

Quiz 01 (Set C)
SIAS, Krea University (AY 2025-26)
Mathematical Methods for Economics (Course Code: ECON211)
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Multiple Choice Questions

1. (1 point) There are two sets A and B .

$$A = \{x : x \text{ is a prime number}\}$$

$$B = \{x : x \text{ is an even number}\}$$

The universal set is $\mathbb{U} = \{x : 0 \leq x \leq 20\}$.

What is $A \cap B^c$?

- A. $\{1, 7, 11, 19\}$
- B. $\{1, 3, 5, 7, 9, 11, 13, 17, 19\}$
- C. $\{3, 5, 7, 11, 13, 17, 19\}$
- D. \emptyset

Answer: C

Solution: Write the two sets and their complements.

$$A = \{2, 3, 5, 7, 11, 13, 17, 19\}$$

$$B = \{0, 2, 4, 6, 8, 10, 12, 14, 16, 18, 20\}$$

$$A^c = \{0, 1, 4, 6, 8, 9, 10, 12, 14, 15, 16, 18, 20\}$$

$$B^c = \{1, 3, 5, 7, 9, 11, 13, 15, 17, 19\}$$

Therefore, $A \cap B^c = \{3, 5, 7, 11, 13, 17, 19\}$.

2. (1 point) If $x^{-2}y^3 = 5$, compute $\frac{1}{40}(x^2y^{-3} + 2x^{-10}y^{15})$.

- A. 156.255
- B. 15.6255
- C. 1562.55
- D. 312.51

Answer: A

Solution:

$$\underbrace{x^2y^{-3}}_A + \underbrace{2x^{-10}y^{15}}_B$$

$$A = (x^{-2}y^3)^{-1} = \frac{1}{5} = 0.2$$

$$B = (2(x^{-2}y^3)^3) = 2 \times (5)^5 = 2 \times 3125 = 6250$$

$$A + B = 6250.2$$

$$\frac{(A + B)}{40} = 156.255$$

3. (1 point) Consider the following statements:

Statement (i): If we take the power of a product, we can distribute the exponent over the different factors.

$$(xy)^a = x^a \times y^a$$

Statement (ii): We can also distribute the exponents when we take power of a sum.

$$(x + y)^a = x^a + y^a$$

- A. Both (i) and (ii) are correct.

- B. Statement (i) is correct but statement (ii) is wrong.
- C. Statement (i) is wrong but statement (ii) is correct.
- D. Both (i) and (ii) are wrong.

Answer: B

Solution: Statement (ii) is incorrect. Take for instance,

$$(a + b)^2 = a^2 + b^2 + 2ab \neq a^2 + b^2$$

Short Answer Questions-I

4. (1 point) Simplify the following expression: $2x^2 - 5yz + 10xz - xy$.

Solution:

$$\begin{aligned} 2x^2 - 5yz + 10xz - xy &= 2x^2 + 10xz - xy - 5yz && \text{(rearranging the terms)} \\ &= 2x(x + 5z) - y(x + 5z) && \text{(taking } 2x \text{ and } y \text{ as common)} \\ &= (2x - y)(x + 5z) && \text{(since } a(b - c) - d(b - c) = (a - d)(b - c)) \end{aligned}$$

5. (1 point) Solve for x : $|3 - 6x| \leq 24$.

Solution: If $\epsilon > 0$ then $|x| \leq \epsilon$ if and only if $-\epsilon \leq x \leq \epsilon$. We will use this rule.

$$\begin{aligned} |3 - 6x| &\leq 24 \\ \Rightarrow -24 &\leq 3 - 6x \leq 24 \\ \Rightarrow -24 - 3 &\leq 3 + (-3) - 6x \leq 24 - 3 && \text{(adding -3 to all sides)} \\ \Rightarrow -27 &\leq -6x \leq 21 \\ \Rightarrow \frac{-7}{2} &\leq x \leq \frac{9}{2} && \text{(since we are dividing by -6, we must switch signs.)} \end{aligned}$$

6. (1 point) The shortest side of a triangle is given by x cm. The longest side and the third side are given by $2x$ cm and $2x + 5$ cm respectively. What is the minimum value of x to have the perimeter greater than or equal to 50 cm?

