



Automata Formal Languages & Logic

Preet Kanwal

Department of Computer Science & Engineering

Automata Formal Languages & Logic

Unit 3

Preet Kanwal

Department of Computer Science & Engineering

Example 1:

Construct CFG for $L = \{uvwv^R, |u|=|w|=2, |v|>1, w \in \{a,b\}^*\}$

Solution :

$S \rightarrow A B$

$A \rightarrow aa \mid bb \mid ab \mid ba$

$B \rightarrow aBa \mid bBb \mid A$

Example 2:

Construct a CFG for $L = \{w \in \{a,b\}^* \mid n_a(w) = n_b(w)\}$

Solution :

$S \rightarrow aSb \mid bSa \mid \lambda \mid SS$

Example 3:

Construct a CFG for $L = \{w \in \{a,b\}^* \mid n_a(w) = n_b(w) + 1\}$

Solution :

$S \rightarrow AaA$

$A \rightarrow aAb \mid bAa \mid AA \mid \lambda$

or

$S \rightarrow aSb \mid bSa \mid abS \mid baS \mid a$

Example 4:

Construct a CFG for $L = \{w \mid n_a(w) = 2 \times n_b(w), w \in \{a,b\}^*\}$

Solution :

$S \rightarrow aSaSb \mid bSaSa \mid aSbSb \mid SS \mid \lambda$

Example 5:

Construct a CFG for $L = \{n_a(w) > n_b(w), w \in \{a,b\}^*\}$

Solution :

$S \rightarrow AaA$

$A \rightarrow aAb \mid bAa \mid AA \mid aA \mid Aa \mid \lambda$

Example 6:

Construct a CFG for $L = \{w \in \{a,b\}^* \mid n_a(w) \neq n_b(w)\}$

Solution :

$S \rightarrow AaA \mid BbB$

$A \rightarrow aAb \mid bAa \mid Aa \mid aA \mid \lambda$

$B \rightarrow aBb \mid bBa \mid Bb \mid bB \mid \lambda$

Example 7:

Construct a CFG for $L = \{a^n b^n \cup a^n b^{2n}\}$.

Solution :

$S \rightarrow S1 \mid S2$
 $S1 \rightarrow aS1b \mid \lambda$
 $S2 \rightarrow aS2bb \mid \lambda$

Example 8:

**Construct /a CFG for Language of proper nesting(parenthesis matching)
where $\Sigma = \{ (,) \}$.**

Solution :

$S \rightarrow (S) \mid SS$

$S \rightarrow \lambda$

Example 9:

**Construct /a CFG for Language of proper nesting(parenthesis matching)
where $\Sigma = \{(\{,[\ ,\},\},)\}$.**

Solution :

$S \rightarrow (S) \mid \{S\} \mid [S] \mid SS \mid \lambda$

Example 10:

Construct a CFG for Language to generate arithmetic expressions.

Solution :

$E \rightarrow E + E \mid E - E \mid E * E \mid E / E \mid (E) \mid id \mid number$

Example 11:

Construct a CFG for nested if else.

Solution :

$S \rightarrow \text{if condition then } S$

$S \rightarrow \text{if condition then } S \text{ else } S$

$S \rightarrow \{ \text{statement} \}$

Example 12:

Construct a CFG to take care of variable declarations in C Language.

Solution :

$D \rightarrow \text{Type List}$

$\text{List} \rightarrow \text{List, id} \mid \text{id}$

$\text{Type} \rightarrow \text{int} \mid \text{float} \mid \text{char}$

Example 13:

Construct a CFG to generate nested while loops.

Solution :

$S \rightarrow \text{while}(\text{condition})S \mid \{\text{statement}\}$

Do while loop:

$S \rightarrow \text{while}(\text{condition})S \mid \text{do } S \text{ while } (\text{condition})\{\text{statement}\}$



THANK YOU

Preet Kanwal

Department of Computer Science & Engineering

preetkanwal@pes.edu

+91 80 6666 3333 Extn 724