



## Module 10

I Sengupta &  
P P Das

Objectives &  
Outline

Issues in  
Register  
Allocation

The Problem

GRA by Usage  
Count

Chaitin's  
Algorithm:  
GRA by Graph  
Coloring

Graph Coloring  
Framework

Example  
Register Spill

# Module 10: CS31003: Compilers: Global Register Allocation

Indranil Sengupta  
Partha Pratim Das

Department of Computer Science and Engineering  
Indian Institute of Technology, Kharagpur

*isg@iitkgp.ac.in*  
*ppd@cse.iitkgp.ac.in*

November 03, 2020



# Module Objectives

## Module 10

I Sengupta &  
P P Das

Objectives &  
Outline

Issues in  
Register  
Allocation

The Problem

GRA by Usage  
Count

Chaitin's  
Algorithm:  
GRA by Graph  
Coloring

Graph Coloring

Framework

Example

Register Spill

- Issues in Global Register Allocation
- The Problem
- Register Allocation based on Usage Counts
- Chaitin's graph coloring based algorithm



# Module Outline

## Module 10

I Sengupta &  
P P Das

Objectives &  
Outline

Issues in  
Register  
Allocation

The Problem

GRA by Usage  
Count

Chaitin's  
Algorithm:  
GRA by Graph  
Coloring

Graph Coloring

Framework

Example

Register Spill

1 Objectives & Outline

2 Issues in Register Allocation

3 The Problem

4 GRA by Usage Count

5 Chaitin's Algorithm: GRA by Graph Coloring

- Graph Coloring
- Framework
- Example
- Register Spill



# Some Issues in Register Allocation (1)

## Module 10

I Sengupta &  
P P Das

Objectives &  
Outline

Issues in  
Register  
Allocation

The Problem

GRA by Usage  
Count

Chaitin's  
Algorithm:  
GRA by Graph  
Coloring

Graph Coloring

Framework

Example

Register Spill

- Which values in a program reside in registers? ([Register Allocation](#))
- In which register? ([Register Assignment](#))
  - The two together are usually loosely referred to as **Register Allocation (RA)**
- What is the unit at the level of which register allocation is done?
  - Typical units are basic blocks, functions and regions
  - RA within basic blocks is called [local RA](#)
  - The other two (functions and regions) are known as [global RA](#)
  - Global RA requires lot more time than local RA



# Some Issues in Register Allocation (2)

## Module 10

I Sengupta &  
P P Das

Objectives &  
Outline

Issues in  
Register  
Allocation

The Problem

GRA by Usage  
Count

Chaitin's  
Algorithm:  
GRA by Graph  
Coloring

Graph Coloring

Framework

Example

Register Spill

- Phase ordering between register allocation and instruction scheduling
- In which register? (register assignment)
  - Performing RA first restricts movement of code during scheduling – *not recommended*
  - Scheduling instructions first cannot handle spill code introduced during RA
    - Requires another pass of scheduling
- Tradeoff between speed and quality of allocation
  - In some cases, for example, in Just-In-Time compilation, cannot afford to spend too much time in register allocation
  - Only local or both local and global allocation?



# The Problem

## Module 10

I Sengupta &  
P P Das

Objectives &  
Outline

Issues in  
Register  
Allocation

The Problem

GRA by Usage  
Count

Chaitin's  
Algorithm:  
GRA by Graph  
Coloring

Graph Coloring

Framework

Example

Register Spill

- Global Register Allocation assumes that allocation is done beyond basic blocks and **usually at function level**
- Decision problem related to register allocation
  - Given an intermediate language program represented as a control flow graph and a number  $k$ , is there an assignment of registers to program variables such that
    - no conflicting variables are assigned the same register,
    - no extra loads or stores are introduced, and
    - at most  $k$  registers are used
- This problem has been shown to be NP-hard (Sethi 1970).
- **Graph colouring** is the most popular heuristic used
- However, there are simpler algorithms as well



# Conflicting Variables

## Module 10

I Sengupta &  
P P Das

Objectives &  
Outline

Issues in  
Register  
Allocation

The Problem

GRA by Usage  
Count

Chaitin's  
Algorithm:  
GRA by Graph  
Coloring

Graph Coloring

Framework

Example

Register Spill

- Two variables interfere or conflict if their **live ranges** intersect
  - A variable is **live** at a point  $p$  in the flow graph, if there is a **use** of that variable in the path from  $p$  to the end of the flow graph
  - The **live range** of a variable is the smallest set of program points at which it is live
  - Typically, instruction no. in the basic block along with the basic block no. is the representation for a point



