

29.13.implement_SGD_v3.0

August 6, 2018

1 Implement SGD on boston dataset

Dataset from sklearn load_boston

The GD is $\theta = \theta - \alpha \frac{d}{d\theta} \text{cost function}$ $\text{equ} = y = wtx + b$; $\text{cost} = (y - wtx - b)^2$ determinant wrt $w \Rightarrow -2(y - wtx - b)x$ determinant wrt $b \Rightarrow -2(y - wtx - b)$; in general : loss These are in vec notation

$h = \text{np.dot}(x, \theta)$; $\text{loss} = h - y$; $\text{cost} = \text{np.sum}(\text{loss}^2) / (2m)$; $\text{gradient} = \text{np.dot}(x^T, \text{loss}) / m$; $\theta = \theta - \alpha \text{gradient}$

2 Objective

Implement the model and compare the intercept and weights with sklearn

3 Import data and libraries and split train and test by 80:20

```
In [31]: from sklearn.datasets import load_boston
import numpy as np
import matplotlib.pyplot as plt

boston = load_boston()
print(boston.data.shape)
boston.data[0:1]

y=np.array(boston.target)
x=np.array(boston.data)
from sklearn.preprocessing import normalize, StandardScaler
#x = normalize(x, norm='l1', axis=0)
#y = normalize(y.reshape(-1, 1), norm='l1', axis=0)
#y=y.ravel()
for i in range(len(x[1,:])):
    x[:,i] = ( (x[:,i] - np.min(x[:,i])) / (np.max(x[:,i]) - np.min(x[:,i])) ) )

x_train=x[0:450]
x_test=x[451:505]
y_train=y[0:450]
y_test=y[451:505]
```

(506, 13)

4 Create my model and cost function to calculate cost

```
In [32]: def getWeights(x):
    lenWeights = len(x[1,:]);
    weights = np.random.rand(lenWeights)
    bias = np.random.random();
    return weights,bias

def train(x,y,weights,bias,maxIter):
    converged = False;
    iterations = 1;
    m = len(x);
    alpha = 0.0001;

    while not converged:
        for i in range(len(x)):
            #idx=np.random.randint(m,size=200)
            htheta = np.dot(x[i,:], weights) + bias;
            # Calculate gradient
            error = htheta - y[i];
            grad = (alpha) * ( error * x[i,:] );
            # Update weights and bias
            weights = weights - grad;
            bias = bias - alpha * error;
            iterations = iterations + 1;
            #alpha=alpha/pow(iterations,.25)

            if iterations > maxIter:
                converged = True;
                break

    return weights.transpose(), bias

def predict(x, weights, bias):
    return np.dot(x,weights) + bias
```

5 Use my model on boston data

```
In [33]: import warnings
    warnings.filterwarnings('ignore')

    initialWeights,initialBias = getWeights(x_train);
    weights,bias = train(x_train,y_train,initialWeights,initialBias,50000);
```

```

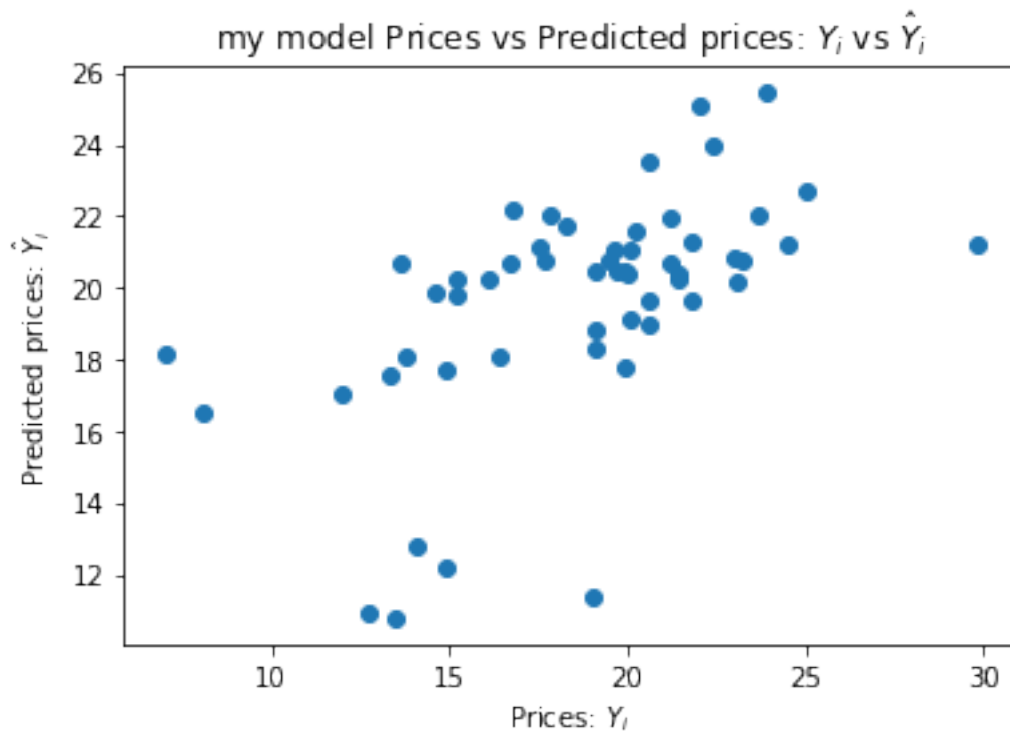
y_pred_test = predict(x_test, weights,bias);
MSE_test1 = .5*np.mean((y_pred_test - y_test)**2);
y_pred_train = predict(x_train, weights,bias);
MSE_train= .5*np.mean((y_pred_train - y_train)**2);
#   sklearnModel = LinearRegression();
#   sklearnModel = sklearnModel.fit(x_train,y_train);
#   sklearnModel1 = sklearnModel.predict(x_test);

#   skMSE = .5*np.mean((sklearnModel1 - y_test)**2);

#print ("Sklearn MSE: " + str(skMSE))
#print("Sklearn coefficient",sklearnModel.intercept_,sklearnModel.coef_)
import pandas as pd
aa=pd.DataFrame({'type':['MyModel'],'train_cost':[MSE_train],'test_cost':[MSE_test1]},

plt.scatter(y_test, y_pred_test)
plt.xlabel("Prices:  $Y_i$ ")
plt.ylabel("Predicted prices:  $\hat{Y}_i$ ")
plt.title("my model Prices vs Predicted prices:  $Y_i$  vs  $\hat{Y}_i$ ")
plt.show()

