Query Language

- A query language is a language in which a user requests information from the database.
- Query languages can be categorized as either procedural or nonprocedural.
- In a procedural language, the user instructs the system to perform a sequence of operations on the database to compute the desired result. For example, relational algebra.
- In a nonprocedural language, the user describes the desired information without giving a specific procedure for obtaining that information. For example, tuple relational calculus and domain relational calculus.
- Most commercial relational database systems offer a query language that includes elements of both procedural and nonprocedural approaches.
- Example: SQL (Structured Query Language).

Relational Algebra

- It is a procedural query language
- It consists of a set of operations that take one or two relations as input and produce a new relation as their result. The six fundamental operations are:
 - select
 - project
 - union
 - set difference
 - Cartesian product
 - rename
- The select, project, and rename operations are called unary operators, because they operate on one relation. The remaining three operations are called binary operations, because they operate on pairs of relations.

Consider the following Relational Database

Here, we use the following relational database to illustrate the operations of relational algebra.

branch (branch-name, branch-city, assets)

customer (customer-name, customer-street, customer-city)

account (account-number, branch-name, balance)

Ioan (Ioan-number, branch-name, amount)

depositor (customer-name, account-number)

borrower (customer-name, loan-number)



• Relation *r*

Α	В	С	D
α	α	1	7
α	β	5	7
β	β	12	3
β	β	23	10

• $\sigma_{A=B \land D > 5}(r)$

Α	В	С	D
α	α	1	7
β	β	23	10

Select Operation

- Notation: $\sigma_p(r)$
- p is called the selection predicate
- Defined as:

$$\sigma_p(\mathbf{r}) = \{t \mid t \in r \text{ and } p(t)\}$$

Where p is a formula in propositional calculus consisting of terms connected by : \land (and), \lor (or), \neg (not) Each term is one of:

<attribute> op <attribute> or <constant>

where *op* is one of: =, \neq , >, \geq < \leq

Examples of selection: To select those tuples of the *loan* relation where the branch is "Perryridge", we write

We can find all tuples of the *loan* relation in which the amount lent is more than \$1200 by writing

$$\sigma_{amount > 1200}$$
 (loan)

Select Operation

To find those tuples pertaining to *loans* of more than \$1200 made by the "Perryridge" branch, we write

```
σ branch-name = "Perryridge" \ amount>1200 (loan)
```

To find all customers who have the same name as their loan officer, we can write

```
\sigma_{customer-name = banker-name} (loan-officer)
```

Project Operation – Example

Relation *r*:

Α	В	С
α	10	1
α	20	1
β	30	1
β	40	2

■ Π_{A,C} (*r*)

Α	С		Α	С
α	1		α	1
α	1	=	β	1
β	1		β	2
β	2			

Project Operation

Notation:

$$\prod_{A_1, A_2, \ldots, A_k} (r)$$

where $A_1,...,A_k$ are attribute names and r is a relation name.

- The result is defined as the relation of k columns obtained by erasing the columns that are not listed
- Duplicate rows are removed from result, since relations are sets
- E.g. To eliminate the *branch-name* attribute of *loan* $\Pi_{loan-number, amount}$ (loan)

Union Operation – Example

■ Relations *r*, *s*:

Α	В		
α	1		
α	2		
β	1		
r			

Α	В		
α	2		
β	3		
S			

 $r \cup s$:

Union Operation

- Notation: $r \cup s$
- Defined as:

$$r \cup s = \{t \mid t \in r \text{ or } t \in s\}$$

- For $r \cup s$ to be valid.
 - 1. r, s must have the same arity (same number of attributes)
 - 2. The attribute domains must be *compatible* (e.g., 2nd column of *r* deals with the same type of values as does the 2nd column of *s*)
- E.g. to find the name of all customers with either an account or a loan

$$\Pi_{customer-name}$$
 (depositor) $\cup \Pi_{customer-name}$ (borrower)

Set Difference Operation – Example

Relations *r*, *s*:

Α	В		
α	1		
α	2		
β	1		
r			

Α	В		
α	2		
β	3		
S			

r − *s*:

Set Difference Operation

- Notation r-s
- Defined as:

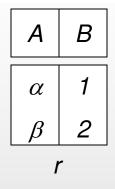
$$r-s = \{t \mid t \in r \text{ and } t \notin s\}$$

