## Assignment4Final

## December 14, 2023

```
[]: # Resizing and cropping each image to a 224 × 224 pixel image.
     import os
     import xml.etree.ElementTree as ET
     from PIL import Image
     import cv2
     import random
     import matplotlib.pyplot as plt
     from skimage import exposure
     import numpy as np
     from scipy.spatial import distance
     from scipy.stats import wasserstein_distance
     from sklearn.decomposition import PCA
     from sklearn.preprocessing import StandardScaler
     from skimage import io, color
[]: # Cropping and resizing the images for Beagle Data set (Data set 1)
     annotations_dir = 'D:\Dataset\Beagle annonations\\n02088364-beagle'
     annotations_files = os.listdir(annotations_dir)
     # Step 2: Load the Images Dataset
     images_dir = 'D:\Dataset\Beaglepng'
     output_dir = 'D:\Dataset\Beagle 224'
     if not os.path.exists(output_dir):
         os.makedirs(output_dir)
     # Step 3: Parse XML Data and Crop & Resize Images
     for xml_file in annotations_files:
         xml_path = os.path.join(annotations_dir, xml_file)
         image_filename = os.path.splitext(xml_file)[0] + '.png'
         image_path = os.path.join(images_dir, image_filename)
         if os.path.exists(image_path):
             tree = ET.parse(xml_path)
             root = tree.getroot()
```

```
# Extract bounding box coordinates
        xmin = int(root.find(".//xmin").text)
        ymin = int(root.find(".//ymin").text)
        xmax = int(root.find(".//xmax").text)
        ymax = int(root.find(".//ymax").text)
        # Load and crop the image
       image = Image.open(image_path)
        cropped_image = image.crop((xmin, ymin, xmax, ymax))
        # Resize the cropped image to 224x224 pixels
       resized_image = cropped_image.resize((224,224), Image.ANTIALIAS)
        # Save the resized image as PNG
       output_path = os.path.join(output_dir, image_filename)
        resized_image.save(output_path, "PNG")
       print(f"Processed: {image_filename}")
print("All images processed and saved.")
# Cropping and resizing the images for Dhole Data set (Data set 2)
annotations_dir = 'D:\Dataset\Dhole annonations\\n02115913-dhole'
annotations_files = os.listdir(annotations_dir)
# Step 2: Load the Images Dataset
images_dir = 'D:\Dataset\Dholepng'
output_dir = 'D:\Dataset\Dhole 224'
if not os.path.exists(output_dir):
   os.makedirs(output_dir)
# Step 3: Parse XML Data and Crop & Resize Images
for xml_file in annotations_files:
   xml_path = os.path.join(annotations_dir, xml_file)
    image_filename = os.path.splitext(xml_file)[0] + '.png'
    image_path = os.path.join(images_dir, image_filename)
   if os.path.exists(image_path):
       tree = ET.parse(xml_path)
       root = tree.getroot()
        # Extract bounding box coordinates
        xmin = int(root.find(".//xmin").text)
        ymin = int(root.find(".//ymin").text)
```

```
xmax = int(root.find(".//xmax").text)
        ymax = int(root.find(".//ymax").text)
        # Load and crop the image
        image = Image.open(image_path)
        cropped_image = image.crop((xmin, ymin, xmax, ymax))
        # Resize the cropped image to 224x224 pixels
       resized_image = cropped_image.resize((224,224), Image.ANTIALIAS)
        # Save the resized image as PNG
       output_path = os.path.join(output_dir, image_filename)
       resized_image.save(output_path, "PNG")
       print(f"Processed: {image_filename}")
print("All images processed and saved.")
# Cropping and resizing the images for Golden retriever Data set (Data set 3)
annotations_dir = 'D:\Dataset\Golden Retriever_
 ⇔annonations\\n02099601-golden_retriever'
annotations_files = os.listdir(annotations_dir)
# Step 2: Load the Images Dataset
images_dir = 'D:\Dataset\Golden Retrieverpng'
output_dir = 'D:\Dataset\Golden retriever 224'
if not os.path.exists(output_dir):
   os.makedirs(output_dir)
# Step 3: Parse XML Data and Crop & Resize Images
for xml_file in annotations_files:
   xml_path = os.path.join(annotations_dir, xml_file)
    image_filename = os.path.splitext(xml_file)[0] + '.png'
    image_path = os.path.join(images_dir, image_filename)
   if os.path.exists(image_path):
       tree = ET.parse(xml_path)
       root = tree.getroot()
        # Extract bounding box coordinates
        xmin = int(root.find(".//xmin").text)
       ymin = int(root.find(".//ymin").text)
       xmax = int(root.find(".//xmax").text)
```

```
ymax = int(root.find(".//ymax").text)
        # Load and crop the image
        image = Image.open(image_path)
        cropped_image = image.crop((xmin, ymin, xmax, ymax))
        # Resize the cropped image to 224x224 pixels
       resized_image = cropped_image.resize((224,224), Image.ANTIALIAS)
        # Save the resized image as PNG
        output_path = os.path.join(output_dir, image_filename)
       resized_image.save(output_path, "PNG")
       print(f"Processed: {image_filename}")
print("All images processed and saved.")
# Cropping and resizing the images for Great Pyreness Data set (Data set 4)
annotations_dir = 'D:\Dataset\Great Pyreness_
 ⇔annonations\\n02111500-Great_Pyrenees'
annotations_files = os.listdir(annotations_dir)
# Step 2: Load the Images Dataset
images_dir = 'D:\Dataset\Great pyrenesspng'
output_dir = 'D:\Dataset\Great Pyreness 224'
if not os.path.exists(output_dir):
   os.makedirs(output_dir)
# Step 3: Parse XML Data and Crop & Resize Images
for xml_file in annotations_files:
   xml_path = os.path.join(annotations_dir, xml_file)
   image_filename = os.path.splitext(xml_file)[0] + '.png'
   image_path = os.path.join(images_dir, image_filename)
   if os.path.exists(image_path):
       tree = ET.parse(xml_path)
       root = tree.getroot()
        # Extract bounding box coordinates
```

```
xmin = int(root.find(".//xmin").text)
ymin = int(root.find(".//ymin").text)
xmax = int(root.find(".//xmax").text)
ymax = int(root.find(".//ymax").text)

# Load and crop the image
image = Image.open(image_path)
cropped_image = image.crop((xmin, ymin, xmax, ymax))

# Resize the cropped image to 224x224 pixels
resized_image = cropped_image.resize((224,224), Image.ANTIALIAS)

# Save the resized image as PNG
output_path = os.path.join(output_dir, image_filename)
resized_image.save(output_path, "PNG")

print(f"Processed: {image_filename}")

print("All images processed and saved.")
```

