

DFA Construction

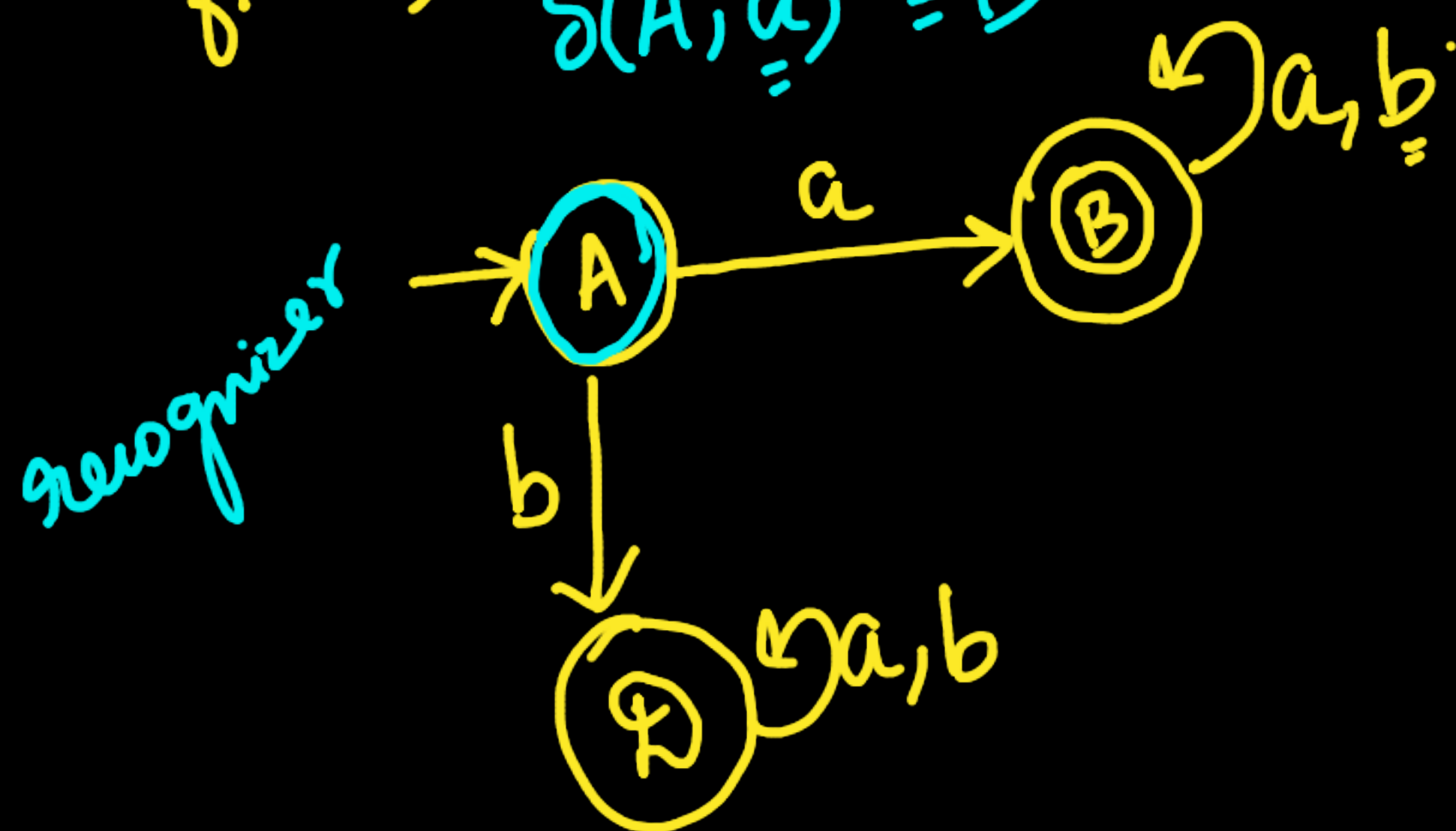
$$L = \{ w : \underline{a}\underline{w}, w \in \{a, b\}^* \}$$

$$L = \{ \underline{a}, \underline{ab}, \underline{aa}, \underline{abbba}, \dots \}$$