# Example

## Module 10

I Sengupta &  
P P Das

Objectives &  
Outline

Issues in  
Register  
Allocation

The Problem

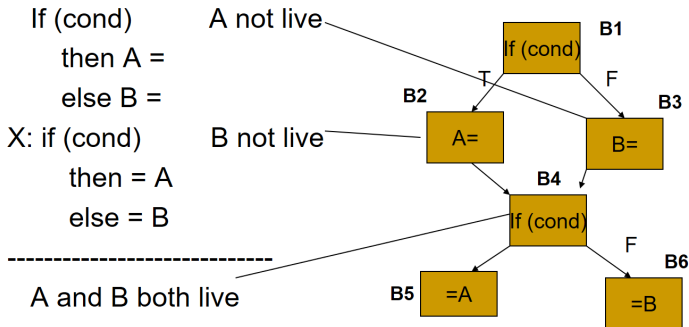
GRA by Usage  
Count

Chaitin's  
Algorithm:  
GRA by Graph  
Coloring

Graph Coloring  
Framework

Example  
Register Spill

- **Live range of A: B2, B4, B5**
- **Live range of B: B3, B4, B6**







# Global Register Allocation via Usage Counts (for Single Loops)

## Module 10

I Sengupta &  
P P Das

Objectives &  
Outline

Issues in  
Register  
Allocation

The Problem

GRA by Usage  
Count

Chaitin's  
Algorithm:  
GRA by Graph  
Coloring

Graph Coloring

Framework

Example

Register Spill

- Allocate registers for variables used within loops
- Requires information about liveness of variables at the entry and exit of each basic block (BB) of a loop
- Once a variable is computed into a register, it stays in that register until the end of the BB (subject to existence of next-uses)
- Load/Store instructions cost 2 units (because they occupy two words)



# Global Register Allocation via Usage Counts (for Single Loops)

## Module 10

I Sengupta &  
P P Das

Objectives &  
Outline

Issues in  
Register  
Allocation

The Problem

GRA by Usage  
Count

Chaitin's  
Algorithm:  
GRA by Graph  
Coloring

Graph Coloring

Framework

Example

Register Spill

- ① For every **usage** of a variable **v** in a BB, **until it is first defined**, do:
  - $\text{savings}(v) = \text{savings}(v) + 1$
  - after **v** is defined, it stays in the register any way, and all further references are to that register
- ② For every variable **v** **computed** in a BB, if it is **live on exit** from the BB,
  - count a savings of 2, since it is not necessary to store it at the end of the BB



# Global Register Allocation via Usage Counts (for Single Loops)

## Module 10

I Sengupta &  
P P Das

Objectives &  
Outline

Issues in  
Register  
Allocation

The Problem

GRA by Usage  
Count

Chaitin's  
Algorithm:  
GRA by Graph  
Coloring

Graph Coloring  
Framework

Example  
Register Spill

- Total savings per variable  $v$  are

$$\sum_{B \in \text{Loop}} (\text{savings}(v, B)) + 2 * \text{liveandcomputed}(v, B)$$

- $\text{liveandcomputed}(v, B)$  in the second term is 1 or 0
- On entry to (exit from) the loop, we load (store) a variable live on entry (exit), and lose 2 units for each
  - But, these are *one time* costs and are neglected
- Variables, whose savings are the highest will reside in registers



# Global Register Allocation via Usage Counts (for Single Loops)

## Module 10

I Sengupta &  
P P Das

Objectives &  
Outline

Issues in  
Register  
Allocation

The Problem

GRA by Usage  
Count

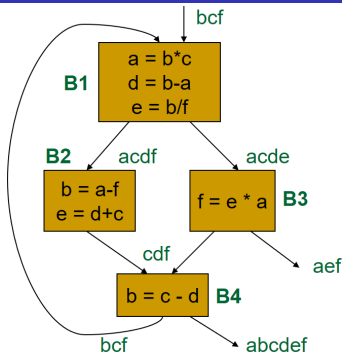
Chaitin's  
Algorithm:  
GRA by Graph  
Coloring

Graph Coloring

Framework

Example

Register Spill



Savings for the variables

	B1	B2	B3	B4	
a:	(0+2)+	(1+0)+	(1+0)+	(0+0)=	4
b:	(3+0)+	(0+0)+	(0+0)+	(0+2)=	5
c:	(1+0)+	(1+0)+	(0+0)+	(1+0)=	3
d:	(0+2)+	(1+0)+	(0+0)+	(1+0)=	4
e:	(0+2)+	(0+0)+	(1+0)+	(0+0)=	3
f:	(1+0)+	(1+0)+	(0+2)+	(0+0)=	4

If there are 3 registers, they will be allocated to the variables, a, b, and d (or f)



# Global Register Allocation via Usage Counts (for Nested Loops)

## Module 10

I Sengupta &  
P P Das

Objectives &  
Outline

Issues in  
Register  
Allocation

The Problem

GRA by Usage  
Count

Chaitin's  
Algorithm:  
GRA by Graph  
Coloring

Graph Coloring

Framework

Example

Register Spill

- We first assign registers for inner loops and then consider outer loops. Let **L1** nest **L2**
- For variables assigned registers in L2, but not in L1
  - load these variables on entry to L2 and store them on exit from L2
- For variables assigned registers in L1, but not in L2
  - store these variables on entry to L2 and load them on exit from L2
- All costs are calculated keeping the above rules



# Global Register Allocation via Usage Counts (for Nested Loops)

## Module 10

I Sengupta &  
P P Das

Objectives &  
Outline

Issues in  
Register  
Allocation

The Problem

GRA by Usage  
Count

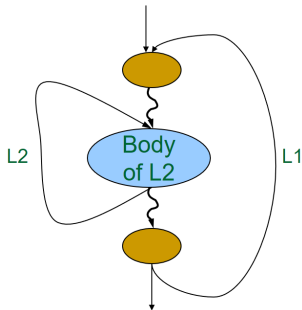
Chaitin's  
Algorithm:  
GRA by Graph  
Coloring

