Capacity

Size

operations

1, 2, 3, 4, 5, 6, 7, 8, 9...

[1]

1

1

1

amortized

[1, 2]

2

2

2 $\rightarrow 2^0 + 1$

↓ ↓

[1, 2, 3, 4]

4

~~3~~
4

3 $\rightarrow 2^1 + 1$

↓

4

1

12 $\rightarrow 2^4 + 1$

[1, 2, 3, 4, 5, 6, 7, 8]

8

~~5~~
~~4~~
7

5 $\rightarrow 2^2 + 1$

1

1

[1, 2, 3, 4, 5, 6, 7, 8, 9]

9

8

1

9 $\rightarrow 2^3 + 1$

What will the avg complexity??

$$\text{avg} = \frac{\text{Total operation}}{\text{Total insertions}}$$

$$= \frac{1 + 2 + 3 + 1 + 5 + 1 + 1 + 1 + 9 + 1 + 1 + 1 + 1 + 1 + 1 + 1 + 1 + 12}{n}$$

$$(1 + 2 + 3 + 1 + 5 + 1 + 1 + 1 + 9 + 1 + 1 + \dots)$$

n

$$(1 + (2^0 + 1) + (2^1 + 1) + 1 + (2^2 + 1) + 1 + 1 + 1 + (2^3 + 1) + \dots)$$

$$\underbrace{(1 + 1 + 1 + 1 + \dots)}_{\rightarrow n \text{ 1's}} + \underbrace{(2^0 + 2^1 + 2^2 + \dots)}_{\rightarrow \log_2 \text{ terms}}$$

$$\underbrace{n + (2^0 + 2^1 + 2^2 + \dots)}_{n} \quad \rightarrow \log_2 \text{ terms}$$

$$\frac{n + (2^0 + 2^1 + 2^2 + \dots)}{n} \xrightarrow{\log_2 n \text{ times}}$$

$$\left(n + \frac{1 \times (2^{\log_2 n} - 1)}{2 - 1} \right)$$

$$\xrightarrow{n}$$

$$\frac{n + (2^{\log_2 n} - 1)}{n}$$

$$2 + 2^2 + 2^3 \dots$$

total no.
of GP

geometric
progression

$$\frac{a(x^n - 1)}{x - 1}$$

→ Sum of GP

first
term

multiplicative
factor

By logarithmic identity $2^{\log_2 n} = \underline{n}$

$$\hookrightarrow \frac{n + (2^{\log_2 n} - 1)}{n}$$

$$\Rightarrow \frac{n + (n - 1)}{n} \Rightarrow \frac{2n - 1}{n} \rightarrow \text{constant}$$

$$\text{avg} \rightarrow \underline{O(1)}$$

$$\text{worst} \rightarrow O(n)$$

$$\text{Best} \rightarrow \Omega(1)$$

$$[1]_1 \rightarrow 1$$

$$[1, 2]_2 \rightarrow 2$$

$$\begin{array}{c} [1, 2, 3]_3 \\ \quad \quad \quad \diagup \end{array}$$

$$\rightarrow 3$$

$$\underline{\underline{O(n)}}$$

$$[1, 2, 3, 4]_4$$

$$\rightarrow 4$$

$$\underline{\underline{O(n)}}$$

⋮

$$\underbrace{(1 + 2 + 3 + 4 + \dots + n)}_n$$

⋮

$$\rightarrow \underline{\underline{O(n)}}$$

[eat, tea, tam, ate, nat, bat]

{

get : [eat, tea, ate]

ant : [tam, nat]

abt : [bat]

}

We can maintain a window of unique chars

↓ st
a b a a c b x a y m n b d a c
↑ en

len $\rightarrow en - st + 1$

ans = 2 3 4 5 6 7

frequency

a: 2 1

b: 1 0 1 2

c: 1

x: 1

y: 1

m: 1

n: 1

}

$$O(N + 2N)$$

$$\sim \underline{\underline{O(N)}}$$

↓
[-3, -2, 7, 1, 3, 5, 2, 6, 11, 10, 4, -4, -5]

ans = 7

frequency

for uniquely identifying any consecutive sequence
→ if we know start of the sequence and
length of the sequence we can generate it.

What if we detect what all elements can be
start of some sequence ??

To check if any element x can become
start of a longest consecutive sequence or not
then we can try to check if $x+1$ is present
in the array or not.

→
[-3, -2, 7, 1, 3, 5, 2, 6, 11, 10, 4, -4, -5]

```
var longestConsecutive = function(nums) {  
  if(nums.length == 0) return 0;  
  let freq = {};  
  for(let i = 0; i < nums.length; i++) {  
    if(!freq[nums[i]]) freq[nums[i]] = 1;  
    else freq[nums[i]]++;  
  }  
  let ans = 1;  
  for(let i = 0; i < nums.length; i++) {  
    // check can nums[i] become start of a sequence  
    if(freq[nums[i] - 1]) continue;  
    // nums[i] is the start point  
    // check the max length sequence it can generate  
    let len = 0;  
    let el = nums[i];  
    while(freq[el]) {  
      el++;  
      len++;  
    }  
    ans = Math.max(ans, len);  
  }  
  return ans;  
};
```

~~ans = 7~~
=

len = 0 1 2 3 4 5 6 7
el = 1 2 3 4 5 6 7 8