



Module 08

I Sengupta &
P P Das

Objectives &
Outline

Optimization
Issues

Basic Block

Control Flow
Graph

Value
Numbering
Extensional Handling

Extended
Basic Blocks

Module 08: CS31003: Compilers: Control Flow Graph and Local Optimization

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Module Objectives

Module 08

I Sengupta &
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Objectives &
Outline

Optimization
Issues

Basic Block

Control Flow
Graph

Value
Numbering

Extensional Handling

Extended
Basic Blocks

- What is code optimization and why is it needed?
- Types of optimizations
- Basic blocks and control flow graphs
- Local optimizations
- Building a control flow graph
- Directed acyclic graphs and value numbering



Module Outline

Module 08

I Sengupta &
P P Das

Objectives &
Outline

Optimization
Issues

Basic Block

Control Flow
Graph

Value
Numbering

Extensional Handling

Extended
Basic Blocks

1 Objectives & Outline

2 Optimization Issues

3 Basic Block

4 Control Flow Graph

5 Value Numbering in Basic Blocks
• Extensional Handling

6 Extended Basic Blocks



Machine-independent Code Optimization

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P P Das

Objectives &
Outline

Optimization
Issues

Basic Block

Control Flow
Graph

Value
Numbering
Extensional Handling

Extended
Basic Blocks

- Intermediate code generation process introduces many inefficiencies
 - Extra copies of variables, using variables instead of constants, repeated evaluation of expressions, etc.
- Code optimization removes such inefficiencies and improves code
- Improvement may be time, space, or power consumption
- It changes the structure of programs, sometimes of beyond recognition
 - Inlines functions, unrolls loops, eliminates some programmer-defined variables, etc.
- Code optimization consists of a bunch of heuristics and percentage of improvement depends on programs (may be zero also)
- Optimizations may be classified as *local* and *global*



Example: Vector Product

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Objectives &
Outline

Optimization
Issues

Basic Block

Control Flow
Graph

Value
Numbering

Extensional Handling

Extended
Basic Blocks

```
int a[5], b[5], c[5];
int i, n = 5;

for(i = 0; i < n; i++) {
    if (a[i] < b[i])
        c[i] = a[i] * b[i];
    else
        c[i] = 0;
}
return;
```

```
// int i, n = 5;
100: t1 = 5
101: n = t1
// for(i = 0; i < n; i++) {
102: t2 = 0
103: i = t2
104: if i < n goto 109 // T
105: goto 129 // F
106: t3 = i
107: i = i + 1
108: goto 104
// if (a[i] < b[i]) {
109: t4 = 4 * i
110: t5 = a[t4]
111: t6 = 4 * i
112: t7 = b[t6]
113: if t5 < t7 goto 115 // T
114: goto 124 // F
```

```
// c[i] = a[i] * b[i];
115: t8 = 4 * i
116: t9 = c + t8
117: t10 = 4 * i
118: t11 = a[t10]
119: t12 = 4 * i
120: t13 = b[t12]
121: t14 = t11 * t13
122: *t9 = t14
123: goto 106 // next
// c[i] = 0;
124: t15 = 4 * i
125: t16 = c + t15
126: t17 = 0
127: *t16 = t17
// }
128: goto 106 // for
// return;
129: return
```



Peep-hole Optimization

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Objectives &
Outline

Optimization
Issues

Basic Block

Control Flow
Graph

Value
Numbering

Extensional Handling

Extended
Basic Blocks

- Eliminating redundant instructions
- Eliminating local def-use of temporary
- Eliminating unreachable code
- Eliminating jumps over jumps
- Algebraic simplifications
- Strength reduction