Graph Coloring

Framework

Example

Register Spill



- **Case 1:** Variables  $x, y, z$  assigned registers in L2, but not in L1
  - Load  $x, y, z$  on entry to L2
  - Store  $x, y, z$  on exit from L2
- **Case 2:** Variables  $a, b, c$  assigned registers in L1, but not in L2
  - Store  $a, b, c$  on entry to L2
  - Load  $a, b, c$  on exit from L2
- **Case 3:** Variables  $p, q$  assigned registers in both L1 and L2
  - No special action



# Chaitin's Formulation of the Register Allocation Problem

## Module 10

I Sengupta &  
P P Das

Objectives &  
Outline

Issues in  
Register  
Allocation

The Problem

GRA by Usage  
Count

Chaitin's  
Algorithm:  
GRA by Graph  
Coloring

Graph Coloring

Framework

Example

Register Spill

- A graph colouring formulation on the interference graph
- Nodes in the graph represent either live ranges of variables or entities called webs
- An edge connects two live ranges that interfere or conflict with one another
- Usually both adjacency matrix and adjacency lists are used to represent the graph.
- Assign colours to the nodes such that two nodes connected by an edge are not assigned the same colour
  - The number of colours available is the number of registers available on the machine
  - A  $k$ -colouring of the interference graph is mapped onto an allocation with  $k$  registers



# Example

## Module 10

I Sengupta &  
P P Das

Objectives &  
Outline

Issues in  
Register  
Allocation

The Problem

GRA by Usage  
Count

Chaitin's  
Algorithm:  
GRA by Graph  
Coloring

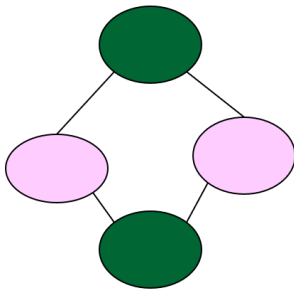
Graph Coloring

Framework

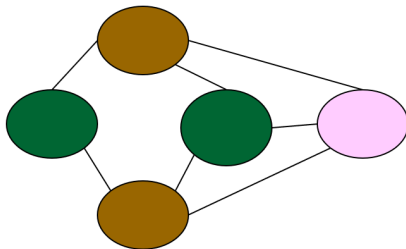
Example

Register Spill

## Two Colorable



## Three Colorable







# Idea behind Chaitin's Algorithm

## Module 10

I Sengupta &  
P P Das

Objectives &  
Outline

Issues in  
Register  
Allocation

The Problem

GRA by Usage  
Count

Chaitin's  
Algorithm:  
GRA by Graph  
Coloring

Graph Coloring

Framework

Example

Register Spill

- Choose an arbitrary node of degree less than  $k$  and put it on the stack
- Remove that vertex and all its edges from the graph
  - This may decrease the degree of some other nodes and cause some more nodes to have degree less than  $k$
- At some point, if all vertices have degree greater than or equal to  $k$ , some node has to be spilled
- If no vertex needs to be spilled, successively pop vertices off stack and colour them in a colour not used by neighbours (reuse colours as far as possible)



# Simple example – Given Graph

## Module 10

I Sengupta &  
P P Das

Objectives &  
Outline

Issues in  
Register  
Allocation

The Problem

GRA by Usage  
Count

Chaitin's  
Algorithm:  
GRA by Graph  
Coloring

Graph Coloring

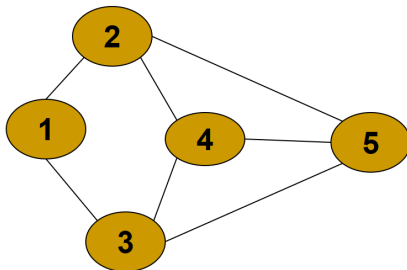
Framework

Example

Register Spill



**STACK**



**3 REGISTERS**



# Simple example – Delete Node 1

## Module 10

I Sengupta &  
P P Das

Objectives &  
Outline

Issues in  
Register  
Allocation

The Problem

GRA by Usage  
Count

Chaitin's  
Algorithm:  
GRA by Graph  
Coloring

Graph Coloring

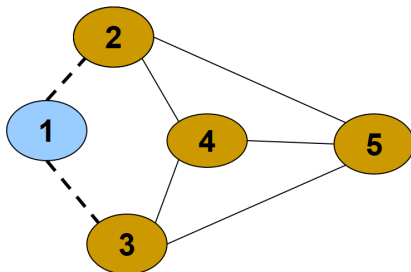
Framework

Example

Register Spill



**STACK**



**3 REGISTERS**



# Simple example – Delete Node 2

## Module 10

I Sengupta &  
P P Das

Objectives &  
Outline

Issues in  
Register  
Allocation

The Problem

GRA by Usage  
Count

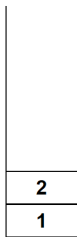
Chaitin's  
Algorithm:  
GRA by Graph  
Coloring

