

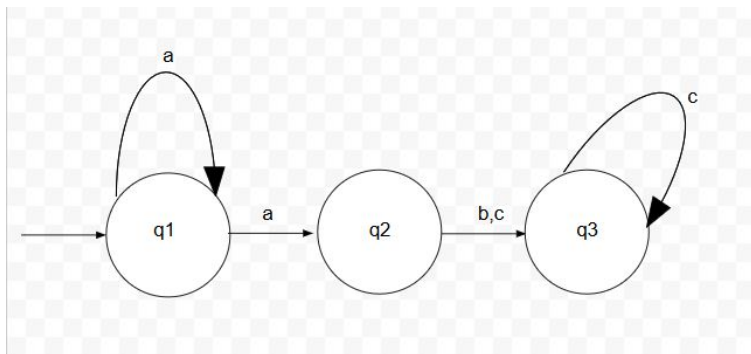
# CSCI 301 M8 Homework

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**Collaboration statement:** By submitting this assignment, I am attesting that this homework is in full compliance with the course's <https://www.instructure.com/courses/1340003/pages/academic-dishonesty-guidelines> Homework Collaboration Policy and with all the other relevant academic honesty policies of the course and university. I discussed this homework with no one and wrote this solution without input from anyone else.

1. (a)  $S \rightarrow A$  (using  $S \rightarrow A$ .  
 $\rightarrow aA$  (using  $A \rightarrow aA$ )  
 $\rightarrow aaA$  (using  $A \rightarrow aA$ )  
 $\rightarrow aaB$  (using  $aA \rightarrow aB$ )  
 $\rightarrow aabB$  (using  $B \rightarrow bB$ )  
 $\rightarrow aabb$  (using  $B \rightarrow bB$ )  
 $\rightarrow aabb$  (using  $B \rightarrow \varepsilon$ )
- (b) i.  $aaabbb$   
 ii.  $aaaabbbb$   
 iii.  $aaaaabbbbb$   
 iv.  $aAb\varepsilon$   
 v.  $aab\varepsilon$   
 vi.  $abb\varepsilon$
- (c)  $\varepsilon \cup a^*b|ab^*$
- (d) If you were to remove  $B \rightarrow b$  as it breaks the rule of right-regular grammars in which  $v \rightarrow a$ , where  $v \in V$  and  $a \in \Sigma$ .
2.  $((a \cup b \cup c)(a \cup b \cup c))^*$



- 3.
4.  $\varepsilon \cup (a^*|a^*b|a^*ccb|b)$
5. We will prove with contradiction  
**Suppose** that  $\{a^n b^n c^{2n} : n \geq 0\}$  is regular.  
**Let** The string  $s = p \geq 1$  be the pumping length, as given by the pumping lemma. Consider the string  $s = a^p b^p c^{2p}$ .

It is clear that  $s \in A$  and  $|s| = 2p \geq p$ .

Hence, by the pumping lemma,  $s$  can be written as  $s = xyz$ , where  $y \neq \varepsilon$ ,  $|xy| \leq p$ , and  $xy^iz \in A$  for all  $i \geq 0$ .

Observe that, since  $|abc| \leq p$ , the string will contain 0s. Moreover, since  $y \neq \varepsilon$ ,  $abc$  contains at least one 0. No strings  $a^0bc = bc, a^2b^2c = abbc, abc^3 = abccc, \dots$ , is contained in our set.

However, by the pumping lemma, all these strings must be in our set.

Hence, we have a contradiction and we conclude that  $\{a^n b^n c^{2^n} : n \geq 0\}$  is not a regular language.