# Mining Causality:

# AI-Assisted Search for Instrumental Variables\*

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#### Abstract

The instrumental variables (IVs) method is a leading empirical strategy for causal inference. Finding IVs is a heuristic and creative process, and justifying its validity—especially exclusion restrictions—is largely rhetorical. We propose using large language models (LLMs) to search for new IVs through narratives and counterfactual reasoning, similar to how a human researcher would. The stark difference, however, is that LLMs can dramatically accelerate this process and explore an extremely large search space. We demonstrate how to construct prompts to search for potentially valid IVs. We contend that multi-step and role-playing prompting strategies are effective for simulating the endogenous decision-making processes of economic agents and for navigating language models through the realm of real-world scenarios, rather than anchoring them within the narrow realm of academic discourses on IVs. We apply our method to three well-known examples in economics: returns to schooling, supply and demand, and peer effects. We then extend our strategy to finding (i) control variables in regression and difference-in-differences and (ii) running variables in regression discontinuity designs.

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# 1 Introduction

Endogeneity is the major obstacle in conducting causal inference in observational settings. Since the credibility revolution (Angrist and Pischke, 2010) and the causal revolution (Pearl, 2000), researchers in social science, statistics and other adjacent fields have developed various identification strategies to overcome endogeneity by restoring versions of quasi-experiments. A leading strategy is the instrumental variables (IVs) method. Over decades, researchers with their ingenuity have discovered IVs in various settings and justified their satisfaction of exclusion restrictions (e.g., IVs are conditionally exogenous of latent variables). With its various applicability, the IVs method has prevailed across all subfields of economics and beyond (e.g., Imbens and Angrist, 1994; Blundell and Powell, 2003; Heckman and Vytlacil, 2005; Hernán and Robins, 2006).

Exclusion restrictions are fundamentally untestable assumptions.<sup>2</sup> Often, in justifying them, researchers resort to *rhetorical* arguments specific to each setting. This non-statistical process follows the discovery of potential candidate IVs, which itself requires researchers' counterfactual reasoning and creativity—and sometimes luck. These elements all contribute to the heuristic processes employed by human researchers.

We demonstrate that large language models (LLMs) can facilitate the discovery of new IVs. Considering that narratives are the primary method of supporting IV exclusion, we believe that LLMs, with sophisticated language processing abilities, are well-suited to assist in the search for new valid IVs and justify them rhetorically, just as human researchers have done for decades. The stark difference, however, is that LLMs can accelerate this process at

<sup>&</sup>lt;sup>1</sup>See Mogstad and Torgovitsky (2024) for a more recent survey.

<sup>&</sup>lt;sup>2</sup>An exception is a favorable situation where one enjoys over-identifying restrictions. We discuss this point in our context below. Unlike the exclusion restriction, the IV relevance is testable from data (Stock and Yogo, 2005; Olea and Pflueger, 2013).

an exponentially faster rate and explore an extremely large search space, to an extent that human researchers cannot match. It is now recognized that artificial intelligence (AI) shows remarkable performances in conducting systematic searches for hypotheses and refining the search (e.g., Jumper et al., 2021; Ludwig and Mullainathan, 2024). Furthermore, LLMs are argued to be capable of conducting counterfactual reasoning—or, perhaps more precisely, exploring alternative scenarios—which makes them a promising tool for causal inference.

There are at least four benefits to pursuing this AI-assisted approach to discovering IVs. First, researchers can conduct a systematic search at a speedy rate, while adapting to the particularities of their settings. Second, interacting with AI tools can inspire ideas for possible domains for novel IVs. Third, the systematic search could increase the possibility of obtaining multiple IVs, which would then enable formal (i.e., statistical) testing of their validity via over-identifying restrictions. Fourth, having a list of candidate IVs would increase the chances of finding actual data that contain IVs or guide the construction of such data, including the design of experiments to generate IVs.

We show how to construct prompts in a way that guides LLMs to search for candidates for valid IVs. The text representation of exclusion restrictions (among others) is the main component of the prompts. We propose a multi-step approach in prompting that divides a discovery task into multiple subtasks, and thus separates counterfactual statements of different complexities. At the same time, we propose using role-playing prompts, arguing that they align with the very source of endogeneity, namely, agents' decisions. By doing so, we equip LLMs with the perspective of agents, enabling them to mimic agents' endogenous decision-making processes and gather contextual information in realistic scenarios. This approach also makes it convenient to impose statistical conditioning that qualifies the characteristics of the agent. Another benefit of multi-stage, role-playing prompts is that they help navigate language models through the realm of real-world scenarios, rather than anchor them within the narrow realm of academic discourses on IVs. Each stage's prompt focuses only

<sup>&</sup>lt;sup>3</sup>Decisions of economic agents have been at the root of challenges for causal analyses in econometrics (e.g., Heckman, 1979; Manski, 1993).

on a portion of the IV assumptions, translated into an agent's real-world problem, thereby minimizing the likelihood that the LLM perceives the task as a search for IVs.<sup>4</sup>

To prove the proposed concept and illustrate the actual performance of an LLM, we conduct discovery exercises using OpenAI's ChatGPT-4 (GPT4), one of the leading LLMs, to find IVs in three well-known examples in empirical economics: returns to schooling, supply and demand, and peer effects. In all three examples, GPT4 produced a list of candidate IVs, some of which appear to be new in the literature and provided rationale for their validity. The list also contains IVs that are popularly used in the literature. Our initial assessment of the results suggests that the proposed method can work in practice. In the peer effect example, we also demonstrate that the proposed method can be effective in exploring relatively new topics for empirical research, which may in turn increase the possibility of finding novel IVs.

From a broader perspective, the proposal is to systematically "search for exogeneity." We extend the exercise to other causal inference methods: (i) searching for control variables in regression and difference-in-differences methods and (ii) searching for running variables in regression discontinuity designs. We construct relevant prompts and run them in well-known examples in the literature.

A list of candidate IVs or control variables produced as a result of the proposed method is not absolute. Rather, we hope that it serves as a valuable benchmark that inspires empirical researchers about which types of variables to consider and which domains to explore. The dialogue carried out with LLMs in the process can also help researchers solidify arguments or counterarguments for the validity of variables. After all, AI—like any machines—cannot be the ultimate authority (at least not yet). We believe a human researcher assisted by AI can choose research designs and conduct causal inference more effectively.

This essay contributes to a recent agenda in the social science literature on using AI to assist creative and heuristic parts of human research processes. This agenda views machine learning and AI as not only data-processing and prediction tools for economic research (Mul-

<sup>&</sup>lt;sup>4</sup>Even if LLMs exhibit *memorization* from academic texts, we still find value in the procedure as long as the list of discovered IVs includes those that are recognized as new by researchers.

lainathan and Spiess, 2017; Athey and Imbens, 2019), but also as tools that can improve conventional research practices themselves. In very interesting work, Ludwig and Mullainathan (2024) use generative models to systematically produce hypotheses that are comprehensible by humans in otherwise daunting settings. They make progress in research areas where the use of AI has been limited because, as they argue, establishing causal relationships in social science is an "open world" problem, unlike "closed world" problems in physical science. In related work, Mullainathan and Rambachan (2024) use predictive (neural network) algorithms to recover old anomalies and discover new ones in economic theory models. We do not attempt to generate hypotheses, although the new variables discovered implicitly maintain a range of hypotheses on their validity.

LLMs has only very recently been used in social science research. Notably, Du et al. (2024) use fine-tuned LLMs (Meta's LLaMA in particular) to predict job transitions and understand career trajectories in labor economics. They show that the prediction accuracy remarkably outperforms those from traditional job transition economic models. Manning et al. (2024) propose to use LLMs to automate the entire process of social scientific research, from data generation to testing causal hypotheses. We employ LLMs in statistical causal inference by incorporating specific structure from econometric assumptions and allowing for human intervention in discovery processes. Overall, this essay contributes to posing philosophical questions on how social science researchers should conduct research in the AI era.

The paper is organized as follows. Section 2 states the IV assumptions and Section 3 proposes the main idea of IV discovery along with the prompting strategies. Section 4 provides the examples of discovered IVs. Sections 5–6 contain extensions: (i) the use of an adversarial LLM to review and refine the discovery process and (ii) the extension of the paper's approach to other causal inference settings. Section 7 concludes.

