Big Data Analytics, The Class

Goal: Generalizations A *model* or *summarization* of the data.

Data Workflow Frameworks

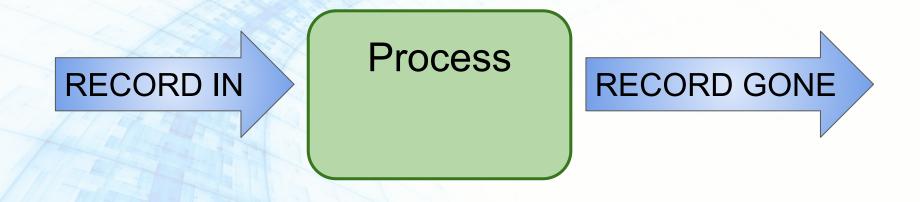
Hadoop File System
Spark **Streaming**MapReduce
Deep Learning Frameworks

Analytics and Algorithms

Similarity Search
Hypothesis Testing
Transformers/Self-Supervision
Recommendation Systems
Link Analysis

What is Streaming?

Broadly:



- (1) Direct: Often, data ...
 - ... cannot be stored (too big, privacy concerns)
 - are not practical to access repeatedly (reading is too long)
 - are rapidly arriving (need rapidly updated "results")

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Examples: Google search queries

Satellite imagery data

Text Messages, Status updates

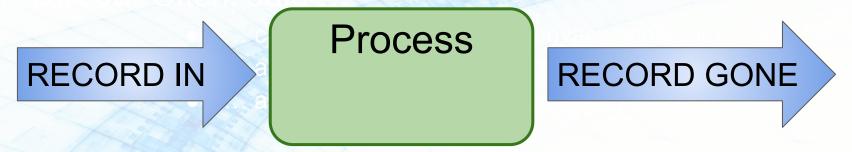
Click Streams

- (1) Direct: Often, data ...
 - ... cannot be stored (too big, privacy concerns)
 - ... are not practical to access repeatedly (reading is too long)
 - are rapidly arriving (need rapidly updated "results")
- (2) **Indirect:** The constraints for streaming data force one to solutions that are often efficient even when storing data.

Streaming Approx Random Sample

Distributed IO (MapReduce, Spark)

Often translates into O(N) or strictly N algorithms.



(2) **Indirect:** The constraints for streaming data force one to solutions that are often efficient even when storing data.

Streaming Approx Random Sample

Distributed IO (MapReduce, Spark)

Streaming Topics

- General Stream Processing Model
- Sampling
- Counting Distinct Elements
- Filtering data according to a criteria

RECORD IN

Process for stream queries

RECORD GONE

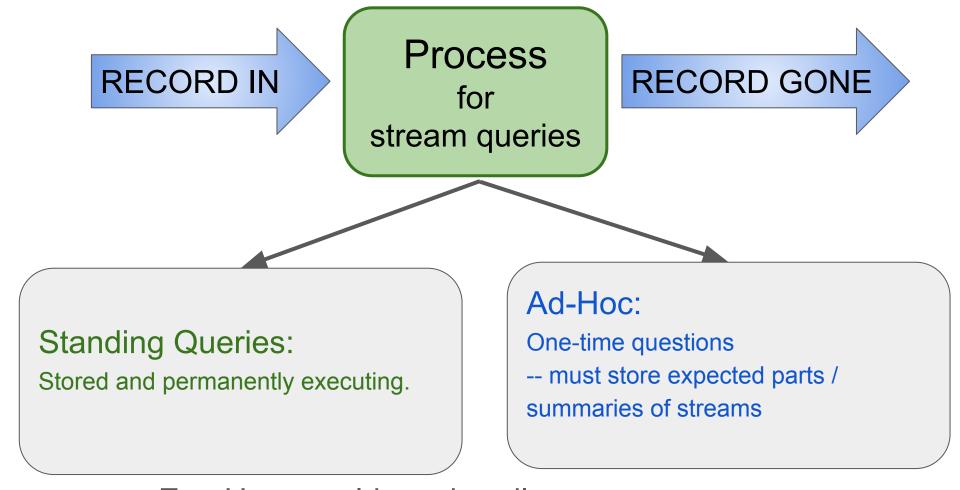
Standing Queries:

Stored and permanently executing.

Ad-Hoc:

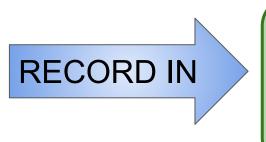
One-time questions

-- must store expected parts / summaries of streams



E.g. How would you handle:

What is the mean of values seen so far?