Solution: The perimeter of a triangle with sides (a , b , and c) is given by $P = a + b + c$. All that we need to do is plug the given values. Let $a = x$, $b = 2x$, and $c = 2x + 5$.

$$\begin{aligned} P &= x + 2x + 2x + 5 \\ P &\geq 50 \quad \text{(given)} \\ x + 2x + 2x + 5 &\geq 50 \\ 5x + 5 &\geq 50 \\ 5x &\geq 45 \\ x &\geq 9 \end{aligned}$$

Short Answer Questions-II

7. (2 points) In a survey of 30 students, it was found that 15 had taken Mathematics, 12 had taken Physics and 11 had taken Chemistry, 5 had taken Mathematics and Chemistry, 9 had taken Mathematics and Physics, 4 had taken Physics and Chemistry and 3 had taken all the three subjects. Find the number of students that had none of the subjects.

Solution: Let M be the set that contains students who took Maths, P who took Physics, and C who took Chem. Therefore, $n(M) = 15$, $n(P) = 12$, and $n(C) = 11$. We also know that:

$$\begin{aligned}n(M \cap C) &= 5 \\n(M \cap P) &= 9 \\n(P \cap C) &= 4 \\n(M \cap P \cap C) &= 3 \\n(\mathbb{U}) &= 30\end{aligned}$$

We are supposed to compute $n(M^c \cap P^c \cap C^c)$.

We know that, for any three sets A, B, C , the following is true:

$$n(A \cup B \cup C) = n(A) + n(B) + n(C) - n(A \cap B) - n(A \cap C) - n(B \cap C) + n(A \cap B \cap C)$$

Given the values, we will apply this formula.

$$\begin{aligned}n(M \cup P \cup C) &= n(M) + n(P) + n(C) - n(M \cap P) - n(M \cap C) - n(P \cap C) + n(M \cap P \cap C) \\ \Rightarrow n(M \cup P \cup C) &= 15 + 12 + 11 - 9 - 5 - 4 + 3 \\ \Rightarrow n(M \cup P \cup C) &= 38 - 18 + 3 \\ \Rightarrow n(M \cup P \cup C) &= 20 + 3 \\ \Rightarrow n(M \cup P \cup C) &= 23\end{aligned}$$

A complement of a set is just all the elements in the universal set excluding the ones within the set. Hence,

$$\begin{aligned}n(M^c \cap P^c \cap C^c) &= n(\mathbb{U}) - n(M \cup P \cup C) \\ \Rightarrow n(M^c \cap P^c \cap C^c) &= 30 - 23 \\ \Rightarrow n(M^c \cap P^c \cap C^c) &= 7\end{aligned}$$

8. (2 points) Solve for x .

$$\frac{(x-4)+3(x+1)}{x+3} \leq 0$$

Solution: Looking at the LHS, we already know what the value of x is not going to be.

$$x \neq -3$$

$$\begin{aligned} \frac{(x-4)+3(x+1)}{x+3} &\leq 0 \\ \frac{4x-1}{x+3} &\leq 0 \end{aligned}$$

There are only two scenarios under which the inequality will hold.

Case-I: the numerator has to be positive (or zero) and the denominator has to be negative (can't be zero).

$$\begin{aligned} 4x-1 &\geq 0 \\ x+3 &< 0 \end{aligned}$$

We have: $x \geq \frac{1}{4}$ and $x < -3$. There does not exist a number that can be simultaneously be less than -3 and also at least as large as $\frac{1}{4}$.

Case-II: the numerator has to be negative (or zero) and the denominator has to be positive.

$$\begin{aligned} 4x-1 &\leq 0 \\ x+3 &> 0 \end{aligned}$$

We have: $x \leq \frac{1}{4}$ and $x > -3$. Therefore,

$$x \in \left(-3, \frac{1}{4}\right]$$

The final answer:

$$x \in \left(-3, \frac{1}{4}\right]$$