

Soln:- 2:-

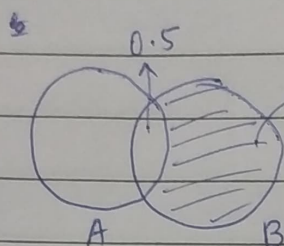
$$(b) P(A) = 0.5$$

$$P(B|A) = 1 \Rightarrow \frac{P(B \cap A)}{P(A)} = 1$$

$$P(B) = 0.75$$

$$\Rightarrow P(B \cap A) = 0.5$$

$$\therefore P(B | \neg A) = \frac{P(B \cap \neg A)}{P(\neg A)}$$



$$= P(B) - P(B \cap A)$$

$$= 0.75 - 0.5$$

$$= 0.25$$

$$\therefore P(B | \neg A) = 0.25 / 0.5 = \frac{1}{2}$$

$$(c) (i) P(ABC) = P(A) \cdot P(B) \cdot P(C|AB)$$

$$= \frac{1}{4} \times \frac{3}{4} \times 1$$

$$= \frac{3}{16}$$

(ii) $P(AB) \Rightarrow \because A \& B$ are independent

$$P(AB) = P(A) \cdot P(B)$$

$$= \frac{1}{4} \times \frac{3}{4}$$

$$= \frac{3}{16}$$

$$\text{iii) } P(C) = P(\overline{C}A) + P(CA) \\ = P(\overline{C}AB) + P(CAB)$$

$$\Rightarrow P(C) = P(CAB) + P(CA\overline{B}) + P(\overline{C}\overline{A}B) + P(\overline{C}\overline{A}\overline{B})$$

$$\therefore P(ABC) = 3/16$$

$$P(A\overline{B}C) = P(A) \cdot P(\overline{B}) \cdot P(C|A\overline{B}) \\ = \frac{1}{4} \times \frac{1}{4} \times 0 = 0$$

$$P(\overline{A}BC) = P(\overline{A})P(B)P(C|\overline{A}B) \\ = \frac{3}{4} \times \frac{3}{4} \times \frac{1}{2} \\ = \frac{9}{32}$$

$$P(\overline{A}\overline{B}C) = P(\overline{A})P(\overline{B})P(C|\overline{A}\overline{B}) \\ = \frac{3}{4} \times \frac{1}{4} \times 0 = 0$$

$$\therefore P(C) = \frac{3}{16} + \frac{9}{32} = \frac{6+9}{32} = \frac{15}{32}$$

$$\therefore P(C) = \frac{15}{32}$$

$$\text{iv) } P(B|C) = P(BC) / P(C) \\ = P(CB) / P(C) \\ = [P(CBA) + P(CB\overline{A})] / P(C) \\ = \left(\frac{3}{16} + \frac{9}{32} \right) / \left(\frac{15}{32} \right) \\ = 1$$

$$(v) P(AB|C) = \frac{P(ABC)}{P(C)}$$

$$= \frac{3/16}{15/32}$$

$$= \frac{6}{15}$$

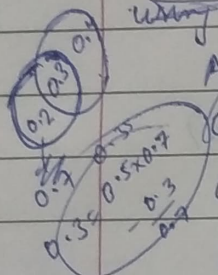
$$= \frac{2}{5}$$

$$= \frac{2}{5}$$

$$(a) (i) P(AB) = P(A)P(B) - P(A|B)$$

$$\therefore P(A|B) = \frac{P(AB)}{P(B)}$$

using truth table.



$$\Rightarrow P(AB) = P(A)P(B) - \frac{P(AB)}{P(B)}$$

\therefore false

$$(ii) P(AB) = P(A)P(B)$$

false because it only holds when A & B are independent

$$(iii) P(AB) = P(A|B)P(B) + P(B|A)P(A)$$

from RHS,

$$\begin{aligned}
 & P(A|B)P(B) + P(B|A)P(A) \\
 &= \frac{P(A \cap B)}{P(B)} P(B) + \frac{P(A \cap B)}{P(A)} P(A) \\
 &= 2P(AB) \neq \text{LHS}
 \end{aligned}$$

\therefore false.

$$(v) \quad P(A) = \sum_{b \in B} P(A | B=b) P(B=b)$$

true

(v) false

$$(vi) \quad P(ABC) = P(C|A)P(B|CA)P(A)$$

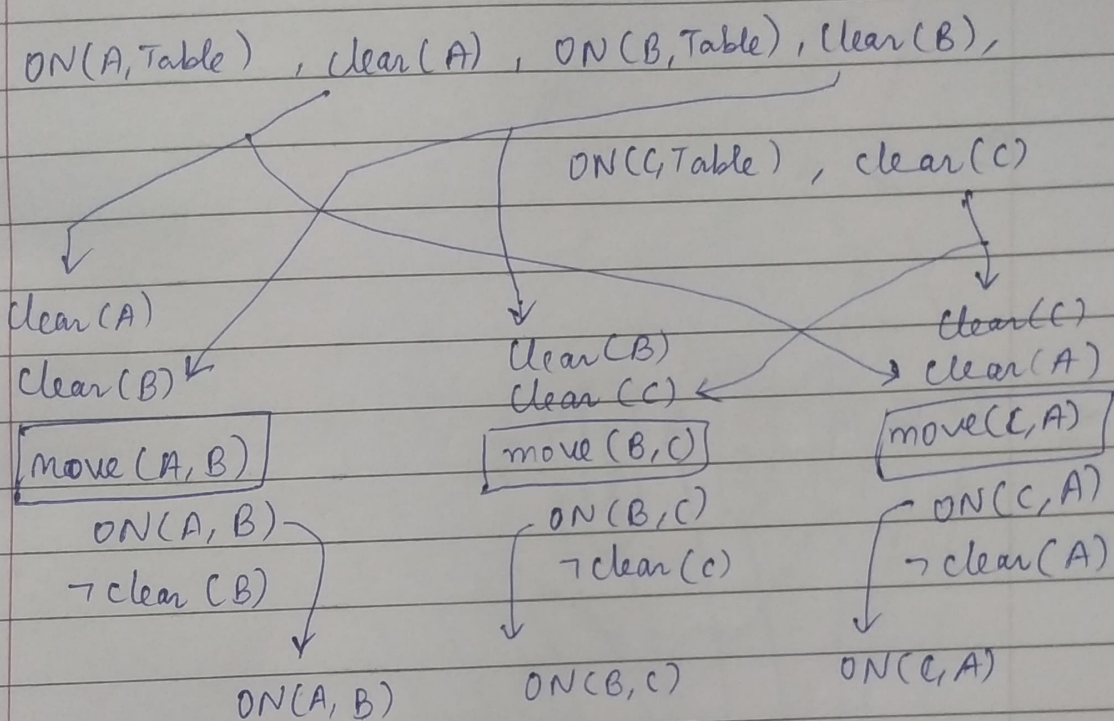
\therefore True

Solⁿ:- 3:- Initial:- ON (A, Table)

ON (B, Table), ON (C, Table)

Goal:- ON (A, B) ON (B, C) ON (C, A)

Initial



Goal

In the above partial order, we observe that for the move (B, C), move (A, B) and move (C, A) operations.

There are threats that which can not be resolved by ordering i.e;

(i) effect → clear (B) of move (A, B)

negates the precondition of move (B, C)
thus implies an ordering was introduced.

(ii) However $\neg \text{clear}(c)$ persists during the step, move (c, A) & negates the precondition
 \therefore Therefore, there is no solution for the partial order plan.

