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*Algorithm 1: Connecting Pairs of Persons (Sumiran)
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- *Algorithm 2: Greedy Approach to Hamiltonian Problem (Qasim)
- *Algorithm 3: Ensuring Convenient Schedules (Alex and Max)

Algorithm 1: Connecting Pairs of Persons

Pseudocode:

- Start at the beginning of the array.
- Check if the adjacent element is one of the pairs
- If so move on to the adjacent to the next element
- If not find an element in the array that is less than or more than one
- Swap elements

Python Implementation:

def let_partner_hold_hands(array):

```
k = []
for i in range(len(array)-1):
#check if the adjacent element is one below or after
    if abs(array[i]-array[i+1])!= 1:
        for j in range(i+2, len(array)-1):
            if abs(array[j]-array[i])==1:
                array[i+1], array[j] = array[j], array[i+1]

# Add an element in our switch array
        k.append(i+1)
    else:
        i = i + 1
    return k
# test case
test_arr = [0,2,1,3]
print(let_partner_hold_hands(test_arr))
```

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E	Efficiency analysis	
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d	ef furtion (ar):	
	K=[]	0(1)
	for i in range (len (array)-1):	0(n)
	if abs(array [i] -array [i+1]) = 1:	0(1)
	for i in range (i+2, len (array)-1):	o(n-2)
	if abs(aray[i])==1;	0(1)
	array (i+1), array [j] = array [j], array [i+2]	0(1)
	K-append (i+1)	0(1)
	return K	
		1
	the state of the s	
=) Tota effeciency	
) O(1) + O(n).O(1).O(n-2).O(1).O(1)+O(1)	
	$= 0(1) + 0(n^2-2n) + 0(1)$	
	$=) O(n^2-2n)$	
	proving efficiency:-	
	$\lim_{n \to \infty} n^2 - 2n = \lim_{n \to \infty} 1 - 2 = 1$	
	$\lim_{n\to\infty} \frac{n^2-2n}{n^2} = \lim_{n\to\infty} 1-\frac{2}{n} \approx 1-0=1$	
	since the limit converges the algorithm has O(n2) ef	Field.

Algorithm 2: Greedy Approach to Hamiltonian Problem

Pseudocode

- Function: find_preferred_starting_city(city_distances, fuel, mpg)
 Input:
 - city distances: an array of distances between consecutive cities
 - fuel: an array of available fuel at each city
 - mpg: miles per gallon the car can travel with 1 unit of fuel

Output:

- index of the preferred starting city
- 2. Initialize variables:
 - n = length of city distances (number of cities)
 - total fuel needed = 0
 - total fuel available = 0
 - current fuel = 0
 - start_city = 0
- 3. Iterate through each city (index i from 0 to n-1):
 - fuel from city i = fuel[i] * mpg (total miles the car can drive from fuel at city i)
 - fuel_needed_to_next_city = city_distances[i] (miles needed to reach the next city)
 - current_fuel = current_fuel + fuel_from_city_i fuel_needed_to_next_city
 - If current fuel < 0:
 - Set start city = i + 1 (we cannot start from this city, so move to the next one)
 - Reset current_fuel to 0
 - total fuel needed = total fuel needed + fuel needed to next city
 - total fuel available = total fuel available + fuel from city i
- 4. If total fuel available < total fuel needed:
 - Return -1 (no valid starting city exists, but the problem guarantees one)
- 5. Return start_city

Explanation: We need to find the city where we can start and visit all cities, returning to the starting city with enough fuel.

Greedy approach: Traverse through each city and track the fuel availability and fuel requirements. If at any point the car doesn't have enough fuel to proceed, mark the next city as a potential starting point. Once the loop finishes, the last start_city will be the valid starting city.

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Time Complexity: The algorithm iterates through all the cities exactly once, making it an O(n) algorithm, where n is the number of cities. Since the document requires the efficiency class, this is O(n).

