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INFO-F-409 - LEARNING DYNAMICS

Assignment One

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1 The Hawk-Dove game

The Hawk-Dove game was first formulated by John Maynard Smith and Georg Prince in 1973 [1]. The aim of the game is to gain a better understanding of conflicts in the animal kingdom. It consists of two players {Player One, Player Two} who have each two actions {Hawk, Dove}. The resulting payoff matrix can be seen in Table 1 where:

- V = fitness value of winning resources in fight
- D = fitness costs of injury
- T = fitness costs of wasting time

and we assume that $V, D, T \geq 0$.

Table 1: Hawk-Dove Payoff Matrix

		Player Two	
		Hawk	Dove
Player One	Hawk	$(V-D)/2$	0
	Dove	V	$V/2-T$

In a mixed strategy game, we consider each player performing his action with a certain probability p or q , which results in the following payoff matrix displayed in Table 2.

Table 2: Hawk-Dove Probability Payoff Matrix

		Player Two	
		P(Hawk)=q	P(Dove)=(1-q)
Player One	P(Hawk)=p	$(V-D)/2$	0
	P(Dove)=(1-p)	V	$V/2-T$

With this table we are able to calculate the payoff of the actions Hawk and Dove for Player One:

Player One's expected payoff for the strategy Hawk(p) is:

$$q \times \frac{V-D}{2} + (1-q) \times V$$

Player One's expected payoff for the strategy Dove(1-p) is:

$$q \times 0 + (1-q) \times \left(\frac{V}{2} - T\right) = (1-q) \times \left(\frac{V}{2} - T\right)$$

The best response set is {Hawk} if:

$$q \times \frac{V-D}{2} + (1-q) \times V < (1-q) \times \left(\frac{V}{2} - T\right)$$

The best response set is {Dove} if:

$$q \times \frac{V-D}{2} + (1-q) \times V > (1-q) \times \left(\frac{V}{2} - T\right)$$

All the players mixed strategies are best responses if:

$$q \times \frac{V-D}{2} + (1-q) \times V = (1-q) \times (\frac{V}{2} - T)$$

As we are dealing with unknown variables, let's rewrite the equation for q :

$$q \times \frac{V-D}{2} + (1-q) \times V = (1-q) \times (\frac{V}{2} - T)$$

$$\frac{qV}{2} - \frac{qD}{2} + V - qV = \frac{V}{2} - T - \frac{qV}{2} + qT$$

$$-\frac{qD}{2} + V = \frac{V}{2} - T + qT$$

$$\frac{V}{2} + T = \frac{qD}{2} + qT$$

$$\frac{V}{2} + T = q(\frac{D}{2} + T)$$

$$V + 2T = q(D + 2T)$$

$$q = \frac{V + 2T}{D + 2T}$$

To find any pure or mixed strategy of this scenario, we have to look at different values for the variables V, D and T . In this case, we must respect the following constraints:

$$0 \leq q \leq 1 \quad \text{and} \quad 0 \leq \frac{V + 2T}{D + 2T} \leq 1 \quad \text{and} \quad V, T, D \geq 0$$

1.1 T=0

Let's start by considering the case where $T = 0$. This leaves gives us the following options:

- $V = 0$ with $D = 0$
- $V = 0$ with $D > 0$
- $V > 0$ with $D = 0$
- $V = D > 0$
- $V > D > 0$
- $D > V > 0$

1.1.1 T=0, V=0, D=0

Any pure or mixed strategy is a best response. This yields the mixed strategy NE (Hawk,Dove) = $(p, 1-p), p \in \{(0 \leq p \leq 1)\}$.

Table 3: $V=T=0, D>0$

		Player Two	
		P(Hawk)=q	P(Dove)=(1-q)
Player One	P(Hawk)=p	$\begin{pmatrix} 0 \\ 0 \end{pmatrix}$	$\begin{pmatrix} 0 \\ 0 \end{pmatrix}$
	P(Dove)=(1-p)	$\begin{pmatrix} 0 \\ 0 \end{pmatrix}$	$\begin{pmatrix} 0 \\ 0 \end{pmatrix}$

1.1.2 $T=0, V=0, D>0$

We have three pure strategy NE: {Dove,Hawk},{Dove,Dove} and {Hawk,Dove}.