<sup>&</sup>lt;sup>5</sup>The latter can be viewed as extremely difficult computation problems where machine learning makes significant progress; e.g., detecting new proteins using AlphaFold (Jumper et al., 2021) or advances in particle physics and cosmology using machine learning (Carleo et al., 2019).

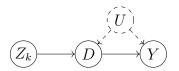


Figure 1: Causal DAG for a Valid IV (X suppressed)

# 2 Notation and IV Assumptions

We first formally state our discovery goal. Let Y be the outcome of interest, D be the potentially endogenous treatment,  $\mathcal{Z}_K \equiv \{Z_1, ..., Z_K\}$  be the list of IVs  $Z_k$ 's with K being the desired number of IVs to discover, and X be the covariates. Let  $Y(d, z_k)$  be the counterfactual outcome given  $(d, z_k)$ . Let " $\bot$ " denote statistical independence. We say  $Z_k$  is a valid IV if it satisfies the following two assumptions:

**Assumption REL** (Relevance). Conditional on X, the distribution of D given  $Z_k = z_k$  is a nontrivial function of  $z_k$ .

**Assumption EX** (Exclusion). For any  $(d, z_k)$ ,  $Y(d, z_k) = Y(d)$ .

**Assumption IND** (Independence). For any d,  $Y(d) \perp Z_k$  conditional on X.

The goal of our exercise is to search for IVs that satisfy Assumptions REL, EX and IND.<sup>6</sup> Suppressing X, Figure 1 depicts the causal direct acyclic graph (DAG) that implies REL, EX and IND and with Y(d) being a transformation of latent confounders U. This diagram is useful in describing our procedures.

# 3 Prompt Construction

We propose a two-step approach for IV discovery. In Step 1, we prompt an LLM to search for IVs that satisfy a verbal description of REL and EX (i.e.,  $(Z_k) \longrightarrow (D) \longrightarrow (Y)$ ). In Step 2, we prompt the LLM to refine the search by selecting—among the IVs found in Step 1—those that satisfy a verbal description of IND (i.e.,  $(Z_k) \longrightarrow (U)$ ). In both steps, the prompts will

<sup>&</sup>lt;sup>6</sup>One can consider a weaker version of IND (i.e., mean independence and nonzero correlation). Although we do not believe our ultimate findings significantly differ from this relaxation, our prompts can reflect it.

involve counterfactual statements. In each step, we ask the LLM to provide rationale for its responses. This feature is useful for the user to understand the LLM's reasoning. The two steps can be conducted in the same session or in separate sessions. However, when submitting different queries, we recommend that each two-step query be conducted in a separate session to avoid interference across queries. In Appendix A.1, we also present a full three-step prompting that focuses on each of Assumptions REL, EX and IND in each step.

We propose a multi-step approach for several reasons: First, LLMs are known to yield better performance when handling subtasks step-by-step, focusing on important details in interpreting the prompts and avoiding errors (Wu et al., 2022). Second, this approach creates more room for the user to inspect intermediate outputs, facilitating the evaluation of final outputs. In particular, Step 2 involves more complex counterfactual statements than Step 1, allowing the user (and the LLM) to apply varying degrees of attention when fine-tuning is needed. Third, intermediate outputs themselves can provide information and offer insights. Finally, this approach significantly reduces the likelihood that LLMs recognize the task as IV discovery and generate text from relevant academic sources.<sup>7</sup>

Alongside the multi-step method, we propose a role-playing approach. It has been reported that LLMs—including GPT4—gather better contextual information and generate more tailored and unique responses when prompts are structured as role-plays. In fact, in most scenarios, the explanatory variable D represents an economic agent's decision, which naturally facilitate role-playing. Additionally, role-playing prompts are more effective in guiding LLMs to respond as the relevant economic agent rather than as a researcher searching for IVs. In Appendix A.3, we compare our multi-step, role-playing prompting strategy with a more direct approach that explicitly states the goal of IV search, arguing that the former is more effective.

To simplify the exposition, in Sections 3.1–3.2, we first demonstrate the prompt construction without introducing covariates (in which case REL and IND should hold uncondition-

<sup>&</sup>lt;sup>7</sup>This would be especially true when each step is conducted in a separate independent session.

 $<sup>^8 \</sup>rm Open AI$  Developer Forum: https://community.openai.com/t/make-chatgpt-better-for-role play-scenarios/344244

ally). We then construct more realistic prompts with covariates in Section 3.3. The prompts presented here can serve as a benchmark for more sophisticated prompts; we discuss them in Section 7.

# 3.1 Step 1: Prompts to Search for IVs

For Step 1, Prompt 1 is a role-playing prompt that queries the search for  $K_0$  IVs (obtaining  $\mathcal{Z}_{K_0}$ ) that satisfy verbal versions of REL and EX (with no X). In all prompts below, each bracketed term represents a user input: [treatment] is the treatment D, [agent] is the economic agent whose decision is D, [scenario] is the specific setting of interest, [outcome] is the outcome Y, and [K\_0] is the desired number of variables  $K_0$ . When prompting, we ask the LLM to play the role of [agent] to make a [treatment] decision in a hypothetical [scenario]. Examples of these inputs are given in Section 4.

#### Prompt 1 (Search for IVs).

you are [agent] who needs to make a [treatment] decision in [scenario]. what are factors that can determine your decision but do not directly affect your [outcome], except through [treatment] (that is, factors that affect your [outcome] only through [treatment])? list [K\_0] factors that are quantifiable. explain the answers.

There are at least two variants of Prompt 1 that may be useful in certain scenarios. First, instead of "list [K\_0] factors that are quantifiable" one may simply write "list [K\_0] factors" or even "list [K\_0] factors that are hard to quantify." This would return candidates of IVs that are harder to measure but can inspire creative data collection (e.g., text, images, or other unstructured data). Second, one can expand Prompt 1 to be more specific about categorizing factors for relevant parties in a given setting. For example, in the schooling scenario (Section 4.1), we request separate lists

for student factors and school factors. This approach can facilitate the user's evaluation of the results.

## 3.2 Step 2: Prompts to Refine the Search for IVs

Take the set of IVs,  $\mathcal{Z}_{K_0} \equiv \{Z_1, ..., Z_{K_0}\}$ , obtained by running Prompt 1 in Step 1. Next, for Step 2 in the same session, Prompt 2 is a role-playing prompt that queries the search for K IVs (obtaining  $\mathcal{Z}_K$ ,  $K \leq K_0$ ) within  $\mathcal{Z}_{K_0}$  that satisfy a verbal version of IND (with no X). Below, [confounders] is the user input for unobserved confounders of concern and [K] is the user choice of K. In this prompt, we ask the LLM to continue playing the same role as in Prompt 1.

#### Prompt 2 (Refine IVs).

you are [agent] in [scenario], as previously described. among the [K\_0] factors listed above, choose [K] factors that are most likely to be unassociated with [confounders], which determine your [outcome]. the chosen factors can still influence your [treatment]. for each chosen factor, explain your reasoning.

Unlike Prompt 1, this prompt contains a statement about variables typically unobserved to researchers, which may pose challenges. We believe that incorporating the researcher's prior knowledge on latent confounders helps simplify the overall search process and yield more desirable results. For instance, in the schooling scenario, one can specify "innate ability and personality and school quality." Alternatively, if the user prefers a more agnostic approach, they can list [confounders] as "other possible factors." Another option is to systematically search for possible unobserved confounders; see Section 6.1 for related prompting strategies. In Prompt 2, we use the term

<sup>&</sup>lt;sup>9</sup>This relates to few-shot learning discussed in Section 7.

"unassociated." If the LLM ever captures the nuance of this word, it reflects the mean independence version of IND, making the search easier. Interestingly, an alternative phasing such as "choose [K] factors that are purely random", which may seem a straightforward way to impose IND without needing to specify unobserved confounders, often fails to produce intended outputs.

There are useful variants of Prompt 2. First, one can omit [K] and instruct the LLM to "choose all factors" from  $\mathcal{Z}_{K_0}$  that are likely to satisfy IND, allowing the LLM to determine K independently; we apply this strategy in all examples later. Second, as a sanity check, one can direct the LLM to select elements in  $\mathcal{Z}_{K_0}$  that violate IND in addition to those that satisfy it. This can be achieved by adding "also choose factors that are, in contrast, associated with [confounders]." To gain further insights, the user can request explanations for factors that she identifies as valid IVs in initial set  $\mathcal{Z}_{K_0}$  from Step 1, but which are somehow not included in the final set  $\mathcal{Z}_K$  by the LLM. We apply the last approach to the application in Section 4.2.2.

