

Supervised Learning - Regression

classmate

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Bias

- Bias →
- phenomenon that skews result of an algorithm in favor or against an idea
 - systematic error in ML models → incorrect assumptions.
 - Diff b/w average prediction of our model & correct value
 - Bias & variance → components of reducible error.

Low Bias → fewer assumptions → form of target function → by model

High Bias → more assumptions → unable to capture imp features of dataset → can't perform well on new data.

examples → Low Bias → decision trees, k-nearest neighbours & SVM.

examples → High Bias → linear discriminant analysis & logistic regn.

* Ways to Reduce High Bias -

- Increase input features as model is underfitted.
- Decrease regularization time period
- Use more complicate models → that have polynomial features
- Increase training data.
- Increase regularization term.

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Variance -

- changes in model when using different portions of training dataset.
- how much random variable differs from its expected value.
- based on single training set.
- measures inconsistency of diff predictions using diff training sets.
- Model \rightarrow high variance \rightarrow low bias & viceversa.
- comes with highly complex model with lot of features.
- contributes to flexibility of model.

high variance signs \rightarrow

- Noise in dataset
- overfitting
- complexity
- Forcing data points together.

- Low variance \rightarrow ^{small/} low variation in prediction of target functions.
- High variance \rightarrow large variation in prediction of target functions.

To Reduce High Variance

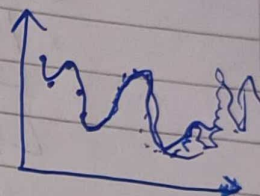
- Reduce input features or no. of parameters as a model is overfitted.
- Do not use a much complex model
- Increase training data.
- Increase the regularization term.

* Bias & Variance trade-off -

- Tradeoff b/w bias & variance is inversely proportional to variance
- tackle by either increasing a) complexity of model
b) Training dataset.

* Overfitting.

- statistical model fits against its matching data.
- Algo/ model can't perform well on unseen data.
- low bias & high variance.
- ~~unable~~ to match input data to target data.
- model \rightarrow ~~is~~ complex enough \rightarrow match all datapoint & performs well
- Reasons \rightarrow
 - noisy data
 - training data is too small
 - large no. of features.

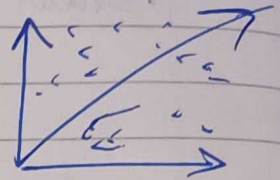


To avoid Overfitting

- Cross validation
- Train with more data.
- Removing features
- Early stopping the training
- Regularization
- Ensemble.

* Underfitting -

- Data model is unable to capture relationship b/w input & output.
 - occurs when model is too simple.
 - High bias low variance.
 - Larger quantity of features.
 - less data \rightarrow for model.
- To avoid underfitting.



- \rightarrow • growing educational time of model
- \rightarrow • By increasing the wide variety of functions.

* Regression -

- functional relationship between two or more ^{correlated} variables that often empirically determined from data & used to predict values of one variable given value of others.
- variable \rightarrow influence on output \rightarrow known as explanator, indepd. input or predictor variable.
- variable \rightarrow outcome depends on other variables \rightarrow dependant variable.
- dataset in which target values are known.

(correlation b/w dependant & indepdent variables).

desired output \rightarrow one or more continuous input \rightarrow regression.

* Linear Regression -

- ml algo \rightarrow supervised learning
- predict dependent variable based on independent.
- finding straight line that best approximates set of points on graph.
- simple linear regression \rightarrow only 1 independent variable
- multiple linear regression \rightarrow more than 1 independent variable
- $x \rightarrow$ independent variable
- $y \rightarrow$ ~~dependent variable~~ Output.

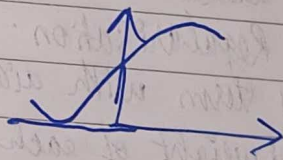
$$y = \beta_0 + \beta_1 + \beta_2 x_2 + \beta_3 x_3 + \dots + \beta_n x_n + \epsilon$$

Disadv \rightarrow • outliers affect.

• oversimplifies real world problems.

Use cases \rightarrow • Demand Forecasting • Healthcare • Other predictions.

* Logistic Regression.



