

CSCI 564 Advanced Computer Architecture

Lecture 13: Multiprocessors

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Why Parallel Computers?

- Parallelism: Doing multiple things at a time
- Things: instructions, operations, tasks
- Main Goal
 - Improve performance (Execution time or task throughput)
 - Execution time of a program governed by Amdahl's Law
- Other Goals
 - Reduce power consumption
 - ($4N$ units at freq $F/4$) consume less power than (N units at freq F)
 - Why?
 - Improve cost efficiency and scalability, reduce complexity
 - Harder to design a single unit that performs as well as N simpler units

Types of Parallelism and How to Exploit Them

- Instruction Level Parallelism
 - Different instructions within a stream can be executed in parallel
 - Pipelining, out-of-order execution
 - Dataflow
- Data Parallelism
 - Different pieces of data can be operated on in parallel
 - SIMD: Vector processing, array processing
 - GPUs
- Task Level Parallelism
 - Different “tasks/threads” can be executed in parallel
 - Multithreading
 - Multiprocessing (multi-core)

Task-Level Parallelism: Creating Tasks

- Partition a single problem into multiple related tasks (threads)
 - Explicitly: Parallel programming
 - Easy when tasks are natural in the problem
 - Web/database queries
 - Difficult when natural task boundaries are unclear
 - Transparently/implicitly: compiler vectorization
- Run many independent tasks (processes) together
 - Easy when there are many processes
 - Batch simulations, different users, cloud computing workloads
 - Does not improve the performance of a single task

Multiprocessing Fundamentals

Multiprocessor Types

- Loosely coupled multiprocessors
 - No shared global memory address space
 - Multicomputer network
 - Network-based multiprocessors
 - Usually programmed via message passing
 - Explicit calls (send, receive) for communication
- Tightly coupled multiprocessors
 - Shared global memory address space
 - Traditional multiprocessing: symmetric multiprocessing (SMP)
 - Existing multi-core processors, multithreaded processors
 - Programming model similar to uniprocessors (i.e., multitasking uniprocessor) except
 - Operations on shared data require synchronization

Main Issues in Tightly-Coupled MP

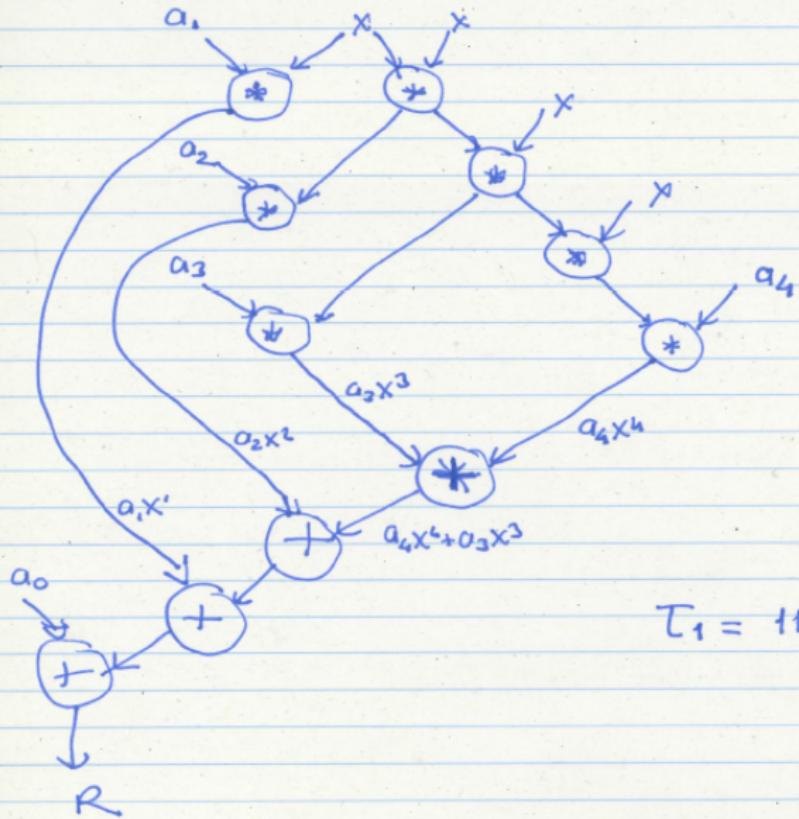
- Shared memory synchronization
 - Locks, atomic operations
- Cache consistency
 - More commonly called cache coherence
- Ordering of memory operations
 - What should the programmer expect the hardware to provide?
- Resource sharing, contention, partitioning
- Communication: Interconnection networks
- Load imbalance

Parallel Speedup Example

- $a_4x^4 + a_3x^3 + a_2x^2 + a_1x + a_0$
- Assume each operation 1 cycle, no communication cost, each op can be executed in a different processor
- How fast is this with a single processor?
 - Assume no pipelining or concurrent execution of instructions
- How fast is this with 3 processors?