Graph Coloring

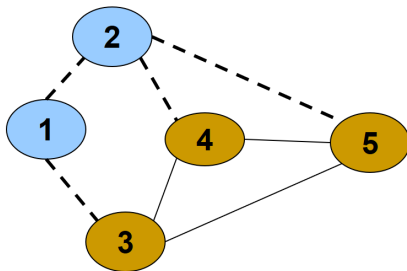
Framework

Example

Register Spill



**STACK**



**3 REGISTERS**



# Simple example – Delete Node 4

## Module 10

I Sengupta &  
P P Das

Objectives &  
Outline

Issues in  
Register  
Allocation

The Problem

GRA by Usage  
Count

Chaitin's  
Algorithm:  
GRA by Graph  
Coloring

Graph Coloring

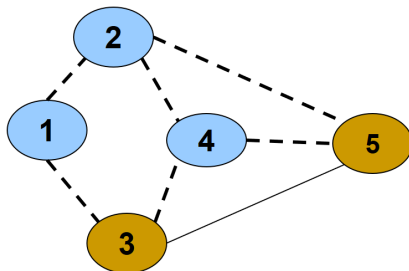
Framework

Example

Register Spill

4
2
1

**STACK**



**3 REGISTERS**



# Simple example – Delete Node 3

## Module 10

I Sengupta &  
P P Das

Objectives &  
Outline

Issues in  
Register  
Allocation

The Problem

GRA by Usage  
Count

Chaitin's  
Algorithm:  
GRA by Graph  
Coloring

Graph Coloring

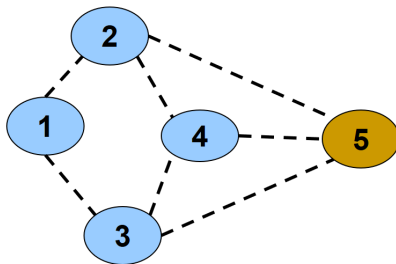
Framework

Example

Register Spill

3
4
2
1

**STACK**



**3 REGISTERS**



# Simple example – Delete Node 5

## Module 10

I Sengupta &  
P P Das

Objectives &  
Outline

Issues in  
Register  
Allocation

The Problem

GRA by Usage  
Count

Chaitin's  
Algorithm:  
GRA by Graph  
Coloring

Graph Coloring

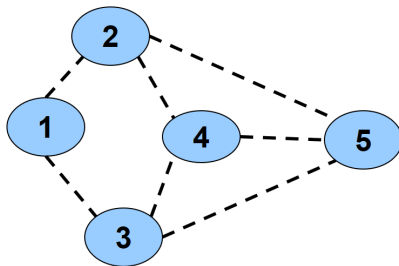
Framework

Example

Register Spill

5
3
4
2
1

**STACK**



**3 REGISTERS**



# Simple example – Colour Node 5

## Module 10

I Sengupta &  
P P Das

Objectives &  
Outline

Issues in  
Register  
Allocation

The Problem

GRA by Usage  
Count

Chaitin's  
Algorithm:  
GRA by Graph  
Coloring

Graph Coloring

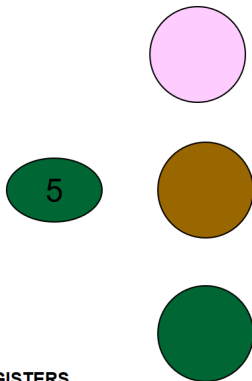
Framework

Example

Register Spill

3
4
2
1

**STACK**



**3 REGISTERS**





# Simple example – Colour Node 3

## Module 10

I Sengupta &  
P P Das

Objectives &  
Outline

Issues in  
Register  
Allocation

The Problem

GRA by Usage  
Count

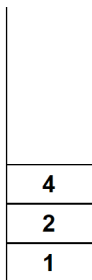
Chaitin's  
Algorithm:  
GRA by Graph  
Coloring

Graph Coloring

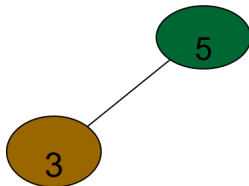
Framework

Example

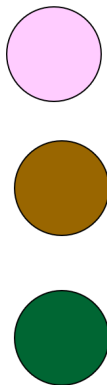
Register Spill



**STACK**



**3 REGISTERS**





# Simple example – Colour Node 4

## Module 10

I Sengupta &  
P P Das

Objectives &  
Outline

Issues in  
Register  
Allocation

The Problem

GRA by Usage  
Count

Chaitin's  
Algorithm:  
GRA by Graph  
Coloring

Graph Coloring

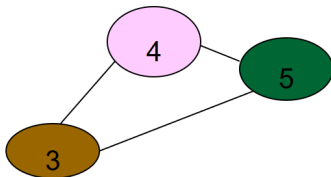
Framework

Example

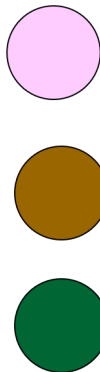
Register Spill



**STACK**



**3 REGISTERS**





# Simple example – Colour Node 2

## Module 10

I Sengupta &  
P P Das

Objectives &  
Outline

Issues in  
Register  
Allocation

The Problem

GRA by Usage  
Count

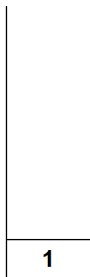
Chaitin's  
Algorithm:  
GRA by Graph  
Coloring