# 3.3 Extension: Prompts to Search and Refine with Covariates

Typically, IVs are argued to be valid after conditioning on a list of covariates (as reflected in REL-IND). The IV discovery with covariates can be approached in at least two different ways. We can prompt the LLM to either (i) search for IVs conditional on predetermined covariates; or (ii) jointly search for IVs and covariates that satisfy REL-IND. We focus on option (i); option (ii) is discussed in Appendix A.2. Whenever covariates are searched, option (i) can be viewed as initiating an IV search in a new independent session with the searched covariates.

We construct a prompt that introduces the notion of conditioning variables; role-playing prompts are suitable for this purpose. Here, we only modify Prompt 2. Although REL also involves conditioning on X, we find that results are not sensitive to a relevant modification of Prompt 1. Prompt  $2_x$  qualifies both [agent] and [scenario] by [covariates],

the pre-determined user choice of covariates. It extends Prompt 2 by modifying the first sentence. Prompt  $2_x$  is intended to be run after completing Prompt 1.

## **Prompt 2**<sub>x</sub> (Refine IVs with Covariates).

suppose you are [agent] in [scenario] with [covariates]. among the [K\_0] factors listed above, choose [K] factors that are most likely to be unassociated with [confounders], which determine your [outcome]. the chosen factors can still influence your [treatment]. for each chosen factor, explain your reasoning.

The recommended approach for incorporating [covariates] is to assign specific values for the covariates. For instance, in the schooling scenario, one can write "suppose you are an asian female high school student from california who considers attending a private college." Alternatively, one can simply use terms like "specific" or "particular" along with the name of chosen covariates (e.g., "suppose you are a high school student with specific gender, race, and regional origin who considers attending a college of specific type").

# 4 Discovered IVs

Using Prompts 1 and  $2_x$  described in the previous section, we aim to identify candidates for IVs in four well-known examples in economics: returns to schooling, supply and demand, and peer effects. These examples are chosen for their significance in the empirical economics literature (representing labor economics, industrial organization, and development economics, respectively). They commonly employ the IVs method as an empirical strategy. The main purpose of this exercise is to evaluate the performance of LLMs in executing the proposed

<sup>&</sup>lt;sup>10</sup>One can run multiple queries across different values of covariates for robustness, although this does not appear to be necessary in most cases unless extreme values are assigned in the initial run.

method and to demonstrate the practical applicability of the method.

To summarize the findings, in all the examples, LLMs appear to discover new candidates for IVs and candidates that are related to well-known IVs in the literature. When Also, many candidates demonstrate high levels of specificity to their context. With the results produced, we hope to spark debates and inspire the discovery of new and better IVs.

The prompts we construct in each example slightly deviate from the templates of Prompts 1 and  $2_x$  to better adapt to the scenario and enhance the flow of English language. For each example, we present results from the *initial single* run of the prompts without any curation or further refinement. When the results match the IVs described in the literature exactly, we include the corresponding references (to the best of our knowledge) and their citation counts. Results across sessions are largely consistent, although they can vary when different values of  $K_0$  and K are chosen. We use GPT4 as our LLM.

#### 4.1 Returns to Education

Suppose we are interested in estimating the causal effects of educational attainment (e.g., college attendance, years of schooling) on earnings. The main latent confounders in this setting is unobserved individual and school characteristics (e.g., student ability and personality, school quality) that affect both the schooling decisions and future earnings. To address this endogeneity and recover meaningful causal effects (e.g., local average treatment effects (Imbens and Angrist, 1994)), IVs such as distance to schools, tuition fees, and compulsory schooling laws have been widely used in the literature (Card, 1999).

#### 4.1.1 Returns of College Attendance

As the first example, we focus on the returns to college attendance. The following is the prompts we use. We choose  $K_0 = 40$  and let GPT4 choose K. We explicitly request separate lists for individual factors and school factors.

#### Prompt 1-1 (Example: Returns to College).

you are a high school graduate. you need to make a college attendance decision. what would be factors (factors of schools and factors of yourself) that can determine your decision but that do not directly affect your future earnings, except through college attendance (that is, that affect your earnings only through college attendance)? list forty factors that are quantifiable, twenty for school factors and twenty for factors of yourself. explain the answers.

#### **Prompt 2**<sub>x</sub>-1 (Example: Returns to College).

suppose you are a student with family income \$10K per year, who is asian female from california, whose parents have college education, who is catholic. among the forty factors listed above, choose all factors that are not associated with your innate ability and personality and school quality, which determine earnings. create separate lists for school factors and factors of yourself. for each factor chosen, explain your reasoning.

Table 1 presents the results from a single session of running Prompts 1-1 and  $2_x$ -1. It contains IVs suggested by GPT4 and GPT4's rationale for the suggestions. In the table, we find IVs that are already popular in the literature (e.g., #1, 3, 5) as well as IVs that seem to be new (to our best knowledge) (e.g., #6, 7, 9, 11, 12, 13, 14). The latter have potential to be valid, especially after being conditioned on additional covariates that are not considered in the prompt. Producing all these results took less than one minute in total. The rationale given by GPT4 can be elaborated further by requesting it in the same session, which we do

<sup>&</sup>lt;sup>11</sup>GPT4 also provide the summary of overall rationale, which is not reported here for succinctness.

#	IVs Suggested	Rationale Provided	Citations
1	Distance from Home to	This is purely geographical and independent of	Card ('95),
	College	personal attributes.	1955; Card
			('01), 3134
2	Personal Savings for	While this might be influenced by a student's	
	Education	ability to save, it's largely determined by external	
		economic conditions and family support.	
3	Number of Siblings	This depends on family decisions and the	Griliches
	Attending College	educational pursuits of siblings, unrelated to the	('77), 2393
		student's personal capabilities or characteristics.	
4	Parents' Educational	A demographic factor that precedes the student's	
	Background	own choices and abilities.	
5	Religious Affiliations	A personal and family cultural factor, not	
		necessarily a direct influence on personal academic	
		or career potential.	
6	Campus Crime Rates	Safety measures and local crime statistics are	
		external to the student's attributes.	
7	Diversity of Student Body	Reflects the school's admissions policies and	
		demographic outreach, independent of any one	
		student's traits.	
8	Library Size (Volumes	A resource factor that's determined by the	
	Held)	institution's funding and priorities.	
9	Availability of Online	Indicates the institution's commitment to flexible	
	Courses	learning options, independent of student	
		characteristics.	
10	Campus Facilities Quality	Dependent on the school's investment in	
	(Gyms, Labs, etc.)	infrastructure.	
11	Campus Housing	Dictated by the university's accommodations and	
	Capacity	facilities, not by student traits.	
12	Proximity to Urban	Geographic location of the school relative to cities.	
	Centers		
13	Environmental	Reflects the institution's environmental policies and	
	Sustainability Rating	infrastructure.	
14	Technology Integration in	Indicates the level of modern technological adoption	
	Classrooms	by the school.	

Table 1: Returns to College: Suggested IVs and Rationale for Validity

Notes: IVs for college attendance are presented. All IVs are discovered and explained by GPT4 from a single run of Prompts 1-1 and  $2_x$ -1 with  $K_0 = 40$  and K left unspecified. The first 5 rows are categorized by GPT4 to be student-related factors, and the next 9 rows to be school-related factors. The total running time was less than 1 minute.

not present here for brevity. 12

#### 4.1.2 Returns to Years of Education

As a second example, we consider the returns to years of schooling. We omit the prompts as they are similar as before, except that we impose the following role: "you are a student beginning high school in the united states. you need to make a decision on how many more years you will stay in school." Table 2 contains the IVs suggested by GPT4. Some candidates (e.g., #3, 4) are similar to those found in the first example. Notably, GPT4 also finds variables (e.g., #1, 2) that are related to compulsory schooling laws, the popular IVs in the literature. Local regional characteristics (e.g., #5, 6, 7) are also interesting findings.

# 4.2 Supply and Demand

#### 4.2.1 Production Function Estimation

Consider estimating a production function that captures the causal relationship between inputs and outputs. The key identification challenge is that input decisions can be correlated with unobserved productivity shocks, which directly influence outputs. To address this, IVs such as input prices have been proposed in the literature (Griliches and Mairesse, 1995), which have been subsequently criticized (Olley and Pakes, 1996; Levinsohn and Petrin, 2003; Ackerberg et al., 2015).

