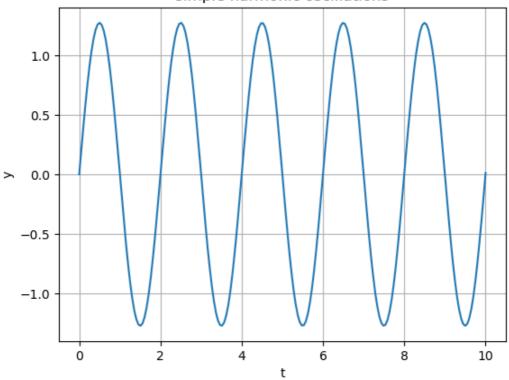
## **Simple Harmonic Oscillations (SKP)**

$$y'' + \omega^2 y = 0$$

```
In [1]: import numpy as np
         import matplotlib.pyplot as plt
         import scipy as sp
         from scipy.integrate import odeint
         from scipy.integrate import solve_ivp
         T = 2 # time period of oscillations
         w = 2*np.pi/T
         # Write the differential equation. (x=t,dy/dx=yp)
         def dSdx(x,S):
             y, yp = S
             return [yp, -w**2*y]
         def dydx(x,y,yp):
             return yp
         def dypdx(x,y,yp):
             return -w**2*y
         x_0, y_0, yp_0 = 0, 0, 4 # initial conditions
         x_min, x_max = x_0, 10 # lower and upper limit of x dx = (x_max-x_0)/1000 # infinitesimal length
```

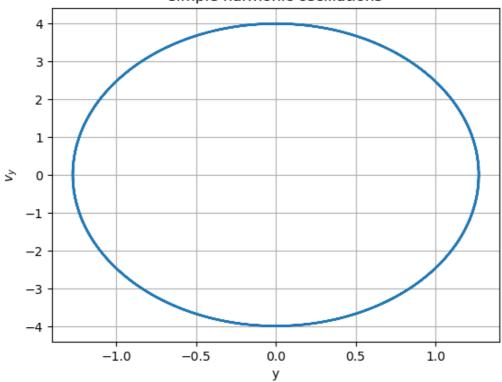
```
In [2]: # Using solve_ivp
y0, yp0 = y_0, yp_0
S0 = (y0,yp0)
x = np.linspace(x_min, x_max,200)
sol = solve_ivp(dSdx, t_span=(min(x), max(x)), y0=S0, t_eval=x)
y1 = sol.y[0]
plt.plot(x,y1)
plt.xlabel('t')
plt.ylabel('y')
plt.title('simple harmonic oscillations')
plt.grid()
plt.show()
```

## simple harmonic oscillations



```
In [3]: # Using solve_ivp
    y0, yp0 = y_0, yp_0
    S0 = (y0,yp0)
    x = np.linspace(x_min, x_max,200)
    sol = solve_ivp(dSdx, t_span=(min(x), max(x)), y0=S0, t_eval=x)
    y1 = sol.y[0]
    yp1 = sol.y[1]
    plt.plot(y1,yp1)
    plt.xlabel('y')
    plt.ylabel('$v_y$')
    plt.title('simple harmonic oscillations')
    plt.grid()
    plt.show()
```

## simple harmonic oscillations



```
# ALL IN ONE
# Using odeint
y0, yp0 = y_0, yp_0
S0 = (y0, yp0)
x = np.linspace(x min, x max, 200)
sol = odeint(dSdx, y0=S0, t=x, tfirst=True)
y1 = sol.T[0]
plt.plot(x,y1, '--', label='Using odeint')
# Using solve_ivp
y0, yp0 = y_0, yp_0
S0 = (y0, yp0)
x = np.linspace(x_min, x_max, 200)
sol = solve_ivp(dSdx, t_span=(min(x), max(x)), y0=S0, t_eval=x)
y1 = sol.y[0]
plt.plot(x,y1, '--', label='Using solve_ivp')
# Euler's Method
x, y, yp = x_0, y_0, yp_0
xmax = x_max
h = dx
xx, yy, yyp = [], [], []
while abs(x) < abs(xmax):
    xx.append(x)
    yy.append(y)
```

```
yyp.append(yp)
   x += h
   y += h*dydx(x,y,yp)
   yp += h*dypdx(x,y,yp)
plt.plot(xx,yy, '--', label='Euler\'s Method')
# Modified Euler's Method
x, y, yp = x_0, y_0, yp_0
xmax = x_max
h = dx
xx, yy, yyp = [], [], []
while abs(x) < abs(xmax):
   xx.append(x)
   yy.append(y)
   yyp.append(yp)
   x += h
   dy = (h/2)*(dydx(x,y,yp) + dydx(x + h, y + h*dydx(x,y,yp), yp +
h*dypdx(x,y,yp)))
    dyp = (h/2)*(dypdx(x,y,yp) + dypdx(x + h, y + h*dydx(x,y,yp), yp +
h*dypdx(x,y,yp)))
   y += dy
   yp += dyp
plt.plot(xx,yy, '--', label='Modified Euler\'s Method')
# Runge - Kutta Method
x, y, yp = x_0, y_0, yp_0
xmax = x_max
h = dx
xx, yy, yyp = [], [], []
while abs(x) < abs(xmax):
   xx.append(x), yy.append(y), yyp.append(yp)
   x += h
   k1 = h * dydx(x,y,yp)
   11 = h * dypdx(x,y, yp)
    k2 = h * dydx(x + (h/2), y + (k1/2), yp + (l1/2))
   12 = h * dypdx(x + (h/2), y + (k1/2), yp + (11/2))
   k3 = h * dydx(x * (h/2), y + (k2/2), yp + (12/2))
   13 = h * dypdx(x + (h/2), y + (k2/2), yp + (12/2))
    k4 = h * dydx(x + h, y + k3, yp + 13)
    14 = h * dypdx(x + h, y + k3, yp + 13)
   y += (1/6)*(k1 + 2*(k2 + k3) + k4)
   yp += (1/6)*(11 + 2*(12 + 13) + 14)
plt.plot(xx,yy, '--', label='Runge - Kutta Method')
plt.xlabel('t')
plt.ylabel('y')
plt.title('simple harmonic oscillations')
plt.legend()
plt.grid()
plt.show()
```