Player One's expected payoff for the strategy Hawk(p) is $-q \times \frac{D}{2}$. Player One's expected payoff for the strategy Dove(1-p) is 0. Solving for q gives $q = 0$ which does not yields a mixed strategy NE.

Table 4: $D>V=T=0$

		Player Two	
		P(Hawk)=q	P(Dove)=(1-q)
Player One	P(Hawk)=p	-D/2 -D/2	0 0
	P(Dove)=(1-p)	0 0	0 0

1.1.3 $T=0, V>0, D=0$

We find the pure strategy NE {Hawk,Hawk}.

Table 5: $V>T=D=0$

		Player Two	
		P(Hawk)=q	P(Dove)=(1-q)
Player One	P(Hawk)=p	V/2 V/2	0 V
	P(Dove)=(1-p)	0 V	V/2 V/2

1.1.4 $T=0, V=D>0$

We find the pure strategy NE's: {Hawk,Hawk}, {Hawk,Dove} and {Dove,Hawk}.

Table 6: $V=D>T=0$

		Player Two	
		P(Hawk)=q	P(Dove)=(1-q)
Player One	P(Hawk)=p	0 0	0 0
	P(Dove)=(1-p)	0 V	V/2 V/2

1.1.5 $T=0, V>D>0$

The action {Hawk, Hawk} is always positive as we have $V > D$. We find the pure strategy NE {Hawk,Hawk}.

Table 7: $V > D > T=0$

		Player Two	
		P(Hawk)=q	P(Dove)=(1-q)
Player One	P(Hawk)=p	$(V-D)/2$	0
	P(Dove)=(1-p)	0	$V/2$

1.1.6 $T=0, D > V > 0$

The action {Hawk, Hawk} is always negative as we have $D > V$. We find two pure strategy NE's: {Dove,Hawk} and {Hawk,Dove}.

Table 8: $D > V > T=0$

		Player Two	
		P(Hawk)=q	P(Dove)=(1-q)
Player One	P(Hawk)=p	$(V-D)/2$	0
	P(Dove)=(1-p)	0	$V/2$

Player One's expected payoff for the strategy Hawk(p) is:

$$q \times \frac{V-D}{2} + (1-q) \times V = \frac{qV}{2} - \frac{qD}{2} + V - qV$$

Player One's expected payoff for the strategy Dove(1-p) is:

$$q \times 0 + (1-q) \times V/2 = (1-q) \times (V/2) = \frac{V}{2} - \frac{qV}{2}$$

All the players mixed strategies are best responses if:

$$\frac{qV}{2} - \frac{qD}{2} + V - qV = \frac{V}{2} - \frac{qV}{2}$$

$$V - \frac{qD}{2} = \frac{V}{2}$$

$$2V - qD = V$$

$$-qD = -V$$

$$q = \frac{V}{D}$$

We find the mixed strategy NE $q = \frac{V}{D}$.

1.2 $V = 0$

Setting $V = 0$ gives us the following options:

- $D = 0$ with $T = 0$ (already covered)
- $D = 0$ with $T > 0$
- $D > 0$ with $T = 0$ (already covered)
- $D = 2T > 0$
- $D > 2T > 0$
- $2T > D > 0$

1.2.1 $V=0, D=0, T>0$

We find three pure strategy NE's: {Hawk,Hawk}, {Hawk,Dove} and {Dove,Hawk}.

Table 9: $T>V=D=0$

		Player Two	
		P(Hawk)=q	P(Dove)=(1-q)
Player One	P(Hawk)=p	$\begin{matrix} 0 \\ 0 \end{matrix}$	$\begin{matrix} 0 \\ 0 \end{matrix}$
	P(Dove)=(1-p)	$\begin{matrix} 0 \\ 0 \end{matrix}$	$\begin{matrix} -T \\ -T \end{matrix}$

1.2.2 $V=0, D=2T>0$

Setting $D = 2T$ gives the following payoff matrix:

Table 10: $D=2T>V=0$

		Player Two	
		P(Hawk)=q	P(Dove)=(1-q)
Player One	P(Hawk)=p	$\begin{matrix} -T \\ -T \end{matrix}$	$\begin{matrix} 0 \\ 0 \end{matrix}$
	P(Dove)=(1-p)	$\begin{matrix} 0 \\ 0 \end{matrix}$	$\begin{matrix} -T \\ -T \end{matrix}$

We find two pure strategy NE's: {Hawk,Dove} and {Dove,Hawk}. Player One's expected payoff for the strategy Hawk(p) is: $-qT$. Player One's expected payoff for the strategy Dove(1-p) is: $-T + qT$. All the players mixed strategies are best responses if:

$$-qT = -T + 2qT$$

$$2qT - T = 0$$

$$q = \frac{1}{2}$$

We find the mixed strategy NE: $q = \frac{1}{2}$.