Graph Coloring

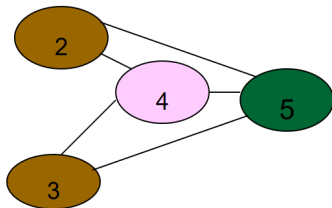
Framework

Example

Register Spill



**STACK**



**3 REGISTERS**





# Simple example – Colour Node 1

## Module 10

I Sengupta &  
P P Das

Objectives &  
Outline

Issues in  
Register  
Allocation

The Problem

GRA by Usage  
Count

Chaitin's  
Algorithm:  
GRA by Graph  
Coloring

Graph Coloring

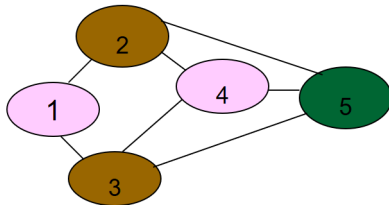
Framework

Example

Register Spill



**STACK**



**3 REGISTERS**





# Steps in Chaitin's Algorithm

## Module 10

I Sengupta &  
P P Das

Objectives &  
Outline

Issues in  
Register  
Allocation

The Problem

GRA by Usage  
Count

Chaitin's  
Algorithm:  
GRA by Graph  
Coloring

Graph Coloring

Framework

Example

Register Spill

- Identify units for allocation
  - Renames variables/symbolic registers in the IR such that each live range has a unique name (number)
- Build the interference graph
- Coalesce by removing unnecessary move or copy instructions
- Colour the graph, thereby selecting registers
- Compute spill costs, simplify and add spill code till graph is colourable



# The Chaitin Framework

## Module 10

I Sengupta &  
P P Das

Objectives &  
Outline

Issues in  
Register  
Allocation

The Problem

GRA by Usage  
Count

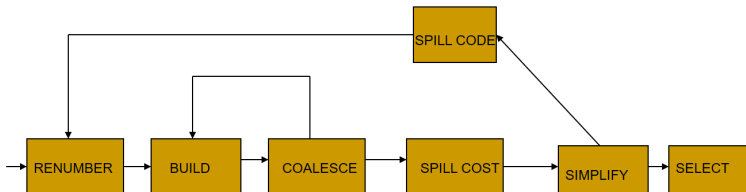
Chaitin's  
Algorithm:  
GRA by Graph  
Coloring

Graph Coloring

**Framework**

Example

Register Spill





# Example of Renaming

## Module 10

I Sengupta &  
P P Das

Objectives &  
Outline

Issues in  
Register  
Allocation

The Problem

GRA by Usage  
Count

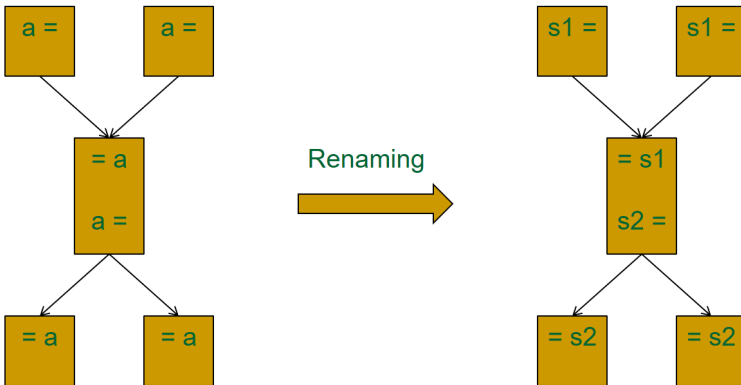
Chaitin's  
Algorithm:  
GRA by Graph  
Coloring

Graph Coloring

Framework

Example

Register Spill





# An Example

## Module 10

I Sengupta &  
P P Das

Objectives &  
Outline

Issues in  
Register  
Allocation

The Problem

GRA by Usage  
Count

Chaitin's  
Algorithm:  
GRA by Graph  
Coloring

Graph Coloring

Framework

Example

Register Spill

### Original code

1.  $x = 2$
2.  $y = 4$
3.  $w = x + y$
4.  $z = x + 1$
5.  $u = x * y$
6.  $x = z * 2$

### Code with symbolic registers

1.  $s1 = 2;$  (lv of  $s1$ : 1-5)
2.  $s2 = 4;$  (lv of  $s2$ : 2-5)
3.  $s3 = s1 + s2;$  (lv of  $s3$ : 3-3)
4.  $s4 = s1 + 1;$  (lv of  $s4$ : 4-6)
5.  $s5 = s1 * s2;$  (lv of  $s5$ : 5-5)
6.  $s6 = s4 * 2;$  (lv of  $s6$ : 6-...)





# An Example: Interference Graph

## Module 10

I Sengupta &  
P P Das

Objectives &  
Outline

Issues in  
Register  
Allocation

The Problem

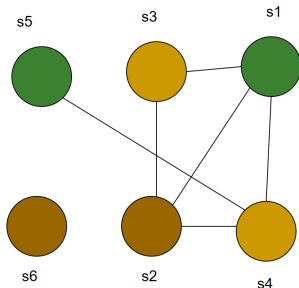
GRA by Usage  
Count

Chaitin's  
Algorithm:  
GRA by Graph  
Coloring

Graph Coloring  
Framework

Example  
Register Spill

## Interference Graph



## Stack Order for Colouring & Register Allocation (Number of Registers = 3)

s1	→	r1	1.	x = 2
s2	→	r2	2.	y = 4
s3	→	r3	3.	w = x + y
s4	→	r3	4.	z = x + 1
s5	→	r1	5.	u = x * y
s6	→	r2	6.	x = z * 2

- |    |               |                    |
|----|---------------|--------------------|
| 1. | s1 = 2;       | (lv of s1: 1-5)    |
| 2. | s2 = 4;       | (lv of s2: 2-5)    |
| 3. | s3 = s1 + s2; | (lv of s3: 3-3)    |
| 4. | s4 = s1 + 1;  | (lv of s4: 4-6)    |
| 5. | s5 = s1 * s2; | (lv of s5: 5-5)    |
| 6. | s6 = s4 * 2;  | (lv of s6: 6- ...) |