- Set differences must be taken between compatible relations.
 - r and s must have the same arity
 - P attribute domains of r and s must be compatible
- For example, we can find the name of all customers of a bank who have an account but not loan by writing

$$\prod_{customer-name}$$
 (depositor) - $\prod_{customer-name}$ (borrower)

Cartesian-Product Operation-Example

Relations *r, s*:



С	D	Ε	
$\begin{bmatrix} \alpha \\ \beta \\ \beta \\ \gamma \end{bmatrix}$	10 10 20 10	a a b b	
S			

rxs:

A	В	С	D	Ε
α	1	α	10	а
α	1	β	10	a
α	1	β	20	b
α	1	γ	10	b
β	2	α	10	a
β	2	β	10	a
β	2	β	20	b
β	2	γ	10	b

Cartesian-Product Operation

- Notation r x s
- Defined as:

$$r \times s = \{t \mid q \mid t \in r \text{ and } q \in s\}$$

- Assume that attributes of r(R) and s(S) are disjoint. (That is, $R \cap S = \emptyset$).
- If attributes of r(R) and s(S) are not disjoint, then renaming must be used.
- For example, suppose that we want to find the names of all customers who have a loan at the "Perryridge" branch. We need the information in both the *loan* and *borrower* relation to do so. For this we can write

```
\sigma_{branch-name = "Perryridge"}(borrower \times loan)
```

The *customer-name* column may contain customers who do not have a loan at the "Perryridge" branch. If a customer has a loan in the "Perryridge" branch, then there is some tuple in *borrower* × *loan* that contains this name and *borrower.loan-number* = *loan.loan-number*. So, if we write,



```
\sigma_{borrower.loan-number = loan.loan-number}(\sigma_{branch-name = "Perryridge"}(borrower \times loan))
```

We can get only those tuples of *borrower×loan* that pertain to customers who have a loan at the "Perryridge" branch.

Finally, since we want only *customer-name*, we do a projection

```
\Pi_{\text{customer-name}} (\sigma_{\textit{borrower.loan-number}} = \textit{loan.loan-number} (\sigma_{\textit{branch-name}} = \textit{"Perryridge"} (\textit{borrower} \times \textit{loan})))
```

Alternatively, we can also write

```
\begin{split} &\Pi_{customer-name}(\sigma_{loan.loan-number = borrower.loan-number}(\\ &(\sigma_{branch-name = "Perryridge"}(loan)) \ x \ borrower)) \end{split}
```

Composition of Operations

 Relational-algebra operations can be composed together into a relational-algebra expression.

Example: $\sigma_{A=C}(r \times s)$

 \blacksquare rxs

	Α	В	С	D	Ε
Γ	α	1	α	10	а
	α	1	β	10	а
	α	1	β	20	b
	α	1	γ	10	b
	β	2	α	10	а
	β	2	β	10	а
	β	2	β	20	b
	β	2	γ	10	b

 \bullet $\sigma_{A=C}(r \times s)$

A	В	С	D	Ε
α	1	α	10	а
$\mid \beta \mid$	2	β	20	a
β	2	β	20	b

Composition of Operations

For example, to find the name of those customers who live in "Harrison" city, we write

 $\Pi_{\text{customer-name}} \left(\sigma_{\text{customer-city}} = \text{"Harrison"} \left(\text{Customer} \right) \right)$

Rename Operation

- Allows us to name, and therefore to refer to, the results of relational-algebra expressions.
- Allows us to refer to a relation by more than one name.
 Example:

$$\rho_X(E)$$

returns the expression E under the name XIf a relational-algebra expression E has arity n, then

$$\rho_{X (A1, A2, ..., An)}(E)$$

returns the result of expression E under the name X, and with the attributes renamed to A1, A2, ..., An.