Here are the prompts we use. As before, we choose  $K_0 = 40$  and let GPT4 choose K; we explicitly request separate lists for market factors and firm and manager factors. Note that in Prompt  $2_x$ -2-1, we use a loose description of covariates (unlike in Prompt  $2_x$ -1 where we assign specific values).

 $<sup>^{12}</sup>$ Appendix A.1 explains an effective way of adjusting the length of responses via a system message.

#	IVs Suggested	Rationale Provided	Citations		
1	Credits Required for	This is a regulatory requirement and does not			
	Graduation	depend on your personal qualities or the inherent			
		quality of your school but can determine the length			
		of time you stay in school.			
2	State Education Laws	Laws mandating education until a certain age or Angri			
		credits affect all students uniformly, irrespective of	Krueger		
		individual abilities or school quality.	('91), 3951;		
			Staiger &		
			Stock ('97),		
			10656		
3	Distance to Nearest	The geographical proximity to higher education	Card ('95),		
	College/University	institutions is an external factor that doesn't	1955; Card		
		depend on your ability but can influence the	('01), 3134		
		decision to pursue further education based on			
		accessibility.			
4	Transportation	The ease of getting to and from educational			
	Availability	institutions is a logistical concern that affects your			
		ability to attend and continue education,			
		independent of personal academic qualities or			
		school resources.			
5	Local Education Funding				
	per Student	at a community or state level, impacting the			
		resources available to you, which can influence			
		educational continuation decisions, yet is not a			
		reflection of personal ability.			
6	Local College Enrollment	Community trends in college enrollment can create			
	Rates	a social environment that encourages further			
		education, which is more about local culture and			
		less about individual capacity.			
7	Local Unemployment	Higher local unemployment might incentivize			
	Rates	staying in school longer as a way to defer entering a			
		tough job market, a decision influenced by economic			
		conditions rather than personal academic prowess.			

Table 2: Returns to Years of Schooling: Suggested IVs and Rationale for Validity

Notes: IVs for years of schooling are presented. All IVs are discovered and explained by GPT4 from a single run of Prompts 1-1 and 2x-1 (modified for this example) with  $K_0 = 40$  and K left unspecified. The total running time was less than 1 minute.

#### Prompt 1-2-1 (Example: Production Functions).

you are a manager at a manufacturing firm. you need to make a decision on how much labor and capital inputs to use to produce outputs. what would be factors (factors of markets and economy and factors of yourself) that can determine your decision but that do not directly affect your output productions, except through the input choices (that is, that affect your firm's outputs only through inputs)? list forty factors that are quantifiable, twenty for market factors and twenty for managerial factors. explain the answers.

#### **Prompt 2**<sub>x</sub>**-2-1** (Example: Production Functions).

suppose you are a manager at a firm with specific level of capital intensity and specific scale of operations, which has a specific market share in a specific industry. among the forty factors listed above, choose all factors that are not influenced by productivity shocks of your firm, which determine outputs. create separate lists for market factors and managerial factors. for each factor chosen, explain your reasoning.

Table 3 presents the results from a single session of running Prompts 1-2-1 and  $2_x$ -2-1. It contains IVs suggested by GPT4 and GPT4's rationale. Interestingly, IVs that are suggested in the literature (i.e., input prices) are not chosen by GPT4 although they appear in the answer to Prompt 1-2-1 (not shown here for brevity). This suggests that these IVs are not deemed by GPT4 to satisfy IND, aligning with similar concerns in the literature (Olley and Pakes, 1996; Levinsohn and Petrin, 2003; Ackerberg et al., 2015). However, GPT4 suggests

<sup>&</sup>lt;sup>13</sup>This result was consistent over multiple runs.

IVs that may influence input prices (e.g., #1, 2, 3, 5, 6, 14), some of which can be arguably exogenous. There are a handful of other IVs suggested as market-related and managerial factors. Among the latter, there are variables related to long-term decisions of the firm, which are argued by GPT4 to not influence short-term productivity shocks. However, long-term decisions affect long-term outputs, which may or may not be relevant to the short-term outputs of concern. Overall, the explanations given by GPT4 are more detailed than those in Table 1, reflecting the random nature of the LLM's responses.

#### 4.2.2 Demand Estimation

Consider estimating demand for consumers in a given market. In estimating the effect of price on demand, the main concern is that price is endogenous, as it is an equilibrium outcome. Researchers have used supply-side IVs that are excluded from the demand equation in a simultaneous system for supply and demand (Angrist et al., 2000) or motivated by structural models (Berry et al., 1995).

Below are the prompts we use, focusing on the setting of Angrist et al. (2000). As before, we choose  $K_0 = 40$  and let GPT4 choose K. Note that in Prompt 2-2-2, covariate information is omitted.

#### Prompt 1-2-2 (Example: Demand).

you are a dealer at a fish market. you need to set the prices of fish. what would be factors that can determine your decision but that do not directly affect the customers' demand for fish, except through the price you set (that is, that affect the demand only through fish prices). list forty factors that are quantifiable. explain your answer.

#	IVs Suggested	Rationale Provided	
1	Interest Rates	Influence the cost of borrowing, affecting decisions on how much	
		capital to acquire or lease for production without altering	
		current productivity levels.	
2	Exchange Rates	Affect the price of imported inputs, which can change input	
		costs and investment decisions in foreign capital, again without	
		directly impacting the productivity of existing inputs.	
3	Tariffs and Trade Policies	Alter the cost structures for imported and exported goods,	
		impacting decisions on where to source inputs or sell outputs,	
		but do not affect the productivity of the inputs themselves.	
4	Regulatory Changes	Can necessitate changes in production processes or input	
		materials, which may affect costs and sourcing decisions without	
		directly impacting the productivity of the inputs once deployed.	
5	Transportation Costs	Affect the total cost of inputs and can influence decisions	
		regarding sourcing and logistics. These costs don't directly alter	
		how effectively inputs are converted into outputs.	
6	Real Estate Prices	Influence decisions about expanding or relocating production	
		facilities, affecting capital expenditure and operational scale	
		without altering current production efficiency.	
7	Environmental	Stricter environmental regulations may force a firm to switch to	
	Regulations	greener, possibly more expensive inputs or production	
		technologies, affecting input choices and costs but not directly	
		modifying the productivity of any specific input set.	
8	Patents and Intellectual	Governed by legal systems and not directly influenced by a	
	Property Rights	firm's internal productivity shocks.	
9	Political Stability	Affect market predictability and investment decisions, impacting	
		where and how much to invest in capital and labor, without	
		changing how these inputs produce once acquired.	
10	Global Economic	Influence market opportunities and risks associated with foreign	
	Conditions	investments, guiding input acquisition strategies without	
		changing input productivity.	

Table 3: (a) Production Functions: Suggested Candidates for IVs (Market Factors)

Notes: IVs for inputs are presented. All IVs are discovered and explained by GPT4 from a single run of Prompts 1-2-1 and  $2_x$ -2-1 with  $K_0 = 40$  and K left unspecified. Panel (a) is categorized by GPT4 to be market-related factors, and Panel (b) to be managerial factors. The total running time was less than 1 minute.

#	IVs Suggested	Rationale Provided
10	Capital Availability	Determines its ability to invest in both labor and capital inputs,
		shaping the scale of operations and types of technology
		employed, without directly changing how productive these
		inputs are
11	Company's Risk	Can decide the extent to which a firm is willing to invest in new,
	Tolerance	potentially more efficient, but riskier technologies or markets,
		affecting input decisions rather than the productivity of current
		inputs
12	Strategic Objectives	Long-term strategic objectives may dictate prioritizing certain
		types of inputs or production scales, influencing the firm's
		approach to markets and technology investments without
		affecting current input productivity.
13	Financial Health of the	The overall financial stability can limit or expand the firm's
	Company	ability to procure and utilize inputs optimally, shaping how
		inputs are managed and financed rather than directly influencing
		their productivity
14	Compliance and Legal	Driven by external legal requirements and internal ethics, not by
	Considerations:	short-term productivity
15	Corporate Social	Strategic decisions about CSR are influenced by long-term
	Responsibility (CSR)	planning and brand image considerations.
	Initiatives	

Table 2: (b) Production Functions: Suggested Candidates for IVs (Managerial Factors)

Notes: IVs for production inputs are presented. All IVs are discovered and explained by GPT4 from a single run of Prompts 1-2-1 and  $2_x$ -2-1 with  $K_0=40$  and K left unspecified. Panel (a) is categorized by GPT4 to be market-related factors, and Panel (b) to be managerial. The total running time was less than 1 minute.

