



BRAC University

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Q.1

a. The given code snippet ~~can~~ has undetermined time complexity. The inner loop will run infinitely times. So, the time complexity is infinity.

b. The time complexity of this code is also infinity. Because the 2nd part of the code will run infinite time.

c. The statement is meaningless because doesn't give any details about the algorithm's performance. The work 'at least' means the lower bound of the algorithm. Big-oh notation means the upper bound. So the statement doesn't make any sense.

Q.2

a. $user_id = 'x'$ $details = [[id, name], \dots, n]$ for $i \rightarrow 0$ to $n+1$:if $user_id == details[i][1]$

return True

return False.

b. Countsort can be used here.

Algorithm:

CountSort (A, Output,

 $C = [0] * \max[A] \rightarrow$ new array; $output = [0] * \text{len}(A)$ for $i \rightarrow 0$ to $\text{len}(A)$: $C[A[i]] += 1$ for $j \rightarrow 0$ to $\text{len}(C)$: $C[j] += C[j-1]$ for $k \rightarrow \text{len}(A)-1$ to 1 : $output[C[A[k]]-1] = A[k]$ $C[A[k]] = C[A[k]-1]$

return output

c. Yes, the crash was a result of the sorting algorithm. It is possible that the sorting algorithm was running out of memory if the maximum number of post count is very big. Due to insufficient memory allocation there will be a crash.

d. Merge Sort has a time complexity of $n \log n$ in best, worst and average case.

```
def mergesort(A, l, h):
```

```
    if (l > h):
```

```
        mid = (l+h)//2
```

```
        mergesort(l
```

```
        LA = mergesort(l, mid, A, l, mid)
```

```
        RA = mergesort(A, mid+1, h)
```

```
        merge(LA, RA, n, m):
```

```
        RA = [0] * (m+n)
```

```
        while (
```


def merge (LA, RA, n, m):

Subject: $MA[0] * (m+n)$

Date: |

Time: |

$i, j, k = 0$

while ($i < n$ and $j < m$):

if $LA[i] < RA[j]$:

$MA[k] = LA[i]$

$i++$

else:

$MA[k] = RA[j]$

$k++$

while $i < n$:

$MA[k] = LA[i]$

$i++$, $k++$

while $j < m$:

$MA[k] = RA[j]$

$j++$, $k++$

return MA

Subject :

Date :

Time :

Q. The searching algorithm is Binary Search.

Algorithm:

Def Binary Search(A, X): # X is the target value

$l = 0$

$h = \text{len}(A) - 1$

while ($l \leq h$):

$\text{mid} = (l + h) // 2$

if x is greater, ignore the left half

if $A[\text{mid}] < x$:

$l = \text{mid} + 1$

if x is smaller, ignore the right half

elif $A[\text{mid}] > x$:

$h = \text{mid} - 1$

else:

return "Found"

return "Not found"

if the element is not present in the list.

Steps to search for post count 9

Since the list is already sorted, the mid element is 5,

→ 9 is greater than 5, so we will do the searching to the right half ([8, 9, 12, 14, 17])

→ The mid element of the right half is 12

→ 12 is greater than 9, so we will search in left half: [8, 9]

→ The mid element is 8, so we will search in the right half: [9]

→ The mid element is 9. We found the target.

Q.3

1. The modified algorithm is:

```
def b-search(array, ele):
    l = 0, h = len(array) - 1
    while (l <= h):
        mid = (l + h) // 2
        if array[mid] < ele:
            l = mid + 1
        elif array[mid] > ele:
            h = mid - 1
        else:
            return mid
    return -1
```

2. To return the first index if there are duplicates.

```
def b-search(array, ele):
    l = 0, h = len(array) - 1, index = -1
    while (l <= h):
        mid = (l + h) // 2
        if array[mid] < ele:
            l = mid + 1
        elif array[mid] > ele:
            h = mid - 1
        else:
            index = mid
            h = mid - 1
```


else:

ind_x = mid

h = mid - 1

return ind_x

3. To return index and first appearance:

def b-search(array, ele):

l = 0, h = len(array) - 1, f-index = -1

while (l ≤ h):

mid = (l + h) // 2

if array[mid] == ele:

l = mid + 1

elif array[mid] > ele:

h = mid - 1

else:

f-index = mid

h = mid - 1

temp = f-index

while (temp < len(array) and array[temp] == ele):

temp += 1

count = temp - f-index

```

if f_index == -1:
    return False
return (f_index, count)

```

4. To find minimum element wave pattern:

```

def find_min_ele(array):
    l = 0, h = len(array) - 1
    while (l <= h):
        mid = (l + h) // 2
        if (mid == 0 or array[mid - 1] > array[mid])
            and (mid == len(array) - 1 or array[mid + 1] > array[mid]):
            return array[mid]
        elif (mid > 0 and array[mid - 1] < array[mid]):
            h = mid - 1
        else:
            l = mid + 1
    return array[mid]

```

Q.4 :

For the given list if we search for $T=2$ the steps will be:

mid	L_idx	R_idx
	0	7
3	0	2
2		

found T

As we can see the list is not sorted.

Coincidentally we have found the value $T=2$ but if the value was ~~23 or 10 or any~~ 1 or anything we would not be able to find it because the array/list is not sorted.

Q.5.

a. Using Binary Search we can solve it.

```
def b_search_find_max(array):
    l=0, h=len(array)-1
    while (l<=h):
        mid=(l+h)//2
        if (array[mid]>array[mid-1]) and (array[mid]>
            array[mid+1]):
            return array[mid]
        elif (array[mid]>array[mid-1]) and (array[mid]<
            array[mid+1]):
            l=mid+1
        else:
            h=mid-1
    return max(array[l], array[h])
```

b. The time complexity of this code is $O(\log N)$.

Q.6

a. Sorting an array before binary search

is useful ~~because~~ when we need to search for a multiple times. Sorting the array takes $O(N \log N)$ time (only once).

Then we can search for the element in $O(\log N)$ time. But if we do linear search it will take $O(N)$ time for each search which is not efficient way to do the searching.

b. Modified countsort algorithm:

```
def countsort(array):  
    # find the max, min of the array  
    min_ele = min(array), max_ele = max(array)  
    count = [0] * (max_ele - min_ele + 1)  
    for val in array:  
        count[val - min_ele] += 1
```

```
for i in range(1, max_ele - min_ele + 1):
```

```
    count[i] += count[i-1]
```

```
output = [0] * len(array)
```

```
for j in range(len(array)-1, -1, -1):
```

```
    output[count[array[j] - min_ele] - 1] = array[j]
```

```
    count[array[j] - min_ele] -= 1
```

```
return output
```

c. Same as the code ~~was~~ in (b).

Here we'll just take the int value using the int() function.

```
def count_sort(array):
```

```
    max = int(max(array)), min = int(min(array))
```

```
    count = [0] * (max - min + 1)
```

```
    for val in array:
```

```
        count[int(val) - min] += 1
```

```

for i in range(1, max-min+1):
    count[i] += count[i-1]
output = [0] * len(array)
for j in range(len(array)-1, -1, -1):
    output[count[int(array[j]) - min] - 1] = array[j]
    count[int(array[j]) - min] -= 1
return output

```

d. Quick Sort is faster than merge sort when the pivot is chosen wisely. If the pivot is chosen poorly Quick sort will have the worst-case time complexity of $O(n^2)$. Merge sort work in $O(N \log N)$ time complexity in every case. If we want to run the code at $O(n \log n)$ time for any case then mergesort is a better option.