Interest

Q. A farmer borrowed Rs.3600 at 15% simple interest per annum. At the end of 4 years, he cleared this account by paying Rs.4000 and a donkey. The cost of the donkey is -

A. Rs. 1000 B. Rs. 1200 C. Rs. 1550 D. Rs. 1760

Soln:

SI for 4 years = Rs.(3600×0.15×4)=Rs.2160

Amount after 4 years = Rs. (3600+2160)= Rs. 5760

Cost of donkey = Rs. (5760-4000)= Rs. 1760

Ans: D

Interest

Q. In 4 years, Rs. 6500 amounts to Rs. 8840 at a certain rate of interest. In what time will Rs.1600 amounts to Rs.1816 at the same rate?

A. 3years B. 1.5years C. 2years D. 2.5years

Ans: B

Interest

Q. P =Rs. 2000, R =10%, N =2yrs , Find A and CI

Soln:

$A = 2000(1 + \frac{10}{100})^2$

$= 2000(\frac{110}{100})^2$

$= 2000(\frac{121}{100})$

= Rs. 2420

CI = 2420 – 2000 = Rs. 420

2000 → 10% =200

10% 10%

2000 ⟶ 2200 ⟶ 2420

CI = 2420 – 2000 = 420

Interest

Q. Simple interest on a certain sum of money for 3 years at 8% per annum is half the compound interest on Rs. 4000 for 2 years at 10% per annum. The sum placed on simple interest is:

A. Rs. 1550 B. Rs. 1650 C. Rs. 1750 D. Rs. 2000

Soln:

$A = P(1+R/100)^N = 4000(1+\frac{10}{100})^2 = 4000 \times (\frac{11}{10})^2 = 4000 \times \frac{11}{10} \times \frac{11}{10}$ = Rs. 4840

OR

$4000 \xrightarrow[1^{st}\ yr]{10\%} 4400 \xrightarrow[2^{nd}\ yr]{10\%} 4840$

CI = A – P

CI = 4840 – 4000 = Rs. 840

Ans: C

$SI = \frac{1}{2} CI$

$\frac{PNR}{100} = \frac{1}{2} \times 840$

$\frac{P \times 3 \times 8}{100} = 420$

$P(sum) = \frac{420 \times 100}{3 \times 8}$

= Rs. 1750

Interest

Q. P =Rs. 4000, R =20% per annum, N =6months.Find CI computed quarterly for given period.

Soln:

N =6months(2 quarterly)

rate(R) = 20 % per annum = 5 % quarterly

After every 3 months CI will be calculated.

by 5%=200 → by 5%=210 →

4000 4200 4410

I = 4410 -4000

= Rs. 410

Interest

Q. Difference between Compound interest & simple interest on a sum placed at 8% p.a. compounded annually for 2 years is Rs 128. Find the Principal

- A.20000 B. 24000 C. 26000 D. 15000
- **Soln**:
- Let the principal be P = Rs. 100.
- time N = 2 years, rate of interest R = 8% per annum
- simple interest = PNR/100=$\frac{100*8*2}{100}$ =Rs. 16
- CI (for 2 years)
- 8% 8%
- 100 → 108 → 116.64
- 16.64

P	SI	CI	Diff
100	16	16.64	0.64

- 0.64 - > 100
- 128 -> ?
- $\frac{12800}{0.64}$ = Rs. 20000

Interest

Q. Difference between Compound interest & simple interest on a sum placed at 8% p.a. compounded annually for 2 years is Rs 128. Find the principal

- A.20000 B. 24000 C. 26000 D. 15000
- **Soln**:
- Let the principal be P = Rs. 100.
- time N = 2 years, rate of interest R = 8% per annum
- simple interest = PNR/100=$\frac{100*8*2}{100}$ =Rs. 16
- compound amount= P(1+R/ 100)^N
- = 100*(1+$\frac{8}{100}$) ^2 = 100 * ($\frac{108}{100}$)^2 = 100($\frac{11664}{10000}$)=$\frac{11664}{100}$ = 116.64
- compound interest = compound amount – principal
- C.I = A - P
  =116.64-100=Rs. 16.64
- the difference between the compound interest and simple interest = 16.64-16.00 = Rs. 0.64
- 0.64 - > 100
- 128 -> ?
- = $\frac{128*100}{0.64}$ = 20000
- Thus, the principal is Rs. 20000.