- used to model & estimate probability of an event
- estimate problem. probability of an event occurring \rightarrow value (independent)
- Is a curve.
- sigmoid curve or S-curve in short.
- outcome data points \rightarrow 0 or 1.
- 0 \rightarrow totally uncertain 1 \rightarrow certain
- solve classification issues.
- predictive evaluation algo.
- predict likelihood of categorical dependent variable.

Type

• Binary \rightarrow 0/1, pass/fail

• Multi \rightarrow cats, dogs, lion

• ordinal \rightarrow low, medium & high

$$f(x) = \frac{1}{1 + e^{-x}}$$

• Lasso Regression -

- lessen complexity of version
- similar to ridge regⁿ except that penalty term includes only absolute weight (instead of rectangular of weights).
- L1 Regularisation
- avoids overfitting of training data & useful for feature selection
- shrinkage method. (least absolute selection & shrinkage operator)
- overcome disadv. of Ridge by not punishing high values of coefficient $\beta \rightarrow$ actually setting them to zero if not relevant.

$$L(x, y) = \text{Min} \left(\sum_{i=1}^n (y_i - w_i x_i)^2 + \lambda \sum_{i=1}^n |w_i| \right)$$

* Ridge Regression -

- small quantity bias delivered \rightarrow higher long time predictions.
- quantity added to bias \rightarrow ridge regression penalty
- L2 Regularisation.
- penalty term with aid of multiply with lambda to the squared weight of each individual features.

$$L(x, y) = \text{Min} \left(\sum_{i=1}^n (y_i - w_i x_i)^2 + \lambda \sum_{i=1}^n (w_i)^2 \right)$$

- Reduce complexity of version.
- clears up trouble if we have greater parameter than samples

$\uparrow \propto$ i.e. $\lambda \rightarrow$ more coefficient become ~~to~~ robust to collinearity.

Gradient Descent Algo -

(finds best fit line for given training dataset)

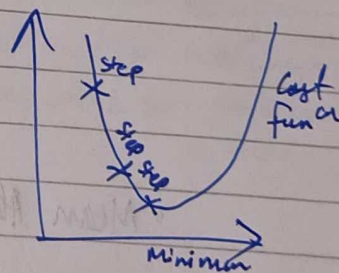
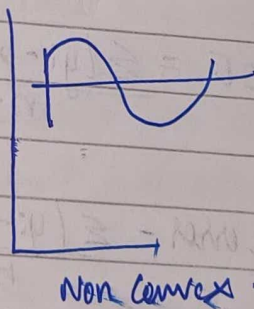
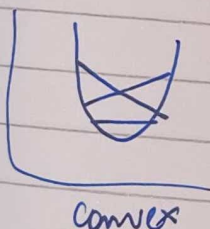
- optimization algo \rightarrow minimize cost function.
- locate least possible value \rightarrow fulfill a given function.

* Types

- Batch \rightarrow process all training ex. for each iteration.
- stochastic \rightarrow process 1 training example per iteration.
- Mini Batch \rightarrow More examples out of total training examples are processed per iteration.

* Funcⁿ requirement

- Differential - $f'(x)$ exists for every x in domain
- Convex - for an univariate funcⁿ line segment connecting two funcⁿ points lays on or above its curve.



Features

- Limitations \rightarrow relatively
- slow close to min.
 - for poorly conditioned convex problems gradient points orthogonally to steepest direction to min. speed

* Evaluation Metrics / Cost function -

- establish events or set of values to represent loss or penalty incurred in gaining something.
- Aka error cost function.
- The objective f's that need to be maximized are called reward/point/utility functions.

- Mean Error (ME) - mean of diff b/w actual & predicted value

$$ME = \frac{\sum (y_i - x_i)}{n}$$

- Mean squared error - diff b/w authentic & expected values extracted by squared the average distinction.

$$MSE = \frac{\sum (y_i - x_i)^2}{n}$$

- Mean Absolute error - $\frac{\sum (y_i - z_i)}{n} \rightarrow$

- RMSE Root Mean Squared Error - P

$$RMSE = \sqrt{MSE} = \sqrt{\frac{\sum (y_i - x_i)^2}{n}}$$

$$R^2 = \frac{\text{sum of squares due to regression}}{\text{total sum of squares.}}$$



shows how well data fits regression model.

$\uparrow R^2 \rightarrow$ Better is model.