

## **Bernoulli Distribution**

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### **Discrete Distribution**



A Discrete Probability Distribution relates to discrete data.

It is often used to **model uncertain events** where the possible values for the variable are either **attribute** or **countable**.

The common discrete probability distributions are **Bernoulli**, **Binomial** and **Poisson**.

#### **Bernoulli Distribution**



## Many real-life events can only have two possible outcomes:

- •A tossed coin can either have a head or a tail.
- •A student can either pass or fail in an exam.
- •A product can either pass or fail in an inspection test.

How do you model the given scenario?



### **Bernoulli Distribution**



## **Bernoulli Distribution / Binary Distribution:**

A Bernoulli trial is a process that result in one of two possible outcomes.

## **Example:**

Success or Failure
Tossing a Coin
Any yes or no question
Was the newborn child a girl?
Is the top card of a shuffled deck an ace?



**Bernoulli Distribution: Applications** 

It is used to **model generic probabilistic situations** with just **two outcomes**.



A person who can be either healthy or sick with a certain disease.

The state of a telephone at a given time that can be either free or busy.

The preference of a person who can be either for or against a certain political candidate.



#### **Bernoulli Distribution**



#### **Conditions of Bernoulli Distribution:**

- It is a single trial. The trial can result in one of the two possible outcomes, labelled success and failure.
- P(success)=p
- Success could mean anything you want to consider as a positive or negative outcome.
- P(failure) = 1-p

Given any probability space, for any event(set of outcomes) one can define a Bernoulli trial, corresponding to whether the event occurred or not.

X ~ Bernoulli(p)

#### **Bernoulli Distribution**



## For any Bernoulli Trial:

#### A random variable X is defined as:

X=1 if success occurs, where probability of success is denoted by p
X=0 if failure occurs, where probability of failure is (1-p)

Then X is said to have a Bernoulli distribution with probability p.

Note: A Bernoulli random variable can only take values 0 and 1.

Probability distribution of X: X ~ Bernoulli(p)

### **Bernoulli Distribution**



Mean = 
$$\sum xp(x)$$
  
=0(1-p) +1\* p  
= p

Variance = 
$$\sum (x\text{-mean})^2 *p(x)$$
  
= $(0-p)^2 (1-p) + (1-p)^2*p$   
= $p*(1-p)$ 

## **Bernoulli Distribution: Example**

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Suppose that a student takes a multiple choice test. The test has 10 questions, each of which has 4 possible answers (only one is correct).

If the student blindly guesses the answer to each question, do the questions form a sequence of Bernoulli trails? If so, identify the trial outcomes and the parameter p.

#### **Solution:**

For each question, either the answer chosen is correct or incorrect.

P(Answer is correct)=1/4; P(Answer is incorrect)=3/4

There are only 2 possible outcomes for each question. Hence each question is a **Bernoulli trial**.

Since there are in total 10 questions, we have a sequence of Bernoulli trials.

## **Bernoulli Distribution: Example**



Approximately 1 in 500 Indian adults are teachers. One Indian adult is randomly selected.

What is the distribution of the number of teachers?

#### **Solution:**

X represents the **Indian adult** is a **teacher**.

X ~ Bernoulli (1/500)

Therefore, the **probability distribution of X** is

X p(x) or P(X=x)

0 499/500

1 1/500

#### **Bernoulli Distribution**



#### Do It Yourself!!!

Candidate A is running for office in a certain district.

Thirty persons are selected at random from the population of registered voters and asked if they prefer candidate A.

Do the responses form a sequence of Bernoulli trials?

If so identify the trial outcomes and the meaning of the parameter p.



# **THANK YOU**

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