

Guide to the coursework

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Networks

- ▶ The coursework deals with **flows** on **networks**
- ▶ A network is a directed graph ...
 - ▶ Nodes
 - ▶ Edges $m \rightarrow n$ for some pairs of nodes m, n
- ▶ With additional data:
 - ▶ Two special nodes, the **source** and the **target**
 - ▶ Each edge has a **capacity** (how much flow it can accommodate)

Flows

- ▶ The coursework deals with **flows** on **networks**
- ▶ A **flow** associates a number with each edge
 - ▶ At least 0, at most the edge's capacity
 - ▶ Flow along an edge $m \rightarrow n$ flows **out of** m and **into** n
 - ▶ For each node n except the source and target, the total flow **into** n must equal the total flow **out of** n
 - ▶ No flow into the source or out of the target
- ▶ We want a flow which **maximises** the flow out of the source.

What to do: part 1

- ▶ Choose a suitable **data structure** to represent networks
 - ▶ The lecture introduced some ways of representing **graphs**
 - ▶ Think about how these can be adapted to accommodate additional data
(capacity and flow for each edge)
- ▶ Implement your data structure
- ▶ You will also need a method for printing a graph
(for debugging and showing steps of your algorithm)

What to do: part 2

- ▶ Implement a parser to read a network from a file
- ▶ The file format is:
 - ▶ One line containing the number N of nodes
 - ▶ Nodes are numbered $0, \dots, N - 1$
 - ▶ The source is always node 0
 - ▶ The target is always node $N - 1$
 - ▶ Several lines describing edges: for example,
2 4 5
means that there is an edge
 - ▶ from node 2
 - ▶ to node 4
 - ▶ with capacity 5

What to do: part 3

- ▶ Choose an algorithm to compute the maximum flow
- ▶ We will describe one (Ford-Fulkerson) in the lecture
- ▶ Implement your algorithm
- ▶ Test it using several examples, such as the benchmarks provided
- ▶ Write your report:
 - ▶ A short explanation of your choice of data structure and algorithm
 - ▶ A run of your algorithm on a small benchmark example
 - ▶ Timing analysis of your implementation