1.2.3 $V=0, D>2T>0$

We find two pure strategy NE's: {Hawk,Dove} and {Dove,Hawk}. Because $D > 2T$, the action {Hawk,Hawk} is more negative than {Dove,Dove}.

Table 11: $D > 2T > V = 0$

		Player Two	
		P(Hawk)=q	P(Dove)=(1-q)
Player One	P(Hawk)=p	$-D/2$	$\textcircled{0}$
	P(Dove)=(1-p)	$\textcircled{0}$	$-T$

Player One's expected payoff for the strategy Hawk(p) is: $-q\frac{D}{2}$.

Player One's expected payoff for the strategy Dove(1-p) is: $-T + qT$.

All the players mixed strategies are best responses if:

$$-q\frac{D}{2} = -T + qT$$

$$qT + \frac{qD}{2} = T$$

$$2qT + qD = 2T$$

$$q(2T + D) = 2T$$

$$q = \frac{2T}{2T + D}$$

We find the mixed strategy NE: $q = \frac{2T}{2T + D}$.

1.2.4 $V=0, 2T > D > 0$

Same pure and mixed strategy NE as previous section. The only difference here is that the action {Dove,Dove} is more negative than {Hawk,Hawk}.

1.3 $D = 0$

Setting $D = 0$ gives us the following options:

- $T = 0$ with $V > 0$ (already covered)
- $T > 0$ with $V = 0$ (already covered)
- $T = 0$ with $V = 0$ (already covered)
- $T = \frac{V}{2} > 0$
- $T > \frac{V}{2} > 0$
- $\frac{V}{2} > T > 0$

1.3.1 $D=0, T=V/2 > 0$

We find the pure strategy NE {Hawk,Hawk}.

Table 12: $T=V/2>D=0$

		Player Two	
		P(Hawk)=q	P(Dove)=(1-q)
Player One	P(Hawk)=p	$\begin{matrix} & \textcircled{V/2} \\ \textcircled{V/2} & \end{matrix}$	$\begin{matrix} & 0 \\ \textcircled{V} & \end{matrix}$
	P(Dove)=(1-p)	$\begin{matrix} & \textcircled{V} \\ 0 & \end{matrix}$	$\begin{matrix} & 0 \\ 0 & \end{matrix}$

1.3.2 $D=0, T>V/2>0$

We find the pure strategy NE {Hawk,Hawk}. The action {Dove,Dove} is always negative.

Table 13: $T>V/2>D=0$

		Player Two	
		P(Hawk)=q	P(Dove)=(1-q)
Player One	P(Hawk)=p	$\begin{matrix} & \textcircled{V/2} \\ \textcircled{V/2} & \end{matrix}$	$\begin{matrix} & 0 \\ \textcircled{V} & \end{matrix}$
	P(Dove)=(1-p)	$\begin{matrix} & \textcircled{V} \\ 0 & \end{matrix}$	$\begin{matrix} & V/2-T \\ V/2-T & \end{matrix}$

1.3.3 $D=0, V/2>T>0$

Same answer as previous configuration. Only difference is that the action {Dove,Dove} is always positive.