(infinite)

$$\delta: Q \times \Sigma \rightarrow Q$$

$$\delta(A, \underline{a}) = B$$



\underline{abb}

$\delta^*(\underline{A}, \underline{abb}) = \delta^*(B, \underline{bb})$

$\hookrightarrow = \delta(B, \underline{b})$

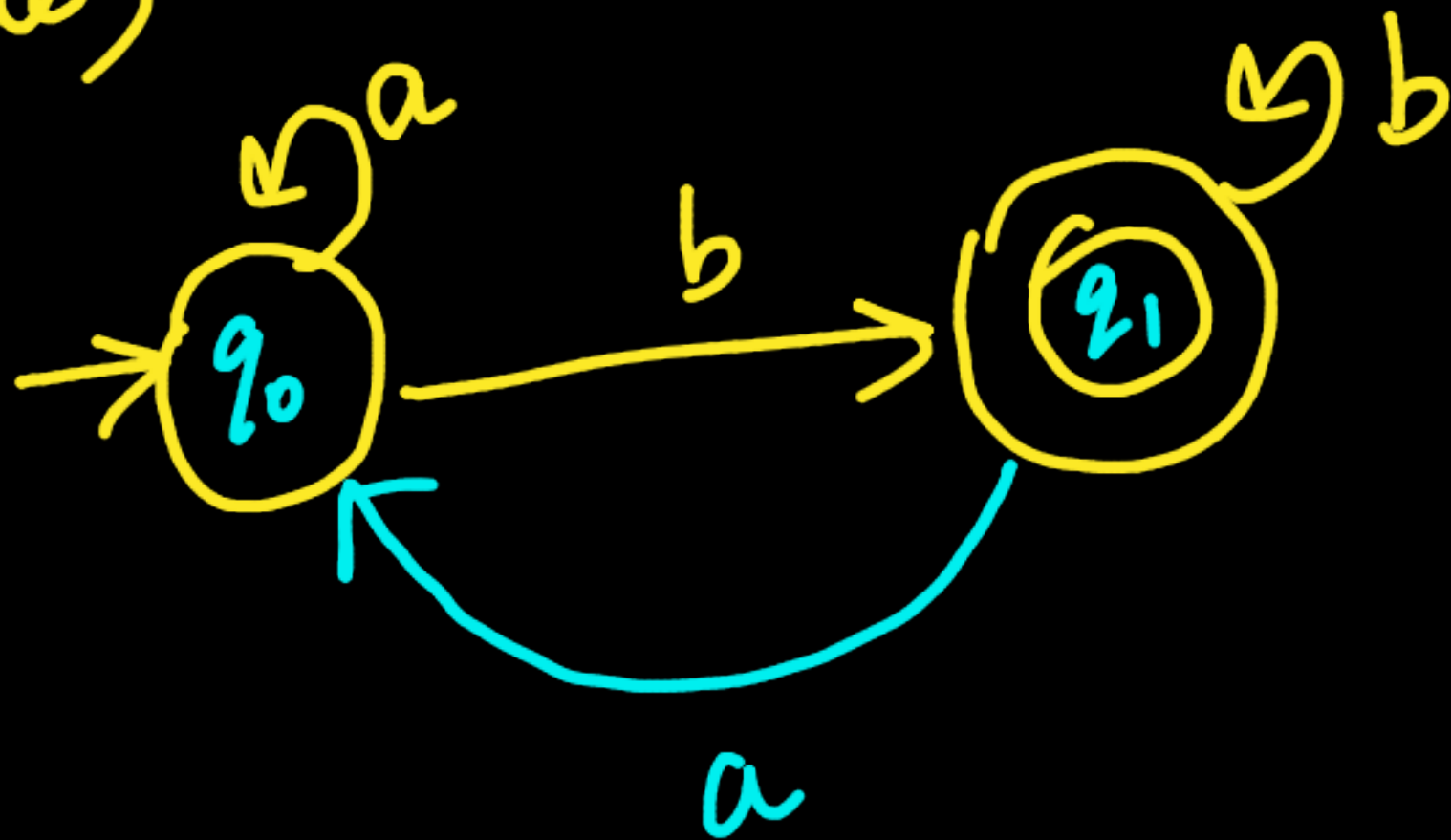
$\hookrightarrow = B \checkmark$

$\boxed{b}ab \times$

$$L = \{ w : w \underline{b}, w \in \{ \underline{a}, \underline{b} \}^* \}$$

$$L = \{ b, \underline{a} \underline{b}, b \underline{b}, (\text{any no. of a's \& b's}) \underline{b} \dots \}$$

(infinite)