#### Prompt 2-2-2 (Example: Demand).

suppose you are a dealer at the fish market who is selling fish and setting its prices on a day of the week. among the factors listed above, choose all factors are not influenced by fish market conditions or customers' characteristics that determine demand for fish. for each factor chosen, explain your reasoning.

Table 5 presents the results from a single session of running Prompts 1-2-2 and 2-2-2. It contains IVs suggested by GPT4 and GPT4's rationale. Many supply-side factors (e.g., costs) are chosen by GPT4, which are reasonable candidates for IVs. The "weather conditions" variable used as IVs in Angrist et al. (2000) appears in the list (#3). Interestingly, another supply-side factor "labor costs" produced by Prompt 1-2-2 is not included in the final list produced by Prompt 2-2-2. When asked "explain why you didn't include 'labor costs' in the final list," GPT4 responded that "labor costs are somewhat flexible and can be adjusted in response to changes in market conditions and customer demand, making them more dynamic than some of the other factors listed."

#### 4.3 Peer Effects

Suppose we are interested in the causal effects of peers on an individual's outcomes within a social network. We consider two well-known examples: (i) the effects of peer farmers on the adoption of new farming technologies (Foster and Rosenzweig, 1995; Conley and Udry, 2010); (ii) the effects of peers on teenage smoking (Gaviria and Raphael, 2001). In both examples, the main source of endogeneity is latent factors that determine the formation of network (e.g., latent homophily). To address this, the literature on peer effects sometimes uses friends of friends as IVs (Bramoullé et al., 2009; Angrist, 2014). In both examples, we construct prompts similar to the first two examples, except that we choose  $K_0 = 20$ .

#	IVs Suggested	Rationale Provided	Citations
1	Fuel Costs	Costs for fuel typically depend on broader economic factors such as oil prices and are not directly affected by market demand for fish or specific customer characteristics.	
2	Fishing Equipment Depreciation	The depreciation of fishing gear like nets and boats is largely a function of use and time, rather than market conditions or customer demand.	
3	Weather Conditions	Weather affects fishing operations directly but is not influenced by market conditions or the specific characteristics of customers.	Angrist, Graddy & Imbens ('00), 454
4	Regulatory Costs	Costs associated with licensing and compliance with fishing regulations are dictated by regulatory bodies and do not fluctuate based on customer demand or market conditions.	
5	Interest Rates	The rates charged on loans for purchasing boats or equipment are determined by financial markets and policy, rather than direct market conditions of the fish market or customer demands.	
6	Insurance Costs	Premiums for insuring fishing equipment and operations are typically based on risk assessments and sector-wide data, rather than being directly influenced by day-to-day market conditions or characteristics of customers.	
7	Utility Costs at Sales Points	The cost of utilities like electricity and water at sales points tends to be fixed or based on usage rates that are independent of market demand specifics.	
8	Economic Conditions	Broader economic factors that affect overall spending and investment patterns influence operational costs but are not dictated by the fish market conditions or customer preferences.	
9	Technological Advances	Investments in technology to improve fishing or sales operations are usually planned based on long-term business strategy and efficiency gains rather than immediate market conditions or specific customer demographics.	
10	Government Subsidies	Subsidies to the fishing industry are determined by government policies, which are independent of daily market conditions or customer demands in the fish market.	
11	Tariffs on Imports	Tariffs imposed on imported fish are a matter of international trade policy and do not change based on daily fluctuations in market demand or customers characteristics.	
12	Employee Training Costs	Costs of training employees in handling and selling fish relate to operational efficiency, which are not directly influenced by the day's market conditions or customer demands.	

Table 5: Demand Estimation: Suggested Candidates for IVs

Notes: IVs for price are presented. All IVs are discovered and explained by GPT4 from a single run of Prompts 1-2-2 and 2-2-2 with  $K_0 = 40$  and K left unspecified. The total running time was less than 1 minute.

#### 4.3.1 Effects of Peer Farmers on New Technology Adoption

Here are the prompts. It is worth noting that, in this example, the role-playing is done from the peer's perspective, rather than from the perspective of the individual whose outcome is of concern.

#### Prompt 1-3-1 (Example: Peer Effects on Technology Adoption).

you are a farmer in a village in rural india. you want to influence your peer farmers in the same village to introduce a new farming technologies that you introduced. what would be factors (factors of farming and village, and factors of yourself) that can determine your influence on peers but that do not directly affect your peers' technology adoption decisions, except through your influence (that is, that affect your peers' decisions only through your influence)? list twenty factors that are quantifiable. explain your answer.

#### **Prompt 2**<sub>x</sub>**-3-1** (Example: Peer Effects on Technology Adoption).

suppose you are a 40 year old male farmer of a specific crop in the village in rural india. among the factors listed above, which factors are not influenced by factors (e.g., similar background and preferences) that brought you and your peers in the same neighborhood and social network from the first place? for each factor chosen, explain your reasoning.

Table 5 presents the results in a single session of running Prompts 1-3-1 and  $2_x$ -3-1. It contains IVs suggested by GPT4 and GPT4's rationale. Interestingly, some IVs that are suggested in the literature (e.g., friends of friends) are not chosen by GPT4. It can be because GPT4 either views them as invalid or is incapable of identifying them. On the

other hand, #10 seems to relate to the IV used in Conley and Udry (2010), which exploits variation in the presence of experienced farmers. Additionally, there are other IVs that seem to be new, notably #9. Finally, GPT4 fails to identify the IV used in Foster and Rosenzweig (1995), namely, endowed land size. The validity of this variable is justified in their paper by the specific historical backgrounds of the Indian villages studied. This implies that, for some IVs, providing LLMs with institutional details can be necessary; see Appendix A.1 for implementing this via system messages.

#### 4.3.2 Effects of Peer Teenagers on Smoking Behavior

Here are the prompts. Again, in this example, the role-playing is done from the peer's perspective. We choose a teenager in urban Indonesia for its relevance, given that the teenage smoking rate in Indonesia has been recently reported as one of the world's highest (Fithria et al., 2021). We consider a social media network in the scenario to illustrate the effectiveness of our approach in exploring relatively recent topics in the literature, thereby highlighting the potential to discover novel IVs.

## Prompt 1-3-2 (Example: Peer Effects on Smoking).

you are a teenager in indonasia who smokes. you want to influence your peers in your social media network to smoke. what would be factors (factors of social media, your school and region, and factors of yourself) that can determine your influence on peers but that do not directly affect your peers' smoking decisions, except through your influence (that is, that affect your peers' decisions only through your influence)? list twenty factors that are quantifiable. explain your answer.

#	IVs Suggested	Rationale Provided	
1	Number of Training	This reflects an individual's initiative to seek additional	
	Sessions Attended	education and may vary widely among farmers with similar	
		backgrounds due to personal choices, availability of time, or	
9	NT 1 C	perception of the value of formal education	
$\begin{vmatrix} 2 \end{vmatrix}$	Number of	This is influenced by an individual's willingness to share	
	Demonstrations Conducted	knowledge and the resources they are willing or able to allocate	
	Conducted	for such activities, which might not be uniformly distributed even among neighbors	
3	Increase in Yield After	This factor depends significantly on how effectively an individual	
	Technology Adoption	implements and adapts new technologies to their specific farming	
	-	practices, which can differ greatly even among farmers growing	
		the same crops	
4	Access to Credit	Individual financial management skills, credit history, and	
		relationships with lending institutions can influence this factor,	
		which isn't necessarily shared among all peers in a community	
5	Participation in Local	Involvement in local governance or committees often depends on	
	Decision Making Bodies	personal ambition, political skills, and community perception of	
		an individual's leadership qualities, which can vary	
		independently of shared initial factors	
6	Awards or Recognitions   Achieving recognition for farming practices or community		
	Received	is heavily dependent on individual effort and excellence and is	
		not uniformly influenced by community-shared characteristics	
7	Communications Skills	Communication effectiveness can be developed through personal	
	Assessment	experience, education, and innate ability, which vary among	
8	Number of Articles or	individuals regardless of their initial common background  This is influenced by an individual's ability to write, research,	
	Case Studies Published	and engage with broader audiences, skills that are not common	
	Case Studies I ublished	to all individuals in a network	
9	Engagement in Social	The level of engagement in modern communication and	
	Media or Technology	technology platforms depends on personal interest in technology,	
	Platforms	availability of resources, and individual attitudes toward	
		innovation	
10	Success Stories	The ability and willingness to document and share success	
	Documented and Shared	stories can be a personal choice influenced by an individual's	
		perspective on self-promotion and communication	

Table 5: Peer Effects on Technology Adoption: Suggested Candidates for IVs

Notes: IVs for peers' decisions are presented. Given the perspective in the prompts, the variables should be understood as factors of peers. IVs for All IVs are discovered and explained by GPT4 from a single run of Prompts 1-3-1 and  $2_x$ -3-1 with  $K_0 = 20$  and K left unspecified. The total running time was less than 1 minute.