```



6 Use SGDREGRESSOR model on boston data

```
In [34]: import warnings
         warnings.filterwarnings('ignore')

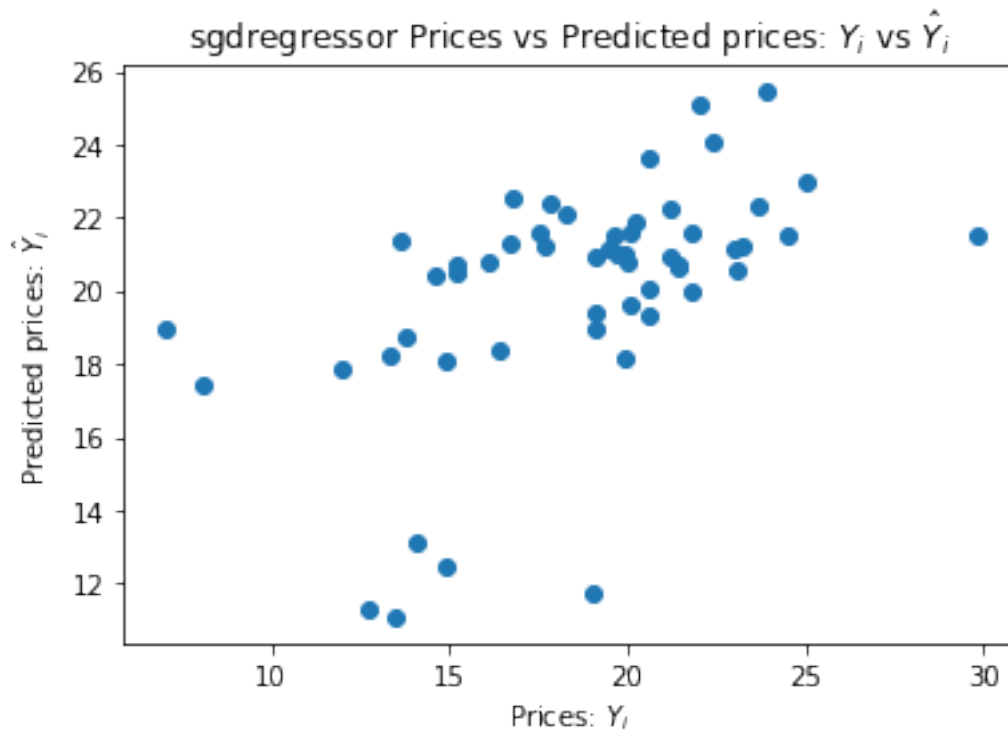
         # Use sklearn
         import pandas as pd
         from sklearn.linear_model import SGDRegressor
         lm = SGDRegressor(fit_intercept=True)
         lm.fit(x_train, y_train)
         #y_pred = lm.predict(x_test)
         y_pred_test = lm.predict(x_test);
         MSE_test = .5*np.mean((y_pred_test - y_test)**2);
         y_pred_train = lm.predict(x_train);
         MSE_train= .5*np.mean((y_pred_train - y_train)**2);

         bb=pd.DataFrame({'type': ['GSDRegressor'], 'train_cost': [MSE_train], 'test_cost': [MSE_test]})

         aa=aa.append(bb)

         plt.scatter(y_test, y_pred_test)
         plt.xlabel("Prices:  $Y_i$ ")
         plt.ylabel("Predicted prices:  $\hat{Y}_i$ ")
         plt.title("sgdregressor Prices vs Predicted prices:  $Y_i$  vs  $\hat{Y}_i$ ")
         plt.show()

         print(aa)
```



	Bias	Coeff \
0	8.71079	[-0.695195996803, 4.4958842513, -0.33813337578...
0	[8.71412791204]	[-0.927339319554, 3.46322494887, -0.6315953976...