$$R = a_4x^4 + a_3x^3 + a_2x^2 + a_1x + a_0$$

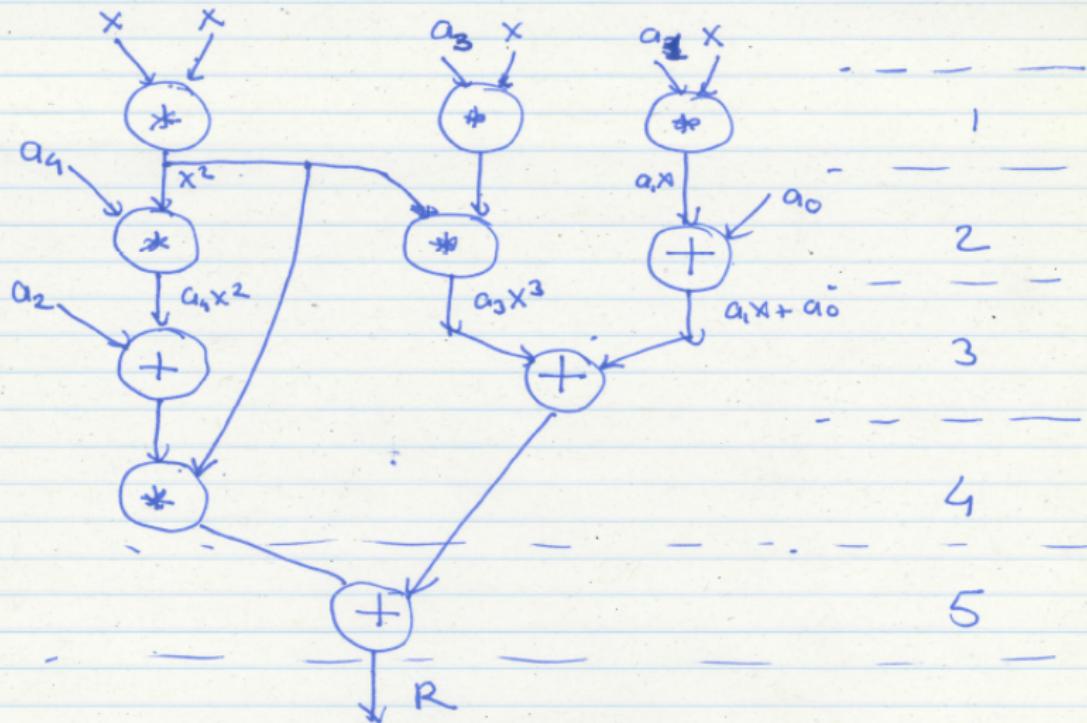
Single processor : 11 operations (draw the data flow graph)



$T_1 = 11$ cycles

$$R = a_n x^n + a_{n-1} x^{n-1} + a_{n-2} x^{n-2} + \dots + a_1 x + a_0$$

Three processors : T_3 (exec. time w/ 3 proc.)



$$T_3 = \underline{5 \text{ cycles}}$$

Speedup with 3 Processors

$$T_3 = \underline{5 \text{ cycles}}$$

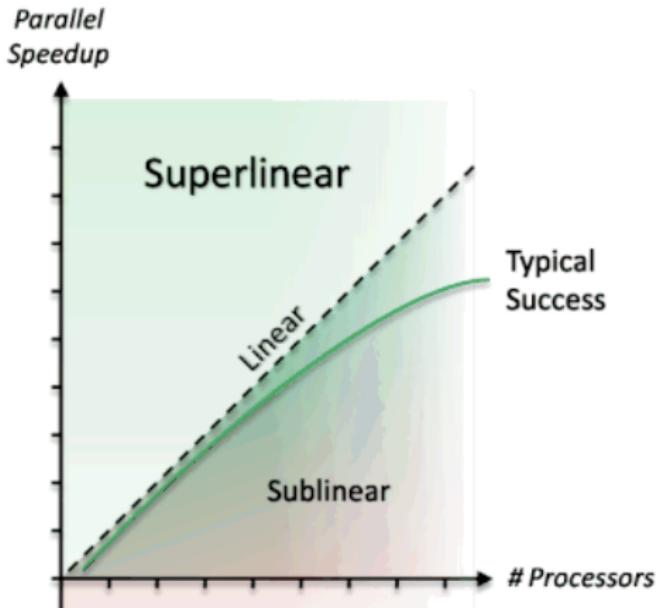
$$\text{Speedup with 3 processors} = \frac{11}{5} = 2.2$$

$$\left(\frac{T_1}{T_3} \right)$$

Is this a fair comparison?

Superlinear Speedup

- Can speedup be greater than P with P processing elements?
- Cache effects
- Working set effects



Revisiting the Single-Processor

Revisit T₁

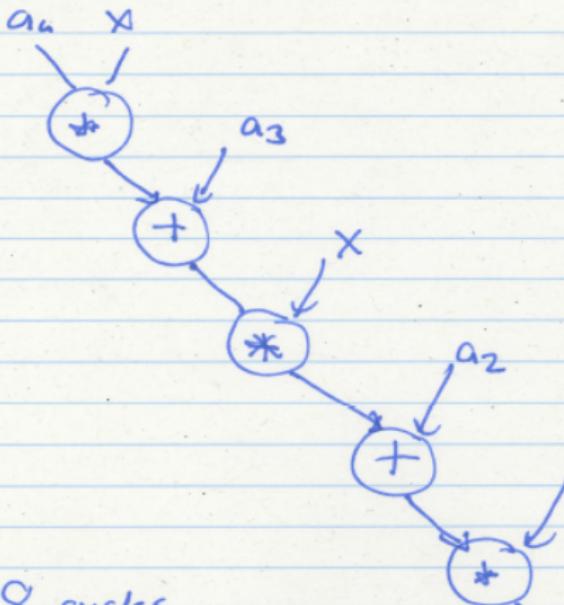
Better single-processor algorithm:

$$R = a_4x^4 + a_3x^3 + a_2x^2 + a_1x + a_0$$

$$R = (((a_4x + a_3)x + a_2)x + a_1)x + a_0$$

(Horner's method)

