

Quiz 01 (Set B)
SIAS, Krea University (AY 2025-26)
Mathematical Methods for Economics (Course Code: ECON211)
25 July 2025

Multiple Choice Questions

1. (1 point) If $x^{-2}y^3 = 5$, compute $\frac{1}{100}(x^2y^{-3} + 2x^{-10}y^{15})$.

- A. 1250.2
- B. 62.5
- C. 6.25
- D. 6250.2

Answer: B

Solution:

$$\underbrace{x^2y^{-3}}_A + \underbrace{2x^{-10}y^{15}}_B$$

$$A = (x^{-2}y^3)^{-1} = \frac{1}{5} = 0.2$$

$$B = (2(x^{-2}y^3)^3) = 2 \times (5)^5 = 2 \times 3125 = 6250$$

$$A + B = 6250.2$$

$$\frac{(A + B)}{100} = 62.50$$

2. (1 point) Consider the following statements:

Statement (i): If we take the quotient of two exponentials with the same base, we simply subtract the exponents:

$$\frac{x^a}{x^b} = x^{a-b}$$

Statement (ii): This property (provided in Statement (i)) does not hold good when b is greater than a .

- A. Both (i) and (ii) are correct.
- B. Statement (i) is correct but statement (ii) is wrong.
- C. Statement (i) is wrong but statement (ii) is correct.
- D. Both (i) and (ii) are wrong.

Answer: B

Solution: Statement (ii) is incorrect.

3. (1 point) There are two sets A and B .

$$A = \{x : x \text{ is a prime number}\}$$

$$B = \{x : x \text{ is an odd number}\}$$

The universal set is $\mathbb{U} = \{x : 0 \leq x \leq 20\}$.

What is $B \cap A^c$?

- A. $\{1, 7, 11, 19\}$
- B. $\{1, 9, 15\}$
- C. \emptyset
- D. $\{9, 15\}$

Answer: B

Solution: Write the two sets and their complements.

$$A = \{2, 3, 5, 7, 11, 13, 17, 19\}$$

$$B = \{1, 3, 5, 7, 9, 11, 13, 15, 17, 19\}$$

$$A^c = \{0, 1, 4, 6, 8, 9, 10, 12, 14, 15, 16, 18, 20\}$$

$$B^c = \{0, 2, 4, 6, 8, 10, 12, 14, 16, 18, 20\}$$

Therefore, $B \cap A^c = \{1, 9, 15\}$.

Short Answer Questions-I

4. (1 point) The shortest side of a triangle is given by x cm. The longest side and the third side are given by $4x$ cm and $4x - 2$ cm respectively. What is the minimum value of x to have the perimeter greater than or equal to 79 cm?

Solution: The perimeter of a triangle with sides (a , b , and c) is given by $P = a + b + c$. All that we need to do is plug the given values. Let $a = x$, $b = 4x$, and $c = 4x - 2$.

$$P = x + 4x + 4x - 2$$

$$P \geq 79 \quad (\text{given})$$

$$x + 4x + 4x - 2 \geq 79$$

$$9x - 2 \geq 79$$

$$9x \geq 81$$

$$x \geq 9$$

5. (1 point) Simplify the following expression: $u^3 + v^3 - u^2v - v^2u$.

Solution:

$$u^3 + v^3 - u^2v - uv^2 = u^3 - u^2v + v^3 - uv^2$$

(rearranging terms)

$$= u^2(u - v) + v^2(v - u)$$

(taking u^2 and v^2 as common)

$$= u^2(u - v) - v^2(u - v)$$

(since $(b - a) = -(a - b)$)

$$= (u^2 - v^2)(u - v)$$

$$= (u + v)(u - v)(u - v)$$

(since $(a^2 - b^2) = (a + b)(a - b)$)

$$= (u + v)(u - v)^2$$

6. (1 point) Solve for x : $|7 - 3x| \leq 11$.

