# **Numerical Methods**

Year: III Semester: II

Teaching Hours/week				Examination Scheme						Total Marks
	Hours	Hours/week		Internal		Final				
			Theory	Practical	Theory		Practical			
Cr	L	T	P	100		Duration	Marks	Duration	Marks	
3	3	2	2	40	25	3	60			125

## Course Objective:

After completion of this course, the students will be able to solve the engineering problems by using the theory of numerical Computational procedures

### **Course Content:**

- 1. Introduction (3 hrs)
  - 1.1. Introduction and Importance of Numerical Method
  - 1.2. Approximation and Errors in computation
  - 1.3. Uses and Importance of Computer programming in Numerical Methods
  - 1.4. Application of Numerical Computing in Civil Engineering
- 2. Solution of non Linear equation

(8 hrs)

- 2.1. Iterative methods and stopping criteria
- 2.2. Bisection method & its Convergence
- 2.3. Newton- Raphson method and its convergence
- 2.4. Secant method and its convergence
- 2.5. Fixed Point method
- 2.6. Evaluation of polynomials using Horner's Rule
- **3.** Curve Fitting

(8 hrs)

- 3.1 Interpolation
  - 3.1.1 Linear interpolation
  - 3.1.2 Lagrange interpolation
  - 3.1.3 Newton's Gregory Forward and Backward interpolation
  - 3.1.4 Newton's Divided Difference interpolation
  - 3.1.5 Central Interpolation (Gauss Forward/ Backward Formulae)
- 3.2. Regression
  - 3.2.1 Least Squares Regression
  - 3.2.2 Fitting Transcendental Equations.
  - 3.2.3 Fitting a polynomial function
- 3.3. Spline Interpolation (Cubic Spline)
- 4. Numerical Differentiation & Integration

(7 hrs)

- 4.1 Differentiating continuous function
  - 4.1.1 Forward Difference Quotient
  - 4.1.2 Backward Difference Quotient
  - 4.1.3 Central Difference quotient

- 4.2 Newton cotes methods of integration
  4.2.1 Trapezoidal rule and composite trapezoidal rule
  4.2.2 Simpson's 1/3 rule & its composite
  - 4.2.3 Simpson's 3/8 rule.
- 4.3 Romberg integration
- 4.4 Gaussian integration (Gaussian Legendre 2 point and 3 point Formula)
- 5. Linear Algebraic Equations

(8 hrs)

- 5.1 Elimination Approach
  - 5.1.1 Basic Gauss Elimination
  - 5.1.2 Gauss Elimination with partial pivoting
  - 5.1.3 Gauss Jordon method
  - 5.1.4 Finding inverse matrix using Gauss Jordan Method
  - 5.1.5 LU decomposition methods
    - 5.1.5.1 Do Little Method
    - 5.1.5.2 Crout's Method
- 5.2 Iterative method
  - 5.2.1 Jacobi method
  - 5.2.2 Gauss-Seidal method
- 5.3 Eigen values and Eigen vectors using power method
- 6. Solution of ordinary differential equations

(7 hrs)

- 6.1 Euler's method
- 6.2 Heun's method
- 6.3 Fourth order Runge-Kutta method
- 6.4 Systems of differential equations using Heun's method
- 6.5 2nd order differential equations using Heun's method
- 7. Solutions of partial differential equations

(4 hrs)

- 7.1 Elliptic equations
  - 7.1.1 Laplace's equations (standard five point formula with iterative method)
  - 7.1.2 Poisson's equations (finite difference formula with iterative method))
- 7.2 Parabolic Equations (Solution of heat equation by Bender –Schmidt recurrence method)
- 7.3 Hyperbolic Equations (Solution of wave equation by finite difference method)

### Laboratories:

- 1. Bisection method, N-R method
- 2. Secant method & Horner's rule
- 3. Lagrange interpolation
- 4. Linear Regression
- 5. Basic Gauss elimination method
- 6. Finding inverse matrix using Gauss Jordan
- 7. Trapezoidal rule ,Simpson's 1/3 rule, Simpson's 3/8 rule
- 8. Solution of differential equation using Euler's, Heun's and R-K method

#### References

- 1. E. Balagurusamy "Numerical Methods" Tatal Mc Graw Hill
- Dr. B.S. Grewal, "Numerical Methods in Engineering and Science", Khanna Publication
- 3. S.Yakwitz and F. szidarouszky "An Introduction to Numerical Computations" 2nd Edition Macmillan Publishing co, New York
- 4. C.F Gerald and P.o. Wheatley "Applied Numerical Analysis",4th Edition, Addipon wesley publishing co. New york.

**Evaluation Scheme: Marks Division** 

Question Type	No. of Questions	Marks	Total Marks
Group A	6	4	24
Group B	6	6	36
Total			60

<sup>\*</sup>Latest edition will be preferable.