Horner, "A new method of solving numerical equations of all orders, by continuous approximation," Philosophical Transactions of the Royal Society, 1819.



$$T_1 = 8 \text{ cycles}$$

Speedup with 3 procs. = $\frac{T_1^{\text{best}}}{T_3^{\text{best}}} = \frac{8}{5} = \underline{1.6}$

(not 2.2)

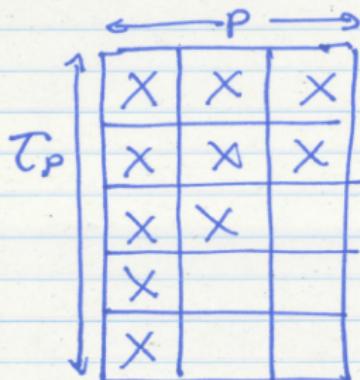
Utilization, Redundancy, Efficiency

- Utilization: How much processing capability is used
 - $U = (\# \text{ Operations in parallel version}) / (\text{processors} \times \text{Time})$
- Redundancy: how much extra work is done with parallel processing
 - $R = (\# \text{ of operations in parallel version}) / (\# \text{ operations in best single processor algorithm version})$
- Efficiency
 - $E = (\text{Time with 1 processor}) / (\text{processors} \times \text{Time with } P \text{ processors})$
 - $E = U/R$

Utilization of a Multiprocessor

Multiprocessor metrics

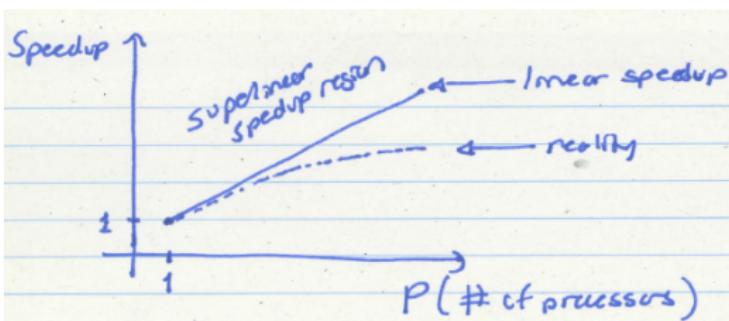
Utilization : How much processing capability we use



$$U = \frac{10 \text{ operations (in parallel version)}}{3 \text{ processors} \times 5 \text{ time units}}$$
$$= \frac{10}{15}$$

$$U = \frac{\text{Ops with proc.}}{P \times T_P}$$

Caveats of Parallelism (I)



Why the reality? (diminishing returns)

$$T_p = \alpha \cdot \frac{T_1}{P} + (1-\alpha) \cdot T_1$$

parallelizable part/fraction
of the single-processor
program

non-parallelizable part

Redundancy: How much extra work due to multiprocessor

$$R = \frac{\text{Ops with } p \text{ proc.}^{\text{best}}}{\text{Ops with } 1 \text{ proc.}^{\text{best}}} = \frac{10}{8}$$

R is always ≥ 1

Efficiency: How much resource we use compared to how much resource we can get away with

$$E = \frac{1 \cdot T_1^{\text{best}}}{p \cdot T_p^{\text{best}}} \quad \begin{array}{l} (\text{tying up 1 proc for } T_p \text{ time units}) \\ (\text{tying up } p \text{ proc for } T_p \text{ time units}) \end{array}$$
$$= \frac{8}{15} \quad \left(E = \frac{U}{R} \right)$$

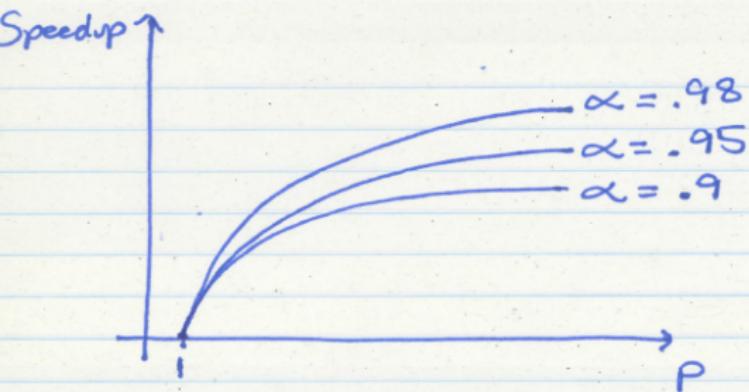
Amdahl's Law

$$\text{Speedup with } p \text{ proc.} = \frac{T_1}{T_p} = \frac{1}{\frac{\alpha}{P} + (1-\alpha)}$$

$$\text{Speedup as } p \rightarrow \infty = \frac{1}{1-\alpha} \rightarrow \text{ bottleneck for parallel Speedup}$$

Amdahl, "Validity of the single processor approach to achieving large scale computing capabilities," AFIPS 1967.