Process for stream queries

RECORD GONE

Important difference from typical database management:

- Input is not controlled by system staff.
- Input timing/rate is often unknown, controlled by users.

E.g. How would you handle:

What is the mean of values seen so far?

Process for stream queries

RECORD IN

RECORD GONE

Important differer

Pagement:

Might hold a sliding window of

records instead of single record.

.., i, h, g, f, e, d, c, b, a

E.g. How would you handle:

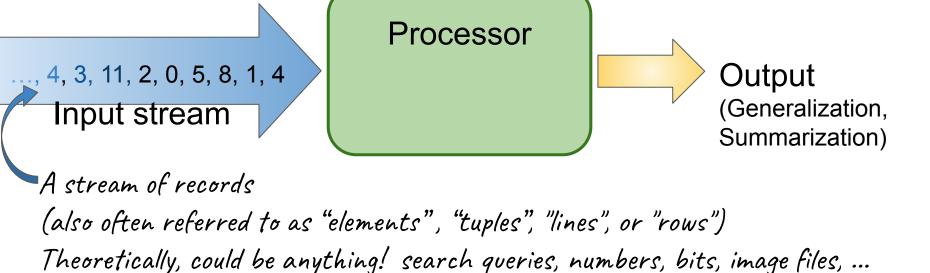
Input is n

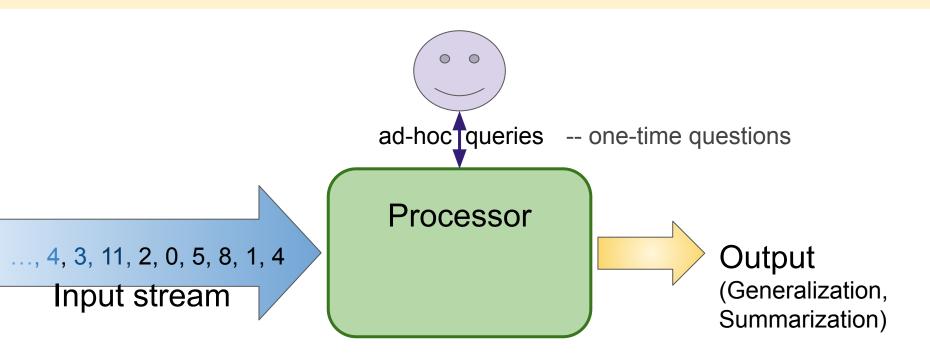
Input timing/rate is a

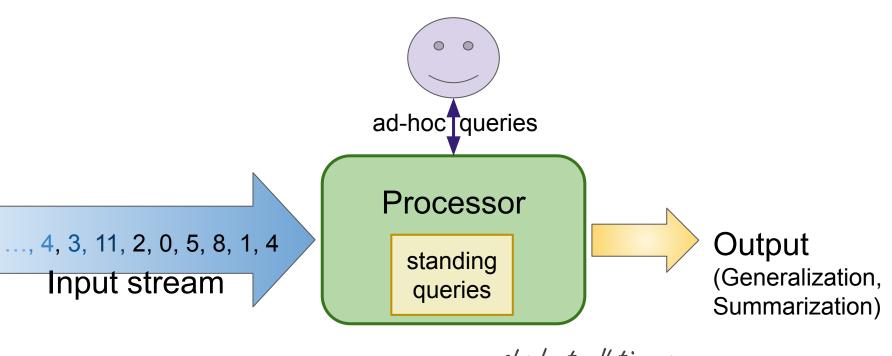
What is the mean of values seen so far?

Example 1 Users.