# An Example: Interference Graph

## Module 10

I Sengupta &  
P P Das

Objectives &  
Outline

Issues in  
Register  
Allocation

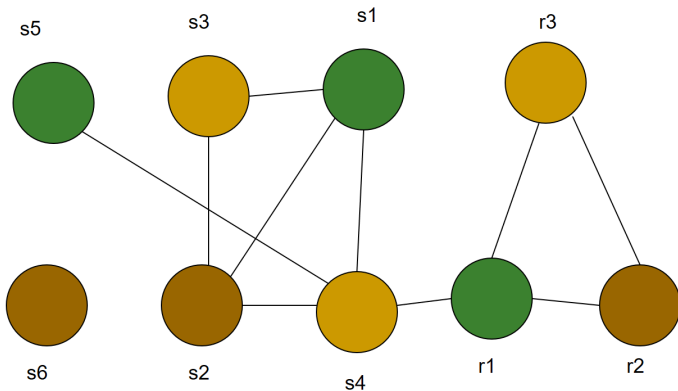
The Problem

GRA by Usage  
Count

Chaitin's  
Algorithm:  
GRA by Graph  
Coloring

Graph Coloring  
Framework

Example  
Register Spill



Interference Graph

Here assume variable Z (s4) cannot occupy r1



# An Example: Interference Graph

## Module 10

I Sengupta &  
P P Das

Objectives &  
Outline

Issues in  
Register  
Allocation

The Problem

GRA by Usage  
Count

Chaitin's  
Algorithm:  
GRA by Graph  
Coloring

Graph Coloring

Framework

Example

Register Spill

s1	→	r1	1.	x = 2
s2	→	r2	2.	y = 4
s3	→	r3	3.	w = x + y
s4	→	r3	4.	z = x + 1
s5	→	r1	5.	u = x * y
s6	→	r2	6.	x = z * 2

1.	s1 = 2;	(lv of s1: 1-5)
2.	s2 = 4;	(lv of s2: 2-5)
3.	s3 = s1 + s2;	(lv of s3: 3-3)
4.	s4 = s1 + 1;	(lv of s4: 4-6)
5.	s5 = s1 * s2;	(lv of s5: 5-5)
6.	s6 = s4 * 2;	(lv of s6: 6- ...)

## Final Code:

3 registers are sufficient  
for no spills

```
r1 = 2
r2 = 4
r3 = r1 + r2
r3 = r1 + 1
r1 = r1 * r2
r2 = r3 * 2
```



# Another Example

## Module 10

I Sengupta &  
P P Das

Objectives &  
Outline

Issues in  
Register  
Allocation

The Problem

GRA by Usage  
Count

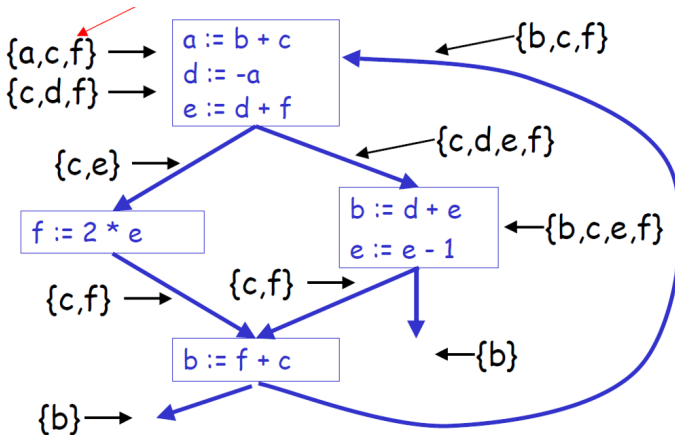
Chaitin's  
Algorithm:  
GRA by Graph  
Coloring

Graph Coloring  
Framework

Example

Register Spill

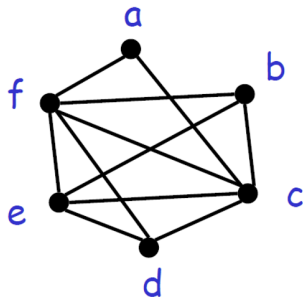
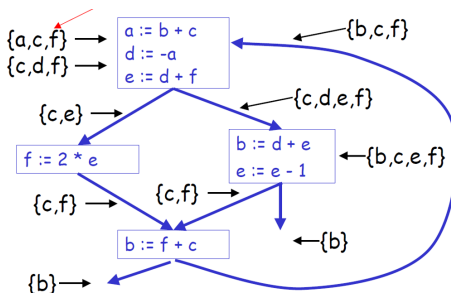
Compute live variables at each point





# Register Interference Graph

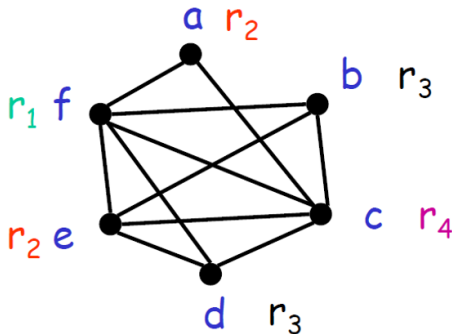
- b and c cannot be in the same register
- b and d can be in the same register