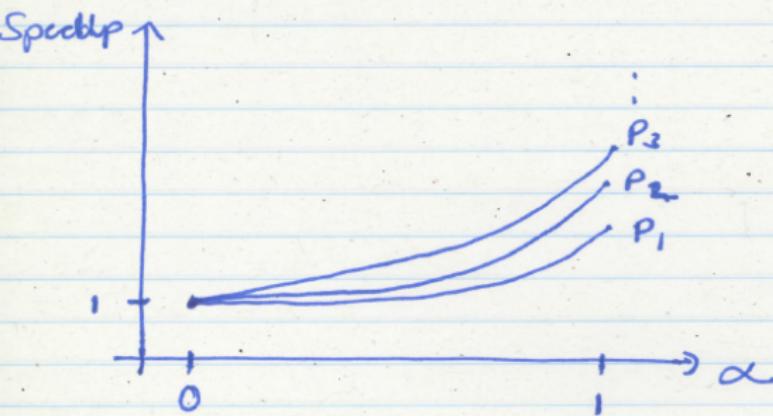
Amdahl's Law Implication 1



Amdahl's Law
illustrated

Adding more and more processors gives less & less benefit: if $\alpha < 1$

Amdahl's Law Implication 2



The benefit (speedup)
is small until $\alpha \approx 1$

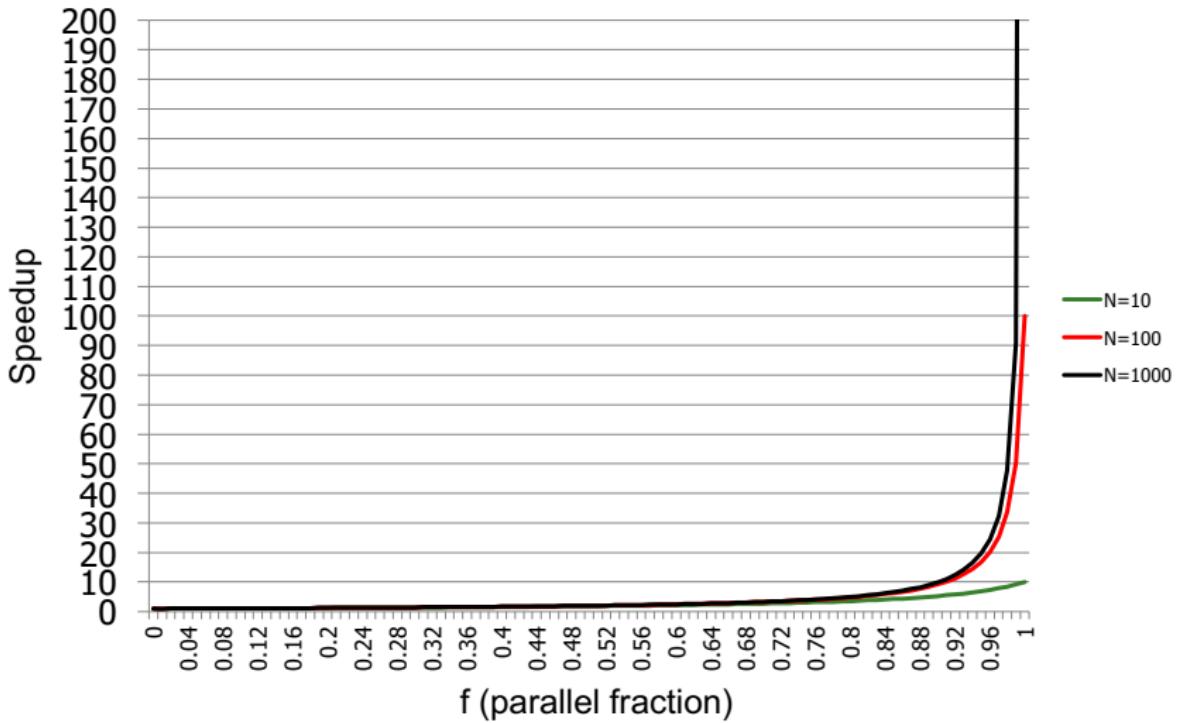
Caveats of Parallelism

- Amdahl's Law
 - f : Parallelizable fraction of a program
 - N : Number of processors

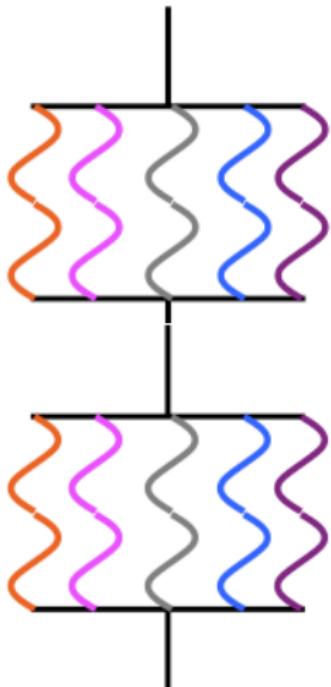
$$\text{Speedup} = \frac{1}{1 - f + \frac{f}{N}}$$

- Amdahl, “[Validity of the single processor approach to achieving large scale computing capabilities](#),” AFIPS 1967.
- Maximum speedup limited by serial portion: Serial bottleneck
- Parallel portion is usually not perfectly parallel
 - [Synchronization](#) overhead (e.g., updates to shared data)
 - [Load imbalance](#) overhead (imperfect parallelization)
 - [Resource sharing](#) overhead (contention among N processors)

Sequential Bottleneck



Why the Sequential Bottleneck?



- Parallel machines have the sequential bottleneck
- Main cause: **Non-parallelizable operations on data** (e.g. non-parallelizable loops)
$$\text{for } (i = 0 ; i < N; i++)$$
$$A[i] = (A[i] + A[i-1]) / 2$$
- Single thread prepares data and spawns parallel tasks (usually sequential)

Asymmetry Enables Customization

c	c	c	c
c	c	c	c
c	c	c	c
c	c	c	c

Symmetric

C1		C2	
		C3	
C4	C4	C4	C4
C5	C5	C5	C5

Asymmetric

- Symmetric: One size fits all
 - Energy and performance suboptimal for different “workload” behaviors
- Asymmetric: Enables customization and adaptation
 - Processing requirements vary across workloads (applications and phases)
 - Execute code on best-fit resources (minimal energy, adequate perf.)