Ans : A

Interest

- If the difference between compound and simple interest is of **two years** than,
  Difference = $P(R)^2/(100)^2$
  Where P = principal amount, R = rate of interest

- If the difference between compound and simple interest is of **three years** than,
  Difference = 3 x $P(R)^2/(100)^2 + P(R/100)^3$.
  Here also, P = principal amount, R = rate of interest

Interest(Assignment)

Q. The difference between simple interest and compound interest on a certain sum of money for 2 years at 4% per annum is Rs 20. Find the sum.

A.12500 B. 25000 C. 12000 D. 17500

Ans: A

Interest(Assignment)

Q. A sum of money placed at compound interest doubles in 7 years. In how many years the principal becomes-

a. 4 times of itself

b. 8 times of itself

Soln:

Let initial value be 100

	7yrs		7yrs		7yrs	
100	⟶	200	⟶	400	⟶	800
	doubles		14 yrs		21yrs	

a. In 14yrs

b. In 21 yrs

OR

100------->200 in 7 years
200------->400 in again 7 years then,
400------->800 in 7 years again, thus
the time becomes= 7+7+7= 21 years.

Interest(Assignment)

Q. When annual compounding is done, a sum amounts to Rs 5000 in 6 years and 7200 in 8 years. What is the int rate?

A. 10% B. 15% C. 20% D. 25%

Soln

Let P be the principal & R the int rate

→ 5000 = P(1+R/100)^6……(1)

→ 7200 = P(1+R/100)^8……(2)

→ 36/25 = (1+R/100)^2

→ Taking square roots of both sides

→ 1+R/100 = 6/5

→ R/100 =1/5

→ R = 20%

Ans: C

Interest(Assignment)

Q. A sum fetched a total simple interest of Rs.7056 at the rate of 8 percent per year in 7 years. What is the sum?

A. Rs 12600 B) Rs 15120 C) Rs 10080 D) Rs 7560

Ans : A

Interest(Assignment)

Q. Find the compound interest on Rs. 15,625 for 9 months at 16% per annum compounded quarterly.

A. Rs. 1851 B. Rs. 1941 C. Rs. 1951 D. Rs. 1961

Ans: C

Interest(Assignment)

Q. What is the difference between the simple interest on a principal of Rs. 500 being calculated at 5% per annum for 3 years and 4% per annum for 4 years?

A.Rs. 5 B.Rs. 10 C.Rs. 20 D.Rs. 40 E. None of these

SI_1 = P N_1R_1/100

$= \frac{500x\ 3\ x\ 5}{100}$ = Rs. 75

SI_2 = P N_2R_2/100

$= \frac{500x\ 4\ x\ 4}{100}$ = Rs. 80

Difference = 80 – 75 = Rs. 5

OR

500 == 15% ↑ ⇒ 575 (1st case)
500 == 16% ↑ ⇒ 580 (2nd case)
difference = 580 -575 = Rs. 5

Ans : A

Interest(Assignment)

Q. A sum of money placed at compound interest doubles itself in 4 years. In how many years will it amount to 8 times?

A. 9 years B. 8 years C. 27 years D. 12 years

Ans: D

Interest(Assignment)

Q. Difference between Compound interest & simple interest on a sum placed at 20% per annum compounded annually for 2 years is Rs. 72. Find the sum.

A. Rs. 2400 B.Rs. 8400 C. Rs.1800 D.Rs. 900

Ans : C

Interest(Assignment)

Q. What is the simple interest on a sum of Rs. 700 if the rate of interest for the first 3 years is 8% per annum and for the last 2 years is 7.5% per annum?

A.Rs. 269.5 B.Rs. 283 C.Rs. 273 D.Rs. 280 E. None of these

Ans: C

Interest(Assignment)

Q. Rs.2100 is lent at compound interest of 5% per annum for 2 years. Find the amount after two years.

- A.Rs. 2300 B.Rs. 2315.25 C.Rs. 2310 D.Rs. 2320 E. None of these
- **Soln:**
- $A = P (1+ R/100)^T$
- $A = 2100(1+5/100)^2$
- $A=2100\times[105/100]2$
- $A= \frac{2100 \text{ x } 11025}{10000}$
- Amount, A=Rs.2315.25
- **Ans : B**

Interest(Assignment)

Q. A man borrowed total Rs 2500 at Simple interest from two money lenders. He paid interest at 12% p.a. to one and 14% p.a. to the other. The total interest paid for the year was Rs.326. How much did he borrow at 14%?

