

Mathematics III

Course Objective:

To round out the students' preparation for more sophisticated applications with an introduction to linear algebra, Fourier Series, Laplace Transforms, integral transformation theorems and linear programming.

1. Determinants and Matrices(11 hours)

- a. Determinant and its properties
- b. Solution of system of linear equations
- c. Algebra of matrices
- d. Complex matrices
- e. Rank of matrices
- f. System of linear equations
- g. Vector spaces
- h. Linear transformations
 - i. Eigen value and Eigen vectors
 - j. The Cayley-Hamilton theorem and its uses
- k. Diagonalization of matrices and its applications

2. Line, Surface and Volume Integrals(12 hours)

- a. Line integrals
- b. Evaluation of line integrals
- c. Line integrals independent of path
- d. Surfaces and surface integrals
- e. Green's theorem in the Plane and its applications
- f. Stoke's theorem (without proof) and its applications
- g. Volume integrals; Divergence theorem of Gauss (without proof) and its applications

3. Laplace Transform(8 hours)

- a. Definitions and properties of Laplace Transform
- b. Derivations of basic formulae of Laplace Transform
- c. Inverse Laplace Transform: Definition and standard formulae of inverse Laplace Transform
- d. Theorems on Laplace transform and its inverse
- e. Convolution and related problems
- f. Applications of Laplace Transform to ordinary differential equations

4. Fourier Series(5 hours)

- a. Fourier Series
- b. Periodic functions
- c. Odd and even functions
- d. Fourier series for arbitrary range
- e. Half range Fourier series

5. Linear Programming(9 hours)

- a. System of Linear Inequalities in two variables
- b. Linear Programming in two dimensions: A Geometrical Approach
- c. A Geometric introduction to the Simplex method
- d. The Simplex method: Maximization with Problem constraints of the form " \leq "
- e. The Dual: Maximization with Problem Constraints of the form " \geq "
- f. Maximization and Minimization with mixed Constraints. The two-phase method (An alternative to the Big M Method)

References:

- 1. E. Kreszig, "Advance Engineering Mathematics", Willey, New York.
- 2. M.M Gutterman and Z.N.Nitecki, "Differential Equation, a First Course", 2nd Edition, saunders, New York.

Evaluation Scheme:

The questions will cover all the chapters of the syllabus. The evaluation scheme will be as indicated in the table below:

| Chapters | Hours | Marks distribution* |
|----------|-------|---------------------|
| 1 | 11 | 20 |
| 2 | 12 | 20 |
| 3 | 8 | 15 |
| 4 | 5 | 10 |
| 5 | 9 | 15 |
| Total | 45 | 80 |

***Note: There may be minor deviation in marks distribution.**