Rename Operation

For example, to find the largest account balance, we write

 $\Pi_{balance}(account) - \Pi_{account.balance}$ $(\sigma_{account.balance} < d.balance (account x \rho_d (account)))$ To find the names of all customers who live on the same street and in the same city as Smith, we write

 $\Pi_{customer.customer-name}(\sigma_{customer.customer-street} = smith-addr.street ^ customer.customer-city = smith-addr.city (Customer x <math>\rho_{smith-addr(street,city)} (\Pi_{customer-street, customer-city} (\sigma_{customer-name} = "Smith" (Customer)))))$

Formal Definition of Relational Algebra

- A basic expression in the relational algebra consists of either one of the following:
 - A relation in the database
 - A constant relation; that is by listing its tuples within { }, for example { (A-101, Downtown, 500), (A-215, Mianus, 700) }
- Let E_1 and E_2 be relational-algebra expressions; the following are all relational-algebra expressions:
 - $P E_1 \cup E_2$
 - $P = E_1 E_2$
 - $P E_1 \times E_2$
 - $P = \sigma_p(E_1)$, P is a predicate on attributes in E_1
 - \cap $\prod_s(E_1)$, S is a list consisting of some of the attributes in E_1
 - $\rho_x(E_1)$, x is the new name for the result of E_1



Additional Operations

We define additional operations that do not add any power to the relational algebra, but that simplify common queries.

- Set intersection
- Natural join
- Division
- Assignment

Set-Intersection Operation - Example

Relation r, s:

Α	В
$\begin{bmatrix} \alpha \\ \alpha \\ \beta \end{bmatrix}$	1 2 1

A B 2 β 3

r

 $r \cap s$

A B α 2

S

Set-Intersection Operation

- Notation: $r \cap s$
- Defined as:
- $r \cap s = \{ t \mid t \in r \text{ and } t \in s \}$
- Assume:
 - r, s have the same arity
 - attributes of r and s are compatible
- Note: $r \cap s = r (r s)$
- For example, to find the name of all customers who have both a loan and an account, we can write

$$\Pi_{\text{customer-name}}$$
 (borrower) $\cap \Pi_{\text{customer-name}}$ (depositor)

Natural-Join Operation

- The natural join is a binary operation that allows us to combine certain selections and a Cartesian product into one operation. It performs Cartesian product and a selection forcing equality on those attributes that appear in both relation schemas, and finally removes duplicate attributes.
- For example, to find the names of all customers who have a loan at the bank, along with the loan number and the loan amount, we can use Cartesian product as follows:

 $\Pi_{customer-name, loan.loan-number, amount}(\sigma_{borrower.loan-number} = loan.loan-number(borrower x loan))$

but we can express the above query by using natural join as follows:

 $\prod_{customer-name, loan-number, amount}(borrower \bowtie loan)$

Note: $r \bowtie s = r \times s$ if $R \cap S = \phi$

Natural-Join Operation

- Notation: r ⋈ s
- Let r and s be relations on schemas R and S respectively. Then, $r \bowtie s$ is a relation on schema $R \cup S$ obtained as follows:
 - Property Consider each pair of tuples t_r from r and t_s from s.
 - If t_r and t_s have the same value on each of the attributes in $R \cap S$, add a tuple t to the result, where

 - \blacksquare t has the same value as t_S on s
- Example:

$$R = (A, B, C, D)$$

$$S = (E, B, D)$$

- Result schema = (A, B, C, D, E)
- $r \bowtie s$ is defined as:

$$\prod_{r.A, r.B, r.C, r.D, s.E} (\sigma_{r.B = s.B} \land r.D = s.D (r \times s))$$



Natural Join Operation – Example

Relations r, s:

Α	В	С	D
α	1	α	а
β	2	γ	а
γ	4	β	b
α	1	γ	а
δ	2	β	b
r			

В	D	E
1 3 1 2 3	a a a b b	$\begin{array}{c} \alpha \\ \beta \\ \gamma \\ \delta \\ \in \end{array}$
S		

 $r \bowtie s$

A	В	С	D	Ε
α	1	α	а	α
α	1	α	а	γ
α	1	γ	а	α
α	1	γ	а	γ
δ	2	β	b	δ

Other Examples

To find the names of all branches with customers who have an account in the bank and who live in Harrison, we write

 $\Pi_{branch-name}(\sigma_{customer-city} = "Harrison" (customer \bowtie account \bowtie depositor)$

To find all customers who have both a loan and an account at the bank, we write

 $\Pi_{customer-name}(borrower \bowtie depositor)$

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Division Operation

$$r \div s$$

- Suited to queries that include the phrase "for all".
- Let r and s be relations on schemas R and S respectively where

$$P = (A_1, ..., A_m, B_1, ..., B_n)$$

$$P = (B_1, ..., B_n)$$

The result of $r \div s$ is a relation on schema

$$R - S = (A_1, ..., A_m)$$

$$r \div s = \{ t \mid t \in \prod_{B \in S}(r) \land \forall u \in s (tu \in r) \}$$