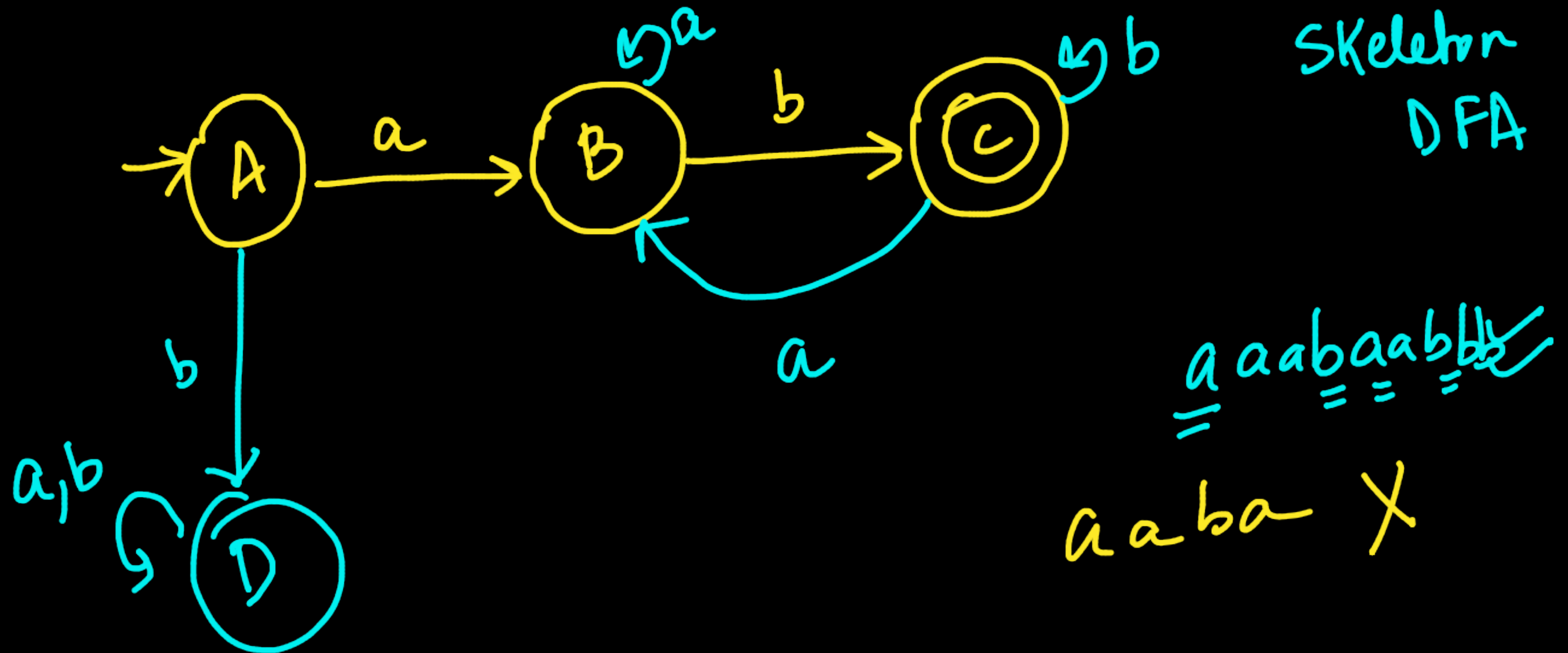


abbab

abba rejected

$$L = \{ w : a \underline{w} b, w \in \{a, b\}^* \}$$