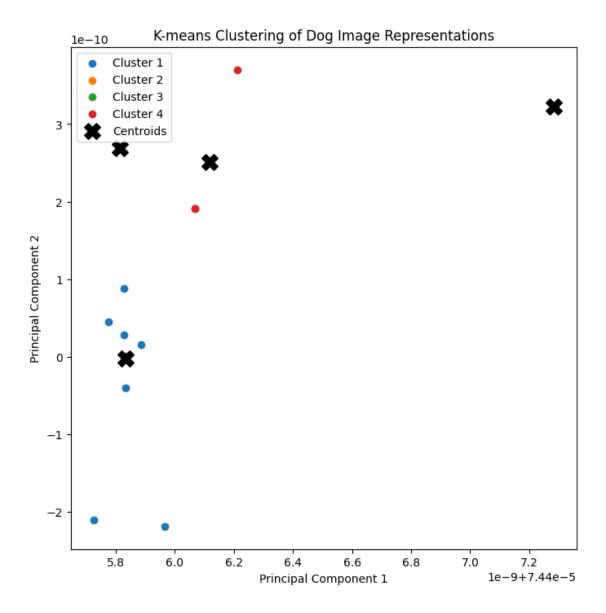
```
[]: # Normalize the resized image dataset.
     from sklearn.preprocessing import StandardScaler
     # Function to normalize a given dataset
     def normalize_images(dataset_path, output_path):
         image_files = os.listdir(dataset_path)
         if not os.path.exists(output_path):
             os.makedirs(output_path)
         # Load, normalize, and save each image
         for image_file in image_files:
             image_path = os.path.join(dataset_path, image_file)
             if os.path.exists(image_path):
                 # Load the image
                 image = Image.open(image_path)
                 # Convert the image to a NumPy array
                 image_array = np.array(image)
                 # Flatten the array to a 1D vector
                 flattened_array = image_array.flatten().reshape(1, -1)
                 # Use StandardScaler to normalize the pixel values
                 scaler = StandardScaler()
                 normalized_array = scaler.fit_transform(flattened_array)
```

```
# Reshape the normalized array back to the original shape
                 normalized image_array = normalized array.reshape(image_array.shape)
                 # Convert the array back to an image
                 normalized_image = Image.fromarray(normalized_image_array.
      ⇔astype('uint8'))
                 # Save the normalized image
                 output_image_path = os.path.join(output_path, image_file)
                 normalized_image.save(output_image_path, "PNG")
     # Normalize the Beagle dataset
     beagle_resized_path = 'D:\Dataset\Beagle 224'
     beagle_normalized_path = 'D:\Dataset\Beagle 224 Normalized'
     normalize_images(beagle_resized_path, beagle_normalized_path)
     # Normalize the Dhole dataset
     dhole resized path = 'D:\Dataset\Dhole 224'
     dhole_normalized_path = 'D:\Dataset\Dhole 224 Normalized'
     normalize_images(dhole_resized_path, dhole_normalized_path)
     # Normalize the Golden Retriever dataset
     golden_retriever_resized_path = 'D:\Dataset\Golden retriever 224'
     golden_retriever_normalized_path = 'D:\Dataset\Golden retriever 224 Normalized'
     normalize_images(golden_retriever_resized_path,__
      →golden_retriever_normalized_path)
     # Normalize the Great Pyrenees dataset
     great_pyrenees_resized_path = 'D:\Dataset\Great Pyreness 224'
     great_pyrenees_normalized_path = 'D:\Dataset\Great Pyreness 224 Normalized'
     normalize_images(great_pyrenees_resized_path, great_pyrenees_normalized_path)
[]: import os
     import numpy as np
     from PIL import Image
     import torch
     import torch.nn as nn
     import torchvision.transforms as transforms
     from torchvision import models
     from sklearn.decomposition import PCA
     from sklearn.cluster import AgglomerativeClustering
     import matplotlib.pyplot as plt
```

```
[]: # Reference: https://kozodoi.me/blog/20210527/extracting-features
     # Function to extract features from the last convolutional layer of ResNet18
     def extract_resnet18_features(dataset_path):
         image_files = os.listdir(dataset_path)
         PREDS = [] # To store Labels
         FEATS = [] # To store Features
         # Load the pre-trained ResNet18 model
         model = models.resnet18(pretrained=True)
         # Remove the fully connected layers (classification head)
         model = nn.Sequential(*list(model.children())[:-2])
         model.eval() # Set the model to evaluation mode
         # Define the transformation to be applied to each image
         transform = transforms.Compose([
             transforms.ToTensor(),
             transforms.Normalize(mean=[0.485, 0.456, 0.406], std=[0.229, 0.224, 0.
      ⇒225]),
         1)
         # Extract features for each image
         for image_file in image_files:
             image_path = os.path.join(dataset_path, image_file)
             if os.path.exists(image_path):
                 # Load and preprocess the image
                 image = Image.open(image_path).convert('RGB')
                 image = transform(image)
                 image = image.unsqueeze(0)
                 # Forward pass through the model
                 with torch.no_grad():
                     features = model(image)
                 # Flatten the feature tensor
                 feature_vector = features.mean([2, 3]).squeeze().numpy()
                 # Store the feature vector and label
                 FEATS.append(feature_vector)
                 PREDS.append(os.path.basename(dataset_path))
         return np.array(FEATS), np.array(PREDS)
     # Define the paths for all 4 datasets
     beagle resized path = 'D:\Dataset\Beagle 224 Normalized'
```