Aside: Examples from Life

- Heterogeneity is abundant in life
 - both in nature and human-made components
- Humans are heterogeneous
- Cells are heterogeneous → specialized for different tasks
- Organs are heterogeneous
- Cars are heterogeneous
- Buildings are heterogeneous
- Rooms are heterogeneous
- ...

General-Purpose vs. Special-Purpose

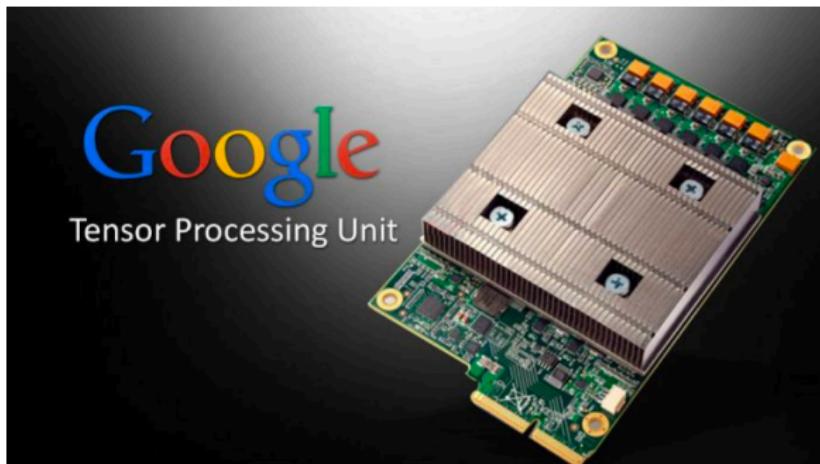
- Asymmetry is a way of enabling specialization
- It bridges the gap between purely general purpose and purely special purpose
 - Purely general purpose: Single design for every workload or metric
 - Purely special purpose: Single design per workload or metric
 - Asymmetric: Multiple sub-designs optimized for sets of workloads/metrics and glued together
- The goal of a good asymmetric design is to get the best of both general purpose and special purpose

Asymmetry Advantages and Disadvantages

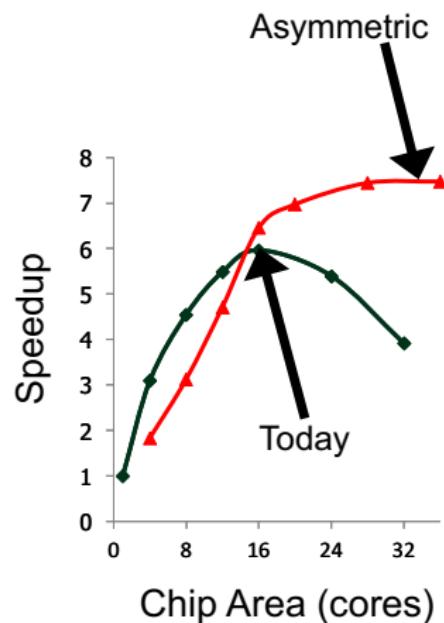
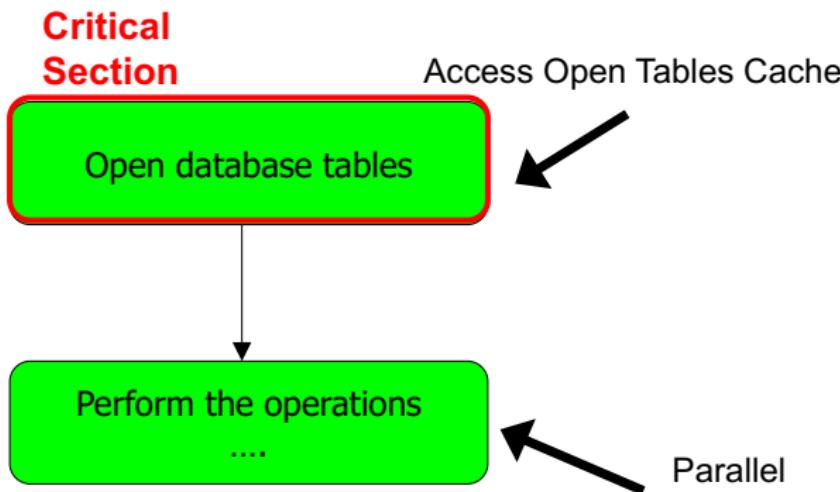
- Advantages over Symmetric Design
 - + Can enable optimization of multiple metrics
 - + Can enable better adaptation to workload behavior
 - + Can provide special-purpose benefits with general-purpose usability/flexibility
- Disadvantages over Symmetric Design
 - Higher overhead and more complexity in design, verification
 - Higher overhead in management: scheduling onto asymmetric components
 - Overhead in switching between multiple components can lead to degradation

Yet Another Example

- Modern processors integrate general purpose cores and GPUs
 - CPU-GPU systems
 - Heterogeneity in execution models



Example from MySQL



Demands in Different Code Sections

- What we want:
- In a serialized code section → one powerful “large” core
- In a parallel code section → many wimpy “small” cores
- These two conflict with each other:
 - If you have a single powerful core, you cannot have many cores
 - A small core is much more energy and area efficient than a large core

“Large” vs. “Small” Cores

Large Core

Small Core

- *Out-of-order*
- *Wide fetch e.g. 4-wide*
- *Deeper pipeline*
- *Aggressive branch predictor (e.g. hybrid)*
- *Multiple functional units*
- *Trace cache*
- *Memory dependence*

- *In-order*
- *Narrow Fetch e.g. 2-wide*
- *Shallow pipeline*
- *Simple branch predictor (e.g. Gshare)*
- *Few functional units*

Large Cores are power inefficient:
e.g., 2x performance for 4x area (power)

Large vs. Small Cores

- Grochowski et al., “[Best of both Latency and Throughput](#),” ICCD 2004.