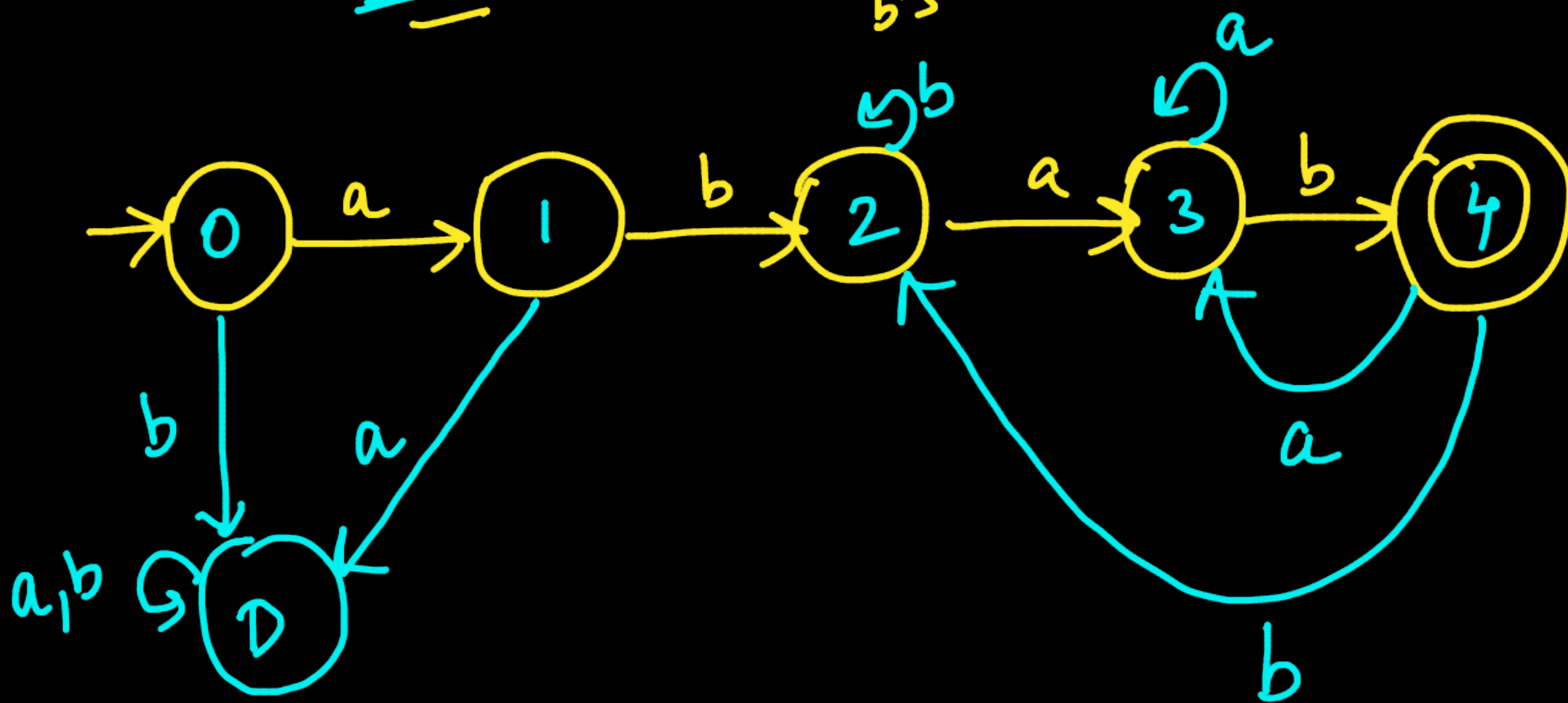
$$L = \{ ab, a \underline{a} b \text{ or } a \underline{b} b, a \dots \overset{a's}{\text{or}} \overset{b's}{b} \}$$