A. Rs 1000 B. Rs 1200 C. Rs 1300 D. Rs 1500

Soln:

Let, x = Principal at 12% & 2500-x = Principal at 14%

SI at Rs.x = $\frac{x \times 1 \times 12}{100} = \frac{12x}{100} = \frac{3x}{25}$

SI at Rs.2500 -x = $\frac{2500-x \times 1 \times 14}{100} = \frac{(2500-x) \times 7}{50} = \frac{17500x - 7x}{50}$

SI at x + SI at 2500-x = 326

Substitute and solving the equation gives x =Rs. 1200

We need Principal at 2500-x = 2500 – 1200 =Rs. 1300

Ans: C

Interest(Assignment)

Q.A certain sum of money amounts to Rs. 704 in two years and Rs 800 in 5 years. Find the Principal.

A. Rs. 640 B. Rs. 600 C. Rs. 550 D. Rs. 450

Ans: A

Interest(Assignment)

Q. What should be the simple interest obtained on an amount of Rs 5,760 at the rate of 6% p.a. after 3 years?

A. Rs 1036.80

B. Rs 1666.80

C. Rs 1336.80

D. Rs 1063.80

E. None of these

Ans : A

Interest(Assignment)

Q. The simple interest on Rs.1820 from March 9, 2012 to May 21, 2012 at 7.5% rate will be

A. Rs. 22.50

B. Rs. 27.30

C. Rs. 28.80

D. Rs. 29

Ans: B

Permutation & Combination

- What is permutation?
- It is the number of ways a group of things can be arranged.

E.g: Consider 3 letters A,B,C . In how many ways they can be arranged?

- A B C
- A C B
- B A C
- B C A
- C A B
- C B A

6 ways to arrange these 3 letters

- For 3 letter / 4 letter words its possible but for more number of letters we need a formula-
- $nPr = \frac{n!}{(n-r)!}$

Permutation & Combination

Q. Consider 4 letters A,B,C,D and arrange them in 3 spaces

- - - 3 spaces

No . Of letters = 4

No of spaces = 3

nPr = $4P_3 = \frac{4!}{(4-3)!} = \frac{4!}{1!}$ =4! = 4 x 3 x 2 x 1 = 24 ways it can be arranged

Q. Arrange 7 letters A,B,C,D,E,F,G in 4 spaces

- - - - 4 spaces

nPr = $7P_4 = \frac{7!}{(7-4)!} = \frac{7!}{3!} = \frac{5040}{6}$ = 840

Permutation & Combination - Remember

0! = 1

1 ! = 1

2! = 2 x 1 = 2

3! = 3 x 2 x 1 = 6

4! = 4 x 3 x 2 x 1 = 24

5! = 5 x 4 x 3 x 2 x 1 = 120

6! = 6 x 5 x 4 x 3 x 2 x 1 = 720

7! = 7 x 6 x 5 x 4 x 3 x 2 x 1 = 5040

Permutation & Combination

Q. In how many ways can the letters of the word 'LEADER' be arranged?

A. 72 B. 144 C. 360 D. 720 E. None of these

Soln:

The word LEADER has 6 letters. So I can be arranged in 6! ways.

Out of these 6 letters , 2 letters are repeated (letter E repeated twice)

So we write it as - $\frac{6!}{2!}$

→ 6! ways to arrange letters in the word LEADER

→ 2! In the denominator as letter E is repeated twice

$$= \frac{6\times5\times4\times3\times2\times1}{2\times1}$$

= 360 ways

Ans : C

Permutation & Combination

Q. Out of 7 consonants and 4 vowels, how many words of 3 consonants and 2 vowels can be formed?

A. 210 B. 1050 C. 25200 D. 21400 E. None of these

Soln:

we need to form a 5letter word with 3consonants & 2vowels = C C C V V

Ways to select, (3 consonants out of 7) AND (2 vowels out of 4)

$= {}^{7}C_{3} \times {}^{4}C_{2} \times 5!$ ← each group has 5 letters and they can be arranged in 5! ways

$= \frac{7\times6\times5}{3\times2\times1} \times \frac{4\times3}{2\times1} \times 5!$

$= 35 \times 6 \times 120$

$= 25200$ ways

Ans : C

Permutation & Combination

Q. From a group of 7 men and 6 women, five persons are to be selected to form a committee so that at least 3 men are there on the committee. In how many ways can it be done?