Python Implementation

```
def find preferred starting city(city distances, fuel, mpg):
  n = len(city distances)
  total fuel needed = 0
  total fuel available = 0
  current fuel = 0
  start_city = 0
  for i in range(n):
     # Calculate the miles the car can travel from the fuel at city i
     fuel from city i = fuel[i] * mpg
     # Calculate the distance to the next city
     fuel_needed_to_next_city = city_distances[i]
     # Update current fuel after moving to the next city
     current fuel += fuel from city i - fuel needed to next city
     # If current fuel is negative, we cannot start from this city
     if current fuel < 0:
       start city = i + 1
       current fuel = 0
     # Track total fuel availability and total fuel needed
     total fuel needed += fuel needed to next city
     total fuel available += fuel from city i
  # If the total available fuel is less than the total needed, return -1 (no valid starting point)
  if total fuel available < total fuel needed:
     return -1
  # Return the preferred starting city
  return start city
# Sample Input
city_distances = [5, 25, 15, 10, 15]
fuel = [1, 2, 1, 0, 3]
mpg = 10
# Call the function
```

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preferred_starting_city = find_preferred_starting_city(city_distances, fuel, mpg)
print(f"The preferred starting city is city {preferred_starting_city}")

Algorithm 3: Ensuring Convenient Schedules

Pseudocode:

Function: find_meeting_slots(busy_schedules, working_periods, duration) Input:

busy schedules: 2D array of busy times for each person

working_periods: List of earliest and latest available times for each person

duration: Minimum meeting duration in minutes

Output:

List of available meeting slots in HH:MM format

Set earliest_start = latest available start time from working_periods Set latest_end = earliest available end time from working_periods Combine and sort all busy schedules into combined busy

Find free slots:

Initialize last_end = earliest_start

For each interval in combined_busy:

If there's enough gap between last_end and interval start, save it as a free slot

Update last_end to the max of last_end and interval end

Check for a final free slot between last end and latest end

Return the free slots in HH:MM format

Python Implementation:

```
def convert_time_to_minutes(time_str):
  hours, minutes = map(int, time_str.split(':'))
  return hours * 60 + minutes

def convert_minutes_to_time(minutes):
  hours = minutes // 60
  mins = minutes % 60
```

```
return f"{hours:02d}:{mins:02d}"
def merge intervals(intervals):
  intervals.sort(key=lambda x: x[0])
  merged = []
  for interval in intervals:
     if not merged or interval[0] > merged[-1][1]:
       merged.append(interval)
     else:
       merged[-1][1] = max(merged[-1][1], interval[1])
  return merged
def find free intervals(busy intervals, daily bounds):
  earliest, latest = daily bounds
  busy intervals = [[earliest, earliest]] + busy intervals + [[latest, latest]]
   busy intervals = merge intervals(busy intervals)
  free intervals = []
  for i in range(1, len(busy intervals)):
     start_free = busy_intervals[i - 1][1]
     end free = busy intervals[i][0]
     if start free < end free:
       free intervals.append([start_free, end_free])
  return free intervals
def intersect intervals(intervals a, intervals b):
  i, j = 0, 0
  intersection = []
  while i < len(intervals a) and j < len(intervals b):
     start = max(intervals a[i][0], intervals b[j][0])
     end = min(intervals a[i][1], intervals b[j][1])
     if start < end:
       intersection.append([start, end])
     if intervals a[i][1] < intervals b[j][1]:
       i += 1
     else:
       i += 1
  return intersection
def find common available times(schedules, daily active periods, meeting duration):
  free times list = []
  for schedule, daily bounds in zip(schedules, daily active periods):
     busy_intervals = [[convert_time_to_minutes(s), convert_time_to_minutes(e)] for s, e in
schedule]
```

```
daily bounds = [convert time to minutes(daily bounds[0]),
convert time to minutes(daily bounds[1])]
     free intervals = find free intervals(busy intervals, daily bounds)
     free times list.append(free intervals)
  common available times = free times list[0]
  for i in range(1, len(free times list)):
     common available times = intersect intervals(common available times, free times list[i])
  meeting duration minutes = meeting duration
  result = ∏
  for start, end in common available times:
    if end - start >= meeting duration minutes:
       result.append([convert minutes to time(start), convert minutes to time(end)])
  return result
# Sample Input
person1 schedule = [['7:00', '8:30'], ['12:00', '13:00'], ['16:00', '18:00']]
person1 daily act = ['9:00', '19:00']
person2 schedule = [['9:00', '10:30'], ['12:20', '13:30'], ['14:00', '15:00'], ['16:00', '17:00']]
person2_daily_act = ['9:00', '18:30']
meeting duration = 30
# Function Call
schedules = [person1 schedule, person2 schedule]
daily active periods = [person1 daily act, person2 daily act]
available times = find common available times(schedules, daily active periods,
meeting duration)
print(available times)
```

Time Complexity: For each of the N persons, their M busy intervals are sorted. Sorting each list of intervals takes O(MlogM) time. Therefore, the time complexity is

O(N*MlogM).