

CSCI 301 M6 Homework

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May 22, 2020

Collaboration statement: By submitting this assignment, I am attesting that this homework is in full compliance with the course's <https://www.instructure.com/courses/1340003/pages/academic-dishonesty-guidelines> Homework Collaboration Policy and with all the other relevant academic honesty policies of the course and university. I discussed this homework with no one and wrote this solution without input from anyone else.

1. (a) $V = \{q_1, q_2, q_3, q_4\}$.

(b) $S = q_1$.

(c) R consists of rules:

$$q_1 \rightarrow aq_1|bq_2|cq_3.$$

$$q_2 \rightarrow \varepsilon.$$

$$q_3 \rightarrow cq_4.$$

$$q_4 \rightarrow bq_2|\varepsilon.$$

(d) $\Sigma = \{a, b, c\}$.

2. (a) $V = \{S\}$.

$$\Sigma = \{0, 1\}.$$

R consists of rules:

$$S \rightarrow \varepsilon|0S1.$$

$$S = S.$$

(b) $\Sigma = \{0, 1\}$.

$$\Gamma = \{\$, S\}.$$

$$Q = \{q_0, q_1, q_2\}.$$

$$\delta = \{$$

$$q_00\$ \rightarrow q_0R\$S$$

$$q_00S \rightarrow q_0RSS$$

$$q_01\$ \rightarrow q_0N\$$$

$$q_01S \rightarrow q_1R\varepsilon$$

$$q_0\square\$ \rightarrow q_0N\varepsilon$$

$$q_0\square S \rightarrow q_0NS$$

$$q_10\$ \rightarrow q_1N\$$$

$$q_10S \rightarrow q_1NS$$

$$q_11\$ \rightarrow q_1N\$$$

$$q_11S \rightarrow q_1R\varepsilon$$

$$q_1\square\$ \rightarrow q_1N\varepsilon$$

$$q_1\square S \rightarrow q_1NS\}.$$

3. (a) $V = \{S\}$.

$$\Sigma = \{0, 1\}.$$

R consists of rules:

$$S \rightarrow \varepsilon|0S1.$$

$$S = S.$$

- (b) $\Sigma = \{0, 1\}$.
 $\Gamma = \{\$, S\}$.
 $Q = \{q_0, q_1, q_2\}$.
 $\delta = \{$
 $q_0 1 \$ \rightarrow q_0 N \$$
 $q_0 1 S \rightarrow q_1 R \varepsilon$
 $q_0 \square \$ \rightarrow q_0 N \varepsilon$
 $q_0 \square S \rightarrow q_0 N S$
 $q_1 1 \$ \rightarrow q_1 N \$$
 $q_1 1 S \rightarrow q_1 R \varepsilon$
 $q_1 \square \$ \rightarrow q_1 N \varepsilon$
 $q_1 \square S \rightarrow q_1 N S$
 $q_0 1 \$ \rightarrow q_0 N \$$
 $q_0 1 S \rightarrow q_1 R \varepsilon$
 $q_0 \square \$ \rightarrow q_0 N \varepsilon$
 $q_0 \square S \rightarrow q_0 N S\}$.
4. (a) $V = \{S\}$.
 $\Sigma = \{0, 1\}$.
R consists of rules:
 $S \rightarrow \varepsilon | 0S1$.
 $S = S$.
- (b) $\Sigma = \{0, 1\}$.
 $\Gamma = \{\$, S\}$.
 $Q = \{q, q'\}$.
 $\delta = \{$
 $q'0 \$ \rightarrow q' N \varepsilon$
 $q'0 S \rightarrow q' R \varepsilon$
 $q'1 \$ \rightarrow q' N \varepsilon$
 $q'1 S \rightarrow q' R \varepsilon$
 $q' \square \$ \rightarrow q' N \varepsilon$
 $q' \square S \rightarrow q' N S\}$.
 $q0 \$ \rightarrow qR \$ S$
 $q0 S \rightarrow qR S S$
 $q1 \$ \rightarrow q' R \$$
 $q1 \$ \rightarrow qR \$ S$
 $q1 S \$ \rightarrow q' R S$
 $q1 S \$ \rightarrow qR R S$
 $q \square \$ \rightarrow qN \$$
 $q \square S \rightarrow qN S$
Input string possibly rejected.