**Prompt 2\_x-3-2** (Example: Peer Effects on Smoking).

suppose you are a teenage boy in urban indonesia who goes to high school and is from middle-income family. among the factors listed above, which factors are not influenced by factors (e.g., similar background and preferences) that brought you and your peers in the same social network from the first place? for each factor chosen, explain your reasoning.

Table 6 presents the results from a single session of running Prompts 1-3-2 and  $2_x$ -3-2. It contains IVs suggested by GPT4 and GPT4's rationale. It is important to note that, given that the prompts are written from the perspective of peers, the variables in the table should be understood as factors influencing *peers* of the focal individual. Given that the setup incorporates modern elements such as social media, we identify many potentially new and interesting IVs, particularly from the social media category (i.e., #1, 2, 3, 4, 7). Interestingly, #7 can be viewed as a "friends of friends" IV.<sup>14</sup>

# 5 Adversarial Large Language Models

One way to refine the answers of an LLM is to request another LLM (or a different session of the same LLM) to play the role of an adversary and review the responses produced by the first LLM, namely the defender LLM. In the adversarial stage, we fully disclose the IV discovery task and ask the adversarial LLM to provide counter-arguments, but without using econometric jargon. These counter-arguments are then given to the defender LLM, which is asked to refine the previous answers. Overall, this process produces more sophisticated responses. We find this to be a useful exercise, which mimics the mental process of a human researcher.

The following is an example prompt given to the adversarial LLM. In the prompt, [the

<sup>&</sup>lt;sup>14</sup>There were other "friends of friends" IVs that are produced from Step 1 but did not survive Step 2.

#	IVs Suggested	Rationale Provided	
1	Engagement Rate	While the number of followers might be initially influenced by	
		shared backgrounds, the engagement rate depends more on the	
		content quality and how it resonates with the audience at any	
		given time, rather than the reasons why the audience initially	
		formed	
2	Frequency of Posts	This is largely a personal choice and strategic decision,	
		independent of peer background. It reflects personal	
		commitment to the platform rather than shared interests or	
		backgrounds	
3	Content Reach	This metric depends on the algorithm and how engaging the	
		content is, which can transcend the initial reasons for network	
		formation	
$\mid 4 \mid$	Number of Platforms	Choosing to diversify presence across various platforms is a	
	Used	strategic decision that doesn't necessarily correlate with shared	
		backgrounds or interests	
5	School Policies on	These are institutional decisions that apply to all students,	
	Smoking	regardless of the factors that brought them together	
6	Local Regulations on	Like school policies, these are determined by local government	
	Tobacco Advertising	and affect all residents uniformly, irrespective of social network	
		formations	
7	Access to Smartphones	This might vary widely even within similar socio-economic	
	Among Peers	backgrounds due to individual family decisions or priorities	
8	Visibility at School	Active participation and visibility in school events are personal	
	Events	choices and efforts that go beyond shared backgrounds, reflecting	
		individual initiative	
9	History of Disciplinary	This is generally a result of personal behavior and choices rather	
	Actions at School	than group influence	
10	Academic Performance	Although there could be a correlation with socio-economic	
		status, individual effort and capability play significant roles,	
		making this somewhat independent of why peers might group	
		together initially	
11	Extracurricular	Holding leadership positions is often based on personal qualities,	
	Leadership Roles	skills, and choices rather than the shared preferences and	
		backgrounds that might define a social network initially	

Table 6: Peer Effects on Smoking: Suggested Candidates for IVs

Notes: IVs for peers' decisions are presented. Given the perspective in the prompts, the variables should be understood as factors of peers. All IVs are discovered and explained by GPT4 from a single run of Prompts 1-3-2 and  $2_x$ -3-2 with  $K_0 = 20$  and K left unspecified. The first four rows concern social media factors; the next three rows concern school and regional factors; and the last four rows concern personal factors. The total running time was less than 1 minute.

list of variables by Defender] is the list provided the defender LLM, generated from running, for example, Prompts 1-2.

#### Prompt AD1.

you are a researcher who wants to find instrumental variables to estimate the effect of [treatment] on [outcome]. below is a list of candidate instrumental variables. for each variable in the list, provide arguments as to why it may not be a valid instrument:

[the list of variables by Defender]

Then, the counter-arguments generated from Prompt AD1 are presented to the defender LLM using the following prompt, which follows Prompts 1–2.

# Prompt 3.

below are counter-arguments for each of your previous answers. based on these arguments, revise your selection and provide a list:

[the arguments by Adversary]

When running Prompt 3, it is important to encourage the defender to create a list, otherwise, it might become pessimistic and reject all the previous selections.

We apply this adversarial process to our examples in Section 4. Overall, the defender provides more sophisticated answers in the end. In the "Returns to College" example (Section 4.1.1), the variables related to geographical proximity or transportation have been retained. The other variables related to school facilities (e.g., library size, technology integration in classrooms) have been modified to factors that may better satisfy exogeneity (e.g., the percentage of renewable energy used on campus, the number of green spaces on campus, campus

medical facilities). New variables also appeared (e.g. language spoken at home). Interestingly, many variables now appear to be weak IVs, which is sensible. In the "Returns to Years of Education" examples (Section 4.1.2), the "state laws" variable survived, but was renamed to the more descriptive "mandatory minimum years of schooling required by state." Other variables were also further refined. "GED program availability" emerged. In the "Demand Estimation" example (Section 4.2.2), the "weather condition" variable was refined to "global climate patterns (e.g., El Niño)," because the counter-argument was that "bad weather can also discourage customers from coming to the market." Many other variables were refined to reflect global and macroeconomic conditions. Again, these variables suffer from being weak IVs or having less individual variation.

# 6 Variables Search in Other Causal Inference Methods

In this section, we demonstrate how prompting strategies similar to those for the IV discovery can be used to find (i) control variables under which treatments are conditionally independent (i.e., exogenous); (ii) control variables under which parallel trends are likely to hold in difference-in-differences; and (iii) running variables in regression discontinuity designs.

# 6.1 Conditional Independence

Using the same notation as in Section 2, consider a conditional independence (CI) assumption that assigns a more crucial role to the vector of control variables  $X \equiv (X_1, ..., X_L)$ :

**Assumption CI.** For any d,  $D \perp Y(d)|X$ .

Assumption CI is commonly introduced in causal inference settings, especially when combined with machine learning to estimate nuisance functions; e.g., debiased/double machine learning methods (Chernozhukov et al., 2024). More traditionally, this assumption is closely related to matching and propensity score matching techniques (Heckman et al., 1998). The

mean independence version of CI (i.e., E[Y(d)|D,X] = E[Y(d)|X]) is relevant to regression methods.

We propose using LLMs to systematically search for X that satisfies a verbal version of CI. The prompt writing is slightly simpler than that for IVs. In particular, we construct prompts that solicit the relationship between X and D (Step 1) and X and Y(d) (Step 2). Therefore, only the second-step prompt involves a counterfactual statement. Let  $L_0$  be the number of controls to be found in Step 1 ( $L_0 \ge L$ ). One may want to choose the value of  $L_0$  to be larger than one would normally use for  $K_0$  and leave L unspecified.

## Prompt C1 (Search for Control Variables).

you are [agent] who needs to make a [treatment] decision in [scenario]. what factors determine your decision? list  $[L_0]$  factors that are quantifiable. explain the answers.