Solution: If $\epsilon > 0$ then $|x| \leq \epsilon$ if and only if $-\epsilon \leq x \leq \epsilon$. We will use this rule.

$$|7 - 3x| \leq 11$$

$$\Rightarrow -11 \leq 7 - 3x \leq 11$$

$$\Rightarrow -11 - 7 \leq 7 + (-7) - 3x \leq 11 - 7$$

(adding -7 to all sides)

$$\Rightarrow -18 \leq -3x \leq 4$$

$$\Rightarrow \frac{-4}{3} \leq x \leq 6$$

(since we are dividing by -3, we must switch signs.)

Short Answer Questions-II

7. (2 points) Solve for x .

$$\frac{(x+2)+3(x-1)}{x-3} \geq 0$$

Solution: Looking at the LHS, we already know what the value of x is not going to be.

$$x \neq 3$$

$$\begin{aligned} \frac{(x+2)+3(x-1)}{x-3} &\geq 0 \\ \frac{4x-1}{x-3} &\geq 0 \end{aligned}$$

There are only two scenarios under which the inequality will hold.

Case-I: the numerator has to be positive (or zero) and the denominator has to be positive (can't be zero).

$$\begin{aligned} 4x-1 &\geq 0 \\ x-3 &> 0 \end{aligned}$$

We have: $x \geq \frac{1}{4}$ and $x > 3$. Therefore,

$$x \in (3, \infty)$$

Case-II: the numerator has to be negative (or zero) and the denominator has to be negative.

$$\begin{aligned} 4x-1 &\leq 0 \\ x-3 &< 0 \end{aligned}$$

We have: $x \leq \frac{1}{4}$ and $x < 3$. Therefore,

$$x \in (-\infty, \frac{1}{4})$$

The final answer:

$$x \in (-\infty, \frac{1}{4}) \cup (3, \infty)$$

8. (2 points) In a survey of 35 students, it was found that 15 had taken Mathematics, 12 had taken Physics and 11 had taken Chemistry, 5 had taken Mathematics and Chemistry, 9 had taken Mathematics and Physics, 4 had taken Physics and Chemistry and 3 had taken all the three subjects. Find the number of students that had none of the subjects.

Solution: Let M be the set that contains students who took Maths, P who took Physics, and C who took Chem. Therefore, $n(M) = 15$, $n(P) = 12$, and $n(C) = 11$. We also know that:

$$\begin{aligned}n(M \cap C) &= 5 \\n(M \cap P) &= 9 \\n(P \cap C) &= 4 \\n(M \cap P \cap C) &= 3 \\n(\mathbb{U}) &= 35\end{aligned}$$

We are supposed to compute $n(M^c \cap P^c \cap C^c)$.

We know that, for any three sets A, B, C , the following is true:

$$n(A \cup B \cup C) = n(A) + n(B) + n(C) - n(A \cap B) - n(A \cap C) - n(B \cap C) + n(A \cap B \cap C)$$

Given the values, we will apply this formula.

$$\begin{aligned}n(M \cup P \cup C) &= n(M) + n(P) + n(C) - n(M \cap P) - n(M \cap C) - n(P \cap C) + n(M \cap P \cap C) \\ \Rightarrow n(M \cup P \cup C) &= 15 + 12 + 11 - 9 - 5 - 4 + 3 \\ \Rightarrow n(M \cup P \cup C) &= 38 - 18 + 3 \\ \Rightarrow n(M \cup P \cup C) &= 20 + 3 \\ \Rightarrow n(M \cup P \cup C) &= 23\end{aligned}$$

A complement of a set is just all the elements in the universal set excluding the ones within the set. Hence,

$$\begin{aligned}n(M^c \cap P^c \cap C^c) &= n(\mathbb{U}) - n(M \cup P \cup C) \\ \Rightarrow n(M^c \cap P^c \cap C^c) &= 35 - 23 \\ \Rightarrow n(M^c \cap P^c \cap C^c) &= 12\end{aligned}$$