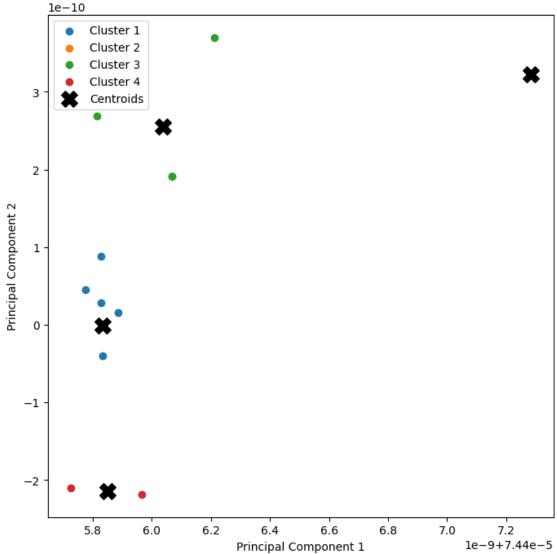
```
dhole_resized_path = 'D:\Dataset\Dhole 224 Normalized'
     golden_retriever_resized_path = 'D:\Dataset\Golden retriever 224 Normalized'
     great_pyrenees_resized_path = 'D:\Dataset\Great Pyreness 224 Normalized'
     # Extract features for each dataset
     beagle_feats, beagle_preds = extract_resnet18_features(beagle_resized_path)
     dhole_feats, dhole_preds = extract_resnet18_features(dhole_resized_path)
     golden_retriever_feats, golden_retriever_preds =_
      Gextract_resnet18_features(golden_retriever_resized_path)
     great_pyrenees_feats, great_pyrenees_preds =__
      →extract_resnet18_features(great_pyrenees_resized_path)
     # Combine features and labels for all datasets
     all_feats = np.concatenate((beagle_feats, dhole_feats, golden_retriever_feats,_u
      ⇒great_pyrenees_feats), axis=0)
     all_preds = np.concatenate((beagle_preds, dhole_preds, golden_retriever_preds,_
      ⇒great_pyrenees_preds), axis=0)
     print('Labels shape:', all_preds.shape)
     print('Features shape:', all_feats.shape)
     # Perform PCA to reduce dimensionality to 2D
     pca = PCA(n_components=2)
     reduced_feats = pca.fit_transform(all_feats)
     print("Reduced features shape:",reduced_feats.shape)
    c:\Users\User\AppData\Local\Programs\Python\Python39\lib\site-
    packages\torchvision\models\_utils.py:208: UserWarning: The parameter
    'pretrained' is deprecated since 0.13 and may be removed in the future, please
    use 'weights' instead.
      warnings.warn(
    c:\Users\User\AppData\Local\Programs\Python\Python39\lib\site-
    packages\torchvision\models\ utils.py:223: UserWarning: Arguments other than a
    weight enum or 'None' for 'weights' are deprecated since 0.13 and may be removed
    in the future. The current behavior is equivalent to passing
    `weights=ResNet18_Weights.IMAGENET1K_V1`. You can also use
    `weights=ResNet18_Weights.DEFAULT` to get the most up-to-date weights.
      warnings.warn(msg)
    Labels shape: (708,)
    Features shape: (708, 512)
    Reduced features shape: (708, 2)
[]: # CLustering
     from sklearn.cluster import KMeans
     # K-means clustering with init='random'
     kmeans = KMeans(n_clusters=4, init='random', random_state=42)
```