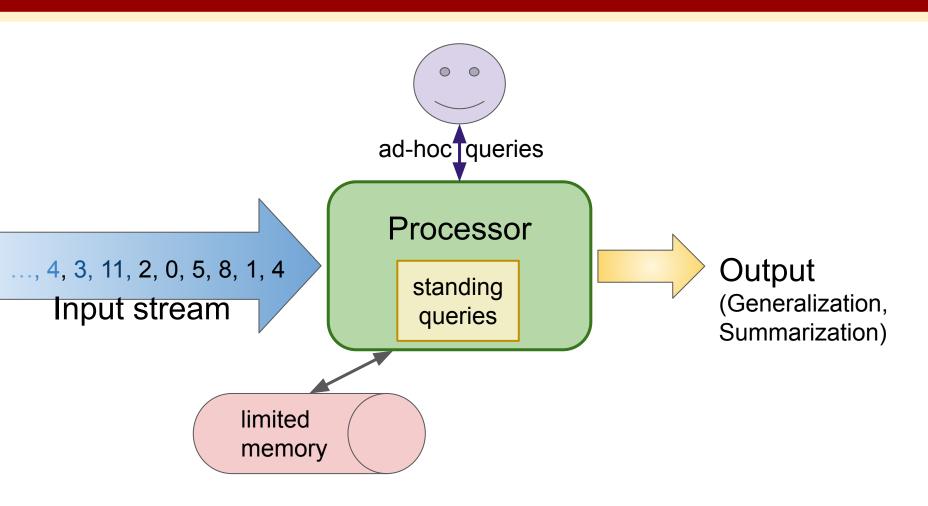
(Leskovec et al., 2014)

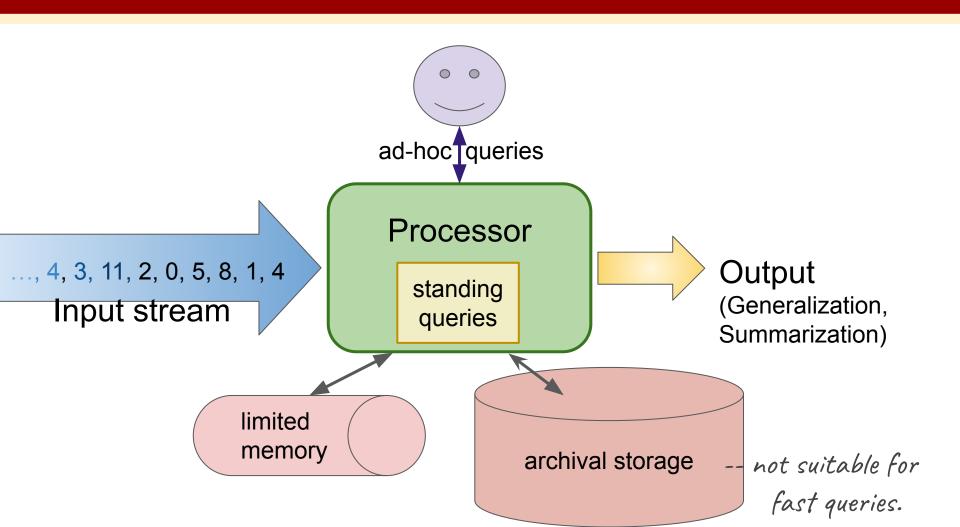






-- asked at all times.

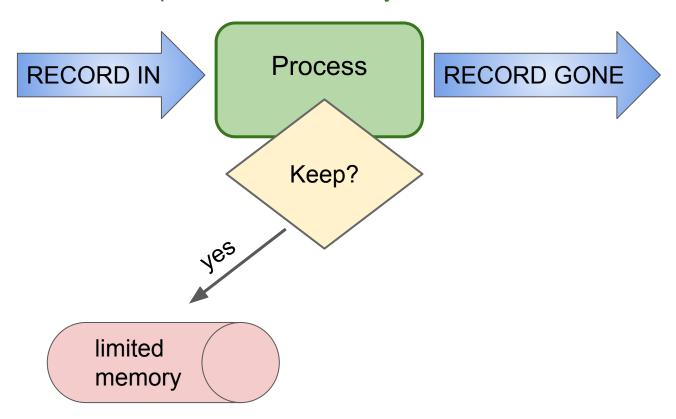




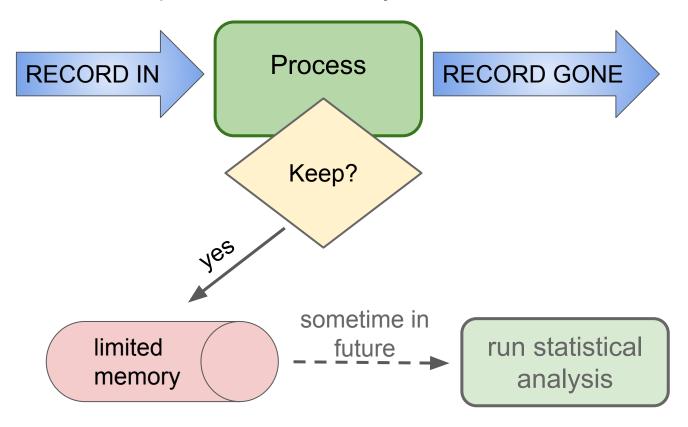
Create a random sample for statistical analysis.