	Large core	Small core
Microarchitecture	Out-of-order, 128-256 entry ROB	In-order
Width	3-4	1
Pipeline depth	20-30	5
Normalized performance	5-8x	1x
Normalized power	20-50x	1x
Normalized energy/instruction	4-6x	1x

Remember the Demands

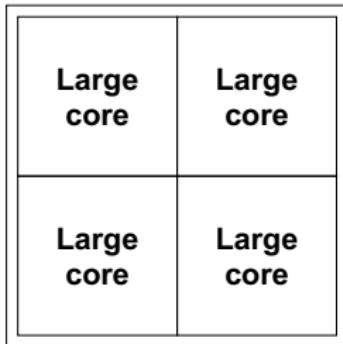
- What we want:
- In a serialized code section → one powerful “large” core
- In a parallel code section → many wimpy “small” cores
- These two conflict with each other:
 - If you have a single powerful core, you cannot have many cores
 - A small core is much more energy and area efficient than a large core
- Can we get the best of both worlds?

Performance vs. Parallelism

Assumptions:

1. *Small cores takes an area budget of 1 and has performance of 1*
2. *Large core takes an area budget of 4 and has performance of 2*

Tile-Large Approach



“Tile-Large”

- Tile a few large cores
- IBM Power 5, AMD Barcelona, Intel Core2Quad, Intel Nehalem
 - + High performance on single thread, serial code sections (2 units)
 - Low throughput on parallel program portions (8 units)

Tile-Small Approach

Small core	Small core	Small core	Small core
Small core	Small core	Small core	Small core
Small core	Small core	Small core	Small core
Small core	Small core	Small core	Small core

“Tile-Small”

- Tile many small cores
- Sun Niagara, Intel Larrabee, Tilera TILE (tile ultra-small)
 - + High throughput on the parallel part (16 units)
 - Low performance on the serial part, single thread (1 unit)

Can we get the best of both worlds?

- Tile Large
 - + High performance on single thread, serial code sections (2 units)
 - Low throughput on parallel program portions (8 units)
- Tile Small
 - + High throughput on the parallel part (16 units)
 - Low performance on the serial part, single thread (1 unit), reduced single-thread performance compared to existing single thread processors
- Idea: Have both large and small on the same chip → Performance asymmetry

Asymmetric Multi-Core

Asymmetric Chip Multiprocessor (ACMP)

Large core	Large core
Large core	Large core

“Tile-Large”

Small core	Small core	Small core	Small core
Small core	Small core	Small core	Small core
Small core	Small core	Small core	Small core
Small core	Small core	Small core	Small core

“Tile-Small”

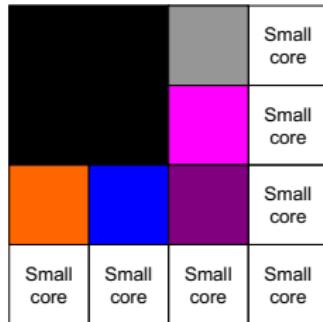
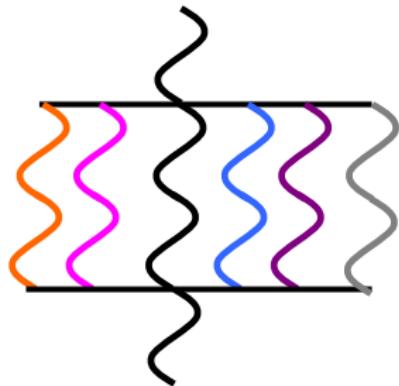
Large core		Small core	Small core
Small core		Small core	Small core
Small core	Small core	Small core	Small core
Small core	Small core	Small core	Small core

ACMP

- Provide one large core and many small cores
 - + Accelerate serial part using the large core (2 units)
 - + Execute parallel part on small cores and large core for high throughput (12+2 units)

Accelerating Serial Bottlenecks

Single thread → Large core



ACMP Approach

ACMP Performance vs. Parallelism

Area-budget = 16 small cores

	“Tile-Large”	“Tile-Small”	ACMP
Large Cores	4	0	1
Small Cores	0	16	12
Serial Performance	2	1	2
Parallel Throughput	$2 \times 4 = 8$	$1 \times 16 = 16$	$1 \times 2 + 1 \times 12 = 14$

The diagram illustrates three different ways to utilize an area budget of 16 small cores for parallel processing:

- “Tile-Large”:** This configuration uses 4 large cores, each equivalent to 4 small cores. It is enclosed in a red rounded rectangle.
- “Tile-Small”:** This configuration uses 16 small cores, arranged in a 4x4 grid. It is enclosed in a red rounded rectangle.
- ACMP:** This configuration uses 1 large core and 12 small cores. The large core is also equivalent to 4 small cores. It is enclosed in a red rounded rectangle.

