EE5803 FPGA Lab Assignment 4

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1 Question

[CBSE 2018 Q6 (d)]: Reduce the following Boolean Expression to its simplest form using K-map and implement its NAND realisation on an Arduino UNO board.

$$G(U, V, W, Z) = \sum_{i} (3, 5, 6, 7, 11, 12, 13, 15)$$
(1)

2 Solution

2.1 Truth table

The truth table for the given boolean expression G is as follows

| U | V | W | Z | G(U, V, W, Z) |
|---|---|---|---|---------------|
| 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 1 | 0 |
| 0 | 0 | 1 | 0 | 0 |
| 0 | 0 | 1 | 1 | 1 |
| 0 | 1 | 0 | 0 | 0 |
| 0 | 1 | 0 | 1 | 1 |
| 0 | 1 | 1 | 0 | 1 |
| 0 | 1 | 1 | 1 | 1 |
| 1 | 0 | 0 | 0 | 0 |
| 1 | 0 | 0 | 1 | 0 |
| 1 | 0 | 1 | 0 | 0 |
| 1 | 0 | 1 | 1 | 1 |
| 1 | 1 | 0 | 0 | 1 |
| 1 | 1 | 0 | 1 | 1 |
| 1 | 1 | 1 | 0 | 0 |
| 1 | 1 | 1 | 1 | 1 |

Table 1: Truth table for Function G

2.2 K-map for simplification

Simplified expression from K-map can be written as

$$G = WZ + VZ + UVW' + U'VW \tag{2}$$

Please refer to Figure 1.

2.3 NAND logic diagram

To realize the above equation using NAND logic, the following steps are followed

$$(G')' = ((WZ + VZ + UVW' + U'VW)')'$$
(3)

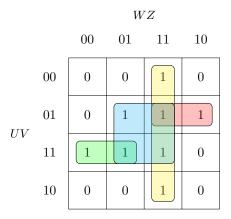


Figure 1: K-map for given boolean expression

$$G = ((WZ)'(VZ)'(UVW')'(U'VW)')'$$
(4)

Please refer to Figure 2.

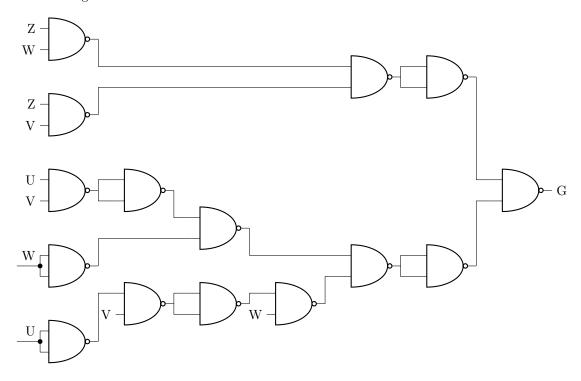


Figure 2: Logic circuit using NAND gate