$L = \{ w : \underline{ab}w\underline{ab}, w \in \{a,b\}^* \}$

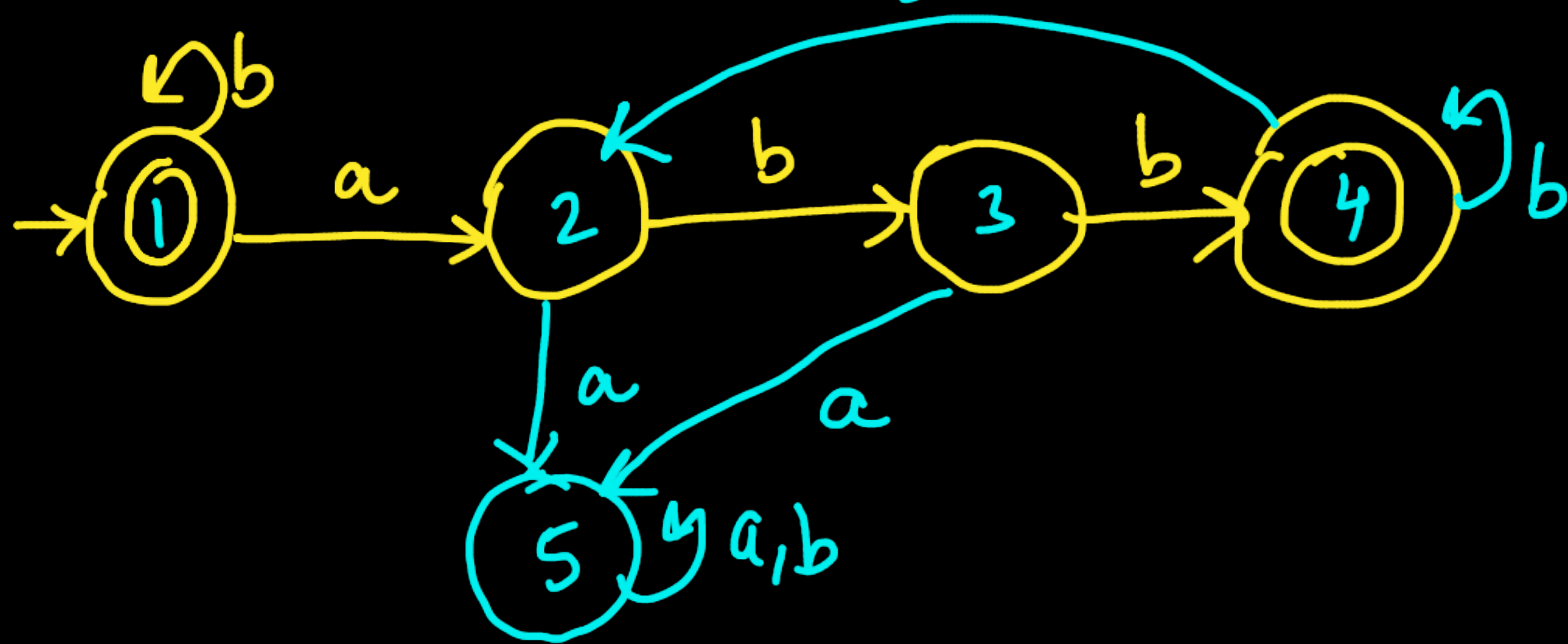
$L = \{ \underline{abab}, ab \text{ any a's or b's } ab, \dots \}$

$abbb \cdot a \cdot \underline{aaab}$
 \underline{aabbab}



Construct DFA to accept the lang
that accepts set of strings where
every a is followed by "bb".