c:\Users\User\AppData\Local\Programs\Python\Python39\lib\sitepackages\sklearn\cluster\\_kmeans.py:1412: FutureWarning: The default value of
`n\_init` will change from 10 to 'auto' in 1.4. Set the value of `n\_init`
explicitly to suppress the warning
 super().\_check\_params\_vs\_input(X, default\_n\_init=10)

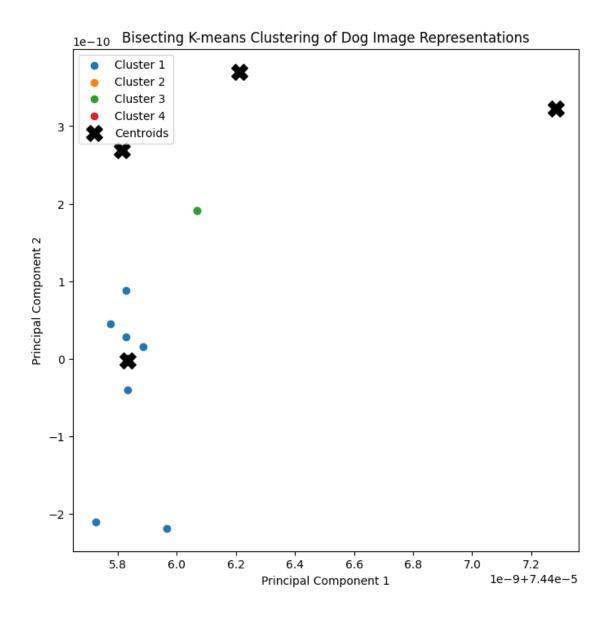


c:\Users\User\AppData\Local\Programs\Python\Python39\lib\sitepackages\sklearn\cluster\\_kmeans.py:1412: FutureWarning: The default value of
`n\_init` will change from 10 to 'auto' in 1.4. Set the value of `n\_init`
explicitly to suppress the warning
 super().\_check\_params\_vs\_input(X, default\_n\_init=10)