Create a random sample for statistical analysis.



Create a random sample for statistical analysis.



Sampling: 2 Versions

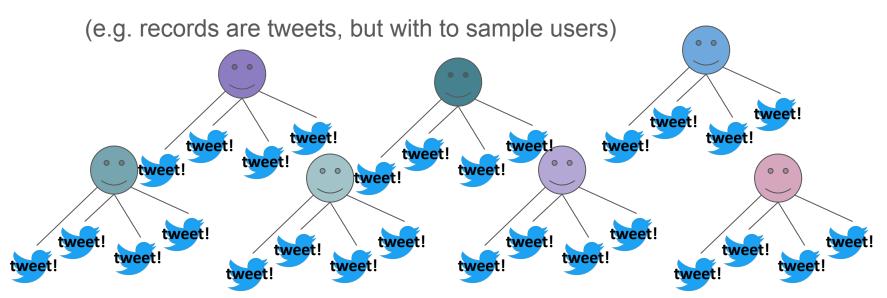
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Sampling: 2 Versions

Create a random sample for statistical analysis.

1. Simple Sampling: Individual records are what you wish to sample.

2. **Hierarchical Sampling:** Sample an attribute of a record.

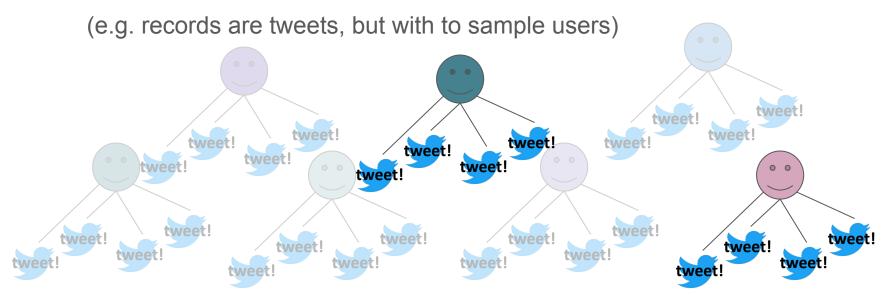


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```
record = stream.next()
 if ?: #keep: e.g., true 5% of the time
     memory.write(record)
                                              RECORD GONE
RECORD IN
                   ves
          limited
          memory
```

Create a random sample for statistical analysis.

```
record = stream.next()
 if random() <= .05: #keep: true 5% of the time</pre>
     memory.write(record)
                                                RECORD GONE
RECORD IN
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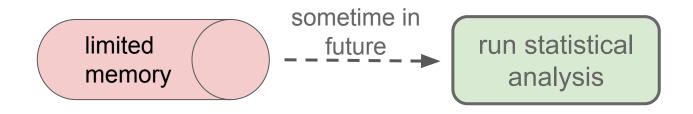
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record = stream.next()
if random() <= .05: #keep: true 5% of the time
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```

Problem: records/rows often are not units-of-analysis for statistical analyses

E.g. user_ids for searches, tweets; location_ids for satellite images



2. **Hierarchical Sampling:** Sample an attribute of a record.

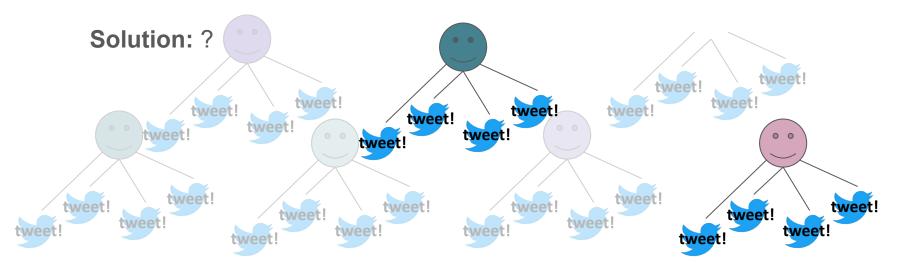
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(e.g. records are tweets, but with to sample users)
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Solution: ?

2. **Hierarchical Sampling:** Sample an attribute of a record.

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Solution: instead of checking random digit; hash the attribute being sampled.

streaming: only need to store hash functions; may be part of standing query

2. **Hierarchical Sampling:** Sample an attribute of a record.

```
(e.g. records are tweets, but with to sample users)
record = stream.next()
if hash(record['user_id']) == 1: #keep
    memory.write(record)
```

Solution: instead of checking random digit; hash the attribute being sampled.

streaming: only need to store hash functions; may be part of standing query

How many buckets to hash into?