#### Prompt C2 (Refine Control Variables).

among the [L\_0] factors listed above, choose all factors that directly determine your [outcome], not only indirectly through [treatment]. the chosen factors can still influence your [treatment]. for each factor chosen, explain your reasoning.

The prompts are constructed to search for confounders and need to be controlled for. Researchers sometimes mistakenly control for "colliders" and/or "mediators" (Pearl, 2000), which are intended to be excluded from the search. Note that Prompts C1–C2 can also be adapted to jointly search for covariates and latent confounders in the IV search. In this case, one can distinguish X from latent confounders by referring to the former as "quantifiable." Also, one may want to use the phrase "demographic factors" to refer to X, as they are common control variables in many empirical applications.

#### 6.2 Difference in Differences

The difference-in-differences (DiD) method is popular in empirical research, partly due to the simplicity and intuitiveness of its main assumption, namely, the parallel trend assumption (stated below). However, this assumption is not directly testable and typically hard to justify (Ghanem et al., 2022; Rambachan and Roth, 2023). It is believed that conditioning on the right control variables can make this assumption more justifiable, which can motivate the search for such controls.

Assumption PT. 
$$E[\Delta Y(0)|D,X] = E[\Delta Y(0)|X]$$
 where  $\Delta Y(0) \equiv Y_{after}(0) - Y_{before}(0)$ .

Assumption PT can be viewed as a mean independence version of CI, where the counterfactual outcome is replaced with the temporal difference of counterfactual (untreated) outcomes before and after the event. Therefore, Prompts C1–C2 can be directly used to search for X that satisfy a verbal version of PT. This can be done by inputting "average temporal changes in [outcome\_t] during the time of no [treatment]" for [outcome] in Prompt C2, where [outcome\_t] refers to  $Y_t$  for  $t \in \{before, after\}$ . The example of such prompts is constructed to revisit the classical empirical example, namely, the effects of minimum wage on the fast food industry's labor markets (Card and Krueger, 1994); see Appendix B.1 for the actual prompts. Table 7 contains the control variables suggested by GPT4, conditional on which the parallel trend is likely to hold, and GPT4's rationale. On the list, #3, 4, 7, 10, 11 are particularly interesting and #11 seems particularly novel. In the table, the first four rows (#1, 2, 3, 4) are chosen by GPT4 from an additional prompt that emphasizes the requirement with respect to  $\Delta Y(0)$ : "be sure to choose all factors that do not determine the average wage level but only determine the temporal changes in average wages." Nonetheless, controls that satisfy the mean version of CI with the level,  $Y_t(0)$  for  $t \in \{before, after\}$ , are also valid controls for PT.

#	Control Variables Suggested	Rationale Provided	
1	Inflation Rates	Higher inflation can decrease the real income of workers if wages don't adjust accordingly, making a case for introducing a minimum wage to maintain purchasing power.	
2	Consumer Price Index (CPI)	A rising CPI without wage increases can reduce workers' real earnings, suggesting a minimum wage could help offset cost of living increases.	
3	Job Vacancy Rates	Low vacancies could keep wages down due to ample labor supply; high rates may drive wages up, affecting the urgency and approach to minimum wage legislation.	
4	Labor Productivity Growth	This affects temporary wage increases linked to efficiency improvements. Productivity gains can lead to bonus payments or higher wages temporarily but don't define starting wage rates.	
5	Employment Growth Rates	Robust job growth in the sector might show the industry can support higher wages, while slow growth suggests caution in wage hikes.	
6	Labor Force Participation Rate	High participation may suppress wages due to increased labor supply, supporting the need for a minimum wage to ensure fair earnings.	
7	Union Membership Rates	Low unionization in fast food often means weaker wage bargaining, possibly justifying minimum wage laws to improve wage standards.	
8	Turnover Rates	High turnover might indicate wage dissatisfaction, pointing to the need for a minimum wage to stabilize the workforce.	
9	Corporate Profit Trends	If profits are high but wages are stagnant, it could suggest that the industry can afford to pay more, bolstering the argument for a minimum wage.	
10	Economic Diversity Score	Dependency on low-wage sectors like fast food in less economically diverse areas might necessitate a minimum wage to ensure living standards.	
11	Percentage of Workforce in Gig Economy	Increased gig work could pressure fast food employers to offer competitive wages, influencing when and how to implement minimum wage laws.	

Table 7: Difference-in-Differences for Minimum Wage: Suggested Control Variables

Notes: All controls are discovered and explained by GPT4 from a single run of Prompts C1-C2, adapted to Assumption PT with  $L_0=40$  and L left unspecified. Among them, the first four row are factors that are chosen from the additional emphatic prompt: "be sure to choose all factors that do not determine the average wage level but only determine the temporal changes in average wages." The total running time was less than 1 minute.

# 6.3 Regression Discontinuity

Regression discontinuity designs (RDDs) are another well-known method for causal inference that closely relates to the IVs method (Lee and Lemieux, 2010).<sup>15</sup> The key for this method to work is to find a running variable (i.e., assignment variable) that satisfies the following:

**Assumption RD.** There exists a variable  $R_j$  and a cutoff  $r_0$  such that D = 1 if  $R_j \ge r_0$  and D = 0 if  $R_j < r_0$ .

One can use LLMs to systematically search for running variables  $\{R_1, ..., R_J\}$  for a given D and Y of interest. We provide the example of prompts here. It is worth noting that, unlike in all the previous cases, none of the prompts below involve counterfactual statements. Therefore, if LLMs outperform a traditional search for running variables, it would be due to their automated and comprehensive search behavior. Similarly as above, we only specify initial  $J_0$  and leave J unspecified.

#### Prompt R1 (Search for Running Variables).

you are [agent] who needs to make a [treatment] decision in [scenario]. what would be the possible criteria based on which your eligibility for [treatment] is determined? provide [J\_0] of the most relevant criteria that are (1) quantifiable and (2) have specific cutoffs determining eligibility. explain the answers.

 $<sup>^{15}</sup>$ For example, the fuzzy RDD estimand can be viewed as the two-stage least squares estimand.

<sup>&</sup>lt;sup>16</sup>In further refining the candidates of running variables to ensure that RRD's continuity assumptions are satisfied, counterfactual prompting would be necessary; see Appendix B.2.

#### Prompt R2 (Refine Running Variables).

among the  $[J_-0]$  criteria listed above, choose all criteria that involve continuous or ordered measures and have precise cutoffs determining eligibility. also report the cutoff value for each criterion from verifiable sources only (ensuring no fabricated or hypothetical numbers are used). explain the answers.

Note that when Prompt R2 is run on GPT4, it will engage in a series of automated web searches. The request for cutoff values may lead the LLM to provide hypothetical numbers as possibilities. When one wants to get the actual values from verifiable sources, it is important to explicitly state that, as we do above. We apply Prompts R1–R2 to a range of famous examples in the literature where RDDs are used as empirical strategies. Table 8 presents the results obtained by running the prompts, which are adapted to each specific context and country of the empirical example. In most cases, a handful of new possible running variables are suggested by GPT4 with specific cutoffs obtained from web sources. Except for one case (i.e., #4), GPT4 also identifies the running variables used in the literature.