A. 564 B. 645 C. 735 D. 756 E. None of these

Soln:

We may have (3 men and 2 women) or (4 men and 1 woman) or (5 men only).

Required number of ways= (7C3 x 6C2) + (7C4 x 6C1) + (7C5)

$$= \left(\frac{7 \times 6 \times 5}{3 \times 2 \times 1} \times \frac{6 \times 5}{2 \times 1}\right) + (7C3 \times 6C1) + (7C2) \rightarrow [\text{using } {}^{n}C_{r} = {}^{n}C_{(n-r)}]$$

$$= 525 + \left(\frac{7 \times 6 \times 5}{3 \times 2 \times 1} \times \frac{6}{1}\right) + \left(\frac{7 \times 6}{2 \times 1}\right)$$

$$= 525 + 210 + 21$$

$$= 756$$

Ans: D

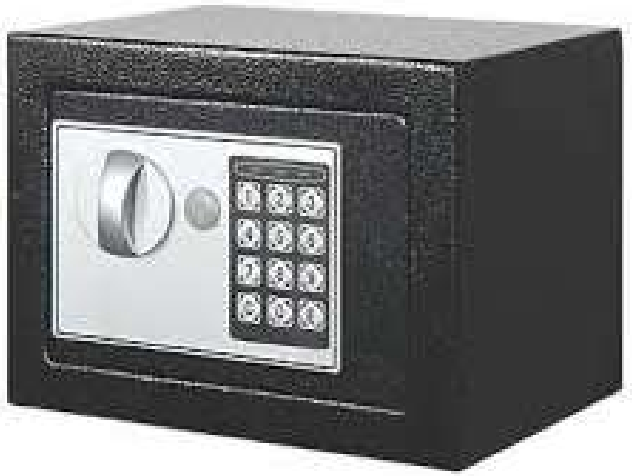
Difference between permutation and combination

Combination (order does not matter)

"My fruit salad is a combination of apples, grapes and bananas" We don't care what order the fruits are in, they could also be "bananas, grapes and apples" or "grapes, apples and bananas", its the same fruit salad.

Permutation (When the order does matter)

"The combination to the safe is 472". Now we **do** care about the order. "724" won't work, nor will "247". It has to be exactly **4-7-2**.



Difference between permutation and combination

What is permutation?

Permutation: The various ways of arranging a given number of things by taking some or all at a time are all called as permutations.
Permutation includes word formation, number formation, circular permutation, etc. **In permutation, objects are to be arranged in particular order.** It is denoted by $^{n}P_{r}$ **or P(n, r).**

Example: Arrange the given 3 numbers 1, 2, 3 by taking two at a time.
Now these numbers can be arranged in 6 different ways: **(12, 21, 13, 31, 23, 32).**

Here,

12 and 21, 13 and 31 or 23 and 32 do not mean the same, because here order of numbers is important.

Difference between permutation and combination

- **What is combination?**

  Combination: Each of different groups or selections formed by taking some or all number of objects is called a combination.

  Combination is used in different cases which include team/group/committee.

  In combination, objects are selected randomly and here order of objects doesn't matter. It is denoted by $^{n}C_{r}$ **or C(n, r) or** $^{n}C_{r} = {}^{n}C_{(n-r)}$.

  Example: If we have to select two girls out of 3 girls X, Y, Z, then find the number of combinations possible.

  Now only two girls are to be selected and arranged. Hence, this is possible in 3 different ways: **(XY, YZ, XZ,).**

  Here,
  You cannot make a combination as XY and YX, because these combinations mean the same.

Permutation & Combination(Assignment)

Q. In a group of 6 boys and 4 girls, four children are to be selected. In how many different ways can they be selected such that at least one boy should be there?

A. 159 B. 194 C. 205 D. 209 E. None of these

Soln:

(1 boy and 3 girls) or (2 boys and 2 girls) or (3 boys and 1 girl) or (4 boys).