Division Operation – Example

Relations *r, s*:

α	1
α	2
α	3
β	1
γ	1
δ	1
δ	3
δ	4
\in	6
\in	1
β	2

В

S

r ÷ *s*:

Α

 α

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Another Division Example

Relations *r, s*:

Α	В	С	D	Ε
α	а	α	а	1
α	а	γ	а	1
α	а	γ	b	1
β	а	γ	а	1
eta eta eta eta eta eta	а	γ	b	3
γ	а	γ	а	1
γ	а	γ	b	1
γ	а	β	b	1

D E
a 1
b 1

r ÷ *s*:

Α	В	С
α	а	γ
γ	а	γ

Division Operation (Cont.)

For example, to find the name of all customers who have an account at all branches located in Brooklyn, we write

$$\Pi_{customer-name, branch-name}$$
 (depositor \bowtie account) $\div \Pi_{branch-name}$ ($\sigma_{branch-city} = \text{``Brooklyn''}$ (branch))

Assignment Operation

- The assignment operation (←) provides a convenient way to express complex queries.
 - Write query as a sequential program consisting of
 - a series of assignments
 - followed by an expression whose value is displayed as a result of the query.
 - Assignment must always be made to a temporary relation variable.
- **Example:** Write $r \div s$ as

$$temp1 \leftarrow \prod_{R-S}(r)$$

 $temp2 \leftarrow \prod_{R-S}((temp1 \times s) - \prod_{R-S,S}(r))$
 $result = temp1 - temp2$

- The result to the right of the \leftarrow is assigned to the relation variable on the left of the \leftarrow .
- May use variable in subsequent expressions.

Extended Relational-Algebra-Operations

- Generalized Projection
- Aggregate Functions
- Outer Join

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Generalized Projection

Extends the projection operation by allowing arithmetic functions to be used in the projection list.

$$\prod_{\mathsf{F1},\mathsf{F2},\ldots,\mathsf{Fn}}(E)$$

- E is any relational-algebra expression
- Each of F_1 , F_2 , ..., F_n are arithmetic expressions involving constants and attributes in the schema of E.
- For example, given relation credit-info(customer-name, limit, credit-balance), find how much more each person can spend:

 $\Pi_{customer-name, \ limit-credit-balance}$ (credit-info)

The attribute resulting from the expression *limit - credit-balance* does not have a name and we can give it name as follows:

 $\Pi_{customer-name, \ limit-credit-balance}$ as credit-available (credit-info)

Aggregate Functions and Operations

Aggregation function takes a collection of values and returns a single value as a result.

avg: average value

min: minimum value

max: maximum value

sum: sum of values

count: number of values

Aggregate operation in relational algebra

$$g_{1, G2, ..., Gn} g_{F1(A1), F2(A2), ..., Fn(An)}(E)$$

- E is any relational-algebra expression
- $G_1, G_2, ..., G_n$ is a list of attributes on which to group (can be empty)
- Fach F_i is an aggregate function
- P Each A_i is an attribute name



Aggregate Operation – Example

Relation *r*:

Α	В	С
α	α	7
α	β	7
β	β	3
β	β	10

 $g_{\text{sum}(C)}^{(r)}$

sum-C

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Aggregate Operation – Example

Relation account grouped by branch-name:

branch-name	account-number	balance
Perryridge	A-102	400
Perryridge	A-201	900
Brighton	A-217	750
Brighton	A-215	750
Redwood	A-222	700

branch-name $g_{sum(balance)}$ (account)

branch-name	balance	
Perryridge	1300	
Brighton	1500	
Redwood	700	

Aggregate Functions (Cont.)