# 7 Conclusions

This essay proposes the agenda to use LLMs to systematically search for variables in designing causal inference. It merely serves as a starting point, and there are potential next steps that can follow. In constructing prompts for IVs, there are many possible ways for sophistication: First, one can consider using previously known IVs in the literature to guide LLMs to discover new ones. This can be done by adding textual demonstration of how Assumptions REL—IND are satisfied with known IVs before starting the proposed prompts. This approach would evoke few-shot learning in LLMs (Brown et al., 2020), which can enhance their performances. This approach would also "orthogonalize" the search (Ludwig and Mullainathan, 2024) to

#	Outcome(s) (Country)	Treatment(s)	Suggested Running Variable, Same as the Literature	Other Suggested Running Variables (Cutoffs for Eligibility)
1	Spending on schools, test scores (US)	State education aid	Relative average property values (Guryan, 2001)	- Percentage of low-income students (e.g., Equity Multiplier 2023-2024, above 70%) - Mobility rate (e.g., Equity Multiplier, above 25%) - Age (e.g., Transitional Kindergarten (TK) expansion 2023-24, 15th b-day by April 2) - Local Control Funding Formula (LCFF) (California)*
2	College enrollment (US)	Financial aid offer	SAT scores, GPA (Van der Klaauw, 2002)	- Expected family contribution (EFC) (e.g., the Pell Grant 2023-2024: below \$6,656)
3	Overall insurance coverage (US)	Medicaid eligibility	Age (Card and Shore-Sheppard, 2004)	- Federal Poverty Level (FPL) (e.g., Washington D.C.: below 215% and below 221% (family of 3); equiv. annual incomes below \$31,347 and \$54,940, reps.) - Household Size (e.g., Modified Adjusted Gross Income (MAGI) rules: expressed as % of FPL, adjusted by 5% FPL disregard)
4	Employment rates (Italy)	Job training program	Attitudinal test score (Battistin and Rettore, 2002) <sup>†</sup>	- Age (e.g., below 35; source: National Policies Platform) - Income: (e.g., below 60%; source: National Policies Platform) - Salary (e.g., EU Blue Card: above 3/2 of average Italian salary; source: ETIAS Italy)
5	Re-employment probability (UK)	Job search assistance, training, education	Age at end of unemployment spell (De Giorgi, 2005)	- Age (e.g., Jobseeker's Allowance (JSA): above 18, with exceptions for some 16 or 17; source: UK Rules) - Minimum Salary (e.g., Skilled Worker visa: above £38,700 or going rate for job type, whichever is higher; source: GOV.UK) - Residency Duration (e.g., JSA: above 3 months prior to claim, for new or returning UK nationals; source: UK Rules)

Table 8: Regression Discontinuity: Suggested Candidates for Running Variables

Notes: All running variables are discovered and explained by GPT4 from a single run of Prompts R1-R2, adapted to each context with  $J_0 = 20$  and J left unspecified. All running variables used in the literature (Column 4) are also found by GPT4, except #4. The total running time for each row was less than 1 minute (even with an automated web search for Prompt R2). The sources indicated are given by GPT4 with links. \*: A formula, not a running variable. †: Not found by GPT4.

focus on novel IVs. Second, the elaborated search can be directed toward finding IVs that are more policy-relevant (Imbens and Angrist, 1994; Heckman and Vytlacil, 2005)) by specifying targeted policies in the prompt. Third, none of the results reported in the current essay are findings aggregated across sessions. To account for and potentially leverage the stochastic nature of LLMs' responses, exploring the possibility of aggregation (e.g., taking the union or intersection of  $\mathcal{Z}_K$ 's across sessions) would be beneficial. Fourth, we can explore the use of multiple LLM agents each assuming distinct roles in the discovery process, analogous to the collaborative and critical interactions among human researchers. An example of this approach is discussed in Section 5, where the responses of one LLM are reviewed and critiqued by another acting as a critic.

Additionally, we can consider having a horse race among multiple LLMs or using an open-source LLM to fine-tune it (e.g., Du et al., 2024) for our purpose. A potential challenge is that the performance metric is hard to define in our context due to the lack of ground truth for valid IVs. In fact, this is the very reason we propose using LLMs from the first place: for any IVs found by human researchers or the machine, there are only more compelling narratives or less compelling ones. In later stages, when data eventually come into play, over-identification tests can potentially be a fruitful framework for the evaluation of LLMs. More broadly, it would be interesting to apply the proposed approach of variable search in other empirical examples and other causal inference methods.

# A Alternative Prompts for IV Search

## A.1 Three-Step Prompts with System Messages

Here, we present three-step prompts that further divide the discovery task into subtasks, where each step corresponds to one of Assumptions REL, EX and IND. This version of prompts, especially when each step is conducted in a separate session, may be more immune to soliciting information from academic sources on IVs.<sup>17</sup> This version also include separate system messages that establish the scenario and role of interest as context information before initiating the main prompts. System messages allow LLMs to recognize top-level instructions that apply to all prompts that follow. The messages may also contain full institutional details across multiple paragraphs and other meta information, such as the specific formats for the LLM's responses.

#### Prompt A0 (System Messages).

you are [agent] who needs to make a [treatment] decision in [scenario]. you will be given questions on your decisions and related outcomes. in answering the questions, always provide explanations for your answers. each answer should be within five words and each explanation should be within twenty words. do you understand your role, the scenario you are in, and the instructions given to you?

#### Prompt A1 (Search for Relevance).

what are factors that can determine your decision? list  $[K_{-}0]$  factors that are quantifiable. explain the answers.

 $<sup>^{17}</sup>$ Nonetheless, in our applications, we find that the final responses from GPT4 are similar to those from the two-step prompts introduced in the main text.

#### Prompt A2 (Search for Exclusion).

among [K\_0] factors listed above, what are factors that affect your [outcome] only through [treatment]? explain the answers.

#### Prompt A3 (Search for Independence).

among the factors listed above, choose [K] factors that are most likely to be unassociated with [confounders], which determine your [outcome]. the chosen factors can still influence your [treatment]. for each factor chosen, explain your reasoning.

## A.2 Alternative Prompts with Covariates

Instead of using user-specified covariates in Prompt  $2_x$ , an alternative way is to search for covariates in Step 1. Prompt  $1_x$  below is designed to jointly search for  $(Z_k, X)$  that satisfy EX and REL2:

**Assumption REL2.** (i) The distribution of D given  $(Z_k, X) = (z_k, x)$  is a nontrivial function of  $(z_k, x)$  and (ii) the distribution of Y(d) given X = x is a nontrivial function of x.

#### **Prompt 1**<sub>x</sub> (Search for IVs and Covariates).

you are [agent] who needs to make a [treatment] decision in [setting]. what are factors that can determine your decision but that do not directly affect your [outcome], except through [treatment] (that is, factors that affect your [outcome] only through [treatment])? list [K\_0] factors. also, what are your characteristics that directly influence [treatment] and directly influence [outcome] (not just through [treatment])? list [L\_0] characteristics. explain the answers.

Instead of running Prompt 11 in Step 1, one can run Prompt  $1_x$  to find an initial set of covariates and select a subset among them at her discretion to run Prompt  $2_x$  in Step 2.

## A.3 Comparison to Direct Approach

An alternative to the proposed prompting strategy (i.e., multi-stage, role-playing prompts) would be to explicitly mention the term "instrumental variables" and inform LLMs that the ultimate objective is to "search for instrumental variables." Additionally, one can verbally train LLMs to understand the IV assumptions before conducting the search. Unfortunately, we find that this direct approach tends to suffer from *memorization*, where LLMs primarily focus on sources from existing academic articles and textbooks relevant to IVs. One can easily verify that, when applying prompts from the direct approach to the examples in Section 4, GPT4 generates answers that are reminiscent of established IVs in the literature. Moreover, when additionally prompted with "did you have sources for your previous responses?," GPT4 responds by citing well-known references in each application that propose IVs. In contrast, when the same question is asked after the proposed procedure, GPT4 responds that it "didn't have specific sources." When pressed to provide sources from the web, in the returns to education application, for example, it cites academic references from behavioral and social sciences on students' decision-making, including qualitative and case studies.

# B Prompts for Section 6

## B.1 Search for Control Variables in Difference-in-Differences

The following prompts are used to produce the results in Table 7 in Section 6.2. This example is motivated from Card and Krueger (1994), who explore the causal effects of minimum wage on labor market outcomes in the fast food industry.

#### Prompt C1-1 (Example: Minimum Wage).

you are the policymaker in the department of labor, deciding whether to increase the minimum wage or not and to which state to introduce this minimum wage law. what factors determine your decision? list forty factors that are quantifiable. explain the answers.

#### Prompt C2-1 (Example: Minimum Wage).

among the forty factors listed above, choose all factors that directly determine the temporal changes in average wages at fast food restaurants, not only indirectly through the minimum wage law. the chosen factors can still determine your decision of introducing minimum wage law. for each factor chosen, explain your reasoning.

# B.2 Further Refining Search for Running Variables in Regression Discontinuity

An additional refinement prompt could follow Prompt R1-R2 in Steps 1-2, as detailed below. Note that this prompt involves a counterfactual statement due to [confounders].

#### **Prompt R3** (Further Refine Running Variables).

among the criteria listed in the last answer above, choose all criteria that are difficult for you to manipulate. the chosen criteria should satisfy the following: [confounders, covariates] just below the cutoff and [confounders, covariates] just above the cutoff are not systematically different. explain the answers.

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