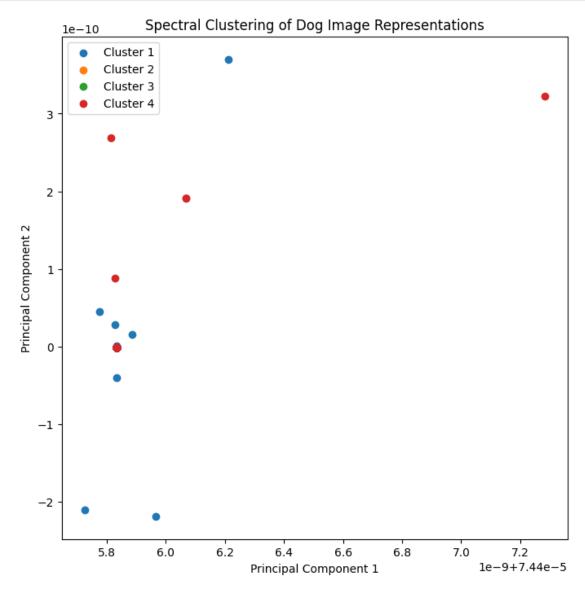




```
[]: from sklearn.cluster import BisectingKMeans
     # Bisecting K-means clustering
     bisecting_kmeans = BisectingKMeans(n_clusters=4, init='random', random_state=42)
     cluster_labels_bisecting = bisecting_kmeans.fit_predict(reduced_feats)
     # Visualizing the Bisecting K-means clustering results
     plt.figure(figsize=(8, 8))
     for cluster_label in np.unique(cluster_labels_bisecting):
         indices = np.where(cluster labels bisecting == cluster label)
        plt.scatter(reduced_feats[indices, 0], reduced_feats[indices, 1],__
      ⇔label=f'Cluster {cluster_label + 1}')
     plt.scatter(bisecting kmeans.cluster_centers_[:, 0], bisecting_kmeans.
      ⇔cluster_centers_[:, 1], marker='X', s=200, c='black', label='Centroids')
     plt.title('Bisecting K-means Clustering of Dog Image Representations')
     plt.xlabel('Principal Component 1')
     plt.ylabel('Principal Component 2')
     plt.legend()
     plt.show()
```



```
plt.title('Spectral Clustering of Dog Image Representations')
plt.xlabel('Principal Component 1')
plt.ylabel('Principal Component 2')
plt.legend()
plt.show()
```



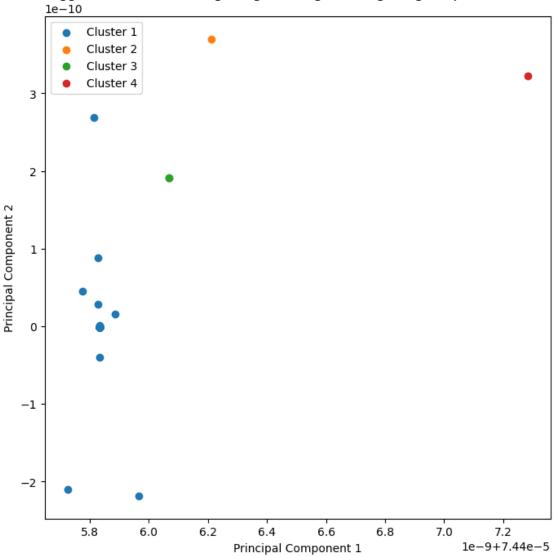
```
[]: from sklearn.cluster import DBSCAN

# DBSCAN
for eps in [0.5]:
   for min_samples in [3]:
```

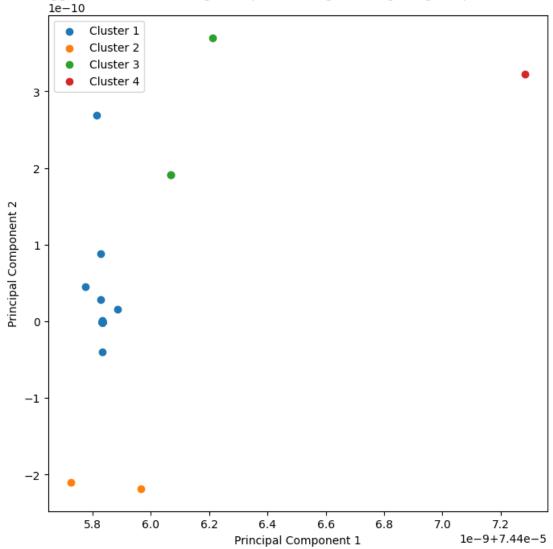
For eps=0.5, min\_samples=3, Number of clusters: 4

```
[]: # Agglomerative Clustering with 'single' linkage
     agglomerative_single = AgglomerativeClustering(n_clusters=4, linkage='single')
     cluster_labels_agglomerative_single = agglomerative_single.
     →fit_predict(reduced_feats)
     # Visualizing the Agglomerative Clustering (Single Linkage) results
     plt.figure(figsize=(8, 8))
     for cluster_label in np.unique(cluster_labels_agglomerative_single):
        indices = np.where(cluster_labels_agglomerative_single == cluster_label)
        plt.scatter(reduced_feats[indices, 0], reduced_feats[indices, 1],__
      ⇔label=f'Cluster {cluster_label + 1}')
     plt.title('Agglomerative Clustering (Single Linkage) of Dog Image⊔
     →Representations')
     plt.xlabel('Principal Component 1')
     plt.ylabel('Principal Component 2')
     plt.legend()
     plt.show()
```