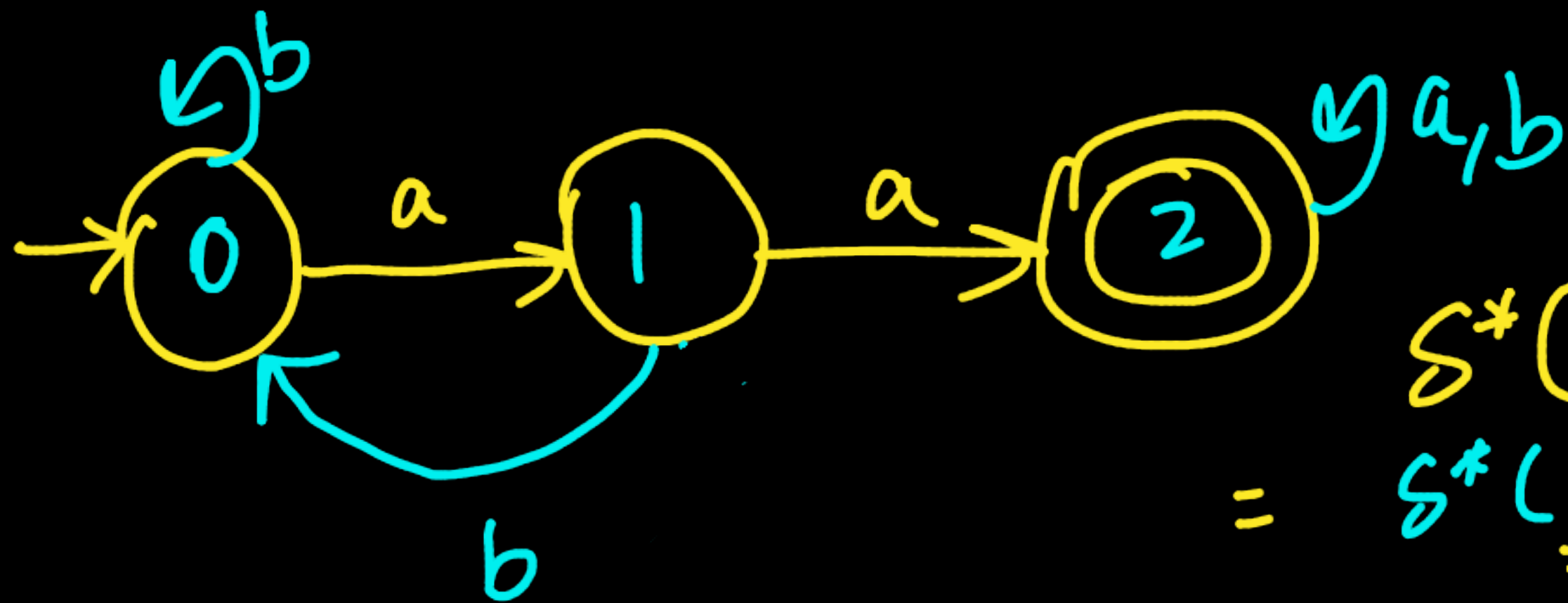
$L = \{ \lambda, b, bb's..., abb, \underline{bb} \underline{a} \underline{bb} \underline{bb} \underline{a} \underline{bb} \underline{bb} \}$



baab
X

Construct a DFA to accept lang
of strings over $\Sigma = \{a, b\}$ where
every string must contain 'aa' as substring.

$L = \{ \text{aa}, \text{b's or a's aa a's or b's} \dots \}$



rejected!

$$\begin{aligned} & \delta^*(0, \text{abb}) \\ &= \delta^*(1, \text{bb}) \end{aligned}$$