Amdahl's Law Modified

- Simplified Amdahl's Law for an Asymmetric Multiprocessor
- Assumptions:
 - Serial portion executed on the large core
 - Parallel portion executed on both small cores and large cores
 - f : Parallelizable fraction of a program
 - L : Number of large processors
 - S : Number of small processors
 - X : Speedup of a large processor over a small one

$$\text{Speedup} = \frac{1}{\frac{1-f}{X} + \frac{f}{S+X*L}}$$

Accelerating Parallel Bottlenecks

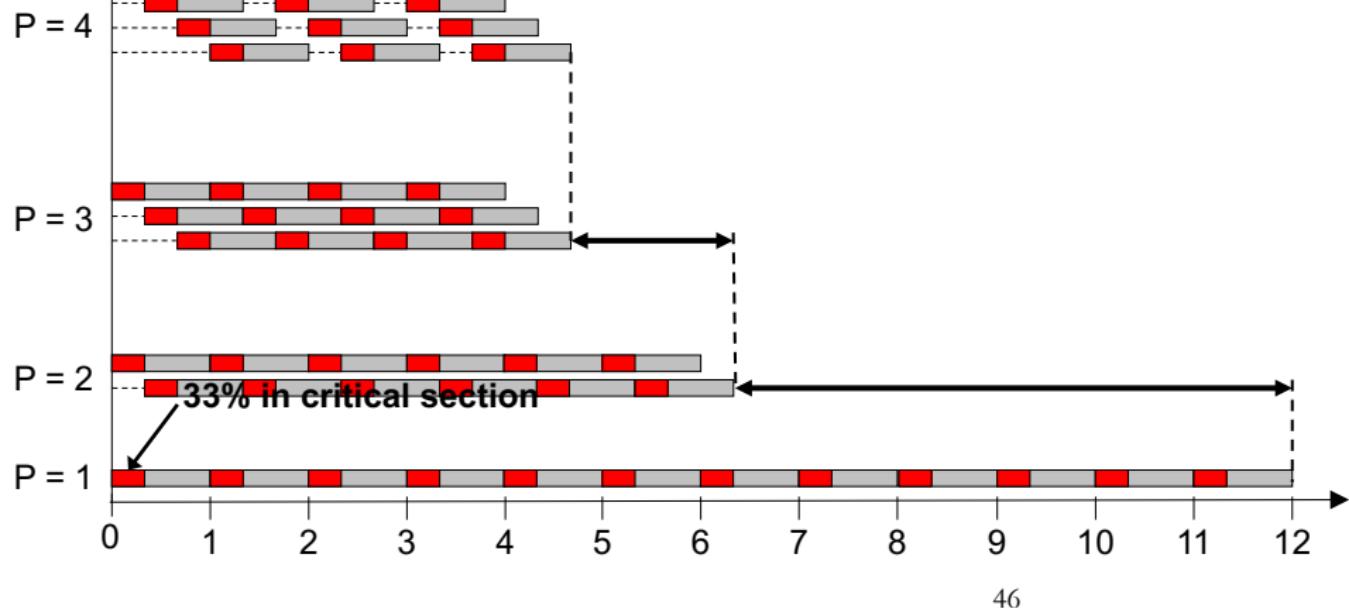
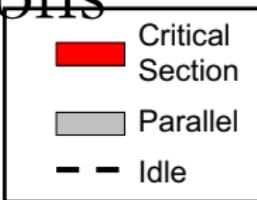
- Serialized or imbalanced execution in the parallel portion can also benefit from a large core
- Examples:
 - Critical sections that are contended
 - Parallel stages that take longer than others to execute
- Idea: Dynamically identify these code portions that cause serialization and execute them on a large core

Accelerated Critical Sections

M. Aater Suleman, [Onur Mutlu](#), Moinuddin K. Qureshi, and Yale N. Patt,
"Accelerating Critical Section Execution with Asymmetric Multi-Core Architectures"
Proceedings of the 14th International Conference on Architectural Support for Programming Languages and Operating Systems (ASPLOS), 2009

