AUTOMATA FORMAL LANGUAGES AND LOGIC



Lecture notes on Equivalence of Regular expressions

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1. Equivalence of two regular expression

Two regular expressions(R1and R2)are equivalent(R1=R2) iff:

$$L(R1) = L(R2)$$

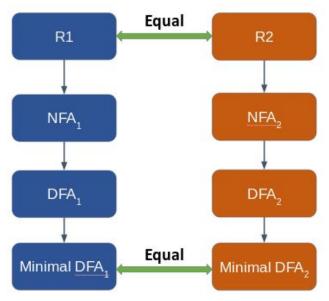
2. Methods to determine the equivalence of Regular Expressions:

We can determine the equivalence using two methods

1) A Formal method

The classical approach to the problem of comparing two regular expressions α and β , i.e.,deciding ifL(R1) =L(R2), typically consists of:

- 1. obtain non-deterministic finite automata, N(R1) and N(R2), which accept the same language as R1 and R2, respectively using Thompson construction method.
- 2. convert the non-deterministic automata to equivalent deterministic ones, $D(R1) \equiv N(R1)$ and $D(R1) \equiv N(R2)$ using subset construction method
- 3. minimise both D(R1) and D(R2).Because, for a given regular language, the minimal automaton is unique

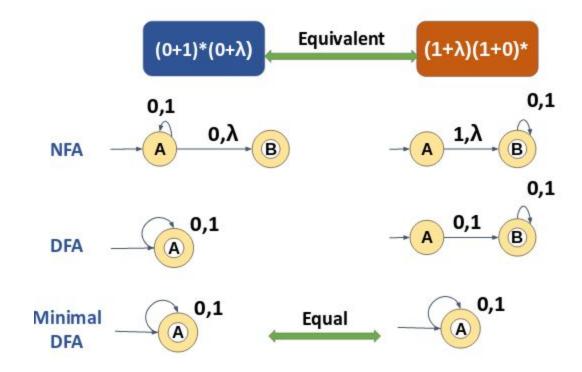


2) An Informal method

In Informal method, the aim is not to prove that the two regular expressions are equal. Instead we focus on proving that they are not equivalent. To show that two regular expressions are not equivalent we have to find a word that belongs to one expression and does not belong to the other.

3. Examples

1) Check the Equivalence of two regular expression using formal method R1 = $(0+1)*(0+\lambda)$ and R2 = $(1+\lambda)(1+0)*$



Since both the minimal DFAs are equal We conclude that the given regex are equivalent.

2) Check the Equivalence of two regular expression using informal method

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R1 = (0+\lambda)(11*0)*(1+\lambda) and R2 = (1+\lambda)(011*)(0+\lambda)
Consider the String 011
011 \in R2
011 \notin R1
So,
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3) Check the Equivalence of two regular expression using informal method R1 = $(1+\lambda)(00*1)*0*$ and R2 = $(0+\lambda)(11*0)1*$

Consider the String 00 $00 \in R1$ $00 \notin R1$ So, $R1 \neq R2$

 $R1 \neq R2$

4) Check the Equivalence of two regular expression using informal method R1 = 0*(10*)* and R2 = (1*0)*1*

 $\ensuremath{\mathsf{R}} 1$ can generate all strings generated by $\ensuremath{\mathsf{R}} 2$ and vice versa , So they are equivalent. Example string :

b, aba, bb, ...