1.4 $T>0, V>0, D>0$

We can now look at configurations without a zero variable. This setting leaves us with the following configurations to consider:

T largest :

- $T = \frac{V}{2} = \frac{D}{2}$
- $T = \frac{V}{2} > \frac{D}{2}$
- $T = \frac{D}{2} > \frac{V}{2}$
- $T > \frac{V}{2} = \frac{D}{2}$
- $T > \frac{V}{2} > \frac{D}{2}$
- $T > \frac{D}{2} > \frac{V}{2}$

V/2 largest :

- $\frac{V}{2} = \frac{D}{2} = T$
- $\frac{V}{2} = \frac{D}{2} > T$
- $\frac{V}{2} = T > \frac{D}{2}$
- $\frac{V}{2} > \frac{D}{2} = T$
- $\frac{V}{2} > \frac{D}{2} > T$
- $\frac{V}{2} > T > \frac{D}{2}$

D/2 largest :

- $\frac{D}{2} = \frac{V}{2} = T$
- $\frac{D}{2} = \frac{V}{2} > T$
- $\frac{D}{2} = T > \frac{V}{2}$
- $D/2 > \frac{V}{2} = T$
- $D/2 > \frac{V}{2} > T$
- $D/2 > T > \frac{V}{2}$

It should be noted that we only consider configurations around their extreme points, i.e. configurations that change the value of a cell(negative, zero or positive). Greyed out items are already considered by previous configurations.

1.4.1 $T=V/2=D/2$

We find three pure strategy NE's: {Hawk,Hawk}, {Dove,Hawk} and {Hawk,Dove}

Table 14: $T=V/2=D/2$

		Player Two	
		P(Hawk)=q	P(Dove)=(1-q)
Player One	P(Hawk)=p	$\begin{matrix} \textcircled{0} \\ \textcircled{0} \end{matrix}$	$\begin{matrix} \textcircled{0} \\ \textcircled{V} \end{matrix}$
	P(Dove)=(1-p)	$\begin{matrix} \textcircled{V} \\ \textcircled{0} \end{matrix}$	$\begin{matrix} 0 \\ 0 \end{matrix}$

1.4.2 $T=V/2>D/2$

We find the pure strategy NE: {Hawk,Hawk}.

Table 15: $T=V/2>D/2$

		Player Two	
		P(Hawk)=q	P(Dove)=(1-q)
Player One	P(Hawk)=p	$\begin{matrix} \textcircled{(V-D)/2} \\ \textcircled{(V-D)/2} \end{matrix}$	$\begin{matrix} 0 \\ \textcircled{V} \end{matrix}$
	P(Dove)=(1-p)	$\begin{matrix} \textcircled{V} \\ 0 \end{matrix}$	$\begin{matrix} 0 \\ 0 \end{matrix}$

1.4.3 $T=D/2>V/2$

We find two pure strategy NE's: {Hawk,Dove} and {Dove,Hawk}. The actions {Hawk,Hawk} and {Dove,Dove} are always negative because $D > V$ and $T > V/2$.

Table 16: $T=D/2>V/2$

		Player Two	
		P(Hawk)=q	P(Dove)=(1-q)
Player One	P(Hawk)=p	$\begin{matrix} \textcircled{(V-D)/2} \\ (V-D)/2 \end{matrix}$	$\begin{matrix} \textcircled{0} \\ \textcircled{V} \end{matrix}$
	P(Dove)=(1-p)	$\begin{matrix} \textcircled{V} \\ \textcircled{0} \end{matrix}$	$\begin{matrix} V/2-T \\ V/2-T \end{matrix}$

To find the mixed strategy NE, we need to calculate q from the payoff matrix, which we already did earlier: $q = \frac{V+2T}{D+2T}$.

1.4.4 $T>V/2=D/2$

We find three pure strategy NE's: {Hawk,Hawk}, {Dove,Hawk} and {Hawk,Dove}. The action {Dove,Dove} is always negative

Table 17: $T=V/2=D/2$

		Player Two	
		P(Hawk)=q	P(Dove)=(1-q)
Player One	P(Hawk)=p	$\begin{matrix} & 0 \\ 0 & \end{matrix}$	$\begin{matrix} & 0 \\ V & \end{matrix}$
	P(Dove)=(1-p)	$\begin{matrix} & V \\ 0 & \end{matrix}$	$\begin{matrix} & V/2-T \\ V/2-T & \end{matrix}$

1.4.5 $T > V/2 > D/2$

We find the pure strategy NE: {Hawk,Hawk}. The action {Dove,Dove} is always negative

Table 18: $T > V/2 > D/2$

		Player Two	
		P(Hawk)=q	P(Dove)=(1-q)
Player One	P(Hawk)=p	$\begin{matrix} & (V-D)/2 \\ (V-D)/2 & \end{matrix}$	$\begin{matrix} & 0 \\ V & \end{matrix}$
	P(Dove)=(1-p)	$\begin{matrix} & V \\ 0 & \end{matrix}$	$\begin{matrix} & V/2-T \\ V/2-T & \end{matrix}$

1.4.6 $T > D/2 > V/2$

We find two pure strategy NE's: {Hawk,Dove} and {Dove,Hawk}. The actions {Dove,Dove} and {Hawk,Hawk} are always negative.