- Result of aggregation does not have a name
 - Can use rename operation to give it a name
 - For convenience, we permit renaming as part of aggregate operation

branch-name $g_{sum(balance)}$ as sum-balance, max(balance) as max-balance (account)

■ There are cases where we must eliminate multiple occurrences of a value before computing an aggregate function. For this, we use the function name with the addition of the hyphenated string "distinct" appended to the end of the function name (for example, count-distinct). For example, to find the number of branches appearing in the *pt-works* relation, we write

9 count-distinct(branch-name)(pt-works)

Outer Join

- An extension of the natural join operation that avoids loss of information.
- Computes the natural join and then adds tuples form one relation that does not match tuples in the other relation to the result of the natural join.
- Uses null values; null signifies that the value is unknown or does not exist
- There are three forms of outer join: left outer join, right outer join and full outer join.
- The *left outer join* takes all tuples in the left relation that did not match with any tuple in the right relation, pads the tuples with null values for all other attributes from the right relation and adds them to the result of the natural join.
- Similarly, right outer join takes all tuples in the right relation that did not match with any tuple in the left relation, pads the tuples with null values for all other attributes from the left relation and adds them to the result of the natural join.
- The full outer join does both of the left outer join and right outer join operations.

Outer Join – Example

Relation loan

loan-number	branch-name	amount
L-170	Downtown	3000
L-230	Redwood	4000
L-260	Perryridge	1700

Relation borrower

customer-name	loan-number	
Jones	L-170	
Smith	L-230	
Hayes	L-155	

Outer Join – Example

Inner Join

loan ⋈ *Borrower*

loan-number	branch-name	amount	customer-name
L-170	Downtown	3000	Jones
L-230	Redwood	4000	Smith

■ Left Outer Join

Ioan Morrower

loan-number	branch-name	amount	customer-name
L-170	Downtown	3000	Jones
L-230	Redwood	4000	Smith
L-260	Perryridge	1700	null

Outer Join – Example

Right Outer Join

loan ⋈ borrower

loan-number	branch-name	amount	customer-name
L-170	Downtown	3000	Jones
L-230	Redwood	4000	Smith
L-155	null	null	Hayes

■ Full Outer Join

loan ⇒ *borrower*

loan-number	branch-name	amount	customer-name
L-170	Downtown	3000	Jones
L-230	Redwood	4000	Smith
L-260	Perryridge	1700	null
L-155	null	null	Hayes



Modification of the Database

- The content of the database may be modified using the following operations:
 - Deletion
 - Insertion
 - Updating
- All these operations are expressed using the assignment operator.

Deletion

- A delete request is expressed similarly to a query, except instead of displaying tuples to the user, the selected tuples are removed from the database.
- Can delete only whole tuples; cannot delete values on only particular attributes
- A deletion is expressed in relational algebra by:

$$r \leftarrow r - E$$

where r is a relation and E is a relational algebra query.

Deletion Examples

Delete all account records in the Perryridge branch.

$$account \leftarrow account - \sigma_{branch-name} = "Perryridge" (account)$$

■Delete all loan records with amount in the range of 0 to 50

loan ← loan −
$$\sigma$$
 amount ≥ 0 and amount ≤ 50 (loan)

■Delete all accounts at branches located in Needham.

$$r_1 \leftarrow \sigma_{branch-city} = \text{``Needham''} (account \bowtie branch)$$
 $r_2 \leftarrow \Pi_{branch-name, account-number, balance} (r_1)$
 $r_3 \leftarrow \Pi_{customer-name, account-number} (r_2 \bowtie depositor)$
 $account \leftarrow account - r_2$
 $depositor \leftarrow depositor - r_3$

Insertion

- To insert data into a relation, we either:
 - specify a tuple to be inserted or
 - write a query whose result is a set of tuples to be inserted
- in relational algebra, an insertion is expressed by:

$$r \leftarrow r \cup E$$

where r is a relation and E is a relational algebra expression.

■ The insertion of a single tuple is expressed by letting *E* be a constant relation containing one tuple.

Insertion Examples

Insert information in the database specifying that Smith has \$1200 in account A-973 at the Perryridge branch.

```
account \leftarrow account \cup \{("Perryridge", A-973, 1200)\}
depositor \leftarrow depositor \cup \{("Smith", A-973)\}
```

■ Provide as a gift for all loan customers in the Perryridge branch, a \$200 savings account. Let the loan number serve as the account number for the new savings account.

```
r_1 \leftarrow (\sigma_{branch-name = "Perryridge"}(borrower \bowtie loan))
account \leftarrow account \cup \prod_{loan-number, branch-name, 200}(r_1)
depositor \leftarrow depositor \cup \prod_{customer-name, loan-number}(r_1)
```

Updating

- A mechanism to change a value in a tuple without charging all values in the tuple
- Use the generalized projection operator to do this task

$$r \leftarrow \prod_{F1, F2, \dots, Fl,} (r)$$

- **Each** F_i is either
 - f the *i*th attribute of r, if the *i*th attribute is not updated, or,
 - if the attribute is to be updated F_i is an expression, involving only constants and the attributes of r, which gives the new value for the attribute

Update Examples

Make interest payments by increasing all balances by 5 percent.

$$account \leftarrow \prod_{AN, BN, BAL * 1.05} (account)$$

where AN, BN and BAL stand for account-number, branch-name and balance, respectively.