Example: Vector Product: Peep-hole Optimization

Module 08

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Objectives &
Outline

Optimization
Issues

Basic Block

Control Flow
Graph

Value
Numbering

Extensional Handling

Extended
Basic Blocks

Peep-hole optimization and potential removals are marked. Recomputed quad numbers are shown:

```
// int i, n = 5;
100: t1 = 5 XXX
100: 101: n = 5 <=== def-use
      // for(i = 0; i < n; i++) {
102: t2 = 0 XXX
101: 103: i = 0 <=== def-use
102: 104: if i < n goto 109 // true exit
103: 105: goto 129 // false exit
      106: t3 = i <=== Unused XXX
104: 107: i = i + 1
105: 108: goto 104
      // if (a[i] < b[i]) {
106: 109: t4 = 4 * i // strength reduction
107: 110: t5 = a[t4]
108: 111: t6 = 4 * i // strength reduction
109: 112: t7 = b[t6]
110: 113: if t5 >= t7 goto 124 <=== Jump-over-Jmp
114: goto 115 XXX
```

```
// c[i] = a[i] * b[i];
111: 115: t8 = 4 * i // strength reduction
112: 116: t9 = c + t8
113: 117: t10 = 4 * i // strength reduction
114: 118: t11 = a[t10]
115: 119: t12 = 4 * i // strength reduction
116: 120: t13 = b[t12]
117: 121: t14 = t11 * t13
118: 122: *t9 = t14
119: 123: goto 106 // next exit
      // c[i] = 0;
120: 124: t15 = 4 * i // strength reduction
121: 125: t16 = c + t15
126: t17 = 0 XXX
122: 127: *t16 = 0 <=== def-use
      // } // End of for loop
123: 128: goto 106
      // return;
124: 129: return
```



Example: Vector Product: Peep-hole Optimization

Module 08

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P P Das

Objectives &
Outline

Optimization
Issues

Basic Block

Control Flow
Graph

Value
Numbering

Extensional Handling

Extended
Basic Blocks

On removal and reduction:

```
100: n = 5
101: i = 0
102: if i < n goto 106
103: goto 124
104: i = i + 1
105: goto 102
106: t4 = i << 2
107: t5 = a[t4]
108: t6 = i << 2
109: t7 = b[t6]
110: if t5 >= t7 goto 120
```

```
111: t8 = i << 2
112: t9 = c + t8
113: t10 = i << 2
114: t11 = a[t10]
115: t12 = i << 2
116: t13 = b[t12]
117: t14 = t11 * t13
118: *t9 = t14
119: goto 104
120: t15 = i << 2
121: t16 = c + t15
122: *t16 = 0
123: goto 104
124: return
```




Local Optimization

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I Sengupta &
P P Das

Objectives &
Outline

Optimization
Issues

Basic Block

Control Flow
Graph

Value
Numbering

Extensional Handling

Extended
Basic Blocks

Local optimization: within basic blocks

- Local Common Sub-Expression (LCSE) elimination
- Constant propagation and constant folding
- Eliminating local def-use of temporary
- Dead-code elimination
- Reordering computations using algebraic laws
- Eliminating redundant instructions



Global Optimization

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P P Das

Objectives &
Outline

Optimization
Issues

Basic Block

Control Flow
Graph

Value
Numbering
Extensional Handling

Extended
Basic Blocks

Global optimization: on whole procedures/programs

- Global Common Sub-Expression (GCSE) elimination
- Constant propagation and constant folding
- Eliminating unreachable code
- Eliminating jumps over jumps
- Eliminating jumps to jumps (chain of jumps)
- Eliminating def-use of temporary
- Eliminating redundant instructions
- Loop invariant code motion
- Partial redundancy elimination
- Loop unrolling and function inlining
- Vectorization and Concurrentization



Basic Blocks and Control-Flow Graphs

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P P Das

Objectives &
Outline

Optimization
Issues

Basic Block

Control Flow
Graph

Value
Numbering

Extensional Handling

Extended
Basic Blocks

- **Basic Blocks** (BB) are sequences of intermediate code with a *single entry* and a *single exit*
- **Control Flow Graphs** (CFG) show control flow among basic blocks
- Basic blocks are represented as **Directed Acyclic Graphs** (DAGs), which are in turn represented using the value-numbering method applied on quadruples
- Optimizations on basic blocks