Table 19: $T > V/2 > D/2$

		Player Two	
		P(Hawk)=q	P(Dove)=(1-q)
Player One	P(Hawk)=p	$\begin{matrix} & (V-D)/2 \\ (V-D)/2 & \end{matrix}$	$\begin{matrix} & 0 \\ V & \end{matrix}$
	P(Dove)=(1-p)	$\begin{matrix} & V \\ 0 & \end{matrix}$	$\begin{matrix} & V/2-T \\ V/2-T & \end{matrix}$

To find the mixed strategy NE, we need to calculate q from the payoff matrix, which we already did earlier: $q = \frac{V+2T}{D+2T}$.

1.4.7 $V/2=D/2 > T$

We find three pure strategy NE's: {Hawk,Hawk}, {Hawk,Dove} and {Dove,Hawk}.

Table 20: $V/2=D/2>T$

		Player Two	
		P(Hawk)=q	P(Dove)=(1-q)
Player One	P(Hawk)=p	$\textcircled{0}$	$\textcircled{0}$
	P(Dove)=(1-p)	\textcircled{V}	$V/2-T$

1.4.8 $V/2>D/2=T$

We find the pure strategy NE: {Hawk,Hawk}.

Table 21: $V/2>D/2=T$

		Player Two	
		P(Hawk)=q	P(Dove)=(1-q)
Player One	P(Hawk)=p	$\textcircled{(V-D)/2}$	0
	P(Dove)=(1-p)	0	\textcircled{V}

1.4.9 $V/2>D/2>T$

Same result as previous section.

1.4.10 $V/2>T>D/2$

Same result as previous section.

1.4.11 $D/2>V/2=T$

We find two pure strategy NE's: {Hawk,Dove} and {Dove,Hawk}.

Table 22: $D/2>V/2=T$

		Player Two	
		P(Hawk)=q	P(Dove)=(1-q)
Player One	P(Hawk)=p	$(V-D)/2$	$\textcircled{0}$
	P(Dove)=(1-p)	$\textcircled{0}$	0

Player One's expected payoff for the strategy Hawk(p) is:

$$q \times \frac{V - D}{2} + (1 - q) \times V = -\frac{qV}{2} - \frac{qD}{2} + V$$

Player One's expected payoff for the strategy Dove(1-p) is:

$$q \times 0 + (1 - q) \times 0 = 0$$

All the players mixed strategies are best responses if:

$$-\frac{qV}{2} - \frac{qD}{2} + V = 0$$

$$qV + qD = 2V$$

$$q(V + D) = 2V$$

$$q = \frac{2V}{(V + D)}$$

We find a mixed strategy NE with $q = \frac{2V}{(V+D)}$.

1.4.12 $D/2 > V/2 > T$

We find two pure strategy NE's: {Hawk,Dove} and {Dove,Hawk}.

Table 23: $D/2 > V/2 = T$

		Player Two	
		P(Hawk)=q	P(Dove)=(1-q)
Player One	P(Hawk)=p	$(V-D)/2$ $(V-D)/2$	$\textcircled{0}$ \textcircled{V}
	P(Dove)=(1-p)	\textcircled{V} $\textcircled{0}$	$V/2-T$ $V/2-T$

To find the mixed strategy NE, we need to calculate q from the payoff matrix, which we already did earlier: $q = \frac{V+2T}{D+2T}$.

1.4.13 $D/2 > T > V/2$

Same response as previous section.