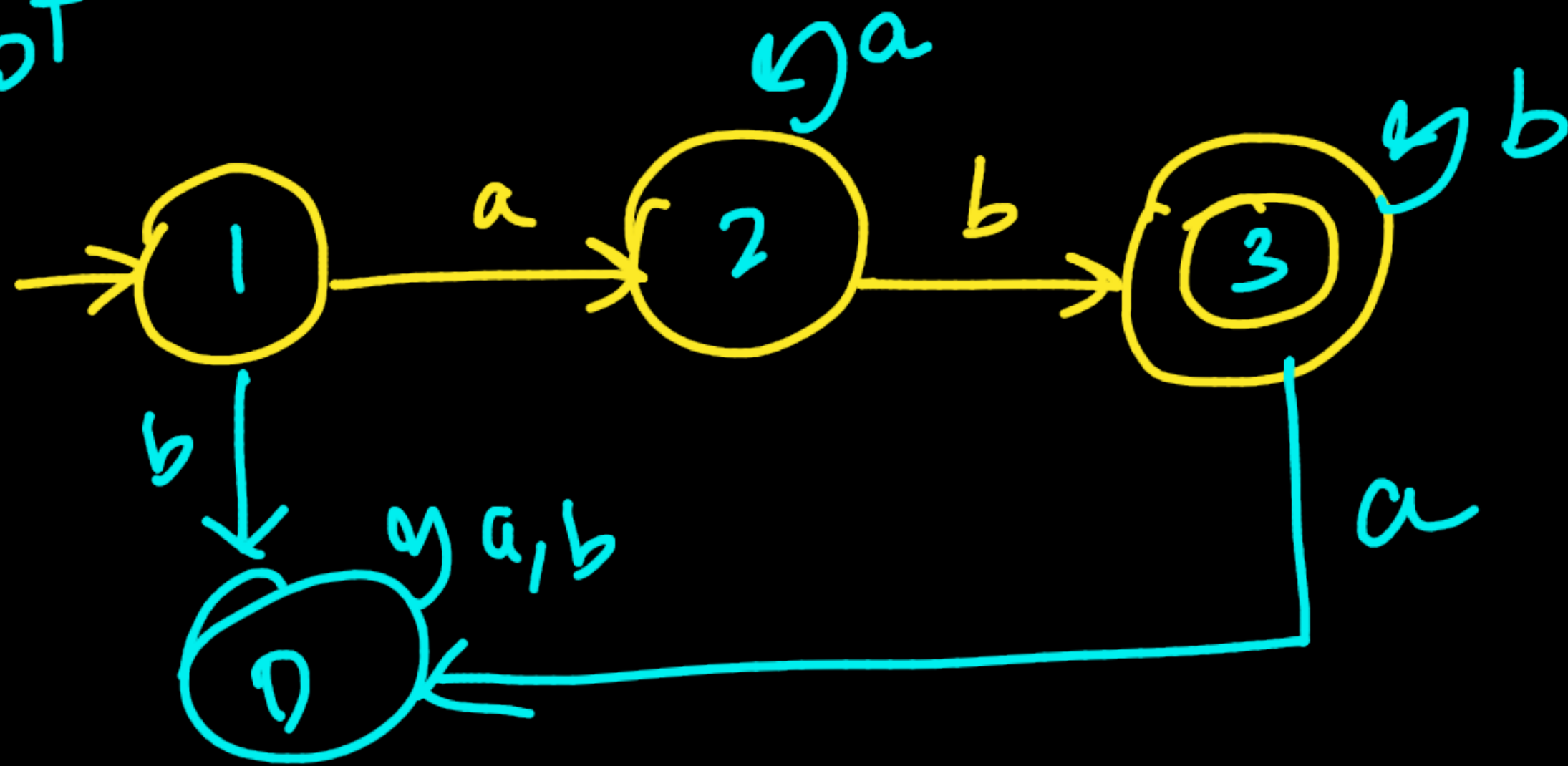
$$= \delta(0, b) = 0 \quad \times \text{Non-final state}$$

Construct DFA to accept the following

$$L = \{ \underline{a^n b^m} \mid n, m \geq 1 \} \quad n \geq 1, m \geq 1$$

$$L = \{ \underline{ab}, \underline{aaaa} \underline{b}, \underline{a} \underline{bbb} \underline{b}, aa \dots bb \dots \}$$

$a^+ b^+$



Construct a DFA to accept the lang

$$L = \{ a^n b^m \mid n, m \geq 0 \} \quad \underline{n \geq 0, m \geq 0} \quad \text{Homework}$$

$$L = \{ \lambda, aa \dots, bbb \dots, aa \dots bbb \dots \}$$