

## Integrate using the substitution provided:

These questions are more difficult than those asked in exam.

1.  $\int \frac{1}{a^2 + x^2}, dx$  [Use  $x = a \tan(\theta)$ ]  $= \frac{1}{a} \arctan\left(\frac{x}{a}\right) + C$

2.  $\int \frac{1}{\sqrt{a^2 - x^2}}, dx$  [Use  $x = a \sin(\theta)$ ]  $= \arcsin\left(\frac{x}{a}\right) + C$

3.  $\int \frac{1}{\sqrt{x^2 + a^2}}, dx$  [Use  $x = a \tan(\theta)$ ]  $= \ln \left| x + \sqrt{x^2 + a^2} \right| + C$

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