Example of Basic Blocks and Control Flow Graph

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Objectives &
Outline

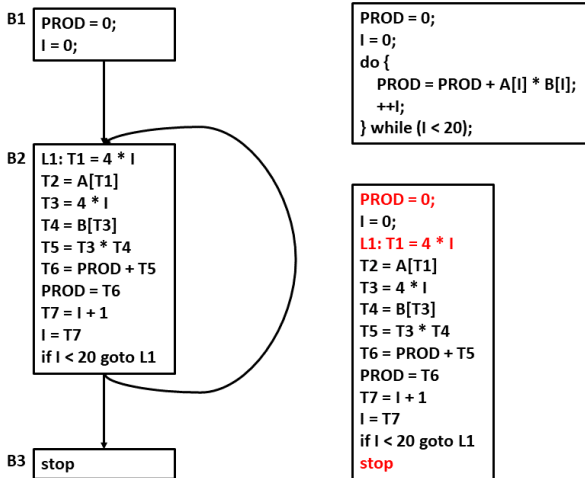
Optimization
Issues

Basic Block

Control Flow
Graph

Value
Numbering
Extensional Handling

Extended
Basic Blocks





Algorithm for Partitioning into Basic Blocks

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Objectives &
Outline

Optimization
Issues

Basic Block

Control Flow
Graph

Value
Numbering

Extensional Handling

Extended
Basic Blocks

- ① Determine the set of *leaders*, the first statements of basic blocks
 - The first statement is a leader
 - Any statement which is the target of a conditional or unconditional *goto* is a leader
 - Any statement which immediately follows a *conditional goto* is a leader
- ② A leader and all statements which follow it upto but not including the next leader (or the end of the procedure), is the basic block corresponding to that leader
- ③ Any statements, not placed in a block, can never be executed, and may now be removed, if desired



Example of Basic Blocks and CFG

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Objectives &
Outline

Optimization
Issues

Basic Block

Control Flow
Graph

Value
Numbering
Extensional Handling

Extended
Basic Blocks

B1
PROD = 0;
I = 0;

B2
L1: T1 = 4 * I
T2 = A[T1]
T3 = 4 * I
T4 = B[T3]
T5 = T3 * T4
T6 = PROD + T5
PROD = T6
T7 = I + 1
I = T7
if I < 20 goto L1

B3
stop

```
PROD = 0;  
I = 0;  
do {  
    PROD = PROD + A[I] * B[I];  
    ++I;  
} while (I < 20);
```

```
PROD = 0;  
I = 0;  
L1: T1 = 4 * I  
T2 = A[T1]  
T3 = 4 * I  
T4 = B[T3]  
T5 = T3 * T4  
T6 = PROD + T5  
PROD = T6  
T7 = I + 1  
I = T7  
if I < 20 goto L1  
stop
```



Control Flow Graph

Module 08

I Sengupta &
P P Das

Objectives &
Outline

Optimization
Issues

Basic Block

Control Flow
Graph

Value
Numbering
Extensional Handling

Extended
Basic Blocks

- The nodes of the CFG are basic blocks
- One node is distinguished as the initial node
- There is a directed edge $B1 \rightarrow B2$, if B2 can immediately follow B1 in some execution sequence:
 - There is a conditional or unconditional jump from the last statement of B1 to the first statement of B2, or
 - B2 immediately follows B1 in the order of the program, and B1 does not end in an unconditional jump
- A basic block is represented as a record consisting of
 - 1 a count of the number of quads in the block
 - 2 a pointer to the leader of the block
 - 3 pointers to the predecessors of the block
 - 4 pointers to the successors of the block

Note: *Jump statements point to basic blocks and not quads so as to make code movement easy*



Example: Vector Product: Control Flow Graph

Module 08

I Sengupta &
P P Das

Objectives &
Outline

Optimization
Issues

Basic Block

Control Flow
Graph

Value
Numbering

Extensional Handling

Extended
Basic Blocks

- 1 First quad of the program
- 2 quad's as target of some goto
- 3 quad's following a conditional goto

```
100: n = 5 [1]
101: i = 0
102: if i < n goto 106 [2]
103: goto 124 [3]
104: i = i + 1 [2]
105: goto 102
106: t4 = 4 * i [2]
107: t5 = a[t4]
108: t6 = 4 * i
109: t7 = b[t6]
110: if t5 >= t7 goto 120
```

```
111: t8 = 4 * i [3]
112: t9 = c + t8
113: t10 = 4 * i
114: t11 = a[t10]
115: t12 = 4 * i
116: t13 = b[t12]
117: t14 = t11 * t13
118: *t9 = t14
119: goto 104
120: t15 = 4 * i [2]
121: t16 = c + t15
122: *t16 = 0
123: goto 104
124: return [2]
```