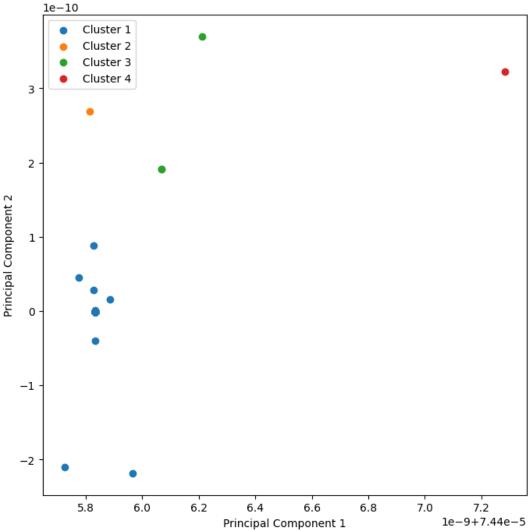
## Agglomerative Clustering (Complete Linkage) of Dog Image Representations



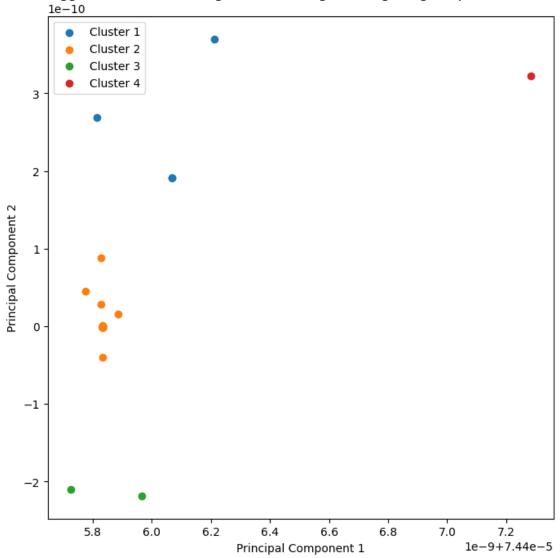
```
[]: # Agglomerative Clustering with 'average' linkage
     agglomerative_average = AgglomerativeClustering(n_clusters=4, linkage='average')
     cluster_labels_agglomerative_average = agglomerative_average.
      fit_predict(reduced_feats)
     # Visualizing the Agglomerative Clustering (Group Average Linkage) results
     plt.figure(figsize=(8, 8))
     for cluster_label in np.unique(cluster_labels_agglomerative_average):
         indices = np.where(cluster_labels_agglomerative_average == cluster_label)
        plt.scatter(reduced_feats[indices, 0], reduced_feats[indices, 1],__
      ⇔label=f'Cluster {cluster_label + 1}')
     plt.title('Agglomerative Clustering (Group Average Linkage) of Dog Image⊔

¬Representations')
     plt.xlabel('Principal Component 1')
     plt.ylabel('Principal Component 2')
     plt.legend()
     plt.show()
```