# Graph Coloring: Example

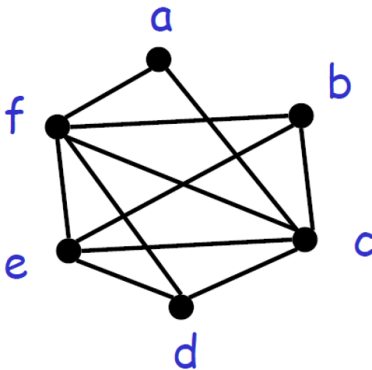
- There is no coloring with less than 4 colors (has two 4-cliques)
- There are 4 colorings of the graph





# Graph Coloring: Example

- Start with the RIG and with  $k = 4$ . Stack =  $\{\}$



- Remove a and then d: Stack =  $\{d, a\}$



# Graph Coloring: Example

## Module 10

I Sengupta &  
P P Das

Objectives &  
Outline

Issues in  
Register  
Allocation

The Problem

GRA by Usage  
Count

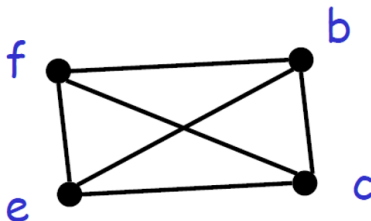
Chaitin's  
Algorithm:  
GRA by Graph  
Coloring

Graph Coloring  
Framework

Example

Register Spill

- Now all nodes have less than 4 neighbors and can be removed. Say, as: c, b, e, f



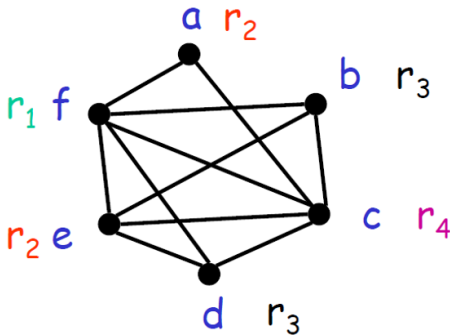
- Stack = {f, e, b, c, d, a}





# Graph Coloring: Example

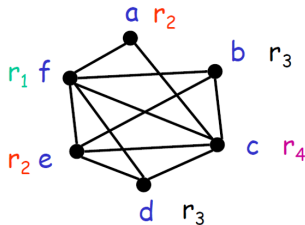
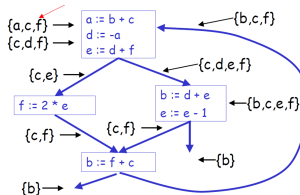
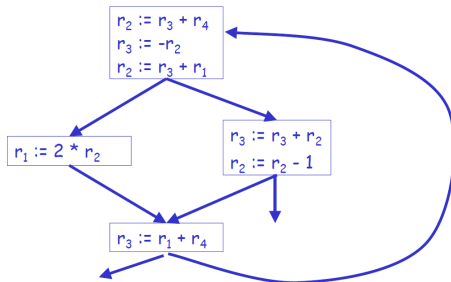
- Start assigning colors to: f, e, b, c, d, a





# Code with Registers Allocated

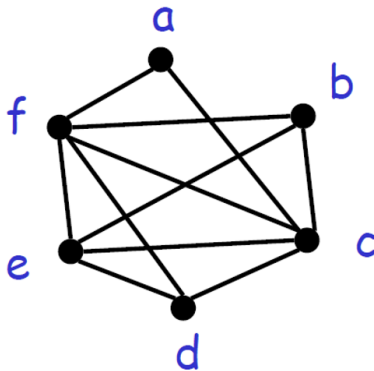
- With the coloring the code becomes





# What if the Heuristic Fails?

- What if during simplification we get to a state where all nodes have  $k$  or more neighbors?
- Let us try a 3-coloring





# What if the Heuristic Fails?

## Module 10

I Sengupta &  
P P Das

Objectives &  
Outline

Issues in  
Register  
Allocation

The Problem

GRA by Usage  
Count

Chaitin's  
Algorithm:  
GRA by Graph  
Coloring

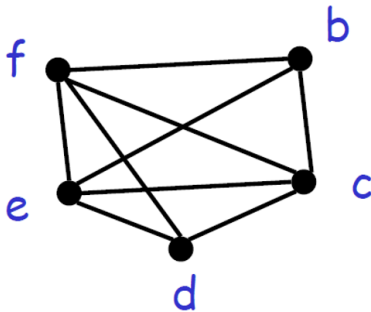
Graph Coloring

Framework

Example

Register Spill

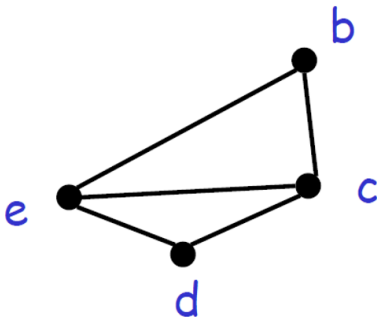
- Remove a and get stuck
- Pick a node as a candidate for spilling
  - A spilled temporary “lives” in memory
- Assume that f is picked as a candidate





# What if the Heuristic Fails?

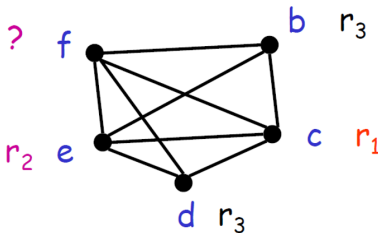
- Remove f and continue the simplification
  - Simplification now succeeds: b, d, e, c