Example: Vector Product: Control Flow Graph

Module 08

I Sengupta &
P P Das

Objectives &
Outline

Optimization
Issues

Basic Block

Control Flow
Graph

Value
Numbering
Extensional Handling

Extended
Basic Blocks

Control Flow Graph is shown below:

```
// Block B1
0: 100: n = 5
1: 101: i = 0
   :    goto B2 [Fall through]

// Block B2
0: 102: if i < n goto B4 [106]
   : 103: goto B7 [124]

// Block B3
0: 104: i = i + 1
   : 105: goto B2 [102]

// Block B4
0: 106: t4 = 4 * i
1: 107: t5 = a[t4]
2: 108: t6 = 4 * i
3: 109: t7 = b[t6]
4: 110: if t5 >= t7 goto B6 [120]
   :    goto B5 [Fall through]
```

```
// Block B5
0: 111: t8 = 4 * i
1: 112: t9 = c + t8
2: 113: t10 = 4 * i
3: 114: t11 = a[t10]
4: 115: t12 = 4 * i
5: 116: t13 = b[t12]
6: 117: t14 = t11 * t13
7: 118: *t9 = t14
   : 119: goto B3 [104]
```

```
// Block B6
0: 120: t15 = 4 * i
1: 121: t16 = c + t15
2: 122: *t16 = 0
   : 123: goto B3 [104]
```

```
// Block B7
0: 124: return
```

There is no unreachable quad to remove.



Example: Vector Product: Control Flow Graph

Graphically the CFG looks like:

```
// Block B1
0: n = 5
1: i = 0
: goto B2

// Block B2
0: if i < n goto B4
: goto B7

// Block B7
0: return

// Block B4
0: t4 = 4 * i
1: t5 = a[t4]
2: t6 = 4 * i
3: t7 = b[t6]
4: if t5 >= t7 goto B6
: goto B5

// Block B5
0: t8 = 4 * i
1: t9 = c + t8
2: t10 = 4 * i
3: t11 = a[t10]
4: t12 = 4 * i
5: t13 = b[t12]
6: t14 = t11 * t13
7: *t9 = t14
: goto B3

// Block B6
0: t15 = 4 * i
1: t16 = c + t15
2: *t16 = 0
: goto B3

// Block B3
0: i = i + 1
: goto B2
```



Optimization of Basic Blocks

Directed Acyclic Graph (DAG) Representation

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Objectives &
Outline

Optimization
Issues

Basic Block

Control Flow
Graph

Value
Numbering

Extensional Handling

Extended
Basic Blocks

```
1: a = 10
2: b = 4 * a
3: t1 = i * j
4: c = t1 + b
5: t2 = 15 * a
6: d = t2 * c
7: e = i
8: t3 = e * j
9: t4 = i * a
10: c = t3 + t4
```



Optimization of Basic Blocks

Directed Acyclic Graph (DAG) Representation

Module 08

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P P Das

Objectives &
Outline

Optimization
Issues

Basic Block

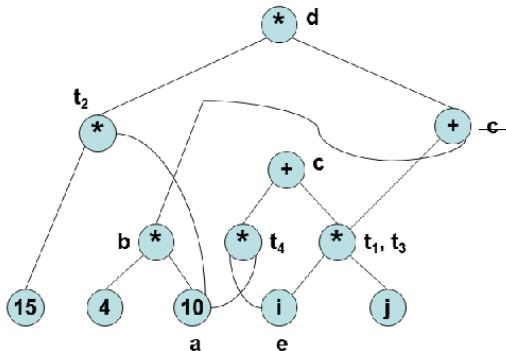
Control Flow
Graph

Value
Numbering

Extensional Handling

Extended
Basic Blocks

```
1: a = 10
2: b = 4 * a
3: t1 = i * j
4: c = t1 + b
5: t2 = 15 * a
6: d = t2 * c
7: e = i
8: t3 = e * j
9: t4 = i * a
10: c = t3 + t4
```





Value Numbering in Basic Blocks

Module 08

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P P Das

Objectives &
Outline

Optimization
Issues

Basic Block

Control Flow
Graph

Value
Numbering

Extensional Handling

Extended
Basic Blocks

- A simple way to represent DAGs is via *value-numbering*
- While searching DAGs represented using pointers etc., is inefficient, *value-numbering* uses hash tables and hence is very efficient
- Central idea is to assign numbers (called value numbers) to expressions in such a way that two expressions receive the same number if the compiler can prove that they are equal for all possible program inputs
- We assume quadruples with binary or unary operators
- The algorithm uses three tables indexed by appropriate hash values:
HashTable, *ValnumTable*, and *NameTable*