Streaming Topics

- General Stream Processing Model
- Sampling
- Counting Distinct Elements
- Filtering data according to a criteria

Counting Moments

Moments:

- Suppose m_i is the count of distinct element i in the data
- ullet The kth moment of the stream is $\sum_{i\in \mathrm{Set}} m_i^k$

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- Oth moment: count of distinct elements
- 1st moment: length of stream
- 2nd moment: sum of squares (measures uneveness; related to variance)

Counting Moments

Moments:

- Suppose m_i is the count of distinct element i in the data
- ullet The kth m is $\sum_{i\in \mathrm{Set}} m_i^{\kappa}$

Trivial: just increment a counter

- 0th momen and or distinct elements
- 1st moment: length of stream
- 2nd moment: sum of squares (measures uneveness; related to variance)

Counting Momen

Applications

Counting...

distinct words in large document.

distinct websites (URLs).

users that visit a site without storing.

unique queries to Alexa.

0th moment

- 0th moment: count of distinct elements
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Counting Momer

Applications

Counting...

distinct words in large document. distinct websites (URLs). users that visit a site without storing. unique queries to Alexa.

0th moment

One Solution: Just keep a set (hashmap, dictionary, heap)

Problem: Can't maintain that many in memory; disk storage is too slow

- 0th moment: count of distinct elements
- 1st moment: length of stream
- 2nd moment: sum of squares (measures uneveness; related to variance)

0th moment

Streaming Solution: Flajolet-Martin Algorithm

General idea:

n -- suspected total number of elements observed pick a hash, *h*, to map each element to log₂n bits (buckets)

• <u>Zna moment. sum or squares</u> (measures *uneveness;* related to variance)

```
Oth moment
Streaming Solution: Flajolet-Martin Algorithm
General idea:
    n -- suspected overestimate of total number of elements observed
    pick a hash, h, to map each element to log<sub>2</sub>n bits (buckets)
    R = 0 #current max number of zeros at tail
    for each stream element, e:
        r(e) = trailZeros(h(e)) #num of trailing 0s from h(e)
        R = r(e) \text{ if } r[e] > R
    estimated_distinct_elements = 2<sup>R</sup>
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Counting Momer

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estimated_distinct_elements = 2^R # m

Zilu moment. Sum of Squares

(measures uneveness; related to variance)

Mathematical Intuition

 $P(\text{trailZeros}(h(e)) >= i) = 2^{-i}$ #P(h(e) == 0) = .5; P(h(e) == 00) = .25; ...P(trailZeros(h(e)) < i) = 1 - 2^{-i}

for m elements: = $(1 - 2^{-i})^m$

P(one e has trailZeros > i) = 1 - $(1 - 2^{-i})^m$ $\approx 1 - e^{-m2^{-i}}$

If $2^{R} >> m$, then $1 - (1 - 2^{-i})^{m} \approx 0$

n -- suspected total number of $If 2^R << m$, then 1 - $(1 - 2^{-i})^m \approx 1$

(DUCKELS)

tail

trailing 0s from h(e)

Counting Momer

Oth moment

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 $\approx 1 - e^{-m2^{-i}}$
If 2^R >> m, then $1 - (1 - 2^{-i})^m \approx 0$

(DUCKELS)

Problem:

Unstable in practice.

Solution:

Multiple hash functions but how to combine?

(measures uneveness; related to variance)

```
0th moment
```

Streaming Solution: Flajolet-Martin Algorithm General idea:

n -- suspected total number of elements 1. Partition into groups of size log n pick a hash, h, to map each element to l

```
Problem:
```

Unstable in practice.

Solution: Multiple hash functions

- 2. Take mean in groups
- 3. Take median of group means

```
Rs = list()
for h in hashes:
   R = 0 #potential max number of zeros at tail
   for each stream element, e:
       r(e) = trailZeros(h(e)) #num of trailing 0s from h(e)
       R = r(e) \text{ if } r[e] > R
   Rs.append(2^R)
```

groupRs = [Rs[i:i+log n] for i in range(0, len(Rs), log n)]

estimated distinct elements = median(map(mean, groupRs))

```
0th moment
```

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Problem:
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Unstable in practice.

Solution: Multiple hash functions

- 1. Partition into groups of size log n
- 2 Take mean in groups
- 7. Take median of group means