1.5 Results

1.5.1 Question 1

The following are all the mixed strategy Nash equilibria (MSNE) of this game:

- $T = V = D = 0$ yields an infinite number of MSNE's: (Hawk,Dove) = $(p, 1 - p)$, $p \in \{(0 \leq p \leq 1)\}$
- $D > V > T = 0$ yields $q = \frac{V}{D}$ as MSNE
- $D = 2T > V = 0$ yields $q = \frac{1}{2}$ as MSNE
- $D > 2T > V = 0$ yields $q = \frac{2T}{2T+D}$ as MSNE

- $T = \frac{D}{2} > \frac{V}{2} > 0$ yields $q = \frac{V+2T}{D+2T}$ as MSNE
- $T > \frac{D}{2} > \frac{V}{2} > 0$ yields $q = \frac{V+2T}{D+2T}$ as MSNE
- $\frac{D}{2} > \frac{V}{2} = T > 0$ yields $q = \frac{2V}{V+D}$ as MSNE
- $\frac{D}{2} > \frac{V}{2} > T > 0$ yields $q = \frac{V+2T}{D+2T}$ as MSNE
- $\frac{D}{2} > T > \frac{V}{2} > 0$ yields $q = \frac{V+2T}{D+2T}$ as MSNE

1.5.2 Question 2

The best response set is {Dove} if:

$$\begin{aligned}
q \times \frac{V-D}{2} + (1-q) \times V &> (1-q) \times \left(\frac{V}{2} - T\right) \\
\frac{qV}{2} - \frac{qD}{2} + V - qV &> \frac{V}{2} - T - \frac{qV}{2} + qT \\
-\frac{qD}{2} + V &> \frac{V}{2} - T + qT \\
2V - qD &> V - 2T + 2qT \\
V + 2T &> 2qT + qD \\
V + 2T &> q(2T + D) \\
\frac{V + 2T}{2T + D} &> q \\
q &< \frac{V + 2T}{D + 2T}
\end{aligned}$$

A pure strategy NE for {Dove, Dove} can only be found in the case where:

$$D > T = V = 0$$

2 Which social dilemma?

Player A is confronted with one of three social dilemma's - the corresponding payoff matrix is shown in tables 24, 25 and 26. The player has to decide whether to cooperate (C) or to defect (D) without knowing which game he is actually facing. Each dilemma has the same probability 1/3 of being played. Opponent B knows the game.

Table 24: Prisonners dilemma

	C	D
C	2, 2	0, 5
D	5, 0	1, 1

Table 25: Stag-Hunt game

	C	D
C	5, 5	0, 2
D	2, 0	1, 1

Table 26: Snowdrift game

	C	D
C	2, 2	1, 5
D	5, 1	0, 0

with this information we can calculate the expected payoff for player A for every possible strategy of Player B - Table 27.

Table 27: Expected payoff for Player A

		Player B							
		(C,C,C)	(C,C,D)	(C,D,C)	(C,D,D)	(D,C,C)	(D,C,D)	(D,D,C)	(D,D,D)
Player A	C	9/3	8/3	4/3	3/3	7/3	6/3	2/3	1/3
	D	12/3	7/3	11/3	6/3	8/3	3/3	7/3	2/3

From this table we can select the best response for Player A for each strategy of Player B - cells marked red in Table 28.

Table 28: Best responses for Player A

		Player B							
		(C,C,C)	(C,C,D)	(C,D,C)	(C,D,D)	(D,C,C)	(D,C,D)	(D,D,C)	(D,D,D)
Player A	C	9/3	8/3	4/3	3/3	7/3	6/3	2/3	1/3
	D	12/3	7/3	11/3	6/3	8/3	3/3	7/3	2/3

Now we have to determine the best responses of Player B against Player A of the three different strategies - marked by green cells in Tables 29, 30 and 31.