Value Numbering in Basic Blocks

Module 08

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Objectives &
Outline

Optimization
Issues

Basic Block

Control Flow
Graph

**Value
Numbering**

Extensional Handling

Extended
Basic Blocks

- Can be used to eliminate common sub-expressions, do constant folding, and constant propagation in basic blocks
- Can take advantage of commutativity of operators, addition of zero, and multiplication by one



Data Structures for Value Numbering

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Objectives &
Outline

Optimization
Issues

Basic Block

Control Flow
Graph

Value
Numbering

Extensional Handling

Extended
Basic Blocks

In the field *Namelist*, first name is the defining occurrence and replaces all other names with the same value number with itself (or its constant value)

ValueNumber Table (VNT) Entry

Indexed by Name Hash Value

Name	Value Number
------	--------------

Name Table (NT) Entry

Indexed by Value Number

Name List	Constant Value	Constant Flag
-----------	----------------	---------------

Hash Table (HT) Entry

Indexed by Expression Hash Value

Expression	Value Number
------------	--------------



Example of Value Numbering

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Objectives &
Outline

Optimization
Issues

Basic Block

Control Flow
Graph

Value
Numbering

Extensional Handling

Extended
Basic Blocks

HLL Program	Quad's before value-numbering	Quad's after value-numbering
a = 10	01. a = 10	a = 10
b = 4 * a	02. b = 4 * a	b = 40
c = i * j + b	03. t1 = i * j	t1 = i * j
d = 15 * a * c	04. c = t1 + b	c = t1 + 40
e = i	05. t2 = 15 * a	t2 = 150
c = e * j + i * a	06. d = t2 * c	d = 150 * c
	07. e = i	e = i
	08. t3 = e * j	t3 = i * j
	09. t4 = i * a	t4 = i * 10
	10. c = t3 + t4	c = t1 + t4
		Quad's 5 & 8 can be deleted



Example of Value Numbering

Module 08

I Sengupta &
P P Das

Objectives &
Outline

Optimization
Issues

Basic Block

Control Flow
Graph

Value
Numbering

Extensional Handling

Extended
Basic Blocks

VN Table	
Name	VN
a	1
b	2
i	3
j	4
t1	5
c	6, 10
t2	7
d	8
e	3
t3	5
t4	9

Name Table		
Index	Name	Val
1	a	10
2	b	40
3	i, e	
4	j	
5	t1, t3	
6	c	
7	t2	150
8	d	
9	t4	
10	c	

Hash Table	
Expr	VN
i * j	5
t1 + 40	6
150 * c	8
i * 10	9
t1 + t4	10

01. a = 10	a = 10
02. b = 4 * a	b = 40
03. t1 = i * j	t1 = i * j
04. c = t1 + b	c = t1 + 40
05. t2 = 15 * a	t2 = 150
06. d = t2 * c	d = 150 * c
07. e = i	e = i
08. t3 = e * j	t3 = i * j
09. t4 = i * a	t4 = i * 10
10. c = t3 + t4	c = t1 + t4



Running the algorithm through the example (1)

Module 08

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P P Das

Objectives &
Outline

Optimization
Issues

Basic Block

Control Flow
Graph

Value
Numbering

Extensional Handling

Extended
Basic Blocks

① $a = 10 :$

- a is entered into *ValnumTable* (with a *vn* of 1, say) and into *NameTable* (with a constant value of 10)

② $b = 4 * a :$

- a is found in *ValnumTable*, its constant value is 10 in *NameTable*
 - We have performed *constant propagation*
 - $4 * a$ is evaluated to 40, and the quad is rewritten
 - We have now performed *constant folding*
 - b is entered into *ValnumTable* (with a *vn* of 2) and into *NameTable* (with a constant value of 40)

③ $t1 = i * j :$

- i and j are entered into the two tables with new *vn* (as above), but with no constant value
- $i * j$ is entered into *HashTable* with a new *vn*
- $t1$ is entered into *ValnumTable* with the same *vn* as $i * j$



Running the algorithm through the example (2)