Pay all accounts with balances over \$10,000 6 percent interest and pay all others 5 percent

$$account \leftarrow \prod_{AN,\ BN,\ BAL \ ^* \ 1.06} (\sigma_{BAL \ > \ 10000} (account)) \ \cup \prod_{AN,\ BN,\ BAL \ ^* \ 1.05} (\sigma_{BAL \ \leq \ 10000} (account))$$

Views

- In some cases, it is not desirable for all users to see the entire logical model (i.e., all the actual relations stored in the database). Security considerations may require that certain data be hidden from users.
- Consider a person who needs to know a customer's loan number but has no need to see the loan amount. This person should see a relation described, in the relational algebra, by

 $\Pi_{customer-name, loan-number}(borrower \bowtie loan)$

Any relation that is not of the conceptual model but is made visible to a user as a "virtual relation" is called a view.

View Definition

A view is defined using the create view statement which has the form

create view v as <query expression>

where <query expression> is any legal relational algebra query expression. The view name is represented by *v*.

- Once a view is defined, the view name can be used to refer to the virtual relation that the view generates.
- View definition is not the same as creating a new relation by evaluating the query expression
 - Rather, a view definition causes the saving of the definition of the view itself, rather than the result of evaluation the relational algebra expression that defines the view; whenever a view relation appears in a query, it is replaced by the stored query expression.

View Examples

 Consider the view (named all-customer) consisting of branches and their customers.

create view all-customer as

```
\Pi_{branch-name, \ customer-name} (depositor\bowtie account) \cup \Pi_{branch-name, \ customer-name} (borrower\bowtie loan)
```

Using the view all-customer, we can find all customers of the Perryridge branch by writing:

```
\Pi_{customer-name}
(\sigma_{branch-name = "Perryridge"}(all-customer))
```

Updates Through View

- Database modifications expressed as views must be translated to modifications of the actual relations in the database.
- Consider the person who needs to see all loan data in the *loan* relation except *amount*. The view given to the person, *branch-loan*, is defined as:

create view branch-loan as

$$\Pi_{branch-name.\ loan-number}$$
 (loan)

Since we allow a view name to appear wherever a relation name is allowed, the person may write:

branch-loan ← branch-loan ∪ {("Perryridge", L-37)}

Updates Through Views (Cont.)

- The previous insertion must be represented by an insertion into the actual relation *loan* from which the view *branch-loan* is constructed.
- An insertion into *loan* requires a value for *amount*. The insertion can be dealt with by either.
 - rejecting the insertion and returning an error message to the user.
 - inserting a tuple ("L-37", "Perryridge", *null*) into the *loan* relation
- Some updates through views are impossible to translate into database relation updates
 - create view v as σ_{branch-name = "Perryridge"} (account))
 v ← v ∪ (L-99, Downtown, 23)
- Others cannot be translated uniquely
 - P all-customer ← all-customer ∪ {("Perryridge", "John")}
 - Have to choose loan or account, and create a new loan/account number!

Views Defined Using Other Views

- One view may be used in the expression defining another view
- A view relation v_1 is said to depend directly on a view relation v_2 if v_2 is used in the expression defining v_1
- A view relation v₁ is said to depend on view relation v₂ if either v₁ depends directly to v₂ or there is a path of dependencies from v₁ to v₂
- A view relation *v* is said to be *recursive* if it depends on itself.

View Expansion

- A way to define the meaning of views defined in terms of other views.
- Let view v_1 be defined by an expression e_1 that may itself contain uses of view relations.
- View expansion of an expression repeats the following replacement step:

repeat

Find any view relation v_i in e_1 Replace the view relation v_i by the expression defining v_i until no more view relations are present in e_1

As long as the view definitions are not recursive, this loop will terminate