Table 29: Prisonners dilemma

	C	D
C	2	5
D	0	1

Table 30: Stag-Hunt game

	C	D
C	5	2
D	0	1

Table 31: Snowdrift game

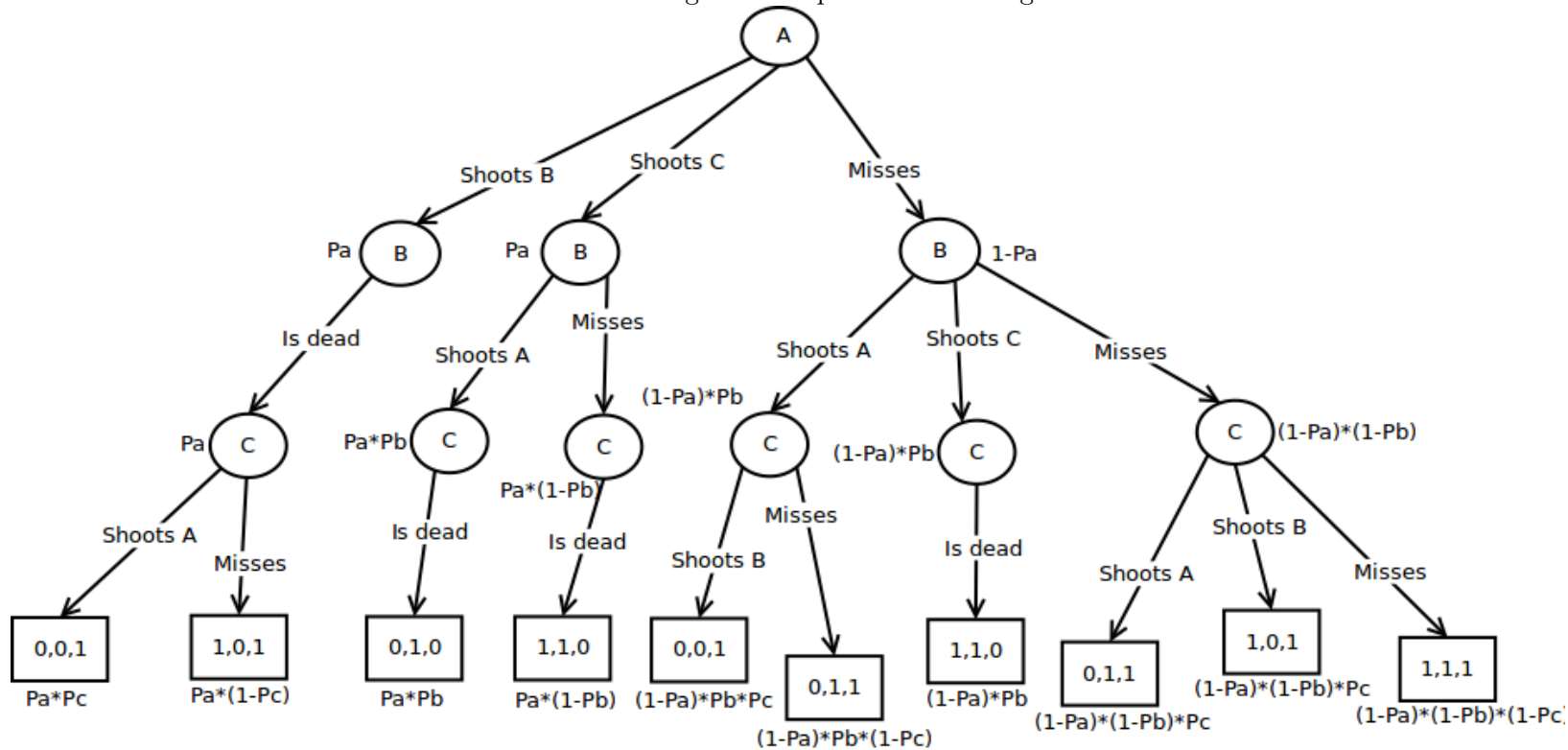
	C	D
C	2	5
D	1	0

The pure strategy Nash Equilibria can now be determined by matching these results. We find two Nash Equilibria at $\{C, (D, C, D)\}$ and $\{D, (D, D, C)\}$.

3 Sequential truel

This scenario considers three persons A,B and C, each of whom has a gun with a single bullet. If alive, each person may shoot at any surviving person. The order in which the scenario is played out is A, then B and then C. The probability that player i hits their target is denoted by p_i where $0 \leq p_i \leq 1$. Every player wishes to optimize her probability of survival. For this exercise we further assume that a player has to target another living player and is not allowed to miss a shoot consciously. The resulting diagram of this game is shown in Figure 1.

Figure 1: Sequential truel diagram



The Diagram shows all possible actions of all players with all possible outcomes. The lowest level leaf indicates which player is still alive and with which probability - $[0,0,1]$ indicates Player A and B being dead while Player C is alive with a probability of $p_a \times p_c$.

References

- [1] J. Maynard Smith and G. R. Price. The logic of animal conflict. *Nature*, 246(5427):15–18, 1973.