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P P Das

Objectives &
Outline

Optimization
Issues

Basic Block

Control Flow
Graph

Value
Numbering

Extensional Handling

Extended
Basic Blocks

- ④ Similar actions continue till $e = i$
 - e gets the same vn as i
- ⑤ $t3 = e * j$:
 - e and i have the same vn
 - hence, $e * j$ is detected to be the same as $i * j$
 - since $i * j$ is already in the HashTable, we have found a *common subexpression*
 - from now on, all uses of $t3$ can be replaced by $t1$
 - quad $t3 = e * j$ can be deleted
- ⑥ $c = t3 + t4$:
 - $t3$ and $t4$ already exist and have vn
 - $t3 + t4$ is entered into *HashTable* with a new vn
 - this is a reassignment to c
 - c gets a different vn , same as that of $t3 + t4$
- ⑦ Quads are renumbered after deletions



Example of Value Numbering

Module 08

I Sengupta &
P P Das

Objectives &
Outline

Optimization
Issues

Basic Block

Control Flow
Graph

Value
Numbering

Extensional Handling

Extended
Basic Blocks

If the same code snippet is translated by our automated scheme, we shall get a more verbose 3 address code. Here we show that this auto-translated code too gets optimized to the same as before

HLL Program	Quad's before value-numbering	Quad's after value-numbering
<pre>a = 10 b = 4 * a c = i * j + b d = 15 * a * c e = i c = e * j + i * a</pre>	<pre>01. a = 10 02. t1 = 4 * a 03. b = t1 04. t2 = i * j 05. t3 = t2 + b 06. c = t3 07. t4 = 15 * a 08. t5 = t4 * c 09. d = t5 10. e = i 11. t6 = e * j 12. t7 = i * a 13. t8 = t6 + t7 14. c = t8</pre>	<pre>01. a = 10 02. t1 = 40 03. b = 40 04. t2 = i * j 05. t3 = t2 + 40 06. c = t3 07. t4 = 150 08. t5 = 150 * t3 09. d = t5 10. e = i 11. t6 = i * j 12. t7 = i * 10 13. t8 = t2 + t7 14. c = t8</pre> <ul style="list-style-type: none">• Quad's 2, 6, 7 & 11 can be deleted• Copy can be propagated (in reverse) to eliminate t5 (between 8 & 9) and t8 (between 13 & 14)• Note that e in 10 cannot be removed as it may be used outside the block



Example of Value Numbering

Module 08

I Sengupta &
P P Das

Objectives &
Outline

Optimization
Issues

Basic Block

Control Flow
Graph

Value
Numbering

Extensional Handling

Extended
Basic Blocks

VN Table	
Name	VN
a	1
t1	2
b	2
i	3
j	4
t2	5
t3	6
c	6
t4	7
t5	8
d	8
e	3
t6	5
t7	9
t8	10
c	10

Hash Table	
Expr	VN
$i * j$	5
$t2 + 40$	6
$150 * t3$	8
$i * 10$	9
$t6 + t7$	10

Name Table		
Index	Name	Val
1	a	10
2	t1, b	40
3	i, e	
4	j	
5	t2, t6	
6	t3, c	
7	t4	150
8	t5, d	
9	t7	
10	t8, c	



Example: Vector Product: LCSE

Module 08

I Sengupta &
P P Das

Objectives &
Outline

Optimization
Issues

Basic Block

Control Flow
Graph

Value
Numbering

Extensional Handling

Extended
Basic Blocks

We need to perform LCSE step for blocks:

```
B4:
// if (a[i] < b[i]) {
// Block B4
0: t4 = 4 * i
1: t5 = a[t4]
2: t6 = 4 * i
3: t7 = b[t6]
4: if t5 >= t7 goto B6
   : goto B5
```

and

```
B5:
// c[i] = a[i] * b[i];
// Block B5
0: t8 = 4 * i
1: t9 = c + t8
2: t10 = 4 * i
3: t11 = a[t10]
4: t12 = 4 * i
5: t13 = b[t12]
6: t14 = t11 * t13
7: *t9 = t14
   : goto B3
```



Example: Vector Product: LCSE (Block B4)

Module 08

I Sengupta &
P P Das

Objectives &
Outline

Optimization
Issues

Basic Block

Control Flow
Graph

Value
Numbering

Extensional Handling

Extended
Basic Blocks

VN Table	
Name	VN
i	1
t4	2
t5	3
t6	2
t7	4

Hash Table	
Expr	VN
4 * i	2
a[t4]	3
b[t6]	2

Name Table			
Index	Name	Val	Flag
1	i	?	No
2	t4, t6	?	No
3	t5	?	No
4	t7	?	No

Input:

```
// Block B4
0: t4 = 4 * i
1: t5 = a[t4]
2: t6 = 4 * i
3: t7 = b[t6]
4: if t5 >= t7 goto B6
   : goto B5
```

