

assignment 6

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Outline

1 question: ex 6.7

2 solution

question

- Suppose $z = x + y$., find pdf of $f_z(z)$, and x and y are independent exponential random variables with parameter a .

solution

since x and y are exponential random variable of parameter a , we get

$$f_x(x) = ae^{-ax} U(x) \quad (1)$$

$$f_y(y) = ae^{-ay} U(y) \quad (2)$$

we can make use of below theorem to obtain this,

$$f_z(z) = \int_{x=0}^z f_{xy}(x, y) dy dx \quad (3)$$

$$= \begin{cases} \int_0^z f_x(x) f_y(z-x) dx & z < 0 \\ 0 & z \leq 0 \end{cases} \quad (4)$$

solution

so from above theorm and using the condition x, y are independent we get,

$$f_z(z) = \int_0^z f_x(x) f_y(z-x) dx \quad (5)$$

$$f_z(z) = \int_0^z a^2 e^{-ax} e^{-a(z-x)} dx \quad (6)$$

$$f_z(z) = a^2 e^{-az} \int_0^z dx \quad (7)$$

$$= za^2 e^{-az} U(z) \quad (8)$$