# What if the Heuristic Fails?

- On the assignment phase we get to the point when we have to assign a color to  $f$
- We hope that among the 4 neighbors of  $f$  we use less than 3 colors  $\Rightarrow$  **optimistic coloring**





# Spilling

## Module 10

I Sengupta &  
P P Das

Objectives &  
Outline

Issues in  
Register  
Allocation

The Problem

GRA by Usage  
Count

Chaitin's  
Algorithm:  
GRA by Graph  
Coloring

Graph Coloring

Framework

Example

Register Spill

- We fail and we must spill temporary  $f$
- We must allocate a memory location as the home of  $f$ 
  - Typically this is in the current stack frame
  - Call this address  $fa$
- Before each operation that uses  $f$ , insert
  - $f := \text{load } fa$
- After each operation that defines  $f$ , insert
  - $\text{store } f, fa$



# Code with Spilling

## Module 10

I Sengupta &  
P P Das

Objectives &  
Outline

Issues in  
Register  
Allocation

The Problem

GRA by Usage  
Count

Chaitin's  
Algorithm:  
GRA by Graph  
Coloring

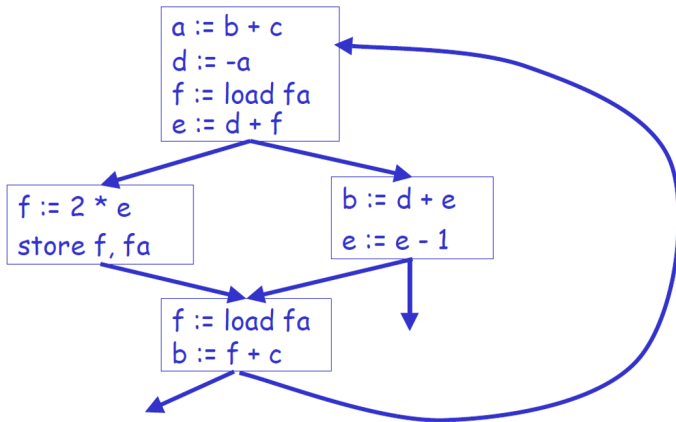
Graph Coloring

Framework

Example

Register Spill

- The new code after spilling  $f$

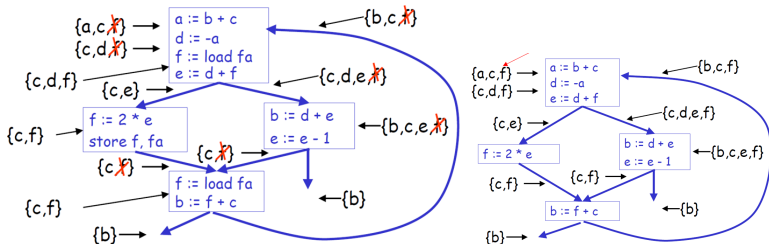






# Recomputing Liveness Information

- The new liveness information after spilling





# Recomputing Liveness Information

## Module 10

I Sengupta &  
P P Das

Objectives &  
Outline

Issues in  
Register  
Allocation

The Problem

GRA by Usage  
Count

Chaitin's  
Algorithm:  
GRA by Graph  
Coloring

Graph Coloring

Framework

Example

Register Spill

- The new liveness information is almost as before
- $f$  is live only
  - Between a  $f := \text{load } fa$  and the next instruction
  - Between a  $\text{store } f, fa$  and the preceding instruction
- Spilling reduces the live range of  $f$
- And thus reduces its interferences
- Which results in fewer neighbors in RIG for  $f$



# Recompute RIG after Spilling

## Module 10

I Sengupta &  
P P Das

Objectives &  
Outline

Issues in  
Register  
Allocation

The Problem

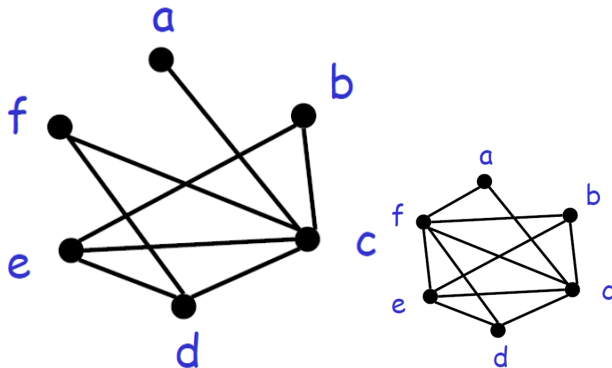
GRA by Usage  
Count

Chaitin's  
Algorithm:  
GRA by Graph  
Coloring

Graph Coloring  
Framework

Example  
Register Spill

- The only changes are in removing some of the edges of the spilled node
- In our case  $f$  still interferes only with  $c$  and  $d$
- And the resulting RIG is 3-colorable





# Spilling

## Module 10

I Sengupta &  
P P Das

Objectives &  
Outline

Issues in  
Register  
Allocation

The Problem

GRA by Usage  
Count

Chaitin's  
Algorithm:  
GRA by Graph  
Coloring

Graph Coloring

Framework

Example

Register Spill

- Additional spills might be required before a coloring is found
- The tricky part is deciding what to spill
- Possible heuristics:
  - Spill temporaries with most conflicts
  - Spill temporaries with few definitions and uses
  - Avoid spilling in inner loops
- Any heuristic is correct