## Agglomerative Clustering (Ward's Linkage) of Dog Image Representations



```
[]: import numpy as np
from sklearn.metrics import fowlkes_mallows_score

true_labels = np.concatenate((np.zeros(beagle_feats.shape[0]),
```

```
np.ones(dhole_feats.shape[0]),
                               2 * np.ones(golden_retriever_feats.shape[0]),
                               3 * np.ones(great_pyrenees_feats.shape[0])))
# function to evaluate and print Fowlkes-Mallows index
def evaluate_fowlkes_mallows(method_name, predicted_labels):
    score = fowlkes_mallows_score(true_labels, predicted_labels)
    print(f"Fowlkes-Mallows index for {method_name}: {score}")
# Evaluate for K-means (init='random')
evaluate fowlkes mallows("K-means (init='random')", cluster labels)
# Evaluate for K-means (init='k-means++')
evaluate_fowlkes_mallows("K-means (init='k-means++')", cluster_labels_pp)
# Evaluate for Bisecting K-means
evaluate fowlkes mallows ("Bisecting K-means", cluster labels bisecting)
# Evaluate for Spectral Clustering
evaluate_fowlkes_mallows("Spectral Clustering", cluster_labels_spectral)
# Evaluate for Agglomerative Clustering (Single Linkage)
evaluate_fowlkes_mallows("Agglomerative Clustering (Single Linkage)", __
 →cluster_labels_agglomerative_single)
# Evaluate for Agglomerative Clustering (Complete Linkage)
evaluate_fowlkes_mallows("Agglomerative Clustering (Complete Linkage)", u
 ⇔cluster_labels_agglomerative_complete)
# Evaluate for Agglomerative Clustering (Group Average Linkage)
evaluate_fowlkes_mallows("Agglomerative Clustering (Group Average Linkage)", __
 ⇔cluster_labels_agglomerative_average)
# Evaluate for Agglomerative Clustering (Ward's Linkage)
evaluate_fowlkes_mallows("Agglomerative Clustering (Ward's Linkage)", __
  ⇒cluster_labels_agglomerative_ward)
Fowlkes-Mallows index for K-means (init='random'): 0.5010296961472338
Fowlkes-Mallows index for K-means (init='k-means++'): 0.4994758234603681
Fowlkes-Mallows index for Bisecting K-means: 0.5010296961472338
Fowlkes-Mallows index for Spectral Clustering: 0.35255621518337577
Fowlkes-Mallows index for Agglomerative Clustering (Single Linkage):
0.5018152540885414
Fowlkes-Mallows index for Agglomerative Clustering (Complete Linkage):
0.50024291569637
Fowlkes-Mallows index for Agglomerative Clustering (Group Average Linkage):
0.5010296961472338
```

Fowlkes-Mallows index for Agglomerative Clustering (Ward's Linkage): 0.4994758234603681

```
[]: from sklearn.metrics import silhouette_score
     # function to evaluate and print Silhouette Coefficient
     def evaluate silhouette coefficient (method name, predicted labels, u

→feature_matrix):
         # Silhouette Coefficient requires more than one cluster
         if len(set(predicted_labels)) > 1:
             score = silhouette_score(feature_matrix, predicted_labels)
             print(f"Silhouette Coefficient for {method_name}: {score}")
         else:
             print(f"Silhouette Coefficient for {method_name}: Not applicable∟
      ⇔(requires more than one cluster)")
     # Evaluate for K-means (init='random')
     evaluate_silhouette_coefficient("K-means (init='random')", cluster_labels,__
      →reduced feats)
     # Evaluate for K-means (init='k-means++')
     evaluate_silhouette_coefficient("K-means (init='k-means++')",_
      Graduater_labels_pp, reduced_feats)
     # Evaluate for Bisecting K-means
     evaluate_silhouette_coefficient("Bisecting K-means", cluster_labels_bisecting, __
      →reduced_feats)
     # Evaluate for Spectral Clustering
     evaluate_silhouette_coefficient("Spectral Clustering", cluster_labels_spectral, __
      →reduced_feats)
     # Evaluate for Agglomerative Clustering (Single Linkage)
     evaluate_silhouette_coefficient("Agglomerative Clustering (Single Linkage)", __
      →cluster_labels_agglomerative_single, reduced_feats)
     # Evaluate for Agglomerative Clustering (Complete Linkage)
     evaluate_silhouette_coefficient("Agglomerative Clustering (Complete Linkage)", __
     cluster_labels_agglomerative_complete, reduced_feats)
     # Evaluate for Agglomerative Clustering (Group Average Linkage)
     evaluate_silhouette_coefficient("Agglomerative Clustering (Group Average_
      Linkage)", cluster labels agglomerative average, reduced feats)
     # Evaluate for Agglomerative Clustering (Ward's Linkage)
     evaluate_silhouette_coefficient("Agglomerative Clustering (Ward's Linkage)", __
      ⇔cluster_labels_agglomerative_ward, reduced_feats)
```

```
Silhouette Coefficient for K-means (init='k-means++'): 0.9884199500083923
        Silhouette Coefficient for Bisecting K-means: 0.9876362681388855
        Silhouette Coefficient for Spectral Clustering: -0.9139062762260437
        Silhouette Coefficient for Agglomerative Clustering (Single Linkage):
        0.9877052903175354
        Silhouette Coefficient for Agglomerative Clustering (Complete Linkage):
        0.9879322052001953
        Silhouette Coefficient for Agglomerative Clustering (Group Average Linkage):
        0.9876362681388855
        Silhouette Coefficient for Agglomerative Clustering (Ward's Linkage):
        0.9884199500083923
[]: # Collecting Fowlkes-Mallows scores for each method
          method_scores = {
                  "K-means (init='random')": fowlkes_mallows_score(true_labels,_
            ⇔cluster_labels),
                  "K-means (init='k-means++')": fowlkes_mallows_score(true_labels,_
            ⇔cluster_labels_pp),
                  "Bisecting K-means": fowlkes_mallows_score(true_labels,_
            ⇔cluster_labels_bisecting),
                  "Spectral Clustering": fowlkes_mallows_score(true_labels,_
            ⇔cluster labels spectral),
                  "Agglomerative (Single Linkage)": fowlkes_mallows_score(true_labels,_
            ⇔cluster_labels_agglomerative_single),
                  "Agglomerative (Complete Linkage)": fowlkes_mallows_score(true_labels, __
            ⇒cluster_labels_agglomerative_complete),
                  "Agglomerative (Group Average Linkage)": fowlkes mallows score(true labels,
            →cluster_labels_agglomerative_average),
                  "Agglomerative (Ward's Linkage)": fowlkes_mallows_score(true_labels,_
            Graph of the state of the 
          }
          # Sorting the methods based on their Fowlkes-Mallows scores
          sorted_methods = sorted(method_scores.items(), key=lambda x: x[1], reverse=True)
          # Print the ranked methods
          print("Ranking based on Fowlkes-Mallows index:")
          for rank, (method, score) in enumerate(sorted_methods, start=1):
                  print(f"{rank}. {method}: {score}")
        Ranking based on Fowlkes-Mallows index:
         1. Agglomerative (Single Linkage): 0.5018152540885414
        2. K-means (init='random'): 0.5010296961472338
        3. Bisecting K-means: 0.5010296961472338
        4. Agglomerative (Group Average Linkage): 0.5010296961472338
```