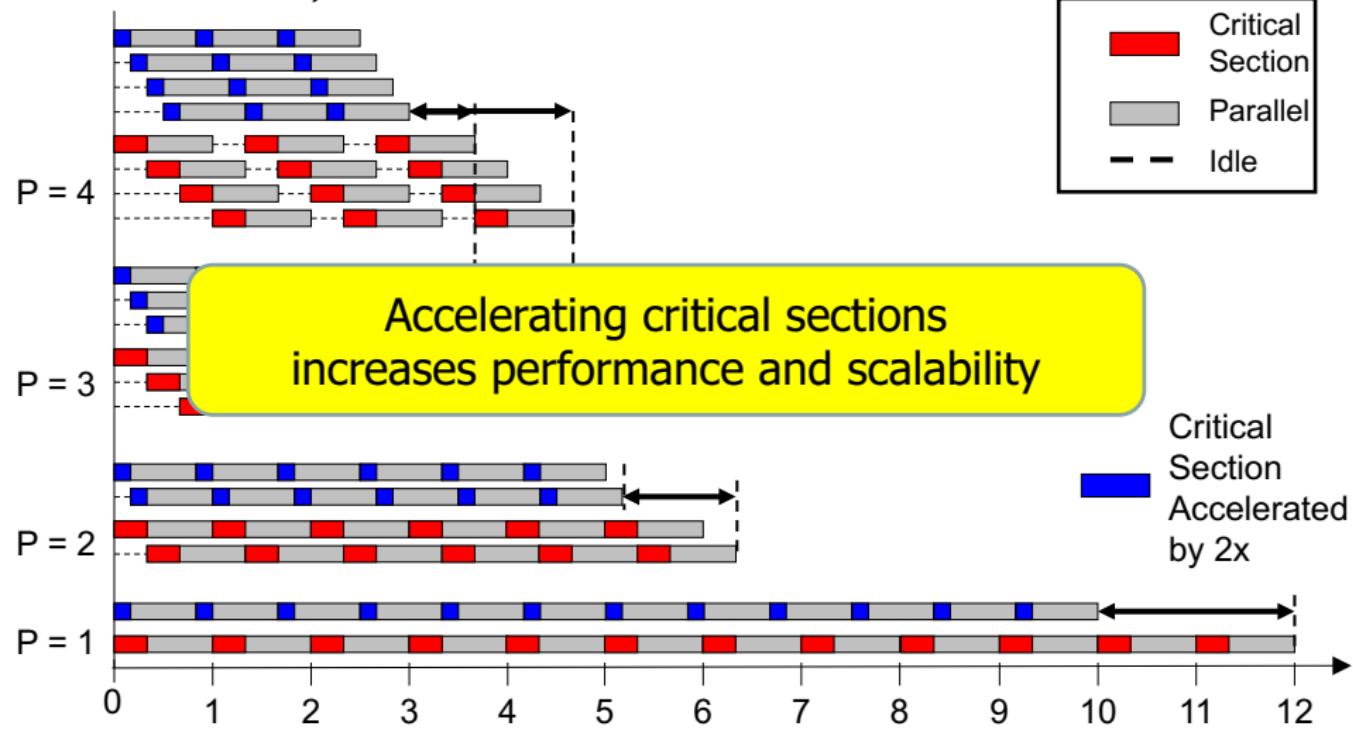
Contention for Critical Sections

12 iterations, 33% instructions inside the critical section



Contention for Critical Sections

12 iterations, 33% instructions inside the critical section



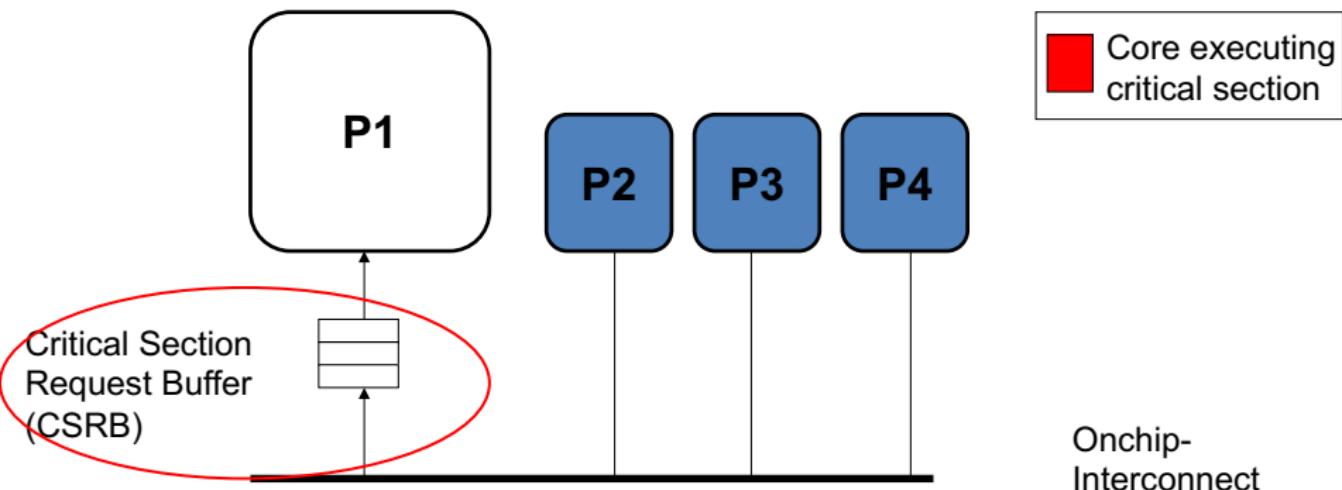
An Example: Accelerated Critical Sections

- Idea: HW/SW ships critical sections to a large, powerful core in an asymmetric multi-core architecture
- Benefit:
 - Reduces serialization due to contended locks
 - Reduces the performance impact of hard-to-parallelize sections
 - Programmer does not need to (heavily) optimize parallel code → fewer bugs, improved productivity
- Suleman et al., “Accelerating Critical Section Execution with Asymmetric Multi-Core Architectures,” ASPLOS 2009, IEEE Micro Top Picks 2010.
- Suleman et al., “Data Marshaling for Multi-Core Architectures,” ISCA 2010, IEEE Micro Top Picks 2011.

Accelerated Critical Sections

```
EnterCS()  
PriorityQ.insert(...)  
LeaveCS()
```

1. P2 encounters a critical section (CSCALL)
2. P2 sends CSCALL Request to CSRB
3. P1 executes Critical Section
4. P1 sends CSDONE signal



Accelerated Critical Sections (ACS)

Small Core

A = compute()

LOCK X

 result = CS(A)

UNLOCK X

print result

Small Core

A = compute()

PUSH A

CSCALL X, Target PC

...

...

...

...

...

...

...

CSCALL Request

Send X, TPC,
STACK_PTR, CORE_ID

Large Core

...
...
...
Waiting in
Critical Section
Request Buffer
(CSRB)

TPC: Acquire X

POP A

result = CS(A)

PUSH result

Release X

CSRET X

← CSDONE Response

POP result

print result

- Suleman et al., “[Accelerating Critical Section Execution with Asymmetric Multi-Core Architectures](#),” ASPLOS 2009.

False Serialization

- ACS can serialize independent critical sections
- Selective Acceleration of Critical Sections (SEL)
 - Saturating counters to track false serialization