After LCSE:

```
// Block B4
0: t4 = 4 * i
1: t5 = a[t4]
2: t6 = t4 XXX
3: t7 = b[t4]
4: if t5 >= t7 goto B6
   : goto B5
```

After removal of useless quad's:

```
// Block B4
0: t4 = 4 * i
1: t5 = a[t4]
2: t7 = b[t4]
3: if t5 >= t7 goto B6
   : goto B5
```



Example: Vector Product: LCSE (Block B5)

Module 08

I Sengupta &
P P Das

Objectives &
Outline

Optimization
Issues

Basic Block

Control Flow
Graph

Value
Numbering

Extensional Handling

Extended
Basic Blocks

VN Table	
Name	VN
i	1
t8	2
t9	3
t10	2
t11	4
t12	2
t13	5
t14	6

Hash Table	
Expr	VN
4 * i	2
t11 * t13	6

Name Table			
Index	Name	Val	Flag
1	i	?	No
2	t8, t10, t12	?	No
3	t9	?	No
4	t11	?	No
5	t13	?	No
6	t14	?	No

Input:

```
// Block B5
0: t8 = 4 * i
1: t9 = c + t8
2: t10 = 4 * i
3: t11 = a[t10]
4: t12 = 4 * i
5: t13 = b[t12]
6: t14 = t11 * t13
7: *t9 = t14
: goto B3
```

After LCSE:

```
// Block B5
0: t8 = 4 * i
1: t9 = c + t8
2: t10 = t8 XXX
3: t11 = a[t8]
4: t12 = t8 XXX
5: t13 = b[t8]
6: t14 = t11 * t13
7: *t9 = t14
: goto B3
```

After removal of useless quad's:

```
// Block B5
0: t8 = 4 * i
1: t9 = c + t8
2: t11 = a[t8]
3: t13 = b[t8]
4: t14 = t11 * t13
5: *t9 = t14
: goto B3
```




Example: Vector Product: CFG after LCSE

Module 08

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P P Das

Objectives &
Outline

Optimization
Issues

Basic Block

Control Flow
Graph

Value
Numbering

Extensional Handling

Extended
Basic Blocks

```
// Block B1
0: n = 5
1: i = 0
  : goto B2

// Block B2
0: if i < n goto B4
  : goto B7

// Block B3
0: i = i + 1
  : goto B2

// Block B4
0: t4 = 4 * i
1: t5 = a[t4]
2: t7 = b[t4]
3: if t5 >= t7 goto B6
  : goto B5
```

```
// Block B5
0: t8 = 4 * i
1: t9 = c + t8
2: t11 = a[t8]
3: t13 = b[t8]
4: t14 = t11 * t13
5: *t9 = t14
  : goto B3

// Block B6
0: t15 = 4 * i
1: t16 = c + t15
2: *t16 = 0
  : goto B3

// Block B7
0: return
```



Handling Commutativity etc.

Module 08

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Objectives &
Outline

Optimization
Issues

Basic Block

Control Flow
Graph

Value
Numbering

Extensional Handling

Extended
Basic Blocks

- When a search for an expression $i + j$ in *HashTable* fails, try for $j + i$
- If there is a quad $x = i + 0$, replace it with $x = i$
- Any quad of the type, $y = j * 1$ can be replaced with $y = j$
- After the above two types of replacements, value numbers of x and y become the same as those of i and j , respectively
- Quads whose LHS variables are used later can be marked as *useful*
- All unmarked quads can be deleted at the end



Handling Array References

Module 08

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P P Das

Objectives &
Outline

Optimization
Issues

Basic Block

Control Flow
Graph

Value
Numbering
Extensional Handling

Extended
Basic Blocks

Consider the sequence of quads:

- ❶ $X = A[i]$
 - ❷ $A[j] = Y$: i and j could be the same
 - ❸ $Z = A[i]$: in which case, $A[i]$ is not a common subexpression here
- The above sequence cannot be replaced by: $X = A[i]$; $A[j] = Y$; $Z = X$
 - When $A[j] = Y$ is processed during value numbering, ALL references to array A so far are searched in the tables and are marked KILLED - this kills quad 1 above
 - When processing $Z = A[i]$, killed quads not used for CSE
 - Fresh table entries are made for $Z = A[i]$
 - However, if we know apriori that $i \neq j$, then $A[i]$ can be used for CSE



