

# Introduction - How to Prove It : Answers to exercises

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- 1.(a.) Factor  $2^{15} - 1 = 32,767$  into two smaller positive integers  
 7, 4681  
 (b.) Find an integer  $x$  such that  $1 < x < 2^{32767} - 1$  and  $2^{32767} - 1$  is divisible  
 by  $x$ .  
 127 i.e.  $2^7 - 1$ .

$n$	Is $n$ prime?	$3^n - 1$	Is $3^n - 1$ prime?	
2	Y	8	N	
3	Y	26	N	
4	N	80	N	
5	Y	242	N	
6	N	728	N	Based on the values of the
7	Y	2186	N	
8	N	6560	N	
9	N	19682	N	
10	N	59048	N	

table I conjecture that  $3^n - 1$  is always even, and so is never prime.

## 3. Euclid's theorem

- (a.) Find a prime different from 2,3,5 and 7.

$$\text{Let } m = 2 * 3 * 5 * 7 + 1 = 211$$

211 is prime (b.) Find a prime different from 2,5 and 11.

$$\text{Let } m = 2 * 5 * 11 + 1 = 111$$

111 has the factor 3, which is different to the primes above.

## 4. Find five consecutive integers that are not prime.

$$\text{Let } n = 5 \text{ and let } x = (n + 1)! + 2 = 722$$

722,723,724,725 and 726 are not prime.

727 is prime.