= (6C1 x 4C3) + (6C2 x 4C2) + (6C3 x 4C1) + (6C4)

= (6C1 x 4C1) + (6C2 x 4C2) + (6C3 x 4C1) + (6C2) → using $^{n}C_{r} = {}^{n}C_{(n-r)}$(to reduce calculation)

$$= (6 \times 4) + \left(\frac{6 \times 5}{2 \times 1} \times \frac{4 \times 3}{2 \times 1}\right) + \left(\frac{6 \times 5 \times 4}{3 \times 2 \times 1} \times 4\right) + \frac{6 \times 5}{2 \times 1}$$

= (24 + 90 + 80 + 15)

= 209

Ans: D

Permutation & Combination(Assignment)

Q. In a group of 6 boys are 4 girls, four children are to be selected. In how many different ways can they be selected such that at least one boy should be there

A. 109 B. 128 C. 138 D. 209

Ans: D

Permutation & Combination(Assignment)

Q. A group consists of 4 girls and 7 boys. In how many ways can a team of 5 members be selected if the team has at least 2 girls?

A. 322 B. 321 C. 401 D. 116

Ans: A

Permutation & Combination(Assignment)

Q. How many 4-letter words with or without meaning, can be formed out of the letters of the word, 'LOGARITHMS', if repetition of letters is not allowed?

A. 40

B. 400

C. 5040

D. 2520

Ans: C

Permutation & Combination(Assignment)

Q. In how many different ways can the letters of the word 'MATHEMATICS' be arranged so that the vowels always come together?

A. 10080

B. 4989600

C. 120960

D. None of these

Ans: C

Permutation & Combination(Assignment)

Q. In how many different ways can the letters of the word 'OPTICAL' be arranged so that the vowels always come together?

A. 120

B. 720

C. 4320

D. 2160

E. None of these

Ans: B

Permutation & Combination(Assignment)

Q. How many Permutations of the letters of the word APPLE are there?

A.600 B.120 C.240 D.60

Ans: D

Permutation & Combination(Assignment)

Q. How many different words can be formed using all the letters of the word ALLAHABAD?

A.7560

B.7890

C.7650

D. None of these

Ans: A

Permutation & Combination(Assignment)

Q. Find the value of ${}^{50}P_2$

A. 4500
B. 3260
C. 2450
D. 1470

Ans : C

Permutation & Combination(Assignment)

Q. How many words can be formed by using letters of the word ‘DELHI’?

a. 50
b. 72
c. 85
d. 120

Ans : D

Permutation & Combination(Assignment)

Q. Find the number of ways the letters of the word ‘RUBBER’ can be arranged?

A. 450
B. 362
C. 250
D. 180

Ans: D

Permutation & Combination(Assignment)

Q. Out of 5 consonants and 4 vowels, how many words of 3 consonants and 2 vowels can be formed?

A. 60
B. 200
C. 5230
D. 7200

Ans : D

Permutation & Combination(Assignment)

Q. In how many ways can a group of 5 men and 2 women be made out of a total of 7 men and 3 women?

A. 63

B. 90

C. 126

D. 45

E. 135

Ans: A

Permutation & Combination(Assignment)

Q. In how many different ways can the letters of the word 'LEADING' be arranged in such a way that the vowels always come together?

A. 360 B. 480 C. 720 D. 5040 E. None of these

Soln:

L E A D I N G ⟶ vowels in this word are E,A I

Remaining letters(consonants) are - L D N G

now we can arrange the vowels together in the remaining spaces as

_ L _ D _ N _ G_ in 5! ways and vowels be rearranged in those spaces in 3! ways

5! X 3! = 720 ways

Ans : C

Permutation & Combination(Assignment)

Q. In how many different ways can the letters of the word 'CORPORATION' be arranged so that the vowels always come together?

A. 810 B. 1440 C. 2880 D. 50400 E. 5760

Soln:

C O R P O R A T I O N------ vowels in this word are O,O,A,I,O

Remaining letters(consonants) are - C R P R T N

now we can arrange the vowels together in the remaining spaces as

_C_R_P_R_T_N_ in 7! ways and vowels be rearranged in those spaces in 5! Ways

But the repeated letters are 2R in consonants and 3O in vowels

$$\frac{7!}{2!} X \frac{5!}{3!} = 50400 \text{ ways}$$

Ans : D


THANK
YOU!