Handling Pointer References

Module 08

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P P Das

Objectives &
Outline

Optimization
Issues

Basic Block

Control Flow
Graph

Value
Numbering

Extensional Handling

Extended
Basic Blocks

Consider the sequence of quads:

- ❶ $X = *p$
 - ❷ $*q = Y$: p and q could be pointing to the same object
 - ❸ $Z = *p$: in which case, $*p$ is not a common sub-expression here
- The above sequence cannot be replaced by: $X = *p$; $*q = Y$; $Z = X$
 - Suppose no pointer analysis has been carried out
 - p and q can point to *any* object in the basic block
 - Hence, When $*q = Y$ is processed during value numbering, ALL table entries created so far are marked KILLED - this kills quad 1 above as well
 - When processing $Z = *p$, killed quads not used for CSE
 - Fresh table entries are made for $Z = *p$



Handling Pointer References and Procedure Calls

Module 08

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Objectives &
Outline

Optimization
Issues

Basic Block

Control Flow
Graph

Value
Numbering

Extensional Handling

Extended
Basic Blocks

- However, if we know apriori which objects p and q point to, then table entries corresponding to only those objects need to be killed
- Procedure calls are similar
- With no dataflow analysis, we need to assume that a procedure call can modify any object in the basic block
 - changing call-by-reference parameters and global variables within procedures will affect other variables of the basic block as well
- Hence, while processing a procedure call, ALL table entries created so far are marked KILLED
- Sometimes, this problem is avoided by making a procedure call a separate basic block



Extended Basic Blocks

Module 08

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Objectives &
Outline

Optimization
Issues

Basic Block

Control Flow
Graph

Value
Numbering
Extensional Handling

Extended
Basic Blocks

- A sequence of basic blocks B_1, B_2, \dots, B_k , such that B_i is the unique predecessor of B_{i+1} ($i \leq i < k$), and B_1 is either the start block or has no unique predecessor
- Extended basic blocks with shared blocks can be represented as a tree
- Shared blocks in extended basic blocks require scoped versions of tables
- The new entries must be purged and changed entries must be replaced by old entries
- Preorder traversal of extended basic block trees is used



Extended Basic Blocks and their Trees

Module 08

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Objectives &
Outline

Optimization
Issues

Basic Block

Control Flow
Graph

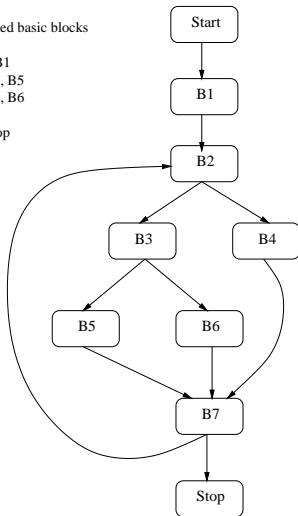
Value
Numbering

Extensional Handling

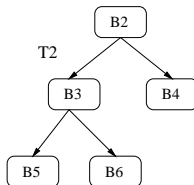
Extended
Basic Blocks

Extended basic blocks

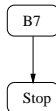
Start, B1
B2, B3, B5
B2, B3, B6
B2, B4
B7, Stop



T1



T2



T3



Value Numbering with Extended Basic Blocks

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Objectives &
Outline

Optimization
Issues

Basic Block

Control Flow
Graph

Value
Numbering
Extensional Handling

Extended
Basic Blocks

```
function visit-ebb-tree(e) // e is a node in the tree
begin
    // From now on, the new names will be entered with a new scope into the tables.
    // When searching the tables, we always search beginning with the current scope
    // and move to enclosing scopes. This is similar to the processing involved with
    // symbol tables for lexically scoped languages
    value-number(e.B);
    // Process the block e.B using the basic block version of the algorithm
    if (e.left  $\neq$  null) then visit-ebb-tree(e.left);
    if (e.right  $\neq$  null) then visit-ebb-tree(e.right);
    remove entries for the new scope from all the tables
    and undo the changes in the tables of enclosing scopes;
end

begin // main calling loop
    for each tree t do visit-ebb-tree(t);
    // t is a tree representing an extended basic block
end
```