Silhouette Coefficient for K-means (init='random'): 0.9876362681388855

5. Agglomerative (Complete Linkage): 0.50024291569637

```
6. K-means (init='k-means++'): 0.49947582346036817. Agglomerative (Ward's Linkage): 0.4994758234603681
```

8. Spectral Clustering: 0.35255621518337577

```
[]: # Collecting Silhouette Coefficient scores for each method
    method_silhouette_scores = {
         "K-means (init='random')": silhouette_score(reduced_feats, cluster_labels),
        "K-means (init='k-means++')": silhouette_score(reduced_feats,_
      ⇔cluster_labels_pp),
         "Bisecting K-means": silhouette_score(reduced_feats,__
      ⇔cluster_labels_bisecting),
         "Spectral Clustering": silhouette_score(reduced_feats,__
      ⇔cluster_labels_spectral),
         "Agglomerative (Single Linkage)": silhouette_score(reduced_feats,_
      ⇔cluster_labels_agglomerative_single),
         "Agglomerative (Complete Linkage)": silhouette_score(reduced_feats, ___
      ⇒cluster_labels_agglomerative_complete),
         "Agglomerative (Group Average Linkage)": silhouette_score(reduced_feats,
      ⇔cluster_labels_agglomerative_average),
         "Agglomerative (Ward's Linkage)": silhouette_score(reduced_feats,_
      ⇒cluster_labels_agglomerative_ward),
     # Sorting the methods based on their Silhouette Coefficient scores
    sorted_methods_silhouette = sorted(method_silhouette_scores.items(), key=lambda_
      # Print the ranked methods
    print("Ranking based on Silhouette Coefficient:")
    for rank, (method, score) in enumerate(sorted_methods_silhouette, start=1):
        print(f"{rank}. {method}: {score}")
```

Ranking based on Silhouette Coefficient:

- 1. K-means (init='k-means++'): 0.9884199500083923
- 2. Agglomerative (Ward's Linkage): 0.9884199500083923
- 3. Agglomerative (Complete Linkage): 0.9879322052001953
- 4. Agglomerative (Single Linkage): 0.9877052903175354
- 5. K-means (init='random'): 0.9876362681388855
- 6. Bisecting K-means: 0.9876362681388855
- 7. Agglomerative (Group Average Linkage): 0.9876362681388855
- 8. Spectral Clustering: -0.9139062762260437