```
Rs = list()
for h in hashes:
```

```
A good approach anytime one has many "low resolution" estimates of a true value.
```

Rs.appe

lling 0s from h(e)

groupRs = [Rs[i:i+log n] for i in range(0, len(Rs), log n)]

estimated_distinct_elements = median(map(mean, groupRs))

2nd moment

Streaming Solution: Alon-Matias-Szegedy Algorithm

(Exercise; Out of Scope; see in MMDS)

- 0th moment: count of distinct elements
- 1st moment: length of stream
- 2nd moment: sum of squares (measures uneveness related to variance)

standard deviation
(square-root of variance for numeric data)

$$s = \frac{1}{N} \sqrt{\sum_{1}^{N} (x_i - \bar{x})^2}$$

standard deviation
(square-root of variance for numeric data)

$$s = \frac{1}{N} \sqrt{\sum_{1}^{N} (x_i - \bar{x})^2} = \sqrt{(\bar{x}^2) - \bar{x}^2} = \sqrt{\frac{\sum_{1}^{N} x^2}{N} - (\frac{\sum_{1}^{N} x}{N})^2}$$

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For streaming, just need to store (1) number of elements, (2) sum of elements, and (3) sum of squares.

standard deviation (square-root of variance for numeric data)

$$s = \frac{1}{N} \sqrt{\sum_{1}^{N} (x_i - \bar{x})^2} = \sqrt{(\bar{x}^2) - \bar{x}^2} = \sqrt{\sum_{1}^{N} x^2 - (\sum_{1}^{N} x)^2}$$

However, challenge:

Sum of squares can blow up!

For streaming, just need to store (1) number of elements, (2) sum of elements, and (3) sum of squares.

Filtering: Select elements with property x

Example: 40B safe email addresses for spam detector

Filtering: Select elements with property x

Example: 40B safe email addresses for spam filter

The Bloom Filter (approximates; allows false positives but not false negatives)

Given:

|S| keys to filter; will be mapped to |B| bits hashes = $h_1, h_2, ..., h_k$ independent hash functions

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Example: 40B safe email addresses for spam filter

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```

Algorithm:

```
set all B to 0 #B is a bit vector
for each i in hashes, for each s in S:
set B[h_i(s)] = 1 #all bits resulting from
```

Filtering: Select elements with property x

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Setup filter

Apply Filter

Filtering: Select elements with property x

Example: 40B safe email addresses for spam fixer The Bloom Filter (approximates; allows FPs)

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    else: #do as if x not in S
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What is the probability of a *false* positive (FP)?

Q: What fraction of |B| are 1s?

(Leskovec et al., 2014)

Filtering: Select elements with property x

Example: 40B safe email addresses for spam filter The Bloom Filter (approximates; allows FPs)

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What is the probability of a *false positive*?

Q: What fraction of |B| are 1s?

A: Analogy:

Throw |S| * k darts at n targets.

1 dart: 1/n

d darts: (1 - 1/n)^d = prob of 0

= e^{-d/n} are **0s**

Filtering: Select elements with property x

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= $e^{-d/n}$ are **0s**

 $= e^{-1}$ for large n

(Leskovec et al., 2014)

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thus, (1 - *e*-^{d/n}) are **1s**

probability all k being 1?

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thus, $(1 - e^{-d/n})$ are **1s**

probability all k being 1? (1 - $e^{-(|S|*k)/n})^k$

|S| size of set k: number of hash functions n: number of buckets

Note: Can expand S as stream continues as long as |B| has room (e.g. adding verified email addresses)

(Leskovec et al., 2014)

Side Note on Generating Hash Functions:

What hash functions to use?

Start with 2 decent hash functions

e.g.
$$h_a(x) = ascii(string) \% large_prime_number$$

 $h_b(x) = (3*ascii(string) + 16) \% large_prime_number$

Add together multiplying the second times i:

$$h_i(x) = h_a(x) + i*h_b(x) \% |BUCKETS|$$

e.g. $h_5(x) = h_a(x) + 5*h_b(x) \% 100$

https://www.eecs.harvard.edu/~michaelm/postscripts/rsa2008.pdf

Popular choices: md5 (fast, predistable); mmh3 (easy to seed; fast)

Streaming Topics

- General Stream Processing Model
- Sampling
 - o approx. random
 - hierarchical approx. random
- Counting Elements
 - distinct elements
 - mean, standard deviation
- Filtering data according to a criteria
 - bloom filter setup + application
 - calculating false positives