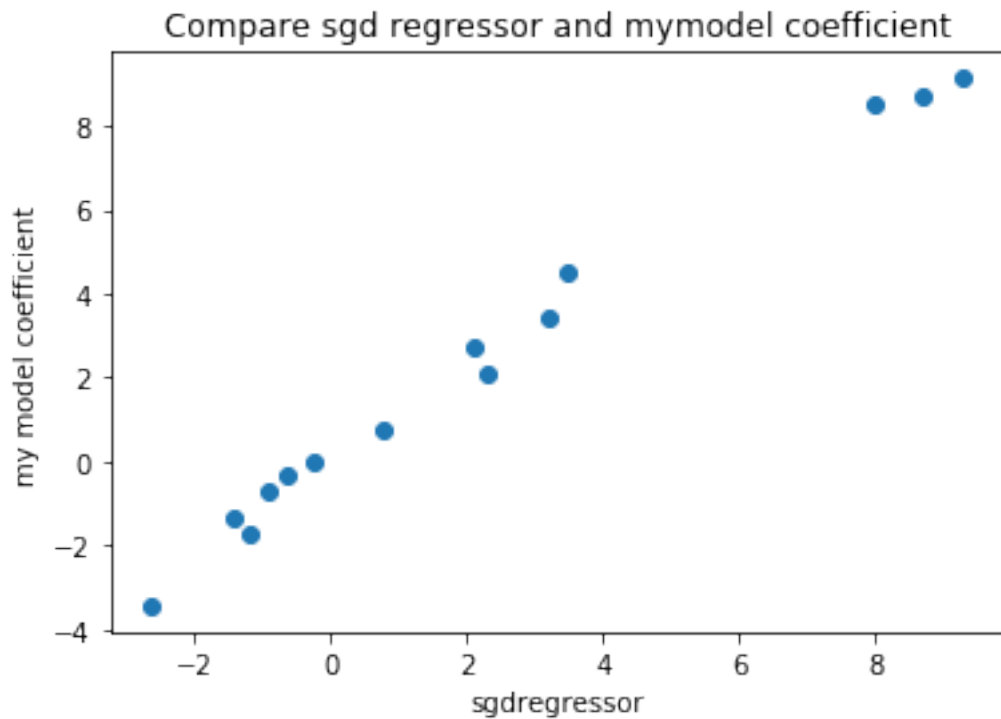
	test_cost	train_cost	type
0	6.91357	27.323244	MyModel
0	7.76666	28.759085	GSDRegressor

7 Score comparison of mymodel and SGDRegressor

```
In [35]: #print('sklearn coef',lm.intercept_,lm.coef_)
         #print('mymodel theta including intercept',newtheta[0],newtheta[1:])
         x1=lm.intercept_.tolist()
         x2=lm.coef_.tolist()
         x1.extend(x2)
         y1=[bias]
         y2=weights.tolist()
         print(type(y1),type(y2))
         y1.extend(y2)
         #y=newtheta.tolist()
         import matplotlib.pyplot as plt
```

```
plt.title("Compare sgd regressor and mymodel coefficient")
plt.xlabel("sgdregressor")
plt.ylabel("my model coefficient")
plt.scatter(np.array(x1),np.array(y1))
plt.show()
```

```
<class 'list'> <class 'list'>
```



8 Observation

1. While trying learning rate of different value sometimes cost is going towards very high value, so tried with higher value
2. After trying more iteration cost is going down with a very small alpha value
3. SGD model is performing quite similar to mymodel
4. Best cost is achieved by different trial cost function
5. Comparison of 2 models

```
In [36]: print(aa)
print ("SGD MSE test: " + str(MSE_test))
print('coefficient of SGD model',lm.intercept_,lm.coef_)

print ("This Model MSE test: " + str(MSE_test1))
print("This model coefficient",bias,weights)
```

```

Bias
0      8.71079 [-0.695195996803, 4.4958842513, -0.33813337578...
0 [8.71412791204] [-0.927339319554, 3.46322494887, -0.6315953976...

test_cost train_cost type
0 6.91357 27.323244 MyModel
0 7.76666 28.759085 GSDRegressor
SGD MSE test: 7.76666041996
coefficient of SGD model [ 8.71412791] [-0.92733932 3.46322495 -0.6315954 2.11319592 -0.254
2.29493099 3.20762966 -1.42943032 -1.17873142 0.78229255 9.29748712
-2.62239983]
This Model MSE test: 6.91357023558
This model coefficient 8.71078644939 [-0.695196 4.49588425 -0.33813338 2.74721491 -0.03185
2.08880604 3.43583274 -1.3375841 -1.72995185 0.